

Recursion

Two way of writing Codes.

Iterative Method

Recursive Method

```
int abc() {
    loop
    return
}
```

Loop

Interactive
function

```
void abc() {
```

ancl

↓
A function that calls itself
is called a recursive
function.

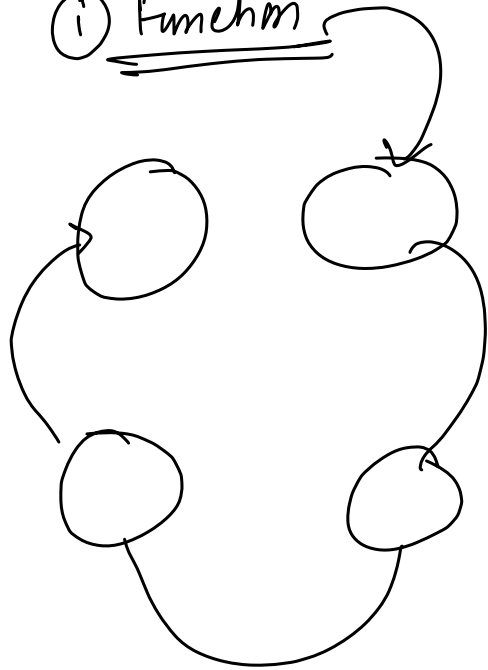
Terminating condition of a recursive function

`void abc (-----) {`

if ()
return;

abc()

(i) Function



Recursive functions have two phases.

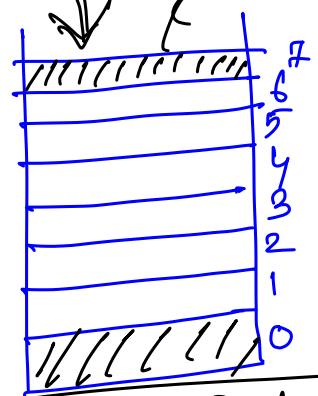
Winding phase

Unwinding phase

```
int main() {  
    ==  
    abc();  
}
```

push
pop

Stack



FIFO

Last in First out

LIFO

```
abc() {  
    ==  
    bcd();  
}
```

```
bcd() {  
    ==  
    cda();  
}
```

```
cda() {  
    ==  
    ppp();  
}
```

winding phase

abc()

bcd()

cda()

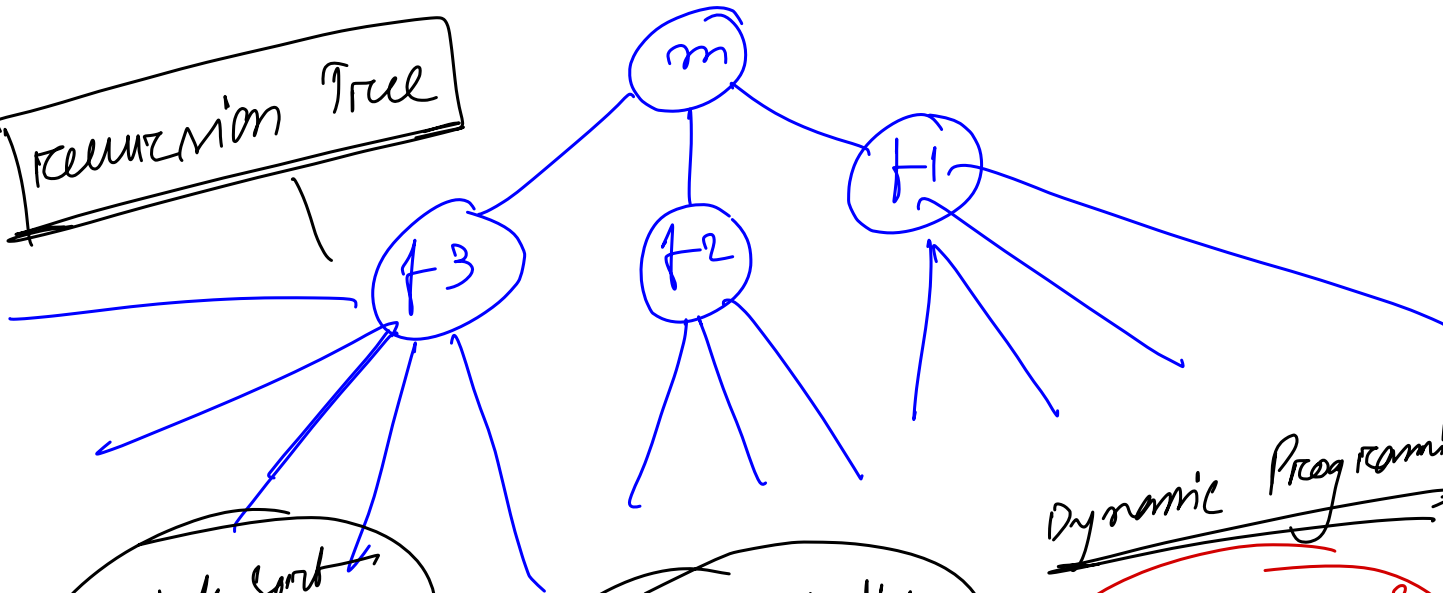
ppp()

unwinding phase

recursive stack



Recursion Tree



quick sort
merge sort

Time Complexity
Space

Dynamic Programming

```
int main() {
    abc(10);
    return 0;
}
```

Iterative way

```
void abc(int n) {
    for (int i = 1; i <= n; i++) {
        printf("%d\t", i);
    }
}
```

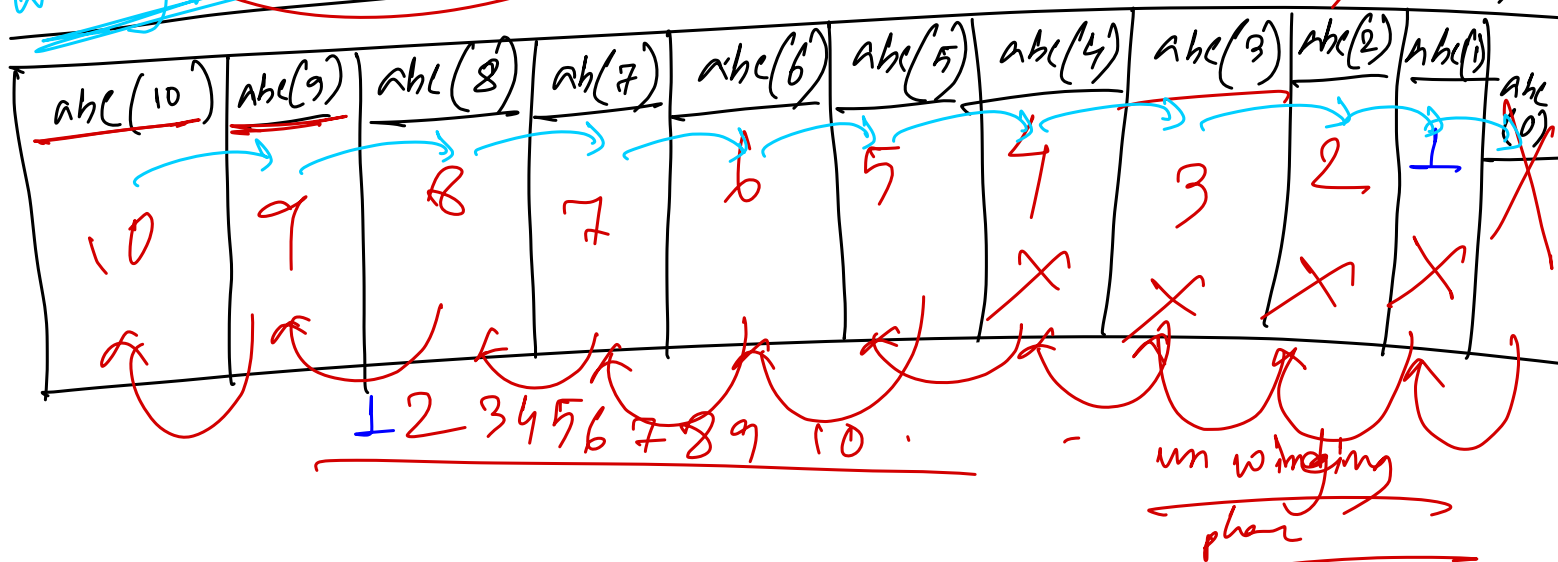
Condition

Recursive way

```
void abc(int n) {
    if (n == 0)
        return;
    abc(n-1);
    printf("%d\t", n);
}
```

Time/Dec

winding phase



Sum of N natural Numbers using Recursion

5

```
int sum (int n) { int a = 0;  
    if (n == 0) return a;  
    a += n;  
    return sum (n-1, a);  
}
```

```
int main() {  
    a = 0  
    n = 5  
    printf("sum = %d", sum(n, a));  
}
```

$a = 5 + 4 + 3 + 2 + 1$
15

int a;

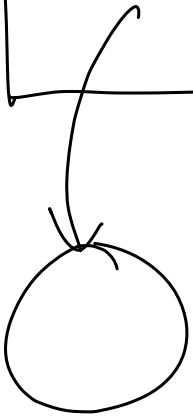
```
int abc (n) {  
    if (n == 0) return a;  
    a += n;  
    abc (n-1);  
}
```

```
main() {  
    abc(5)  
}
```

$$\text{Sum}(5) = 5 + 4 + 3 + 2 + 1$$

$$\text{Sum}(4)$$

$$\text{Sum}(n) = \begin{cases} n + \text{Sum}(n-1) & \rightarrow n > 0 \\ 0 & \rightarrow n == 0 \end{cases}$$



```
int sum(int n) {
    if (n == 0) return 0;
    return n + sum(n-1);
}
```