

PROBLEM 9 :-

Line AB 100 mm long is 30° and 45° inclined to Hp & Vp respectively.

End A is 10 mm above Hp and it's VT is 20 mm below Hp

.Draw projections of the line and it's HT.

SOLUTION STEPS:-

Draw xy, one projector and locate on it VT and V.

Draw locus of a' 10 mm above xy.

Take 30° from VT and draw a line.

Where it intersects with locus of a' name it a_1' as it is TL of that part.

From a_1' cut 100 mm (TL) on it and locate point b_1'

Now from V take 45° and draw a line downwards

& Mark on it distance $VT-a_1'$ i.e.TL of extension & name it a_1

Extend this line by 100 mm and mark point b_1 .

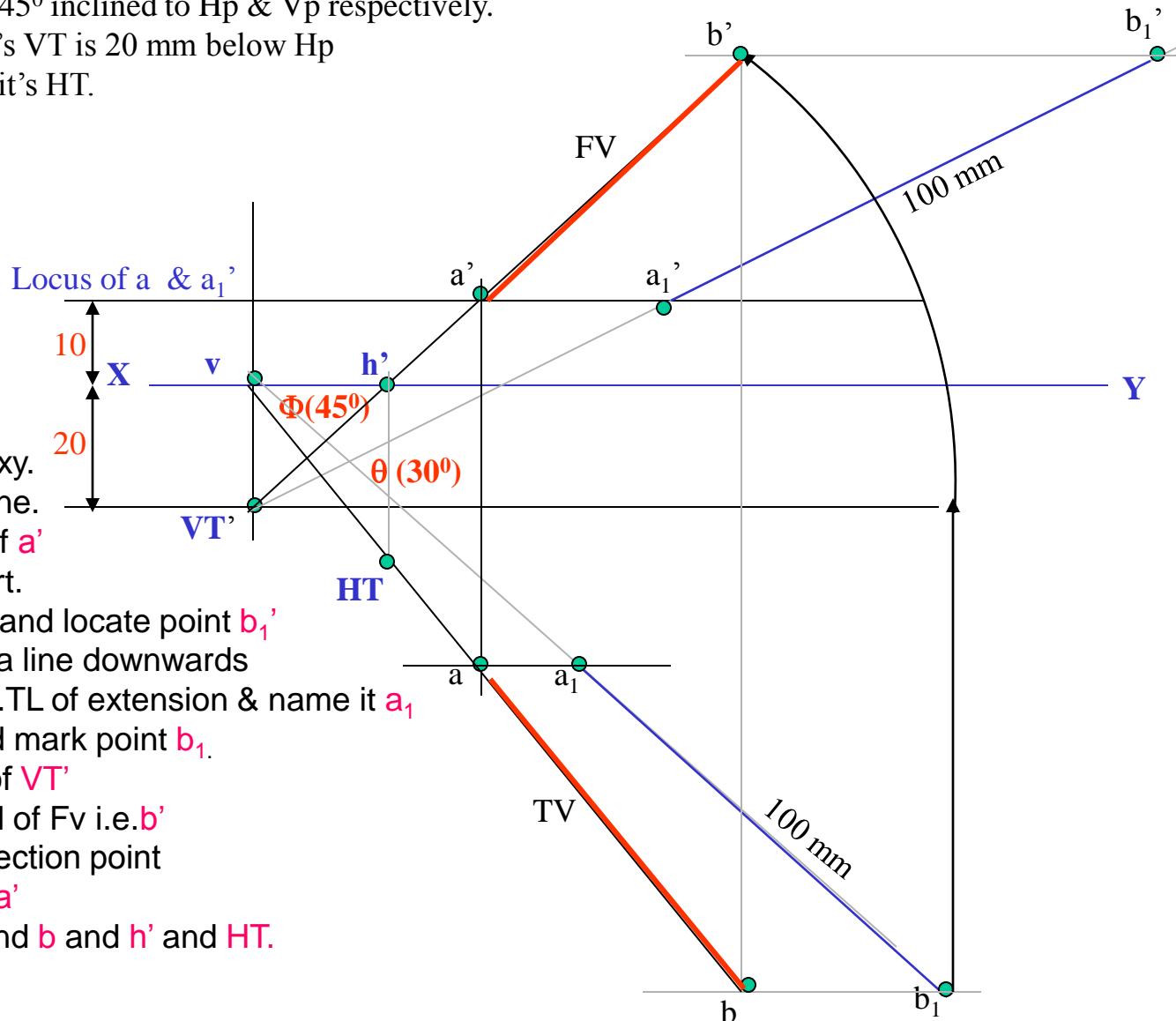
Draw it's component on locus of VT'

& further rotate to get other end of Fv i.e. b'

Join it with VT' and mark intersection point

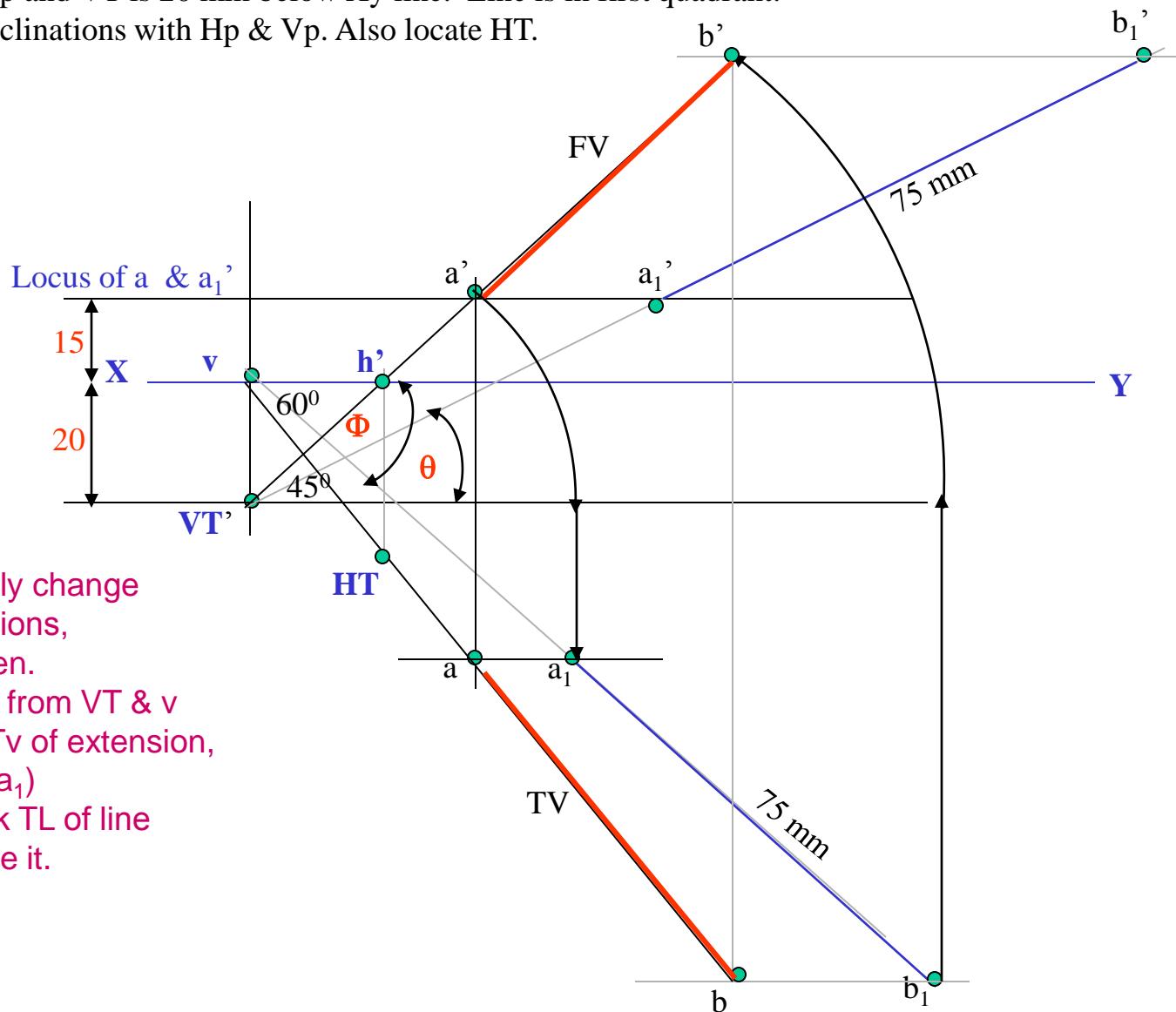
(with locus of a_1') and name it a'

Now as usual locate points a and b and h' and HT.



PROBLEM 10 :-

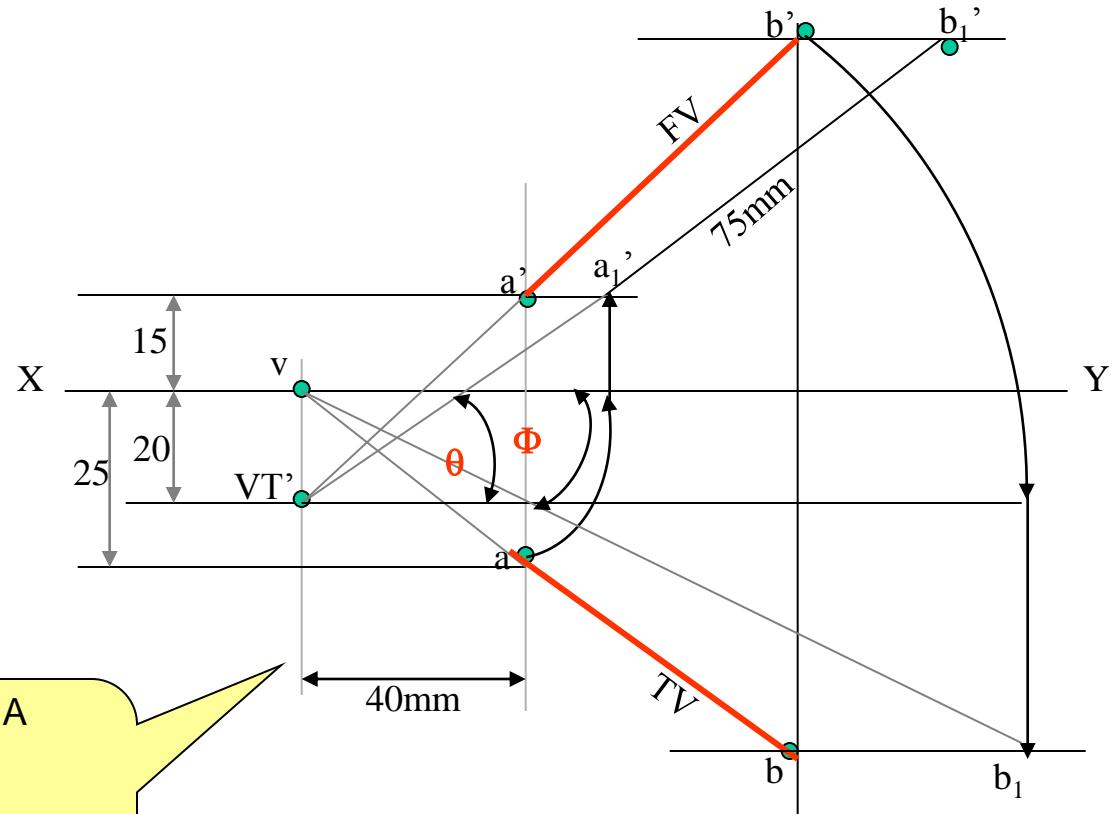
A line AB is 75 mm long. It's Fv & Tv make 45° and 60° inclinations with X-Y line resp
 End A is 15 mm above Hp and VT is 20 mm below Xy line. Line is in first quadrant.
 Draw projections, find inclinations with Hp & Vp. Also locate HT.



SOLUTION STEPS:-

Similar to the previous only change is instead of line's inclinations, views inclinations are given.
 So first take those angles from VT & v Properly, construct Fv & Tv of extension, then determine it's TL(V-a₁) and on it's extension mark TL of line and proceed and complete it.

PROBLEM 11 :- The projectors drawn from VT & end A of line AB are 40mm apart. End A is 15mm above Hp and 25 mm in front of Vp. VT of line is 20 mm below Hp. If line is 75mm long, draw it's projections, find inclinations with HP & Vp



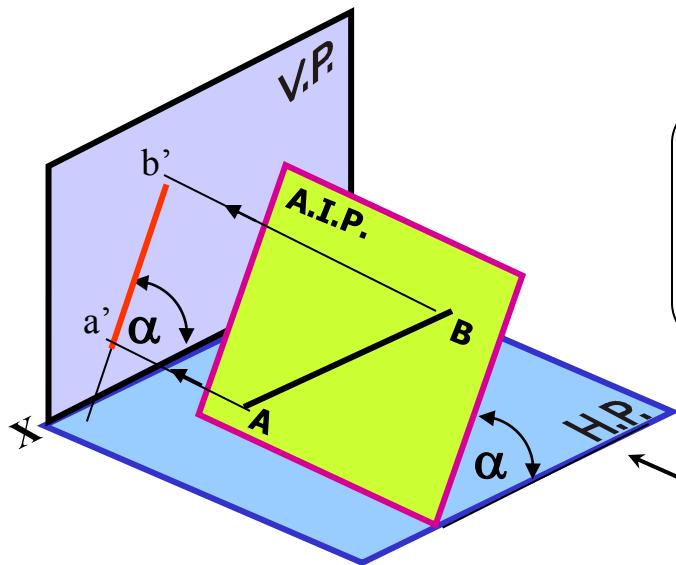
Draw two projectors for VT & end A
Locate these points and then

YES !

YOU CAN COMPLETE IT.

GROUP (C)

CASES OF THE LINES IN A.V.P., A.I.P. & PROFILE PLANE.

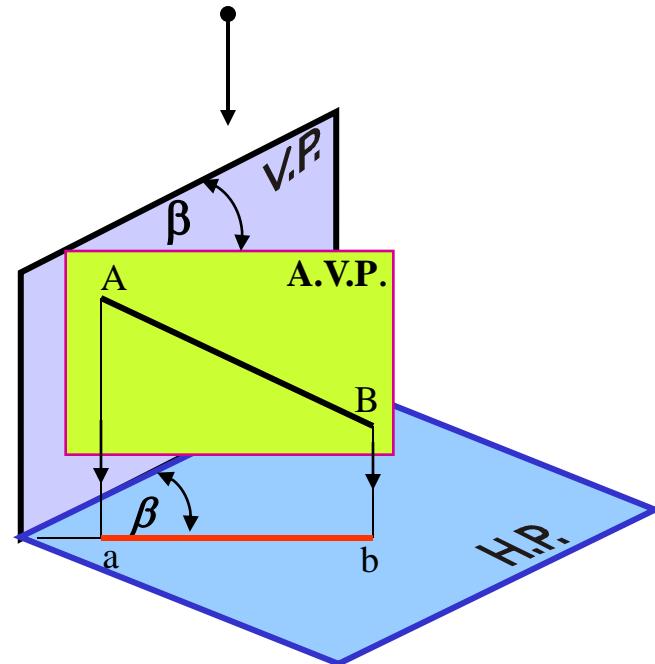


Line AB is in AIP as shown in above figure no 1.
It's FV ($a'b'$) is shown projected on Vp.(Looking in arrow direction)
Here one can clearly see that the

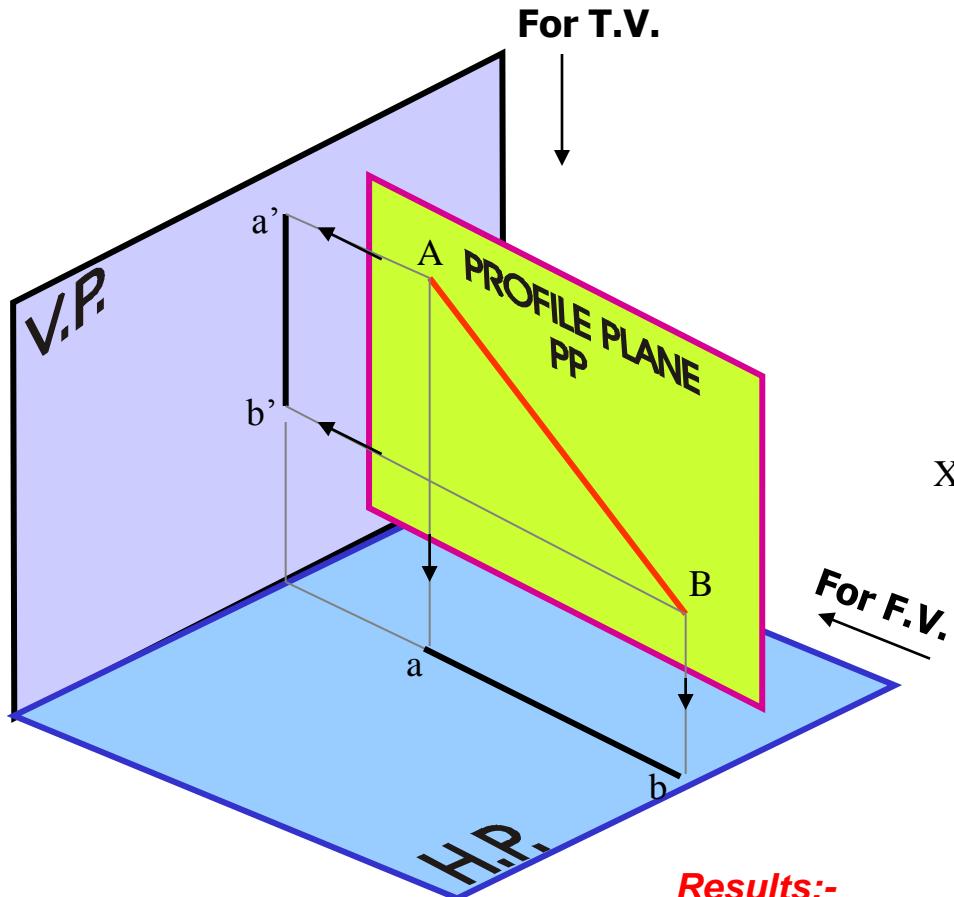
Inclination of AIP with HP = Inclination of FV with XY line

Line AB is in AVP as shown in above figure no 2..
It's TV ($a b$) is shown projected on Hp.(Looking in arrow direction)
Here one can clearly see that the

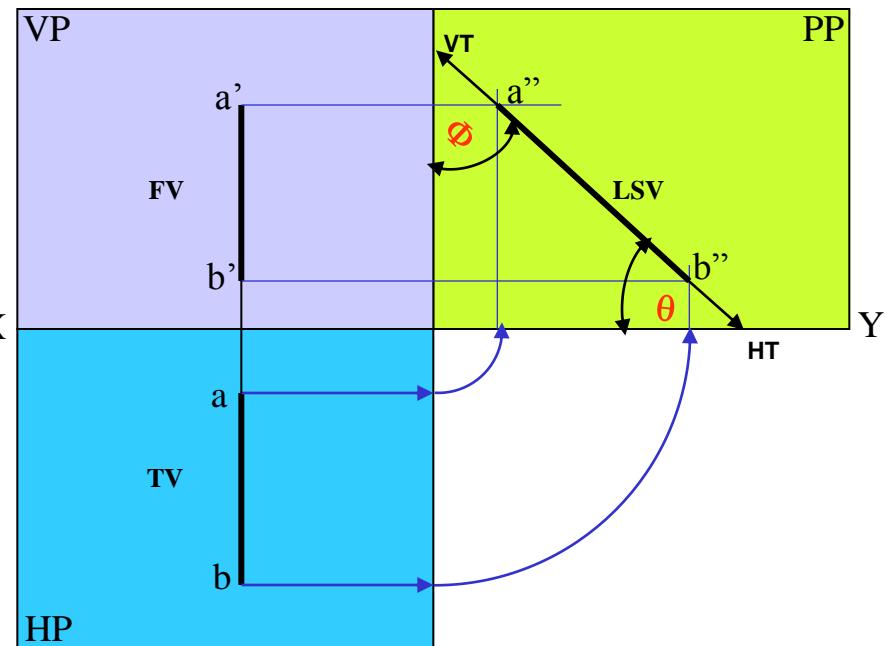
Inclination of AVP with VP = Inclination of TV with XY line



LINE IN A PROFILE PLANE (MEANS IN A PLANE PERPENDICULAR TO BOTH HP & VP)



ORTHOGRAPHIC PATTERN OF LINE IN PROFILE PLANE

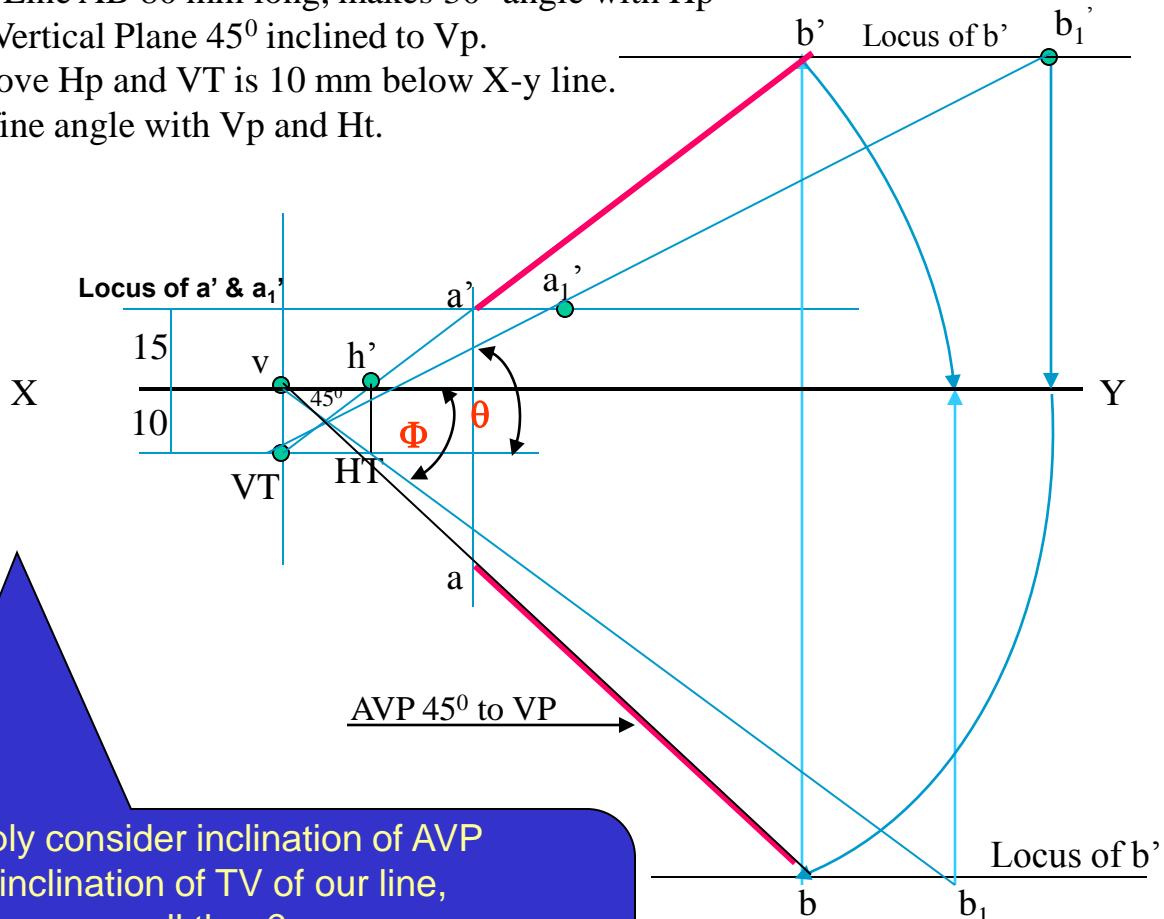


Results:-

1. TV & FV both are vertical, hence arrive on one single projector.
2. It's Side View shows True Length (TL)
3. Sum of it's inclinations with HP & VP equals to 90° ($\theta + \phi = 90^\circ$)
4. It's HT & VT arrive on same projector and can be easily located From Side View.

OBSERVE CAREFULLY ABOVE GIVEN ILLUSTRATION AND 2nd SOLVED PROBLEM.

PROBLEM 12 :- Line AB 80 mm long, makes 30^0 angle with Hp and lies in an Aux. Vertical Plane 45^0 inclined to Vp. End A is 15 mm above Hp and VT is 10 mm below X-y line. Draw projections, fine angle with Vp and Ht.

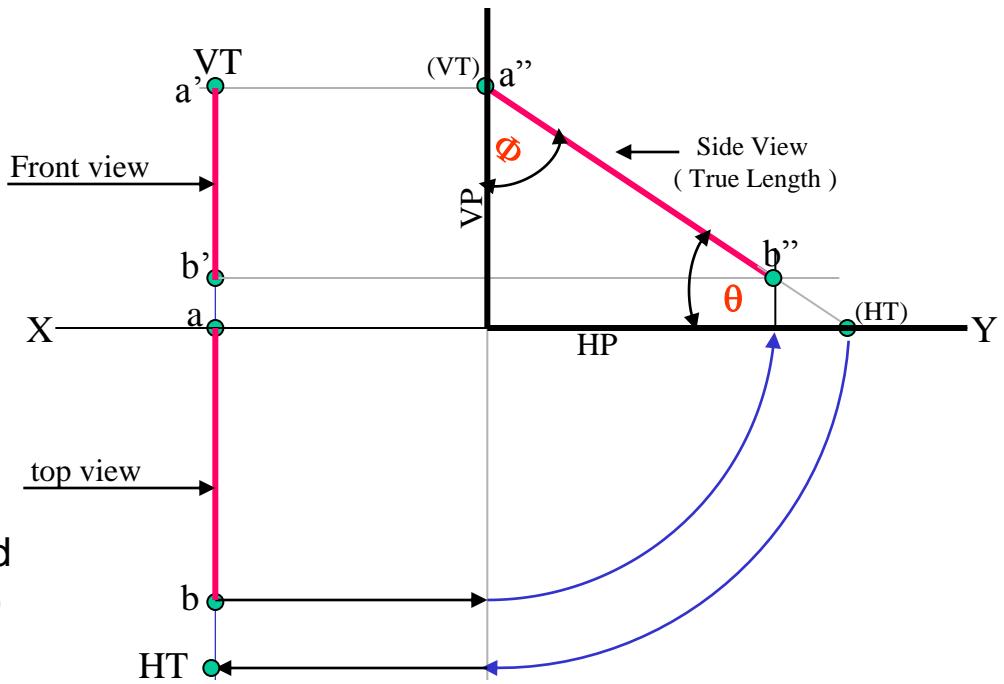


*You sure can complete it
as previous problems!
Go ahead!!*

PROBLEM 13 :- A line AB, 75mm long, has one end A in Vp. Other end B is 15 mm above Hp and 50 mm in front of Vp. Draw the projections of the line when sum of its Inclinations with HP & Vp is 90^0 , means it is lying in a profile plane. Find true angles with ref.planes and it's traces.

SOLUTION STEPS:-

After drawing xy line and one projector
 Locate top view of A i.e point a on xy as
 It is in Vp,
 Locate Fv of B i.e.b' 15 mm above xy as
 it is above Hp. and Tv of B i.e. b, 50 mm
 below xy as it is 50 mm in front of Vp
 Draw side view structure of Vp and Hp
 and locate S.V. of point B i.e. b"
 From this point cut 75 mm distance on Vp and
 Mark a" as A is in Vp. (This is also VT of line.)
 From this point draw locus to left & get a'
 Extend SV up to Hp. It will be HT. As it is a Tv
 Rotate it and bring it on projector of b.
 Now as discussed earlier SV gives TL of line
 and at the same time on extension up to Hp & Vp
 gives inclinations with those planes.



APPLICATIONS OF PRINCIPLES OF PROJECTIONS OF LINES IN SOLVING CASES OF DIFFERENT PRACTICAL SITUATIONS.

In these types of problems some situation in the field
or
some object will be described .
It's relation with Ground (HP)
And
a Wall or some vertical object (VP) will be given.

Indirectly information regarding Fv & Tv of some line or lines,
inclined to both reference Planes will be given
and

you are supposed to draw it's projections
and

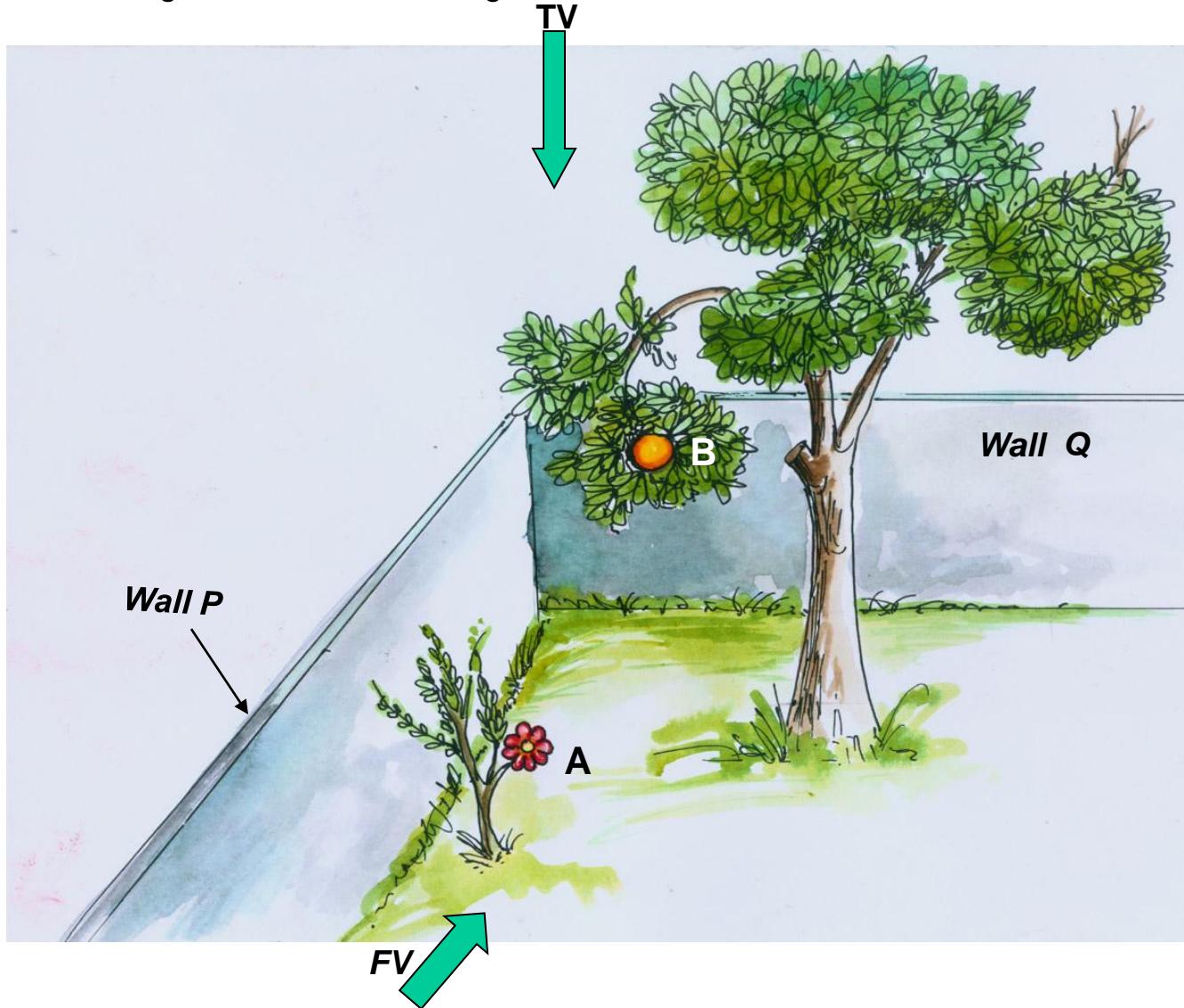
further to determine it's true Length and it's inclinations with ground.

Here various problems along with
actual pictures of those situations are given
for you to understand those clearly.

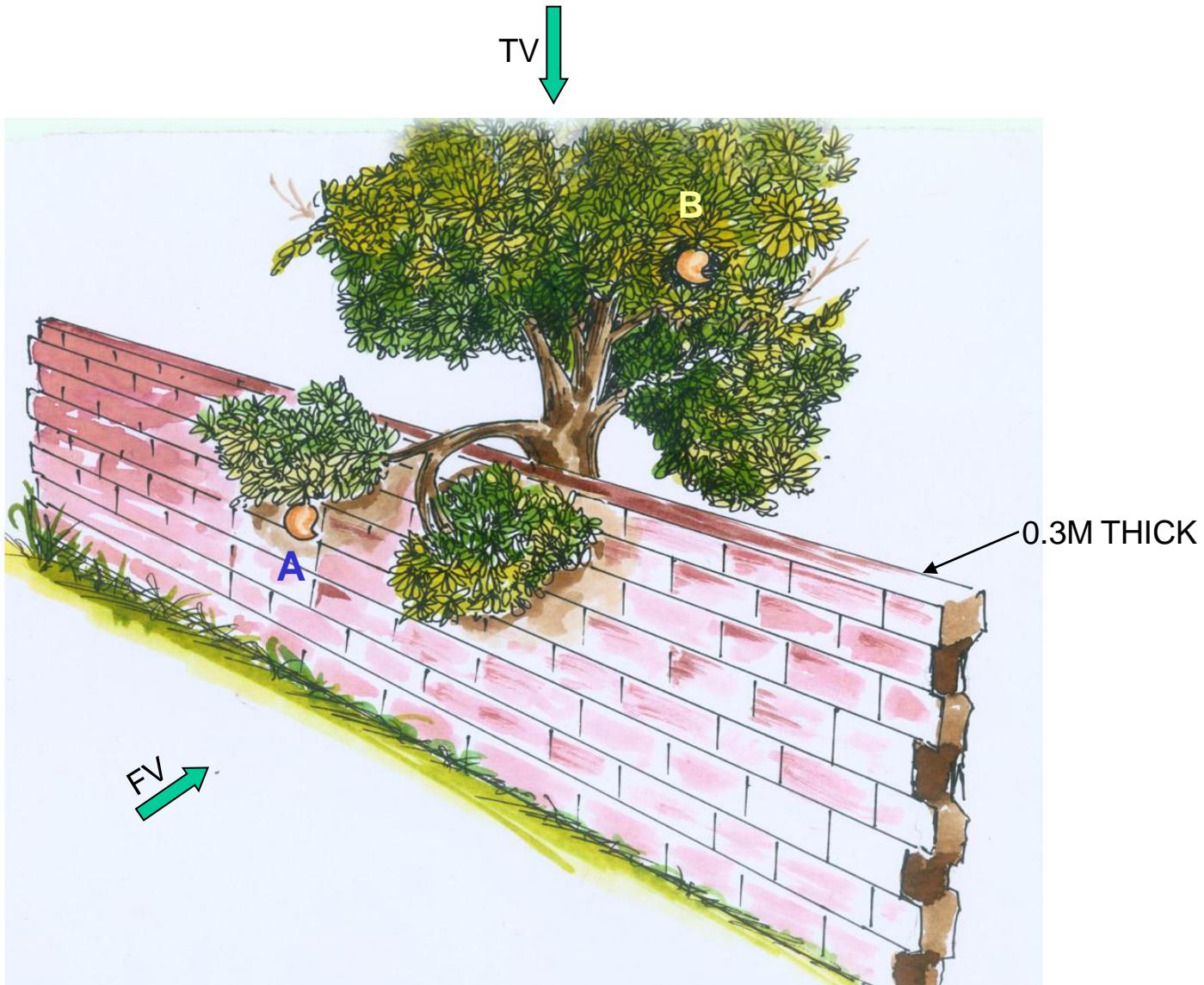
Now looking for views in given **ARROW** directions,
YOU are supposed to draw projections & find answers,
Off course you must visualize the situation properly.

CHECK YOUR ANSWERS
WITH THE SOLUTIONS
GIVEN IN THE END.
ALL THE BEST !!

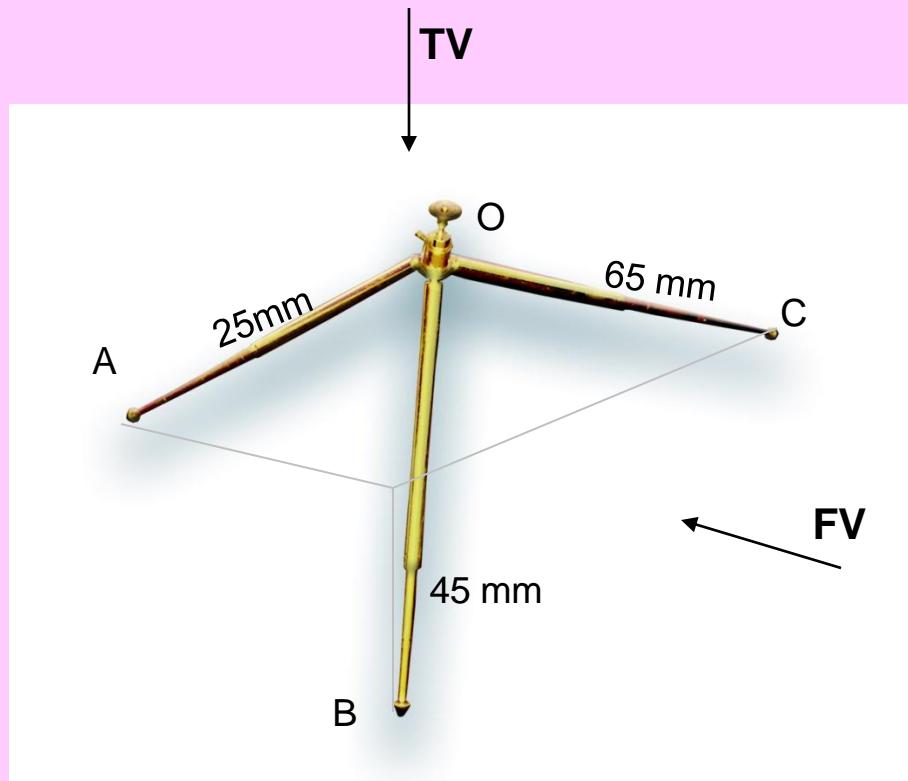
PROBLEM 14:- Two objects, a flower (A) and an orange (B) are within a rectangular compound wall, whose P & Q are walls meeting at 90° . Flower A is 1M & 5.5 M from walls P & Q respectively. Orange B is 4M & 1.5M from walls P & Q respectively. Drawing projection, find distance between them If flower is 1.5 M and orange is 3.5 M above the ground. Consider suitable scale..



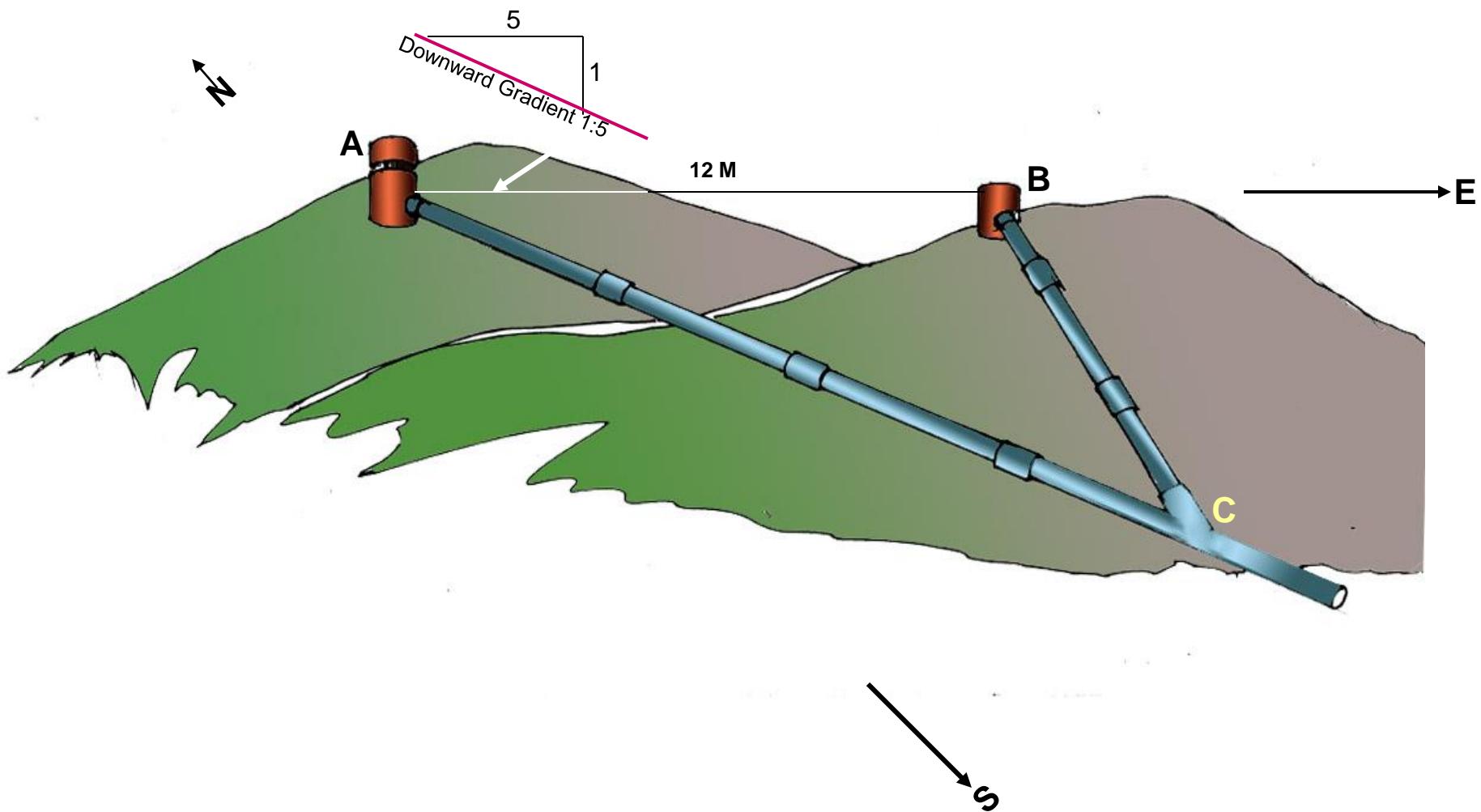
PROBLEM 15 :- Two mangos on a tree A & B are 1.5 m and 3.00 m above ground and those are 1.2 m & 1.5 m from a 0.3 m thick wall but on opposite sides of it. If the distance measured between them along the ground and parallel to wall is 2.6 m, Then find real distance between them by drawing their projections.



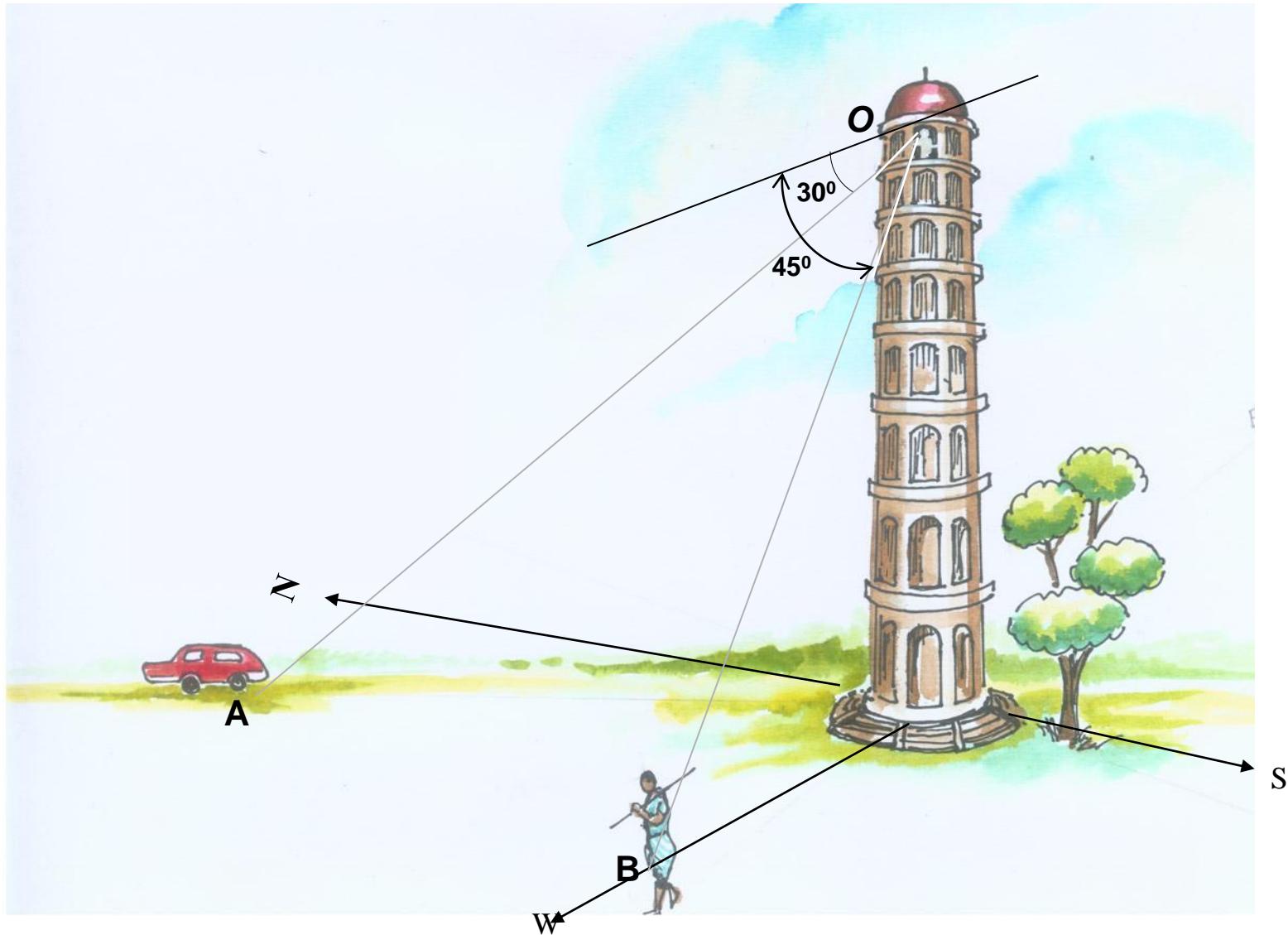
PROBLEM 16 :- oa, ob & oc are three lines, 25mm, 45mm and 65mm long respectively. All equally inclined and the shortest is vertical. This fig. is TV of three rods OA, OB and OC whose ends A,B & C are on ground and end O is 100mm above ground. Draw their projections and find length of each along with their angles with ground.



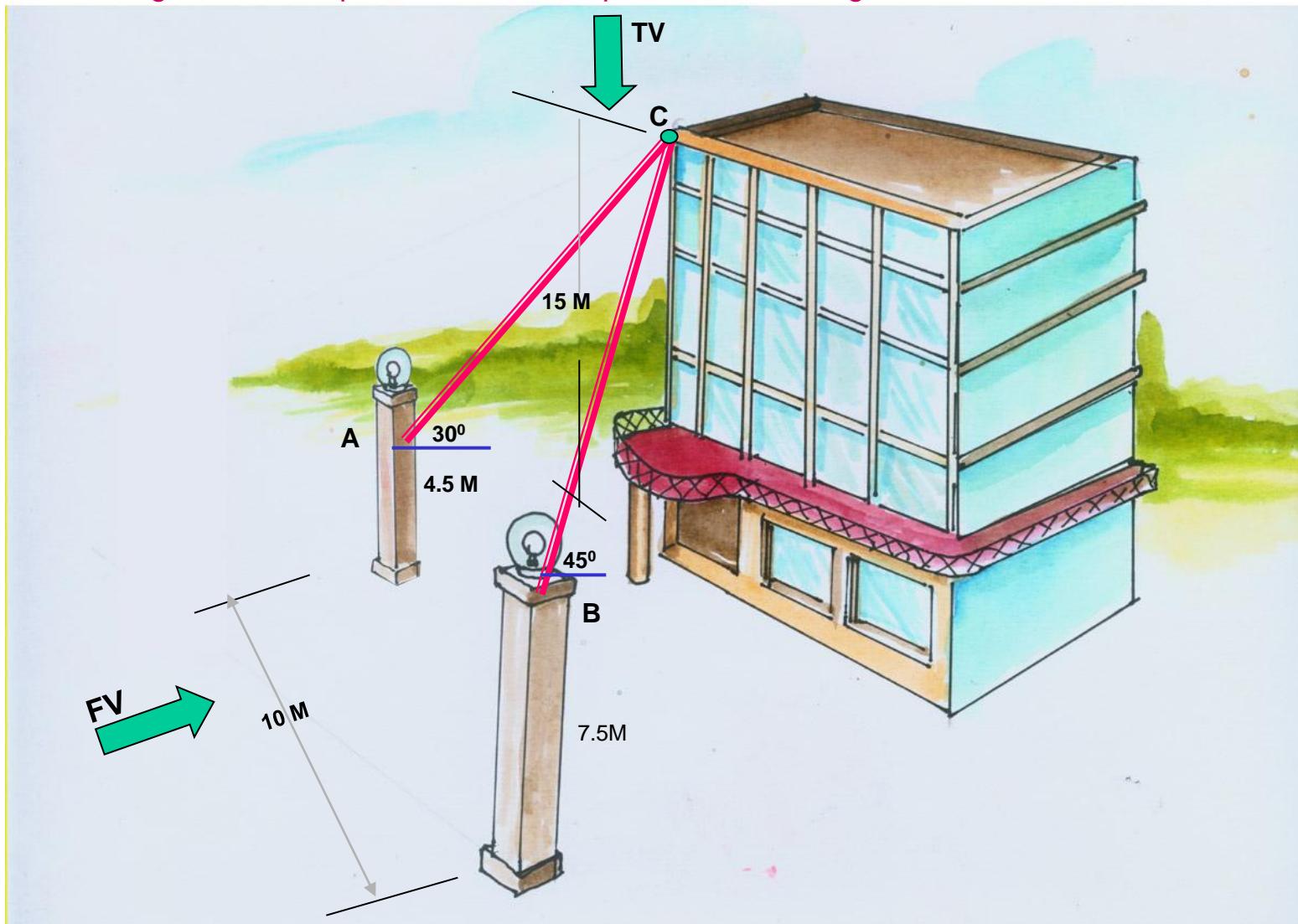
PROBLEM 17:- A pipe line from point **A** has a downward gradient 1:5 and it runs due East-South. Another Point **B** is 12 M from **A** and due East of **A** and in same level of **A**. Pipe line from **B** runs 20° Due East of South and meets pipe line from **A** at point **C**. Draw projections and find length of pipe line from **B** and it's inclination with ground.



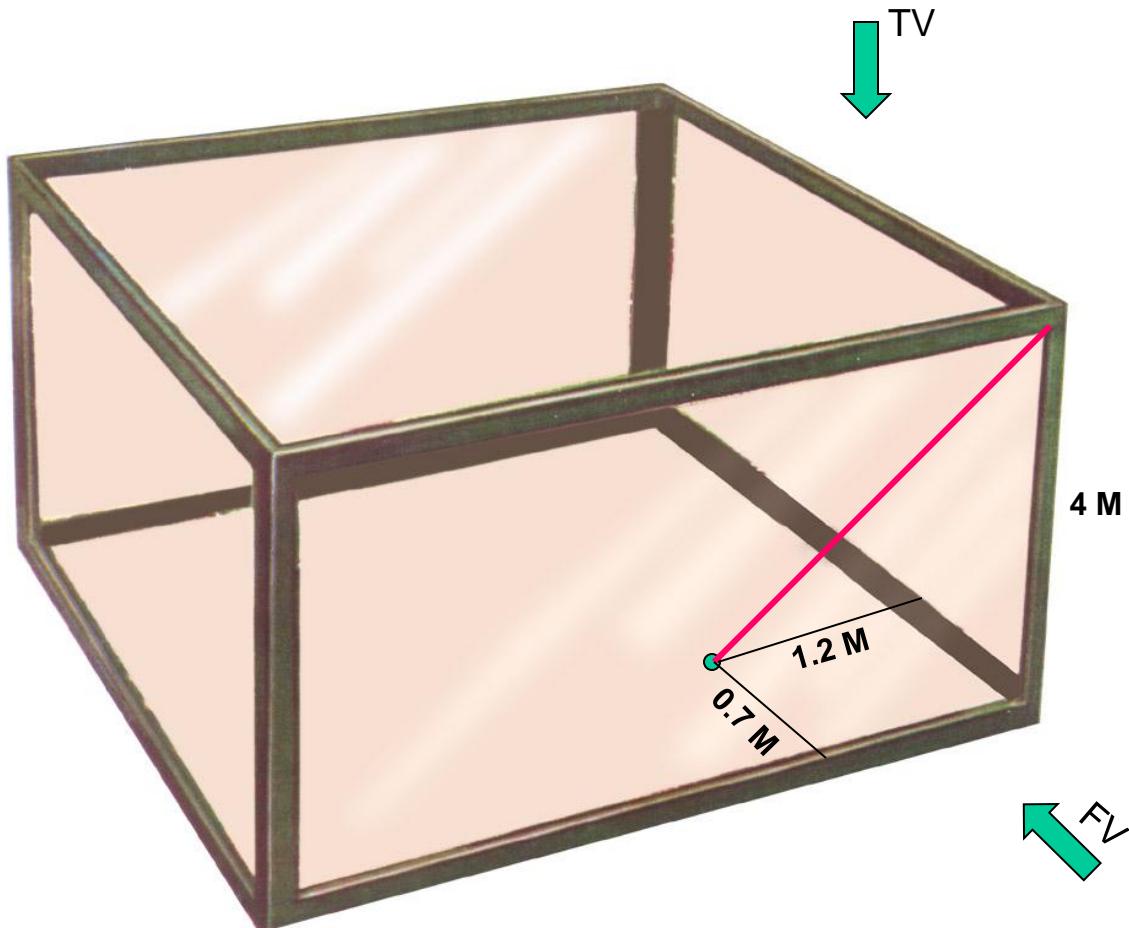
PROBLEM 18: A person observes two objects, A & B, on the ground, from a tower, 15 M high, At the angles of depression 30° & 45° . Object A is is due North-West direction of observer and object B is due West direction. Draw projections of situation and find distance of objects from observer and from tower also.



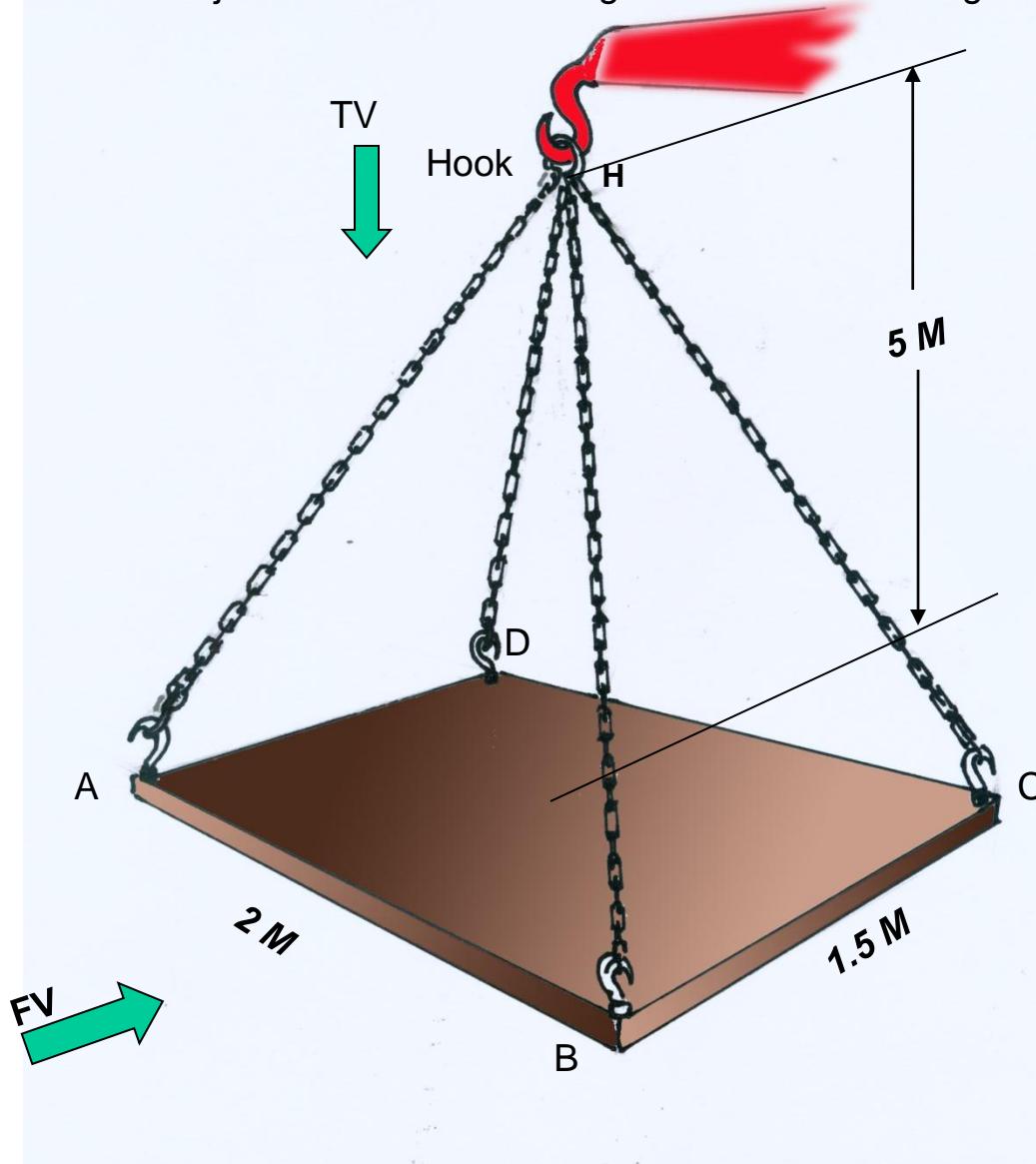
PROBLEM 19:-Guy ropes of two poles fixed at 4.5m and 7.5 m above ground, are attached to a corner of a building 15 M high, make 30° and 45° inclinations with ground respectively. The poles are 10 M apart. Determine by drawing their projections, Length of each rope and distance of poles from building.



PROBLEM 20:- A tank of 4 M height is to be strengthened by four stay rods from each corner by fixing their other ends to the flooring, at a point 1.2 M and 0.7 M from two adjacent walls respectively, as shown. Determine graphically length and angle of each rod with flooring.



PROBLEM 21:- A horizontal wooden platform 2 M long and 1.5 M wide is supported by four chains from it's corners and chains are attached to a hook 5 M above the center of the platform. Draw projections of the objects and determine length of each chain along with it's inclination with ground.



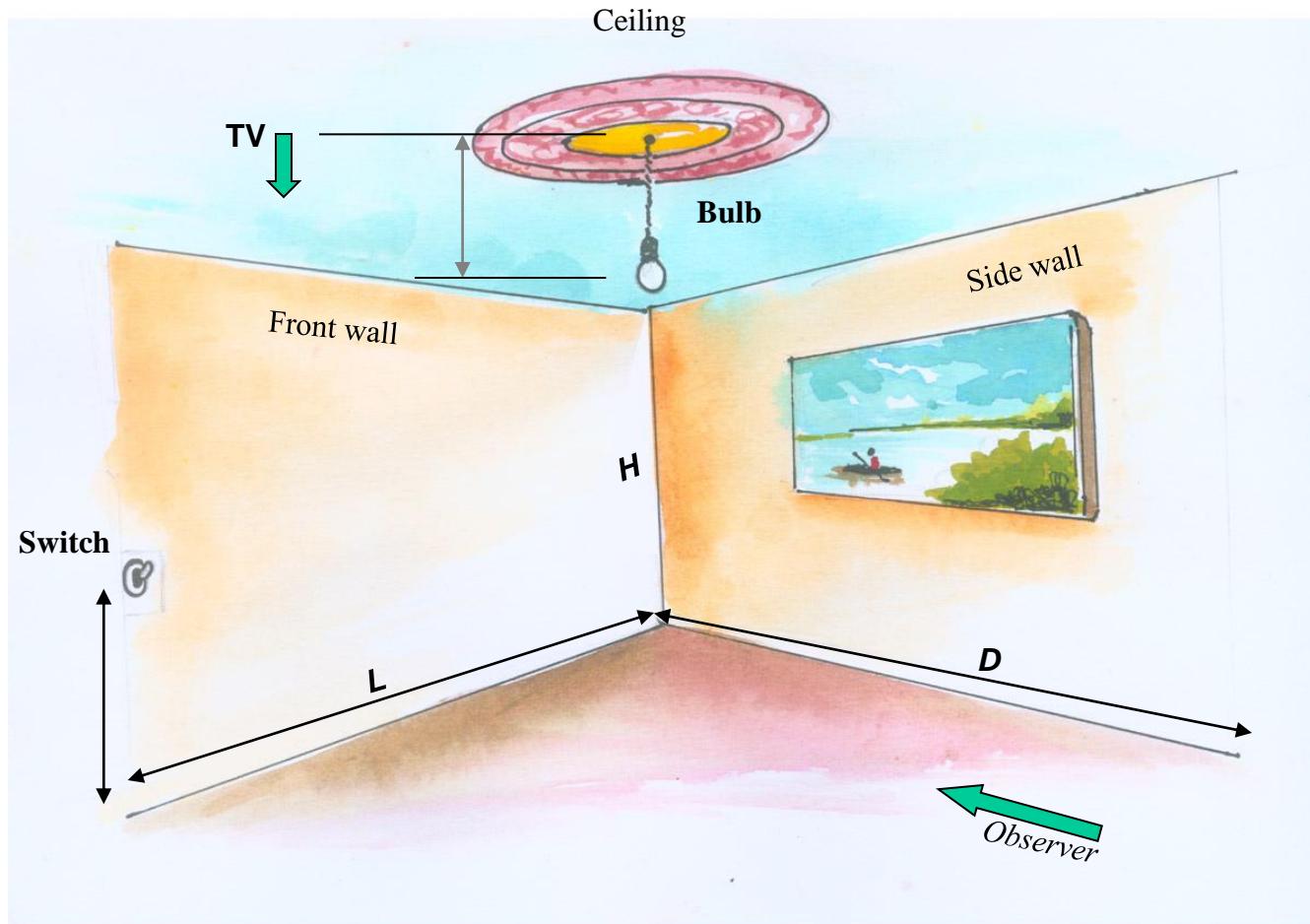
PROBLEM 22.

A room is of size 6.5m L ,5m D,3.5m high.

An electric bulb hangs 1m below the center of ceiling.

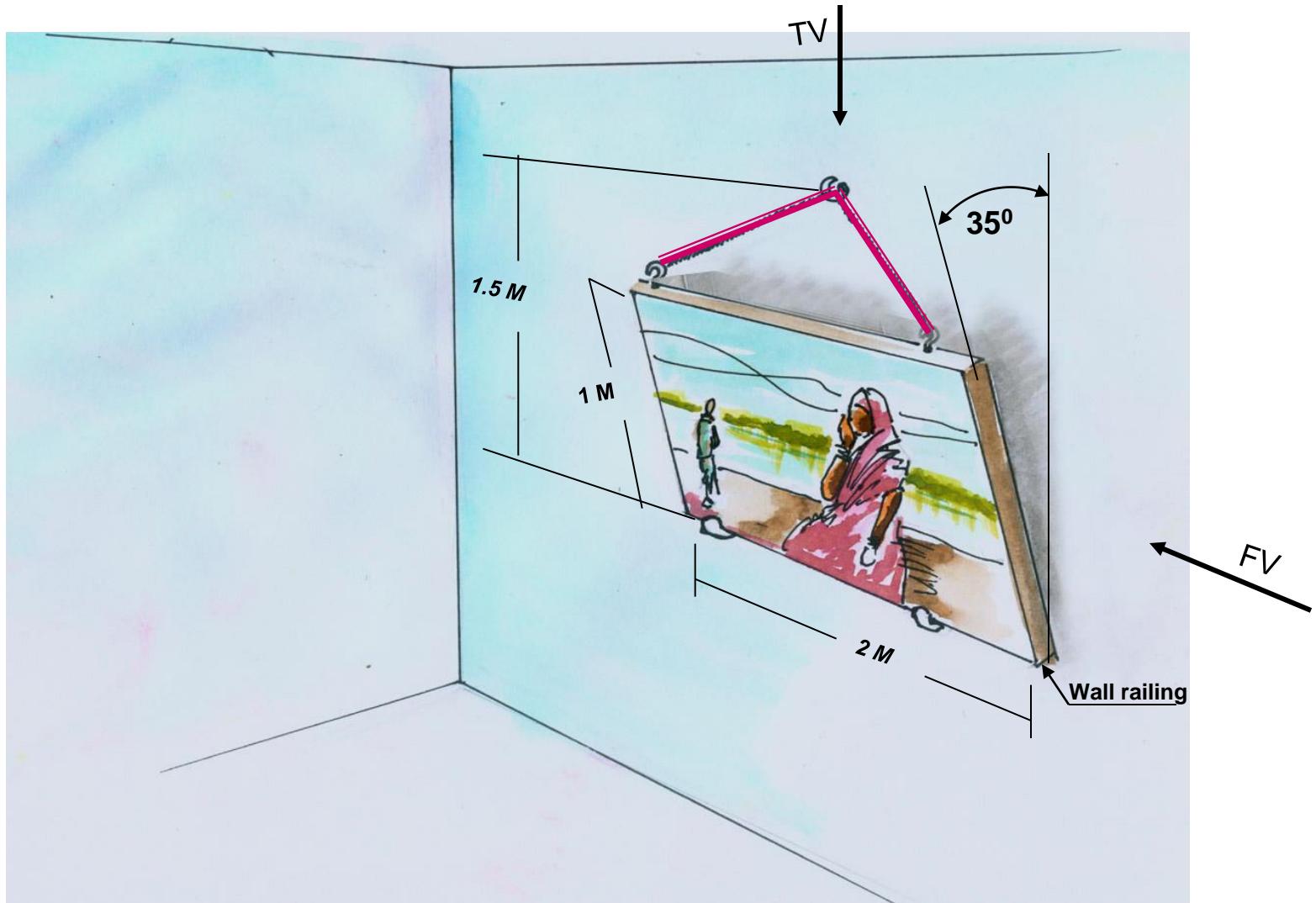
A switch is placed in one of the corners of the room, 1.5m above the flooring.

Draw the projections and determine real distance between the bulb and switch.



PROBLEM 23:-

A PICTURE FRAME 2 M WIDE AND 1 M TALL IS RESTING ON HORIZONTAL WALL RAILING
MAKES 35° INCLINATION WITH WALL. IT IS ATTACHED TO A HOOK IN THE WALL BY TWO STRINGS.
THE HOOK IS 1.5 M ABOVE WALL RAILING. DETERMINE LENGTH OF EACH CHAIN AND TRUE ANGLE BETWEEN THEM



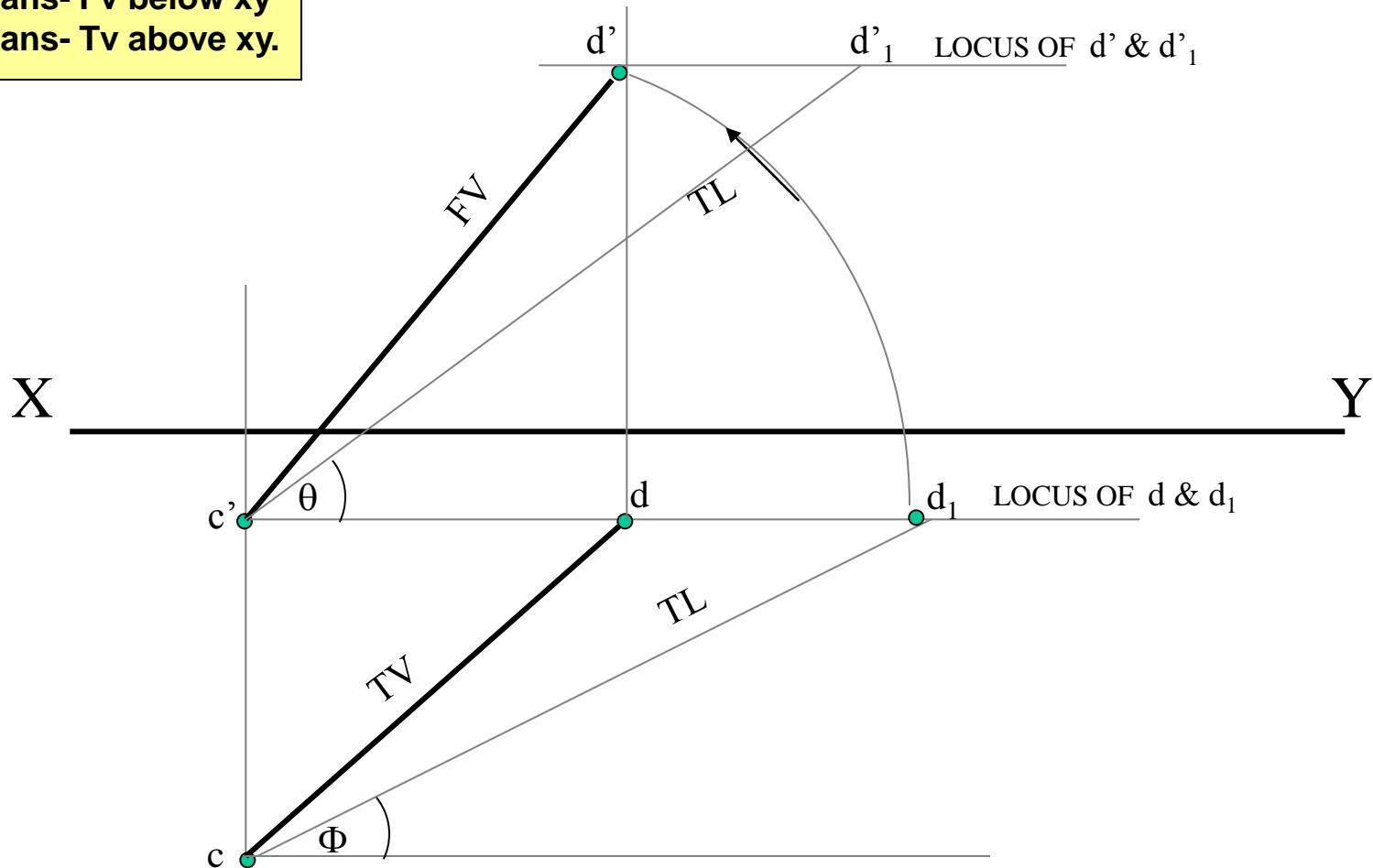
PROBLEM NO.24

T.V. of a 75 mm long Line CD, measures 50 mm.
 End C is 15 mm below Hp and 50 mm in front of Vp.
 End D is 15 mm in front of Vp and it is above Hp.
 Draw projections of CD and find angles with Hp and Vp.

SOME CASES OF THE LINE IN DIFFERENT QUADRANTS.

REMEMBER:

BELOW HP- Means- Fv below xy
BEHIND V p- Means- Tv above xy.



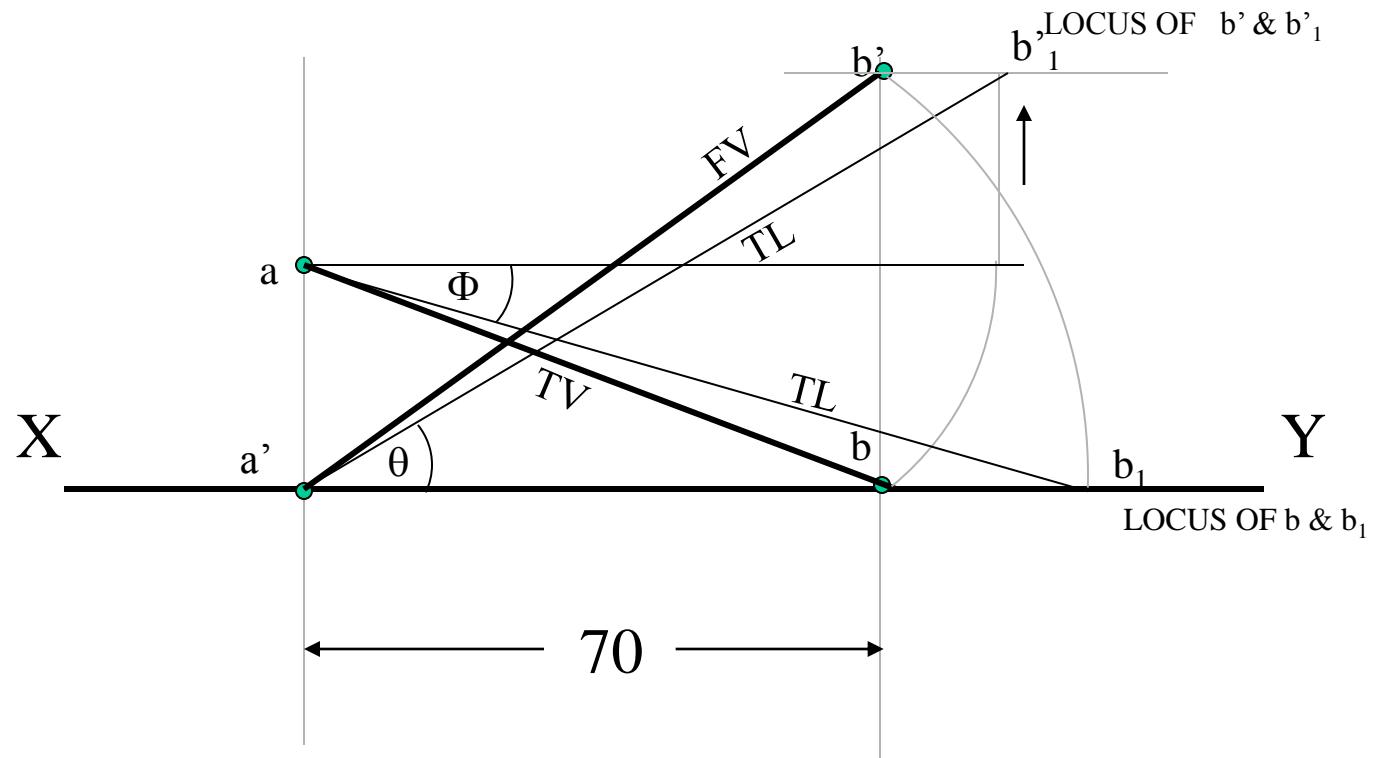
PROBLEM NO.25

End A of line AB is in Hp and 25 mm behind Vp.

End B in Vp. and 50mm above Hp.

Distance between projectors is 70mm.

Draw projections and find it's inclinations with Ht, Vt.



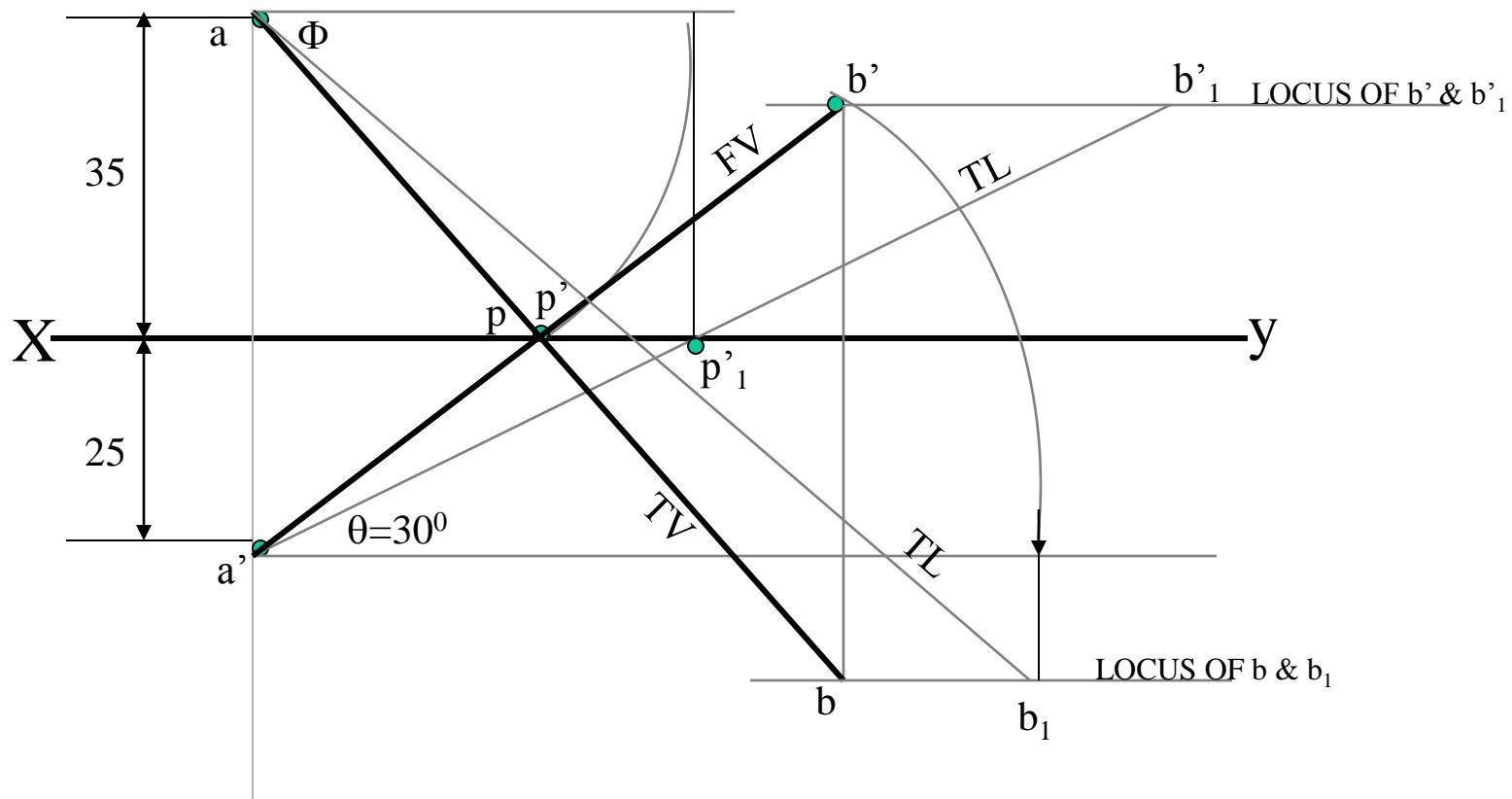
PROBLEM NO.26

End A of a line AB is 25mm below Hp and 35mm behind Vp.

Line is 30° inclined to Hp.

There is a point P on AB contained by both HP & VP.

Draw projections, find inclination with Vp and traces.



PROBLEM NO.27

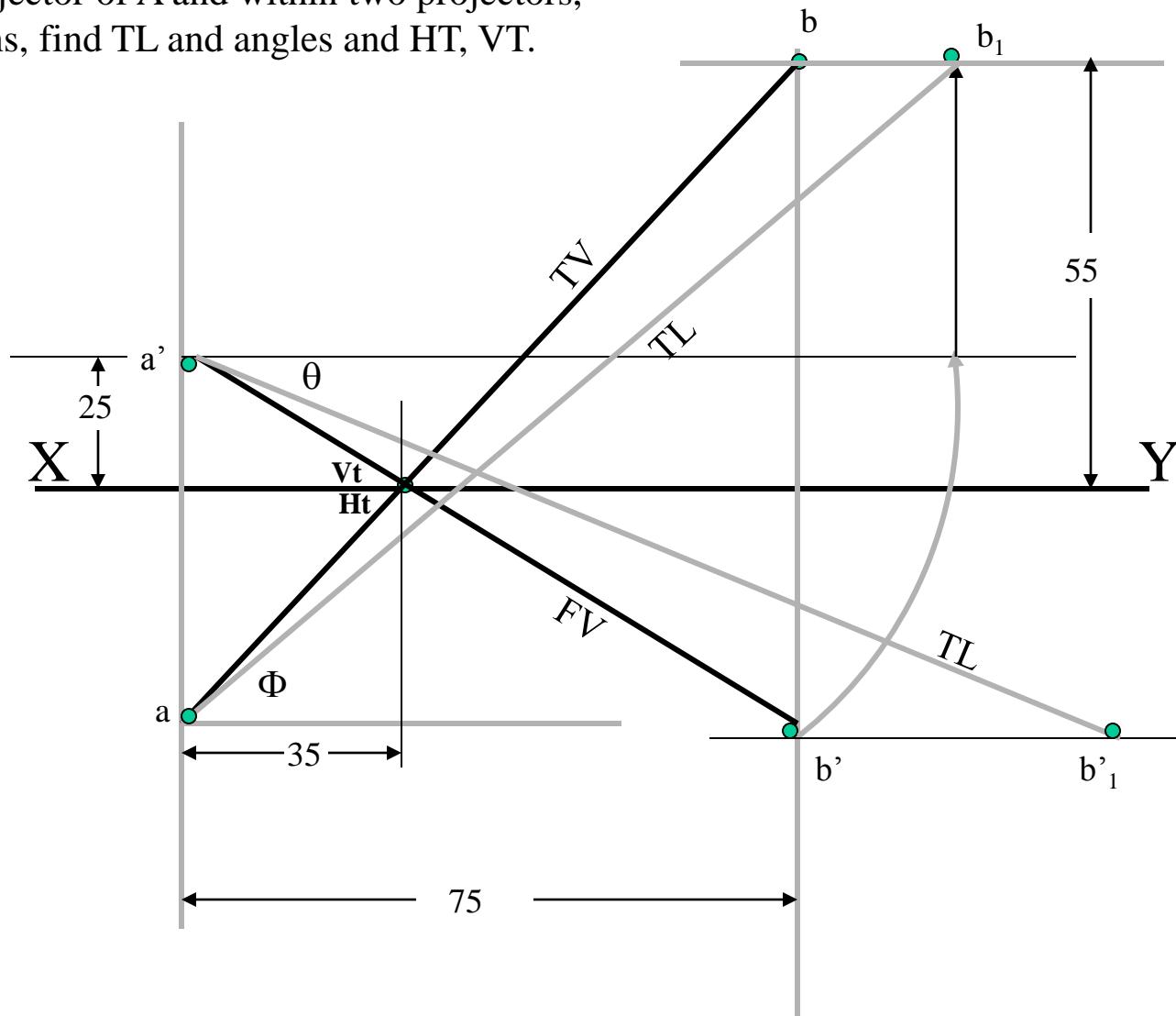
End A of a line AB is 25mm above Hp and end B is 55mm behind Vp.

The distance between end projectors is 75mm.

If both it's HT & VT coincide on xy in a point,

35mm from projector of A and within two projectors,

Draw projections, find TL and angles and HT, VT.



PROJECTIONS OF PLANES

In this topic various plane figures are the objects.

What is usually asked in the problem?

To draw their projections means F.V, T.V. & S.V.

What will be given in the problem?

1. Description of the plane figure.
2. It's position with HP and VP.

In which manner it's position with HP & VP will be described?

1. **Inclination of its SURFACE with one of the reference planes will be given.**
2. Inclination of one of its EDGES with other reference plane will be given
(Hence this will be a case of an object inclined to both reference Planes.)

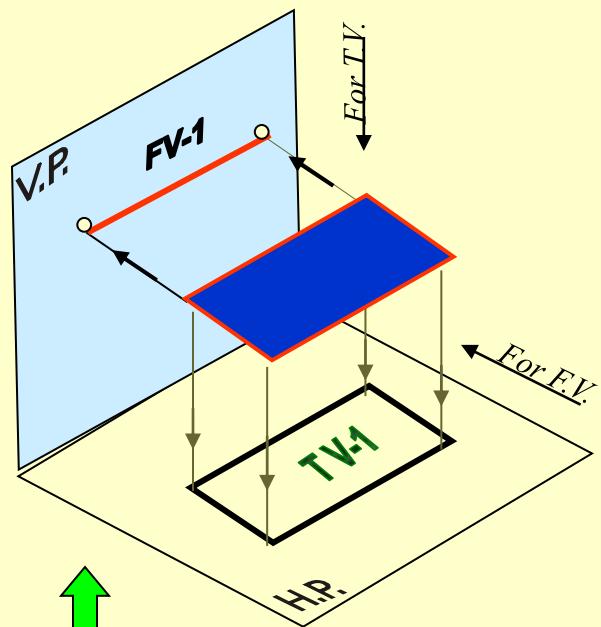
Study the illustration showing
surface & side inclination given on next page.



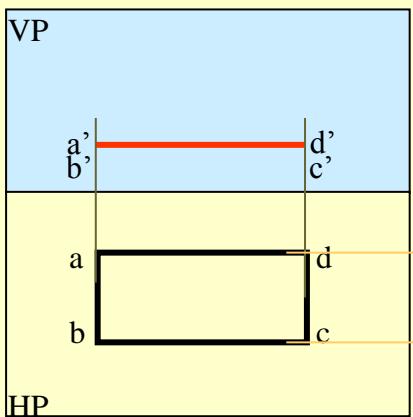
CASE OF A RECTANGLE – OBSERVE AND NOTE ALL STEPS.



SURFACE PARALLEL TO HP PICTORIAL PRESENTATION

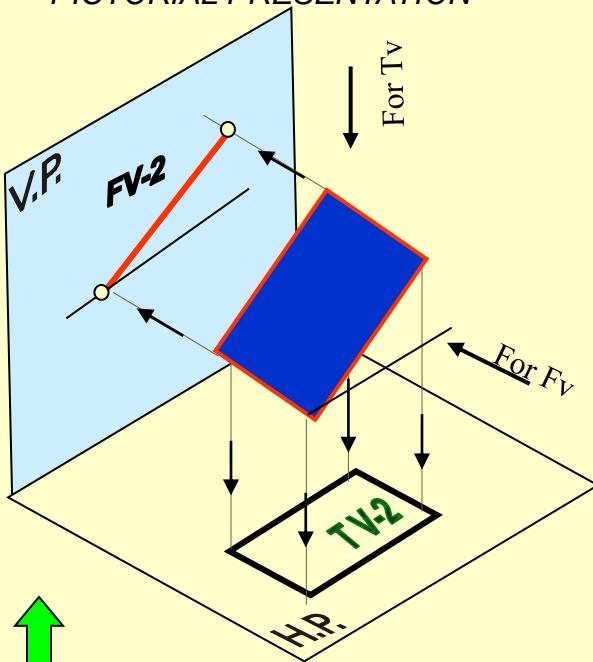


ORTHOGRAPHIC
TV-True Shape
FV- Line // to xy

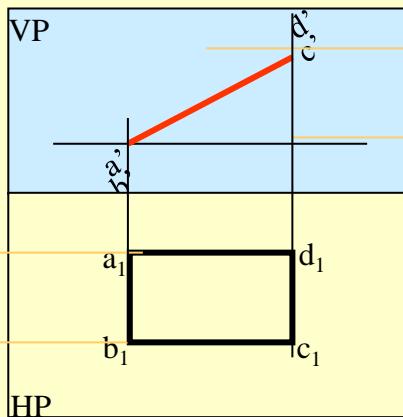


A

SURFACE INCLINED TO HP PICTORIAL PRESENTATION

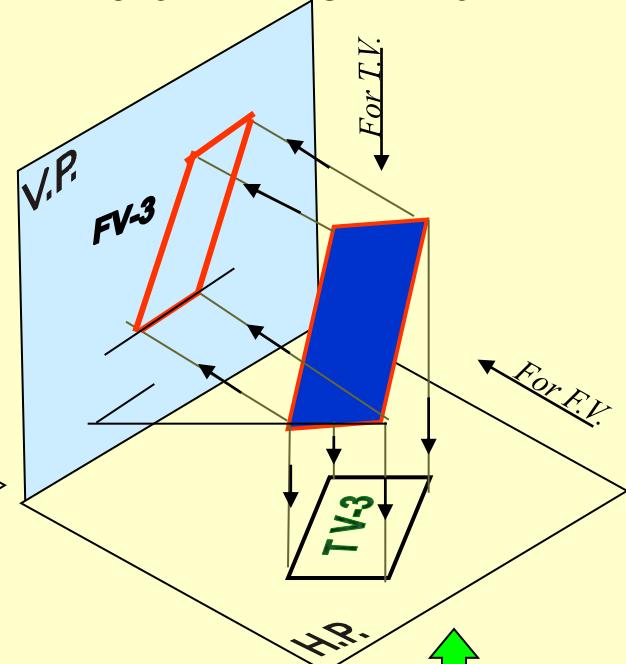


ORTHOGRAPHIC
FV- Inclined to XY
TV- Reduced Shape

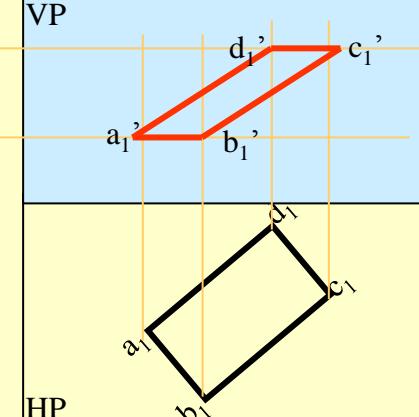


B

ONE SMALL SIDE INCLINED TO VP PICTORIAL PRESENTATION



ORTHOGRAPHIC
FV- Apparent Shape
TV- Previous Shape



C



PROCEDURE OF SOLVING THE PROBLEM:

IN THREE STEPS EACH PROBLEM CAN BE SOLVED: (As Shown In Previous Illustration)

STEP 1. Assume suitable conditions & draw Fv & Tv of initial position.

STEP 2. Now consider surface inclination & draw 2nd Fv & Tv.

STEP 3. After this, consider side/edge inclination and draw 3rd (final) Fv & Tv.

ASSUMPTIONS FOR INITIAL POSITION:

(Initial Position means assuming surface // to HP or VP)

1. If in problem surface is inclined to HP – assume it // HP

Or If surface is inclined to VP – assume it // to VP

2. Now if surface is assumed // to HP- It's TV will show True Shape.

And If surface is assumed // to VP – It's FV will show True Shape.

3. Hence begin with drawing TV or FV as True Shape.

4. While drawing this True Shape –

keep one side/edge (which is making inclination) perpendicular to xy line
(similar to pair no. A on previous page illustration).

A

Now Complete STEP 2. By making surface inclined to the resp plane & project it's other view.

(Ref. 2nd pair B on previous page illustration)

Now Complete STEP 3. By making side inclined to the resp plane & project it's other view.

(Ref. 3nd pair C on previous page illustration)

APPLY SAME STEPS TO SOLVE NEXT ELEVEN PROBLEMS

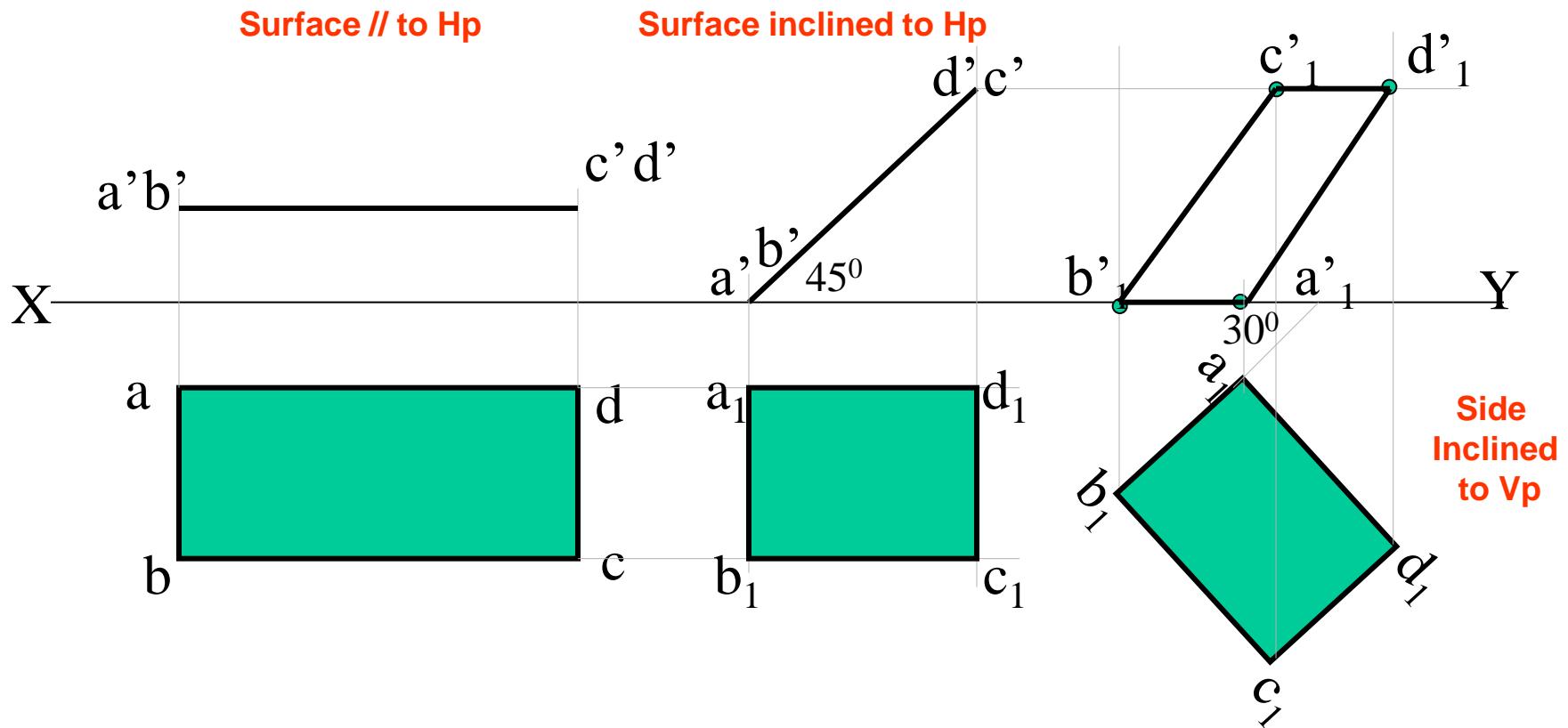
Problem 1:

Rectangle 30mm and 50mm sides is resting on HP on one small side which is 30^0 inclined to VP, while the surface of the plane makes 45^0 inclination with HP. Draw it's projections.

Read problem and answer following questions

1. Surface inclined to which plane? ----- HP
2. Assumption for initial position? -----// to HP
3. So which view will show True shape? --- TV
4. Which side will be vertical? ---One small side.

Hence begin with TV, draw rectangle below X-Y drawing one small side vertical.



Problem 2:

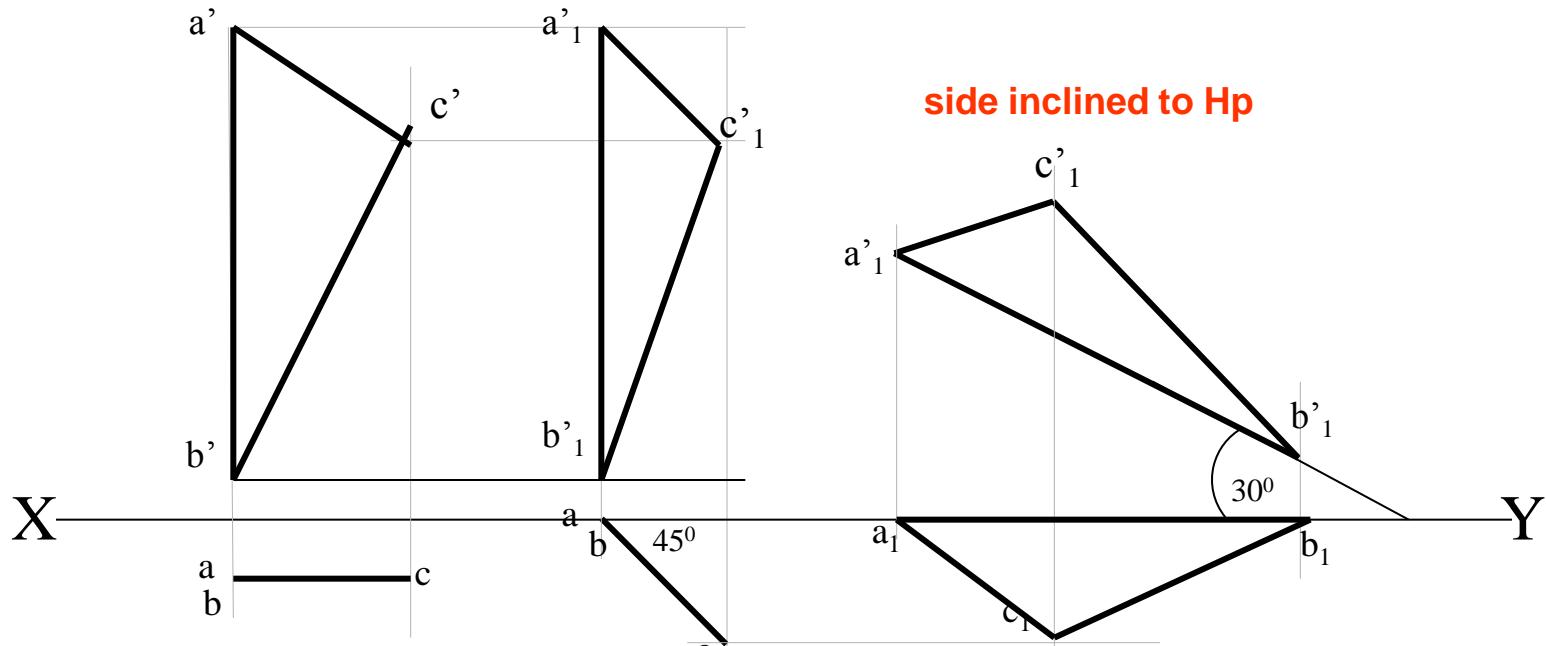
A $30^\circ - 60^\circ$ set square of longest side 100 mm long, is in VP and 30° inclined to HP while its surface is 45° inclined to VP. Draw its projections

(Surface & Side inclinations directly given)

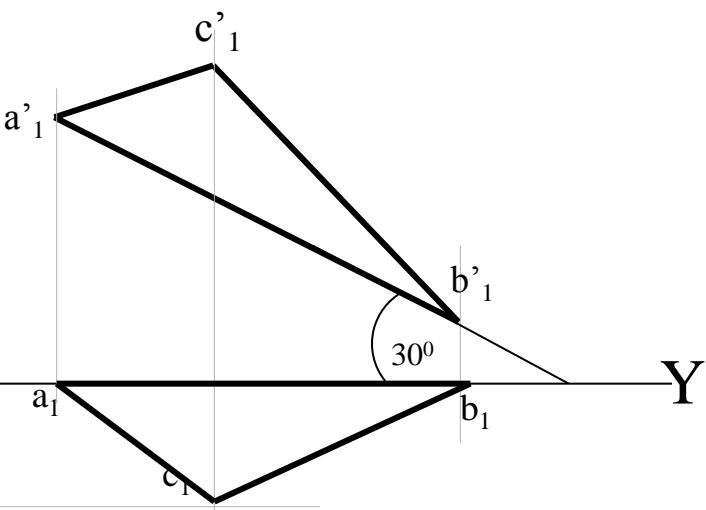
Read problem and answer following questions

- 1 . Surface inclined to which plane? ----- VP
2. Assumption for initial position? -----// to VP
3. So which view will show True shape? --- FV
4. Which side will be vertical? -----longest side.

Hence begin with FV, draw triangle above X-Y keeping longest side vertical.



side inclined to Hp



Surface // to Vp Surface inclined to Vp

Problem 3:

A $30^\circ - 60^\circ$ set square of longest side 100 mm long is in VP and its surface 45° inclined to VP. One end of longest side is 10 mm and other end is 35 mm above HP. Draw its projections

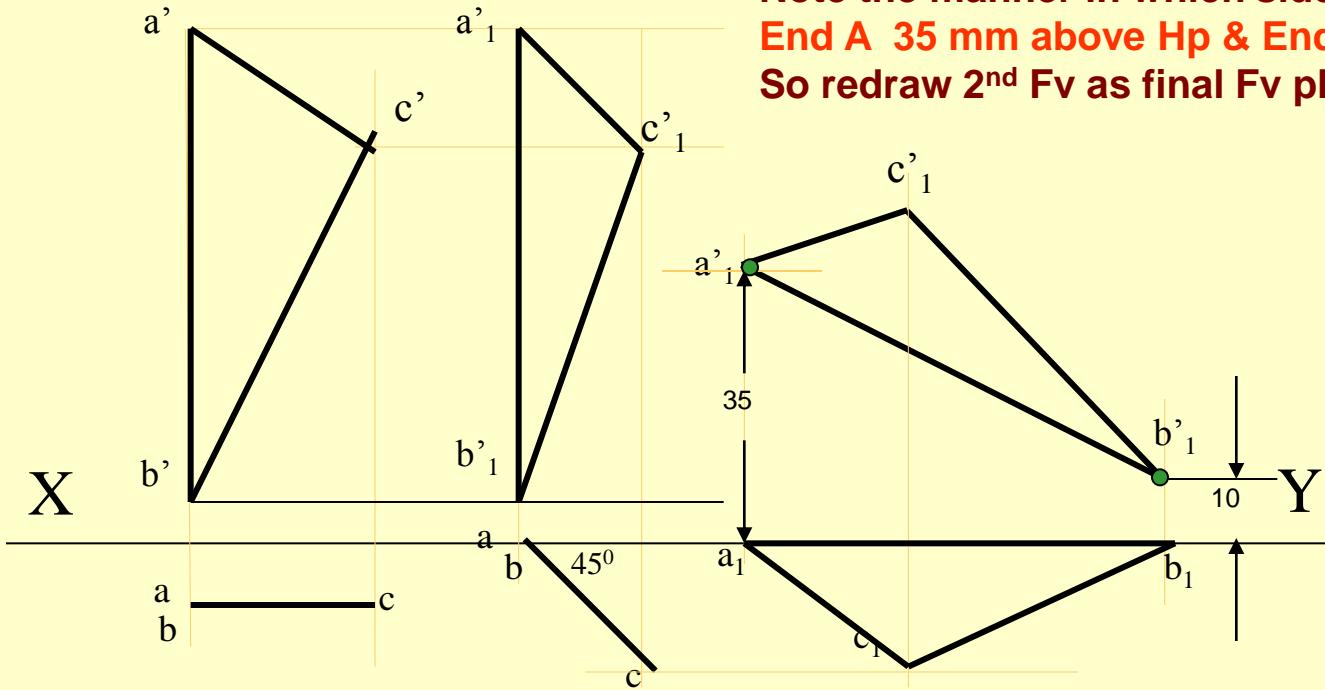
(Surface inclination directly given.
Side inclination indirectly given)

Read problem and answer following questions

- 1 . Surface inclined to which plane? ----- VP
2. Assumption for initial position? -----// to VP
3. So which view will show True shape? --- FV
4. Which side will be vertical? -----longest side.

Hence begin with FV, draw triangle above X-Y
keeping longest side vertical.

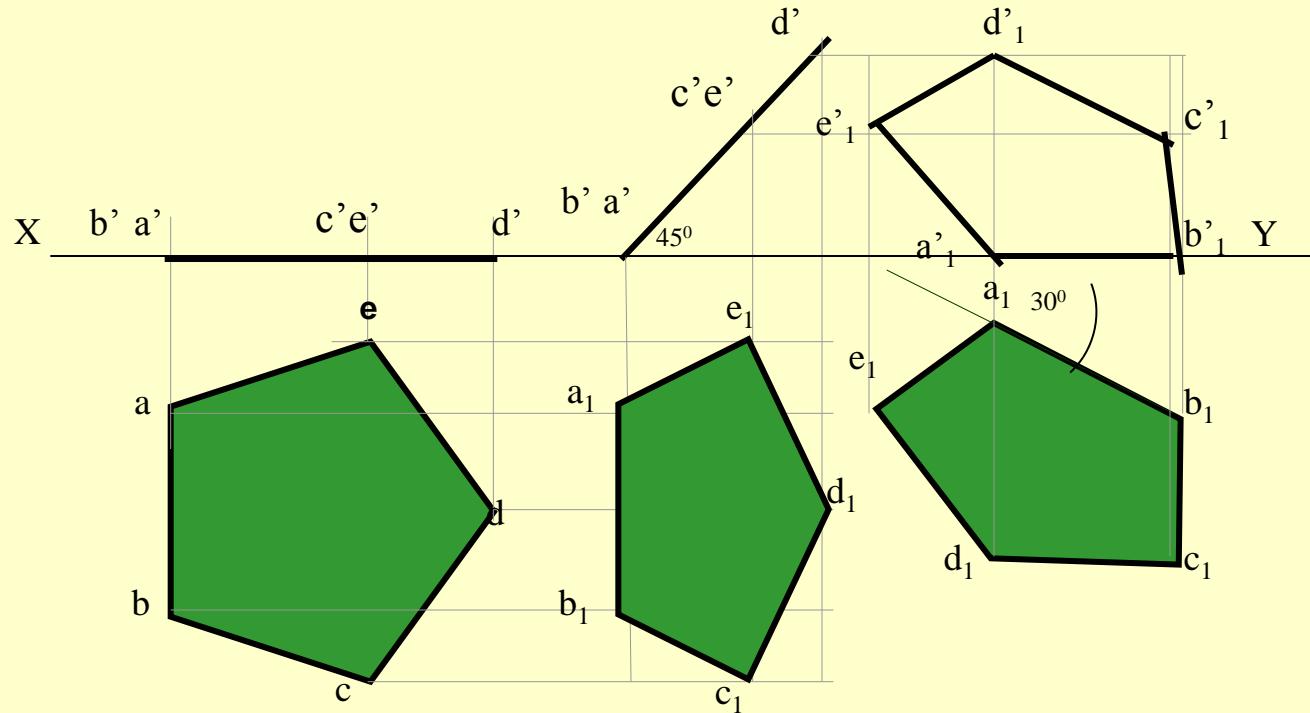
First TWO steps are similar to previous problem.
Note the manner in which side inclination is given.
End A 35 mm above Hp & End B is 10 mm above Hp.
So redraw 2nd Fv as final Fv placing these ends as said.



Problem 4:

A regular pentagon of 30 mm sides is resting on HP on one of its sides with its surface 45^0 inclined to HP.
Draw its projections when the side in HP makes 30^0 angle with VP

**SURFACE AND SIDE INCLINATIONS
ARE DIRECTLY GIVEN.**



Read problem and answer following questions

1. Surface inclined to which plane? ----- **HP**
2. Assumption for initial position? ----- // to **HP**
3. So which view will show True shape? --- **TV**
4. Which side will be vertical? ----- **any side.**

Hence begin with TV, draw pentagon below

X-Y line, taking one side vertical.

Problem 5:

A regular pentagon of 30 mm sides is resting on HP on one of its sides while its opposite vertex (corner) is 30 mm above HP.

Draw projections when side in HP is 30° inclined to VP.

SURFACE INCLINATION INDIRECTLY GIVEN SIDE INCLINATION DIRECTLY GIVEN:

ONLY CHANGE is

the manner in which surface inclination is described:

One side on Hp & its opposite corner 30 mm above Hp.

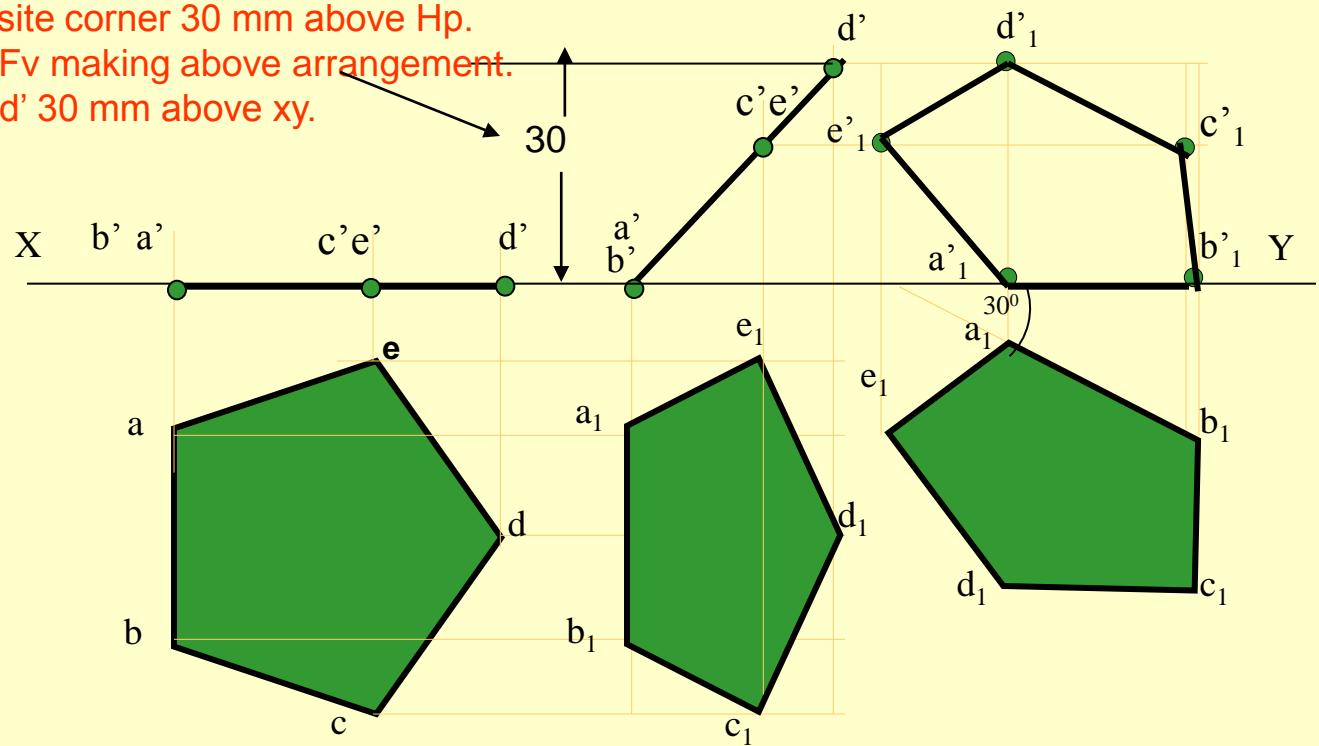
Hence redraw 1st Fv as a 2nd Fv making above arrangement.

Keep a'b' on xy & d' 30 mm above xy.

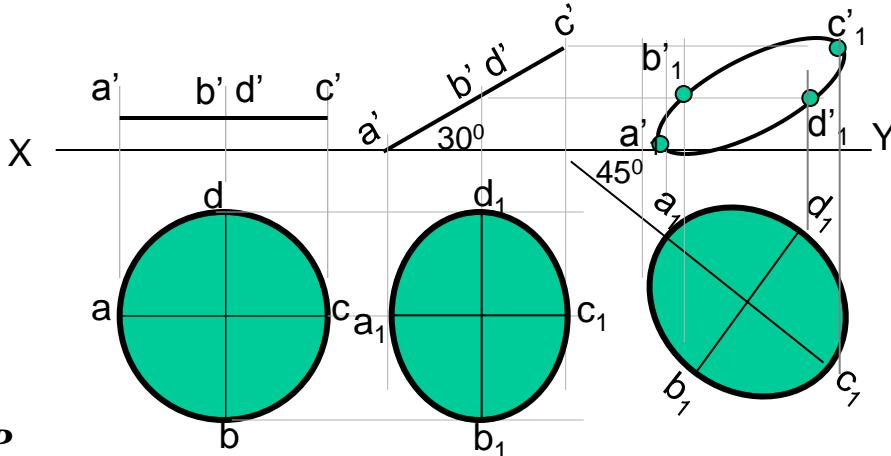
Read problem and answer following questions

1. Surface inclined to which plane? ----- **HP**
2. Assumption for initial position? ----- // to **HP**
3. So which view will show True shape? --- **TV**
4. Which side will be vertical? ----- **any side.**

Hence begin with TV, draw pentagon below X-Y line, taking one side vertical.



Problem 8: A circle of 50 mm diameter is resting on Hp on end A of it's diameter AC which is 30° inclined to Hp while it's Tv is 45° inclined to Vp. Draw it's projections.



Read problem and answer following questions

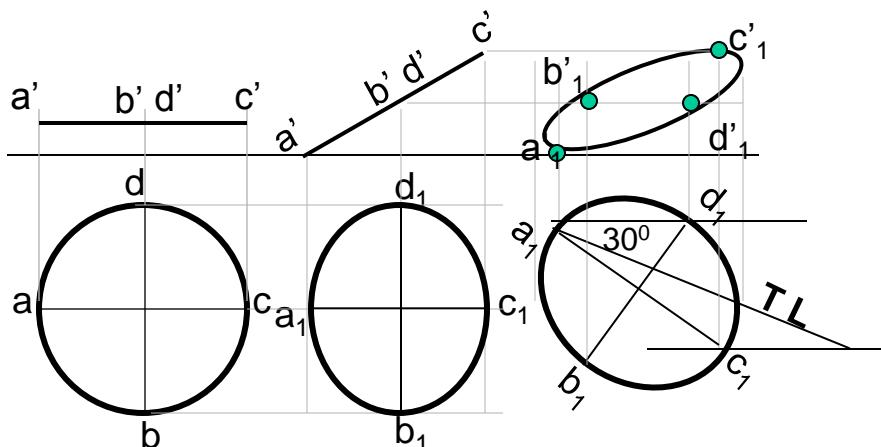
1. Surface inclined to which plane? ----- **HP**
2. Assumption for initial position? ----- // to **HP**
3. So which view will show True shape? --- **TV**
4. Which diameter horizontal? ----- **AC**

Hence begin with TV, draw rhombus below X-Y line, taking longer diagonal // to X-Y

Problem 9: A circle of 50 mm diameter is resting on Hp on end A of it's diameter AC which is 30° inclined to Hp while it makes 45° inclined to Vp. Draw it's projections.

Note the difference in construction of 3rd step in both solutions.

The difference in these two problems is in step 3 only.
In problem no.8 inclination of Tv of that AC is given, It could be drawn directly as shown in 3rd step.
While in no.9 angle of AC itself i.e. it's TL, is given. Hence here angle of TL is taken, locus of c₁ is drawn and then LTV i.e. a₁, c₁ is marked and final TV was completed. Study illustration carefully.



Problem 10: End A of diameter AB of a circle is in HP and end B is in VP. Diameter AB, 50 mm long is 30° & 60° inclined to HP & VP respectively. Draw projections of circle.

- Read problem and answer following questions
1. Surface inclined to which plane? ----- **HP**
 2. Assumption for initial position? ----- // to **HP**
 3. So which view will show True shape? --- **TV**
 4. Which diameter horizontal? ----- **AB**

Hence begin with TV, draw CIRCLE below X-Y line, taking DIA. AB // to X-Y

The problem is similar to previous problem of circle – no.9.

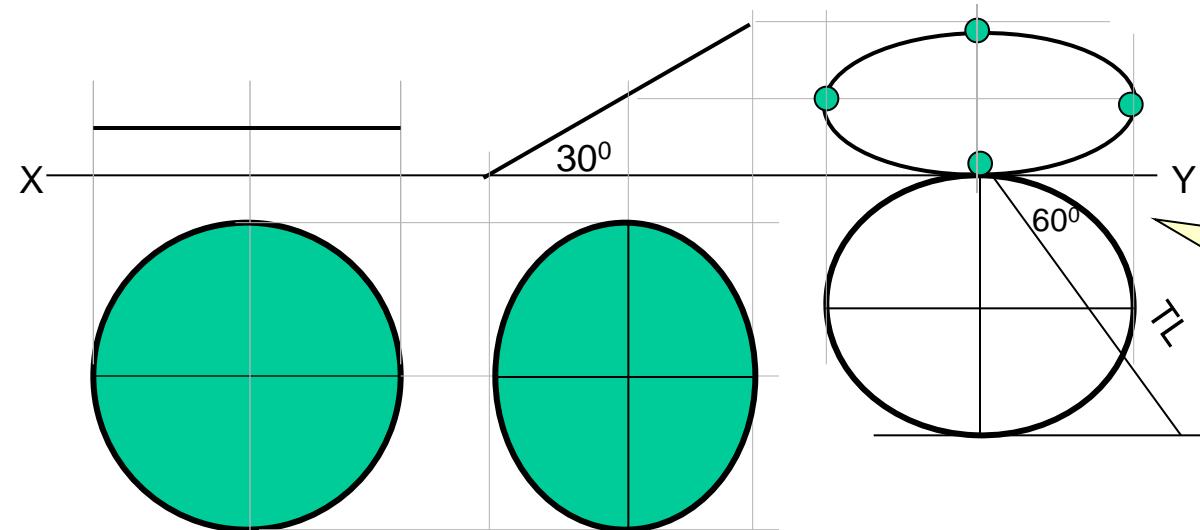
But in the 3rd step there is one more change.

Like 9th problem True Length inclination of dia. AB is definitely expected but if you carefully note - the the SUM of its inclinations with HP & VP is 90° .

Means Line AB lies in a Profile Plane.

Hence it's both Tv & Fv must arrive on one single projector.

So do the construction accordingly AND **note the case carefully..**



SOLVE SEPARATELY
ON DRAWING SHEET
GIVING NAMES TO VARIOUS
POINTS AS USUAL,
AS THE CASE IS IMPORTANT

Problem 11:

A hexagonal lamina has its one side in HP and Its apposite parallel side is 25mm above Hp and In Vp. Draw it's projections.

Take side of hexagon 30 mm long.

Read problem and answer following questions

1. Surface inclined to which plane? ----- **HP**
2. Assumption for initial position? ----- // to **HP**
3. So which view will show True shape? --- **TV**
4. Which diameter horizontal? ----- **AC**

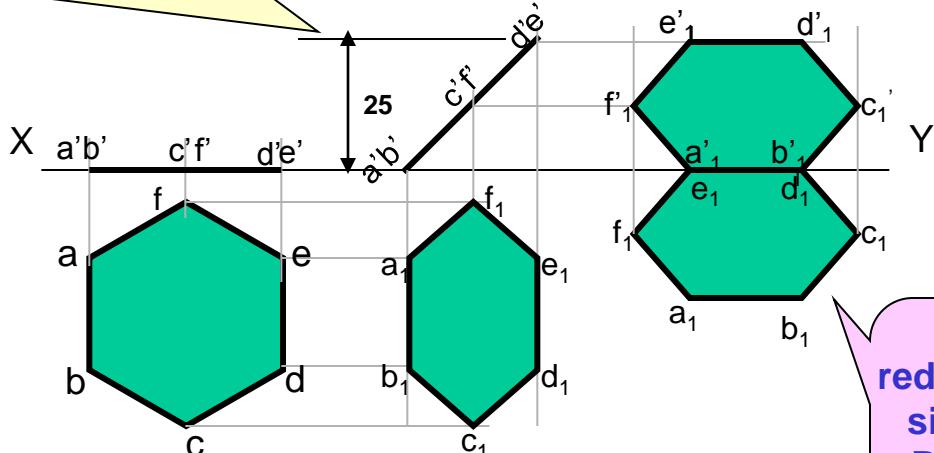
Hence begin with TV, draw rhombus below X-Y line, taking longer diagonal // to X-Y

ONLY CHANGE is the manner in which surface inclination is described:

One side on Hp & its opposite side 25 mm above Hp.

Hence redraw 1st Fv as a 2nd Fv making above arrangement.

Keep a'b' on xy & d'e' 25 mm above xy.



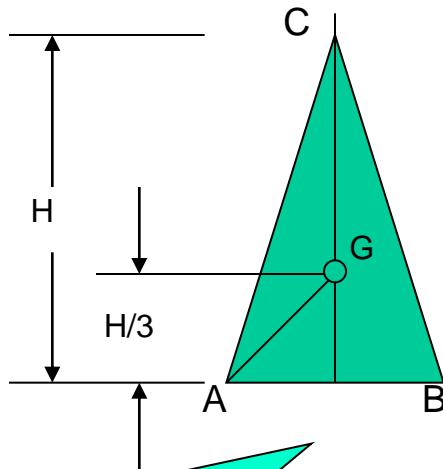
As 3rd step
redraw 2nd Tv keeping
side DE on xy line.
Because it is in VP
as said in problem.

FREELY SUSPENDED CASES.

IMPORTANT POINTS

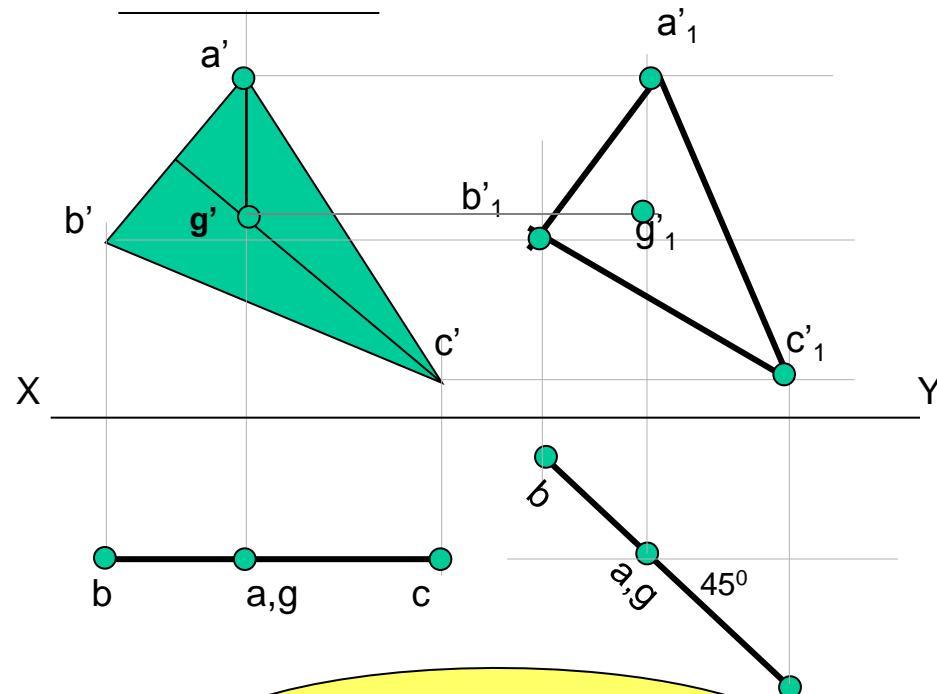
Problem 12:

An isosceles triangle of 40 mm long base side, 60 mm long altitude is freely suspended from one corner of Base side. Its plane is 45° inclined to Vp. Draw its projections.



First draw a given triangle
With given dimensions,
Locate its centroid position
And
join it with point of suspension.

1. In this case the plane of the figure always remains *perpendicular to Hp*.
2. It may remain parallel or inclined to Vp.
3. Hence **TV** in this case will be always a **LINE view**.
4. Assuming surface // to Vp, draw true shape in suspended position as FV.
(Here keep *line joining point of contact & centroid of fig. vertical*)
5. Always begin with FV as a True Shape but in a suspended position.
AS shown in 1st FV.



Similarly solve next problem
of Semi-circle

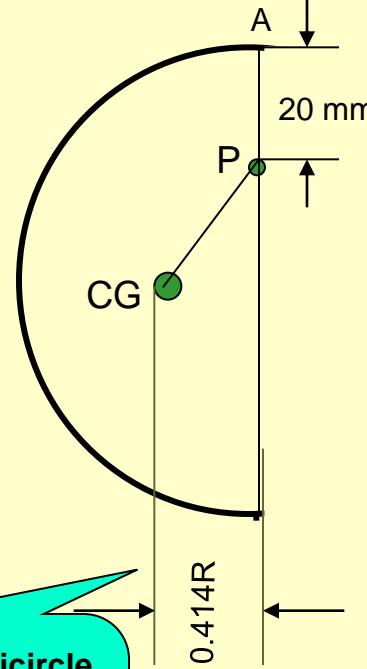
IMPORTANT POINTS



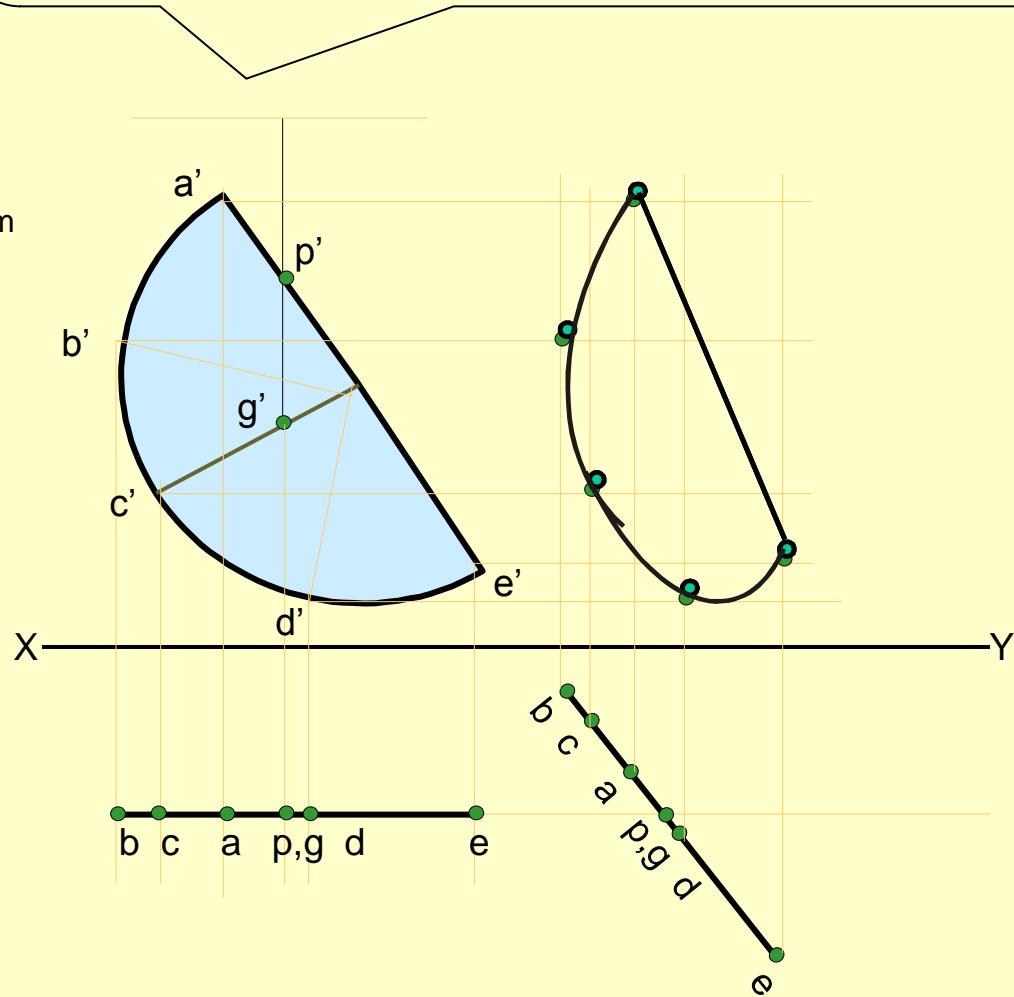
Problem 13

A semicircle of 100 mm diameter is suspended from a point on its straight edge 30 mm from the midpoint of that edge so that the surface makes an angle of 45° with VP. Draw its projections.

1. In this case the plane of the figure always remains ***perpendicular to Hp.***
2. It may remain parallel or inclined to Vp.
3. Hence **TV** in this case will be always a ***LINE view.***
4. Assuming surface // to Vp, draw true shape in suspended position as FV.
(Here keep ***line joining point of contact & centroid of fig. vertical***)
5. Always begin with FV as a True Shape but in a suspended position.
AS shown in 1st FV.



First draw a given semicircle
With given diameter,
Locate it's centroid position
And
join it with point of suspension.



To determine true shape of plane figure when it's projections are given. BY USING AUXILIARY PLANE METHOD

WHAT WILL BE THE PROBLEM?

Description of final Fv & Tv will be given.

You are supposed to determine true shape of that plane figure.

Follow the below given steps:

1. Draw the given Fv & Tv as per the given information in problem.
2. Then among all lines of Fv & Tv select a line showing True Length (T.L.)
(It's other view must be // to xy)
3. Draw x_1-y_1 perpendicular to this line showing T.L.
4. Project view on x_1-y_1 (it must be a line view)
5. Draw x_2-y_2 // to this line view & project new view on it.

It will be the required answer i.e. True Shape.

The facts you must know:-

If you carefully study and observe the solutions of all previous problems,
You will find

**IF ONE VIEW IS A LINE VIEW & THAT TOO PARALLEL TO XY LINE,
THEN AND THEN IT'S OTHER VIEW WILL SHOW TRUE SHAPE:**

NOW FINAL VIEWS ARE ALWAYS SOME SHAPE, NOT LINE VIEWS:

SO APPLYING ABOVE METHOD:

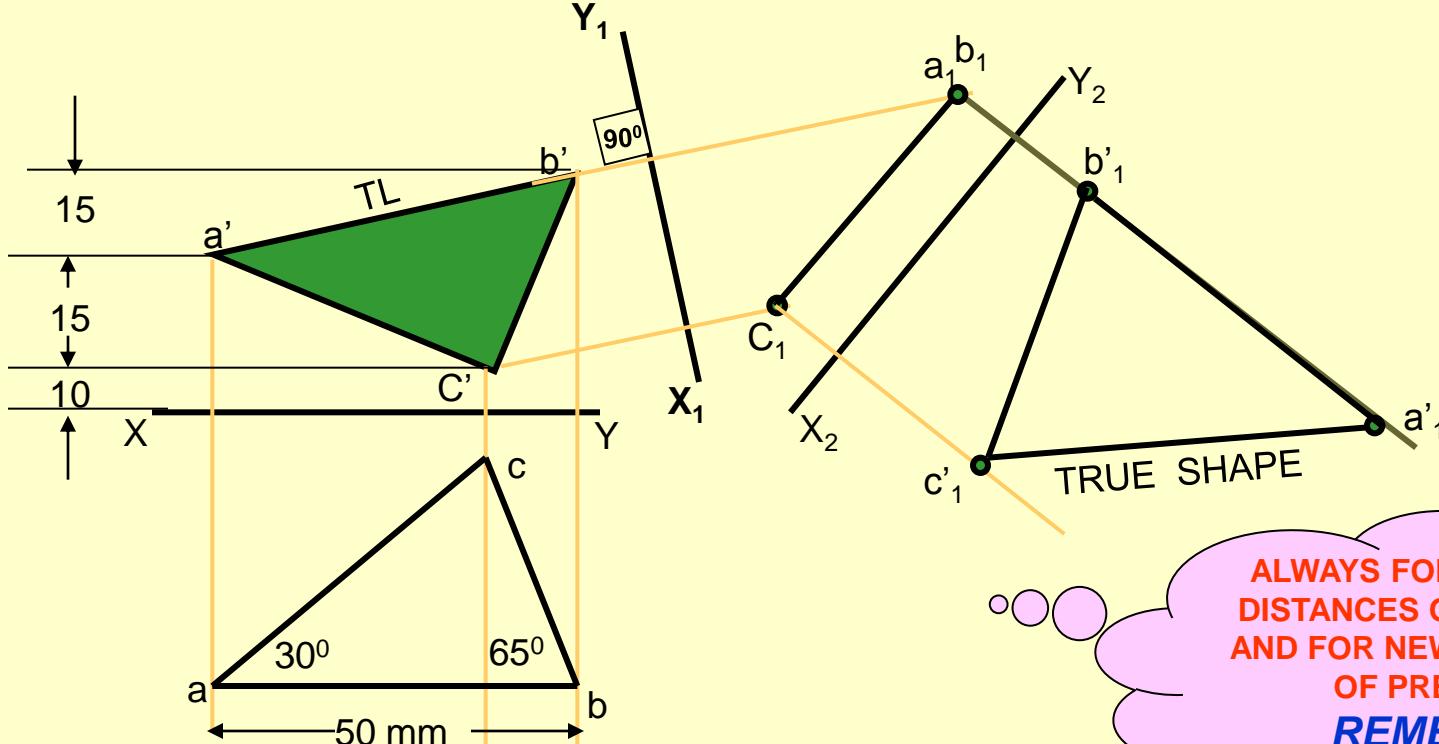
WE FIRST CONVERT ONE VIEW IN INCLINED LINE VIEW .(By using x_1y_1 aux.plane)
THEN BY MAKING IT // TO X_2-Y_2 WE GET TRUE SHAPE.

**Study Next
Four Cases**

Problem 14 Tv is a triangle abc. Ab is 50 mm long, angle cab is 30° and angle cba is 65°. a'b'c' is a Fv. a' is 25 mm, b' is 40 mm and c' is 10 mm above Hp respectively. Draw projections of that figure and find its true shape.

As per the procedure-

1. First draw Fv & Tv as per the data.
2. In Tv line ab is // to xy hence it's other view a'b' is TL. So draw x_1y_1 perpendicular to it.
3. Project view on x_1y_1 .
 - a) First draw projectors from a'b' & c' on x_1y_1 .
 - b) from xy take distances of a,b & c (Tv) mark on these projectors from x_1y_1 . Name points a₁b₁ & c₁.
 - c) This line view is an Aux.Tv. Draw x_2y_2 // to this line view and project Aux. Fv on it.
for that from x_1y_1 take distances of a'b' & c' and mark from x_2y_2 on new projectors.
4. Name points a'₁, b'₁ & c'₁ and join them. This will be the required true shape.



ALWAYS FOR NEW FV TAKE
DISTANCES OF PREVIOUS FV
AND FOR NEW TV, DISTANCES
OF PREVIOUS TV
REMEMBER!!

Problem 15: Fv & Tv of a triangular plate are shown.

Determine its true shape.

USE SAME PROCEDURE STEPS
OF PREVIOUS PROBLEM:

BUT THERE IS ONE DIFFICULTY:

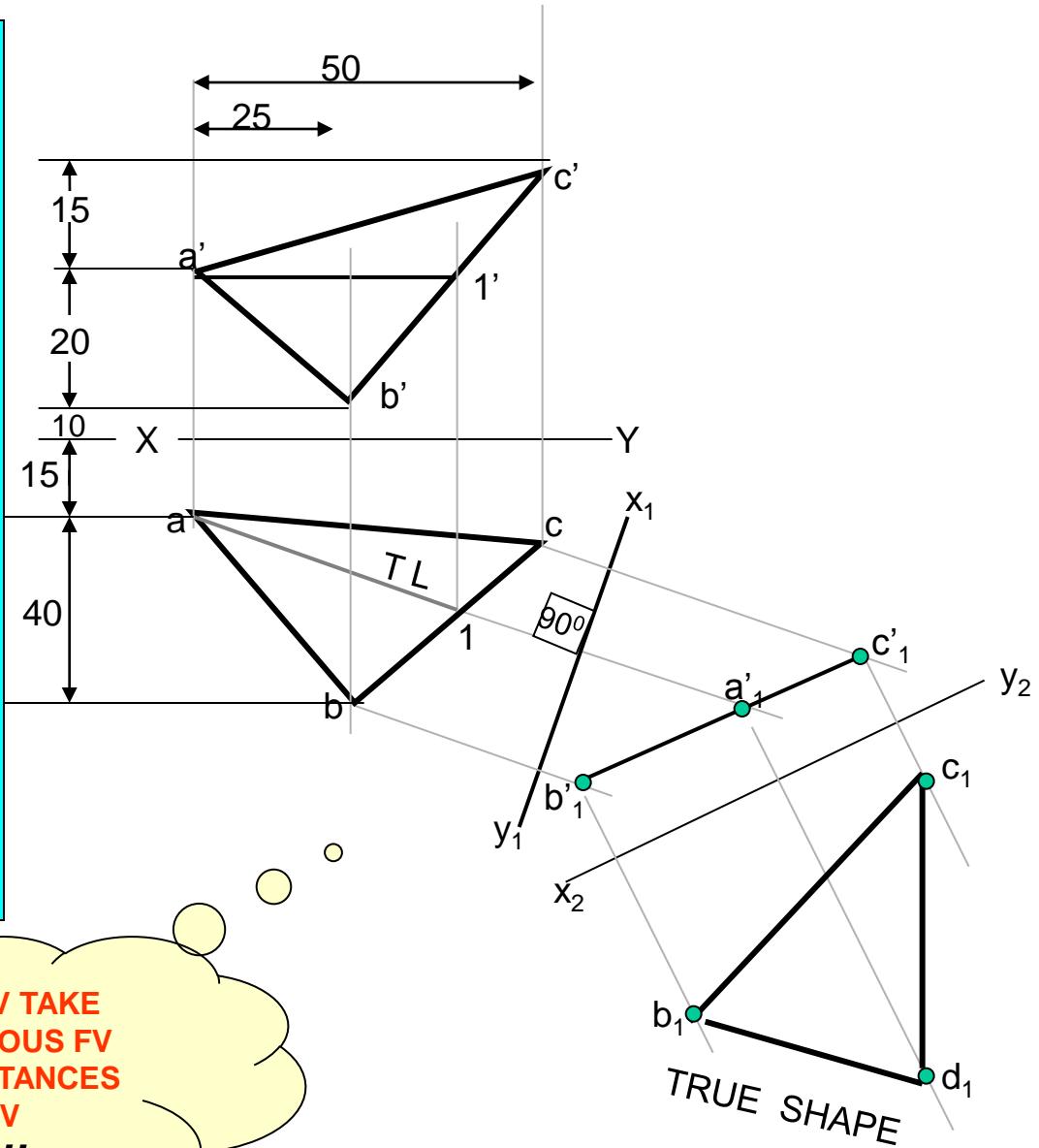
NO LINE IS // TO XY IN ANY VIEW.
MEANS NO TL IS AVAILABLE.

IN SUCH CASES DRAW ONE LINE
// TO XY IN ANY VIEW & IT'S OTHER
VIEW CAN BE CONSIDERED AS TL
FOR THE PURPOSE.

HERE $a' 1'$ line in Fv is drawn // to xy.
HENCE it's Tv $a-1$ becomes TL.

THEN FOLLOW SAME STEPS AND
DETERMINE TRUE SHAPE.
(STUDY THE ILLUSTRATION)

ALWAYS FOR NEW FV TAKE
DISTANCES OF PREVIOUS FV
AND FOR NEW TV, DISTANCES
OF PREVIOUS TV
REMEMBER!!



PROBLEM 16: Fv & Tv both are circles of 50 mm diameter. Determine true shape of an elliptical plate.

ADOPT SAME PROCEDURE.

a'c' is considered as line // to xy.

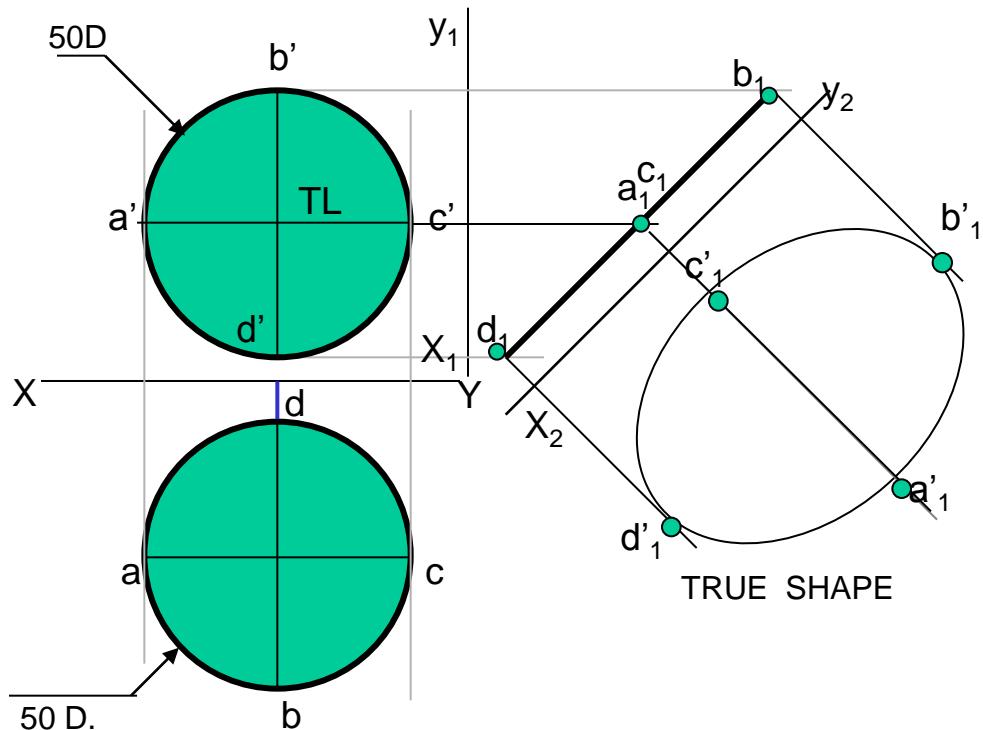
Then a'c' becomes TL for the purpose.

Using steps properly true shape can be
Easily determined.

Study the illustration.

**ALWAYS, FOR NEW FV
TAKE DISTANCES OF
PREVIOUS FV AND
FOR NEW TV, DISTANCES
OF PREVIOUS TV**

REMEMBER!!



Problem 17 : Draw a regular pentagon of 30 mm sides with one side 30° inclined to xy. This figure is Tv of some plane whose Fv is A line 45° inclined to xy. Determine it's true shape.

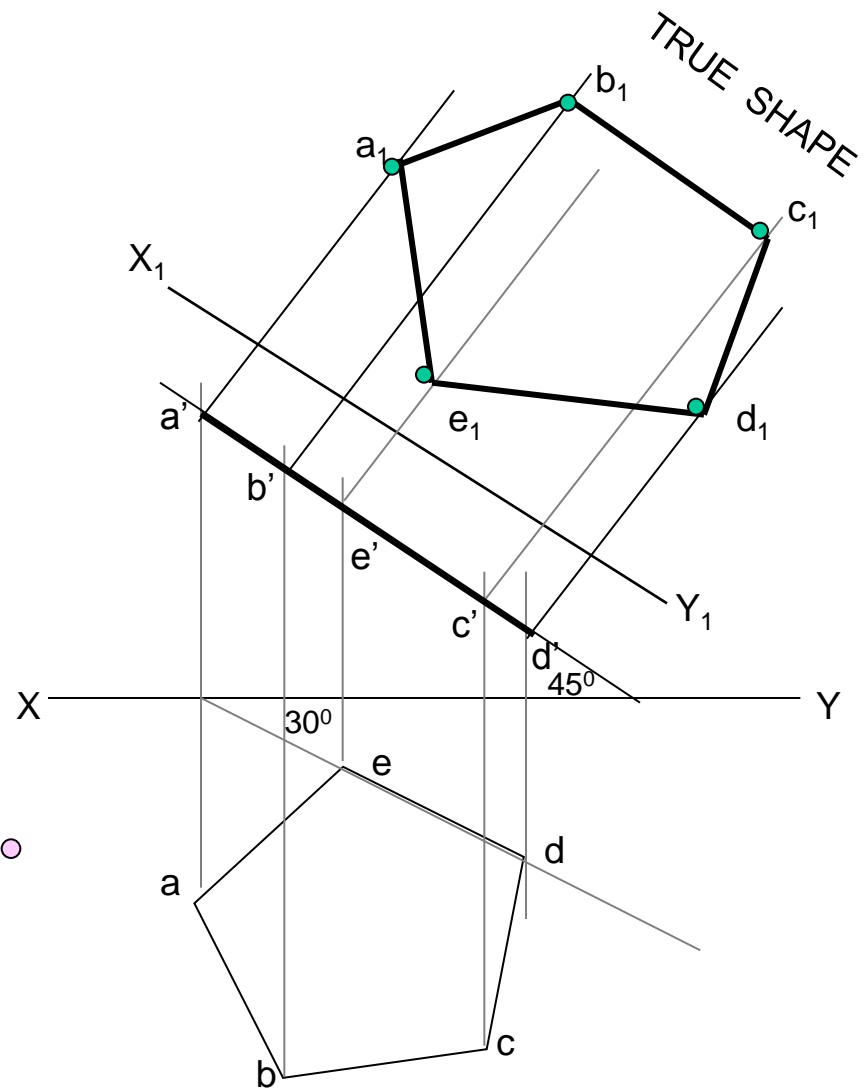
IN THIS CASE ALSO TRUE LENGTH IS NOT AVAILABLE IN ANY VIEW.

BUT ACTUALLY WE DONOT REQUIRE TL TO FIND IT'S TRUE SHAPE, AS ONE VIEW (FV) IS ALREADY A LINE VIEW. SO JUST BY DRAWING X₁Y₁ // TO THIS VIEW WE CAN PROJECT VIEW ON IT AND GET TRUE SHAPE:

STUDY THE ILLUSTRATION..

ALWAYS FOR NEW FV
TAKE DISTANCES OF
PREVIOUS FV AND FOR
NEW TV, DISTANCES OF
PREVIOUS TV

REMEMBER!!



SOLIDS

To understand and remember various solids in this subject properly, those are classified & arranged in to two major groups.

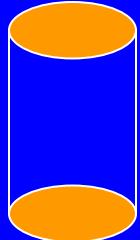
Group A

Solids having top and base of same shape

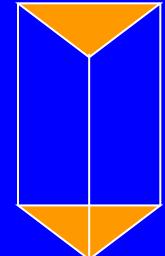
Group B

Solids having base of some shape and just a point as a top, called apex.

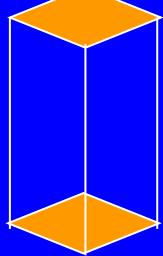
Cylinder



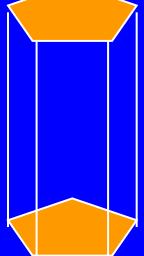
Prisms



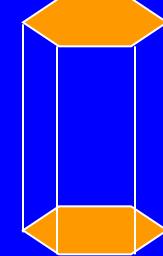
Triangular



Square



Pentagonal

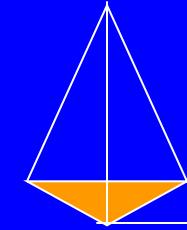


Hexagonal

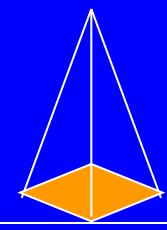
Cone



Pyramids



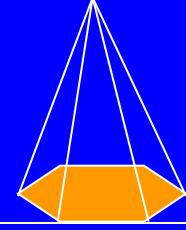
Triangular



Square



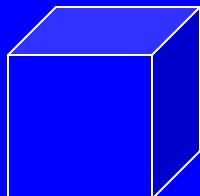
Pentagonal



Hexagonal

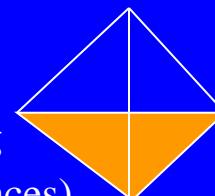
Cube

(A solid having six square faces)



Tetrahedron

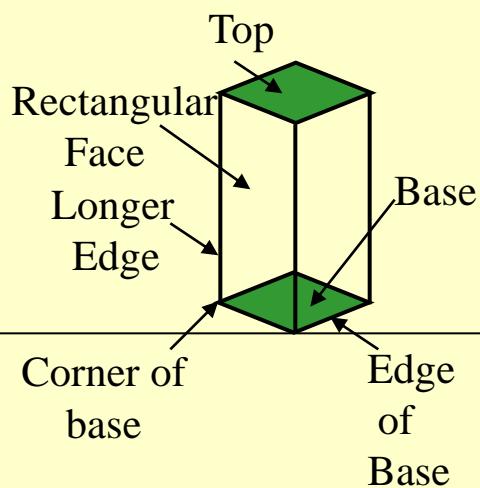
(A solid having Four triangular faces)



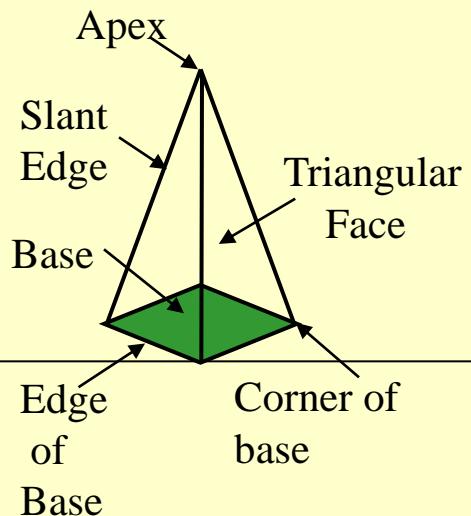
SOLIDS

Dimensional parameters of different solids.

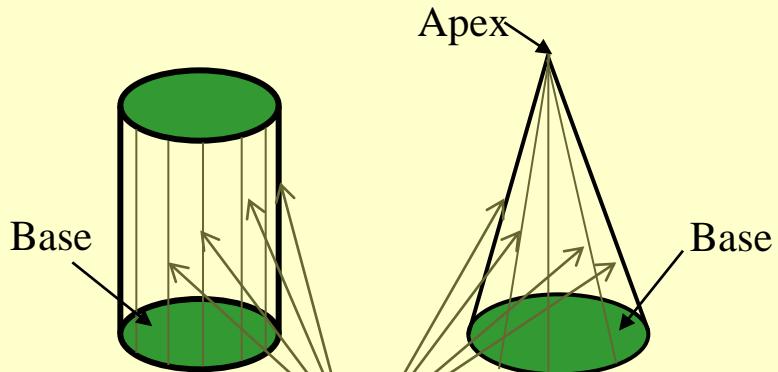
Square Prism



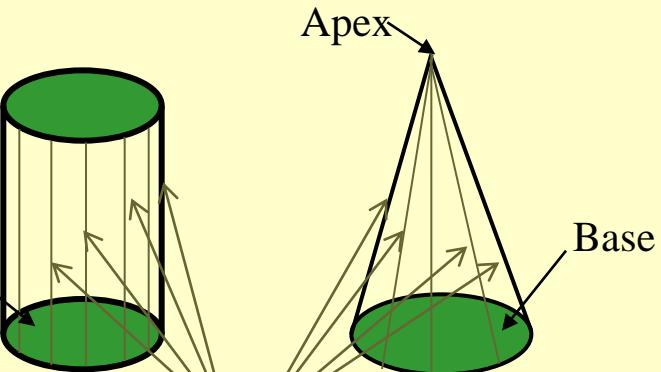
Square Pyramid



Cylinder

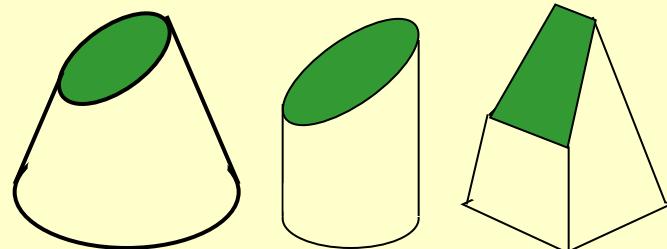


Cone

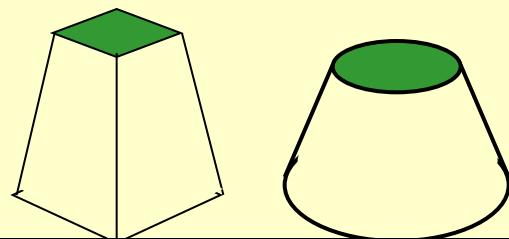


Generators

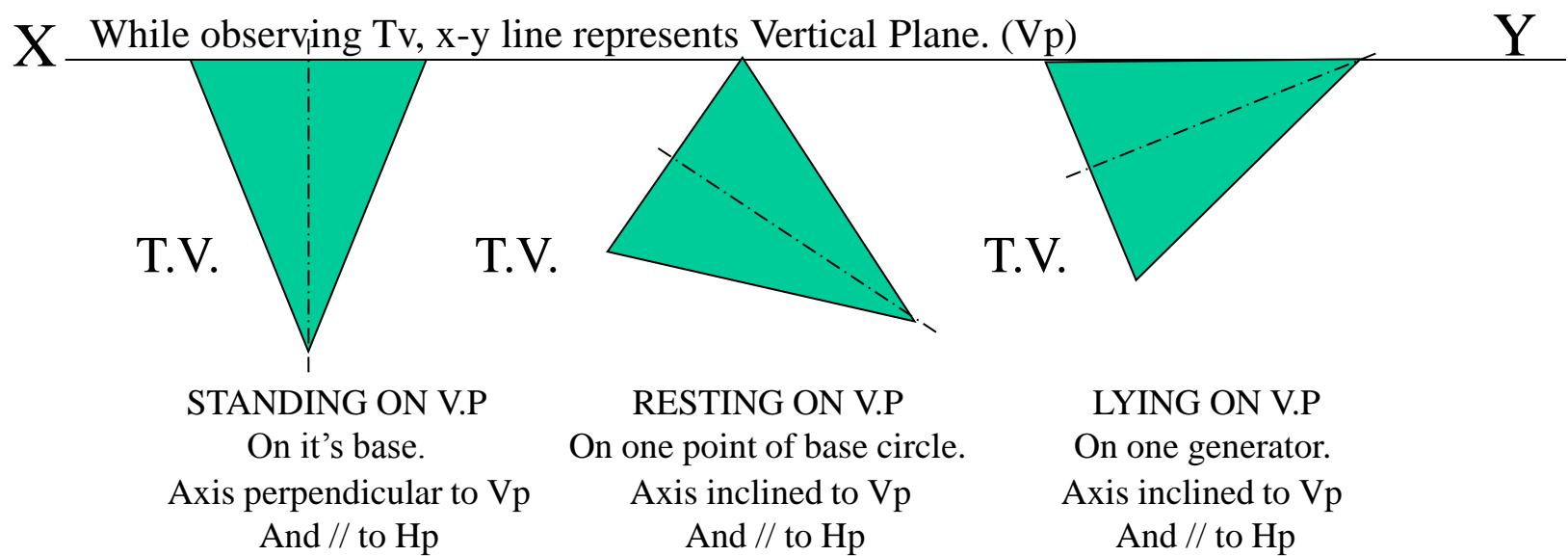
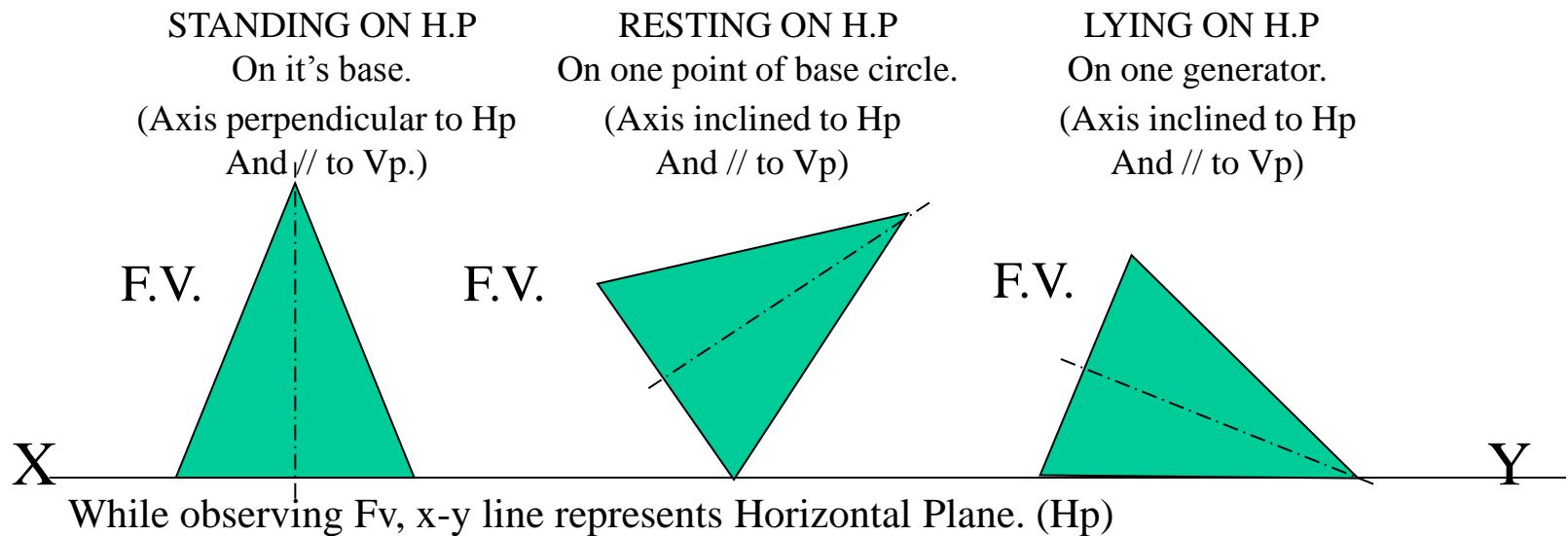
*Imaginary lines
generating curved surface
of cylinder & cone.*



Sections of solids(top & base not parallel)



Frustum of cone & pyramids.
(top & base parallel to each other)



STEPS TO SOLVE PROBLEMS IN SOLIDS

Problem is solved in three steps:

STEP 1: ASSUME SOLID STANDING ON THE PLANE WITH WHICH IT IS MAKING INCLINATION.

(IF IT IS INCLINED TO HP, ASSUME IT STANDING ON HP)

(IF IT IS INCLINED TO VP, ASSUME IT STANDING ON VP)

IF STANDING ON HP - IT'S TV WILL BE TRUE SHAPE OF IT'S BASE OR TOP;

IF STANDING ON VP - IT'S FV WILL BE TRUE SHAPE OF IT'S BASE OR TOP.

BEGIN WITH THIS VIEW:

IT'S OTHER VIEW WILL BE A RECTANGLE (IF SOLID IS **CYLINDER OR ONE OF THE PRISMS**):

IT'S OTHER VIEW WILL BE A TRIANGLE (IF SOLID IS **CONE OR ONE OF THE PYRAMIDS**):

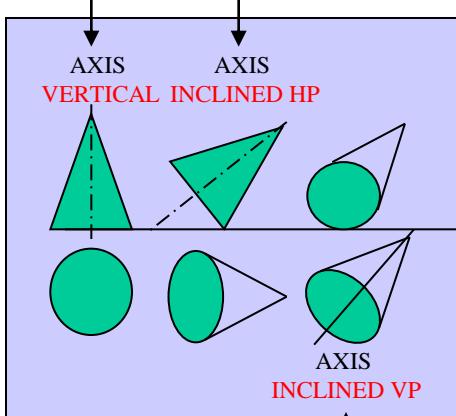
DRAW FV & TV OF THAT SOLID IN STANDING POSITION:

STEP 2: CONSIDERING SOLID'S INCLINATION (AXIS POSITION) DRAW IT'S FV & TV.

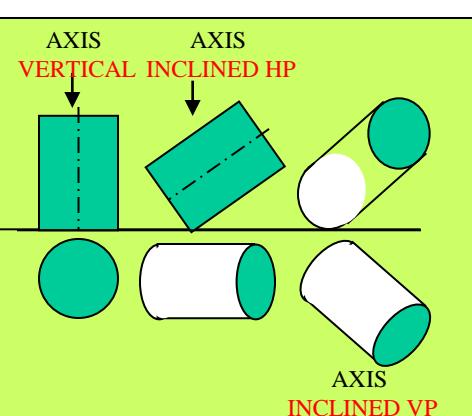
STEP 3: IN LAST STEP, CONSIDERING REMAINING INCLINATION, DRAW IT'S FINAL FV & TV.

GENERAL PATTERN (THREE STEPS) OF SOLUTION:

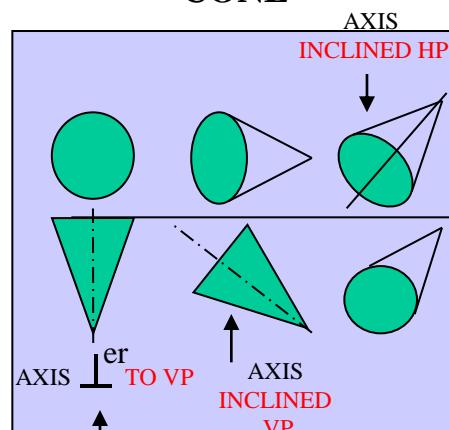
**GROUP B SOLID.
CONE**



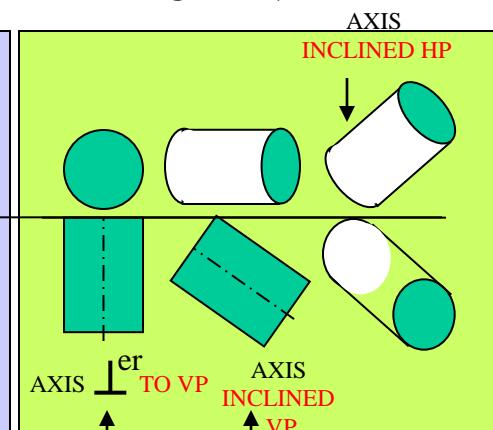
**GROUP A SOLID.
CYLINDER**



**GROUP B SOLID.
CONE**



**GROUP A SOLID.
CYLINDER**



Three steps

If solid is inclined to Hp

Three steps

If solid is inclined to Hp

Three steps

If solid is inclined to Vp

Three steps

If solid is inclined to Vp

Study Next Twelve Problems and Practice them separately !!

CATEGORIES OF ILLUSTRATED PROBLEMS!

PROBLEM NO.1, 2, 3, 4

GENERAL CASES OF SOLIDS INCLINED TO HP & VP

PROBLEM NO. 5 & 6

CASES OF CUBE & TETRAHEDRON

PROBLEM NO. 7

CASE OF FREELY SUSPENDED SOLID WITH SIDE VIEW.

PROBLEM NO. 8

CASE OF CUBE (WITH SIDE VIEW)

PROBLEM NO. 9

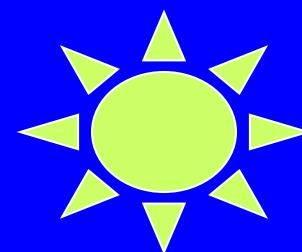
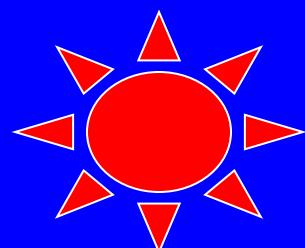
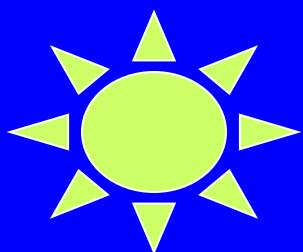
CASE OF TRUE LENGTH INCLINATION WITH HP & VP.

PROBLEM NO. 10 & 11

CASES OF COMPOSITE SOLIDS. (AUXILIARY PLANE)

PROBLEM NO. 12

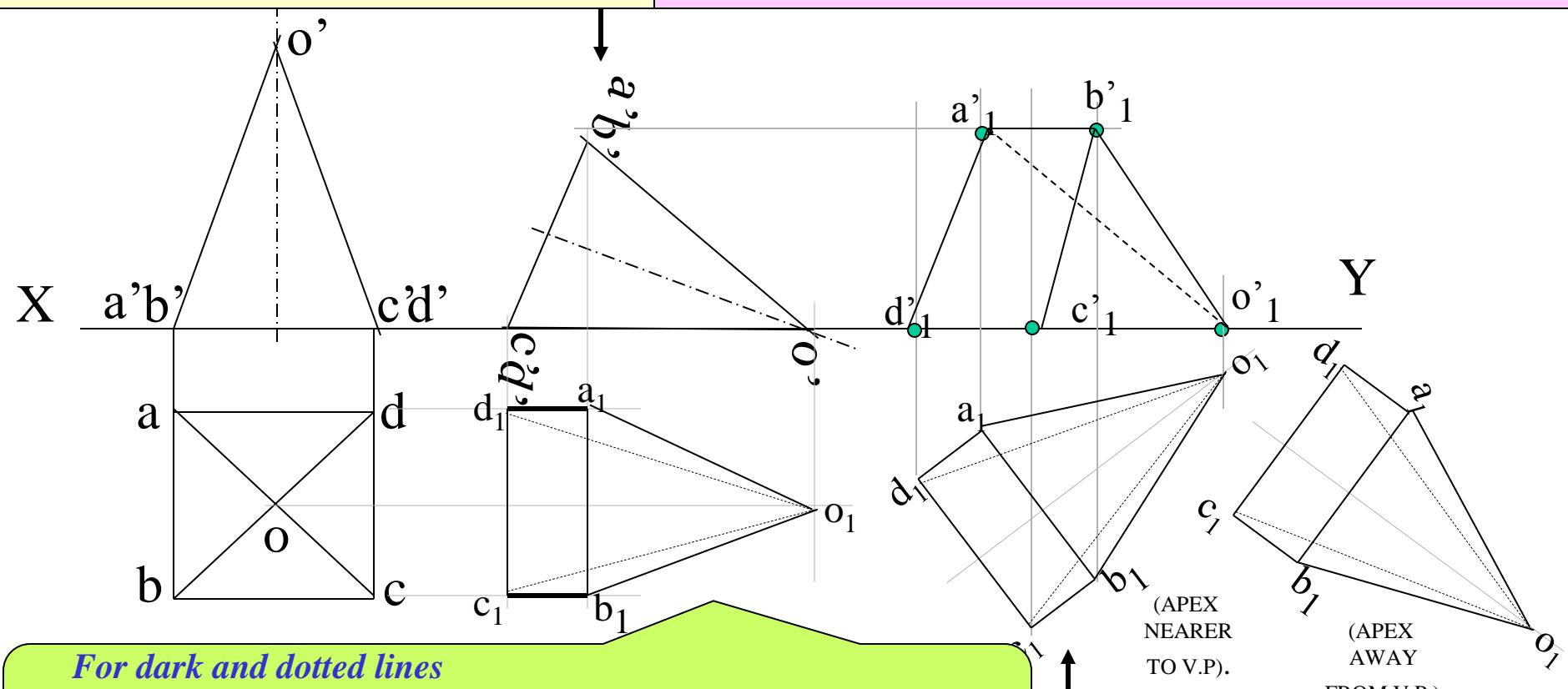
CASE OF A FRUSTUM (AUXILIARY PLANE)



Problem 1. A square pyramid, 40 mm base sides and axis 60 mm long, has a triangular face on the ground and the vertical plane containing the axis makes an angle of 45° with the VP. Draw its projections. Take apex nearer to VP

Solution Steps :

1. Assume it standing on Hp.
2. It's Tv will show True Shape of base(square)
3. Draw square of 40mm sides with one side vertical Tv & taking 50 mm axis project Fv. (a triangle)
4. Name all points as shown in illustration.
5. Draw 2nd Fv in lying position i.e. o'c'd' face on xy. And project it's Tv.
6. Make visible lines dark and hidden dotted, as per the procedure.
7. Then construct remaining inclination with Vp
(Vp containing axis is the center line of 2nd Tv. Make it 45° to xy as shown take apex near to xy, as it is nearer to Vp) & project final Fv.



For dark and dotted lines

1. Draw proper outline of new view DARK.
2. Decide direction of an observer.
3. Select nearest point to observer and draw all lines starting from it-dark.
4. Select farthest point to observer and draw all lines (remaining)from it-dotted.

(APEX
NEARER
TO V.P.)

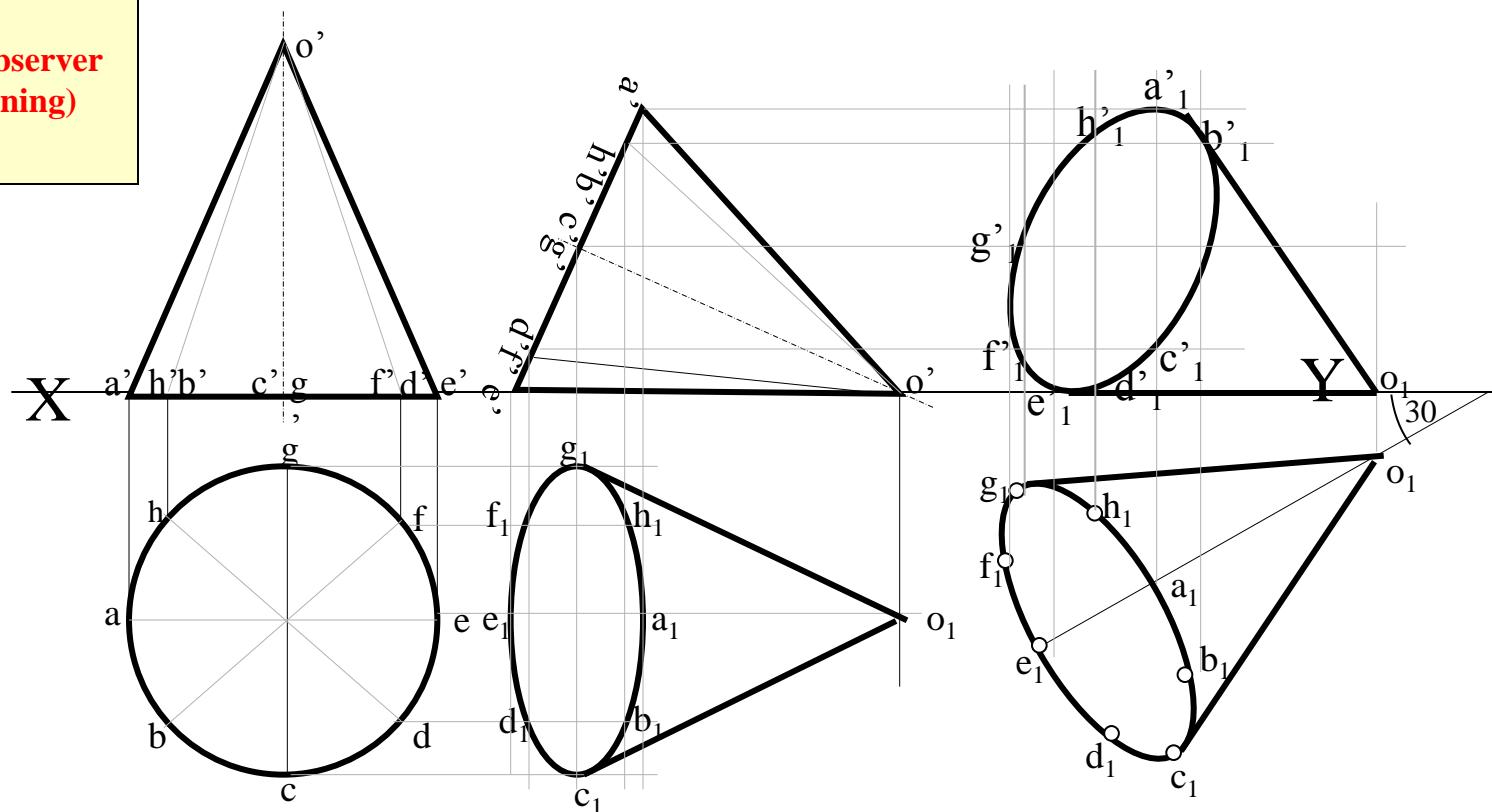
(APEX
AWAY
FROM V.P.)

Problem 2:

A cone 40 mm diameter and 50 mm axis is resting on one generator on Hp which makes 30° inclination with Vp
Draw it's projections.

For dark and dotted lines

1. Draw proper outline of new vie DARK.
2. Decide direction of an observer.
3. Select nearest point to observer and draw all lines starting from it-dark.
4. Select farthest point to observer and draw all lines (remaining) from it- dotted.



Solution Steps:

Resting on Hp on one generator, means lying on Hp:

1. Assume it standing on Hp.
2. It's Tv will show True Shape of base(circle)
3. Draw 40mm dia. Circle as Tv & taking 50 mm axis project Fv. (a triangle)
4. Name all points as shown in illustration.
5. Draw 2nd Fv in lying position i.e.o'e' on xy. And project it's Tv below xy.
6. Make visible lines dark and hidden dotted, as per the procedure.
7. Then construct remaining inclination with Vp (generator o₁e₁ 30° to xy as shown) & project final Fv.

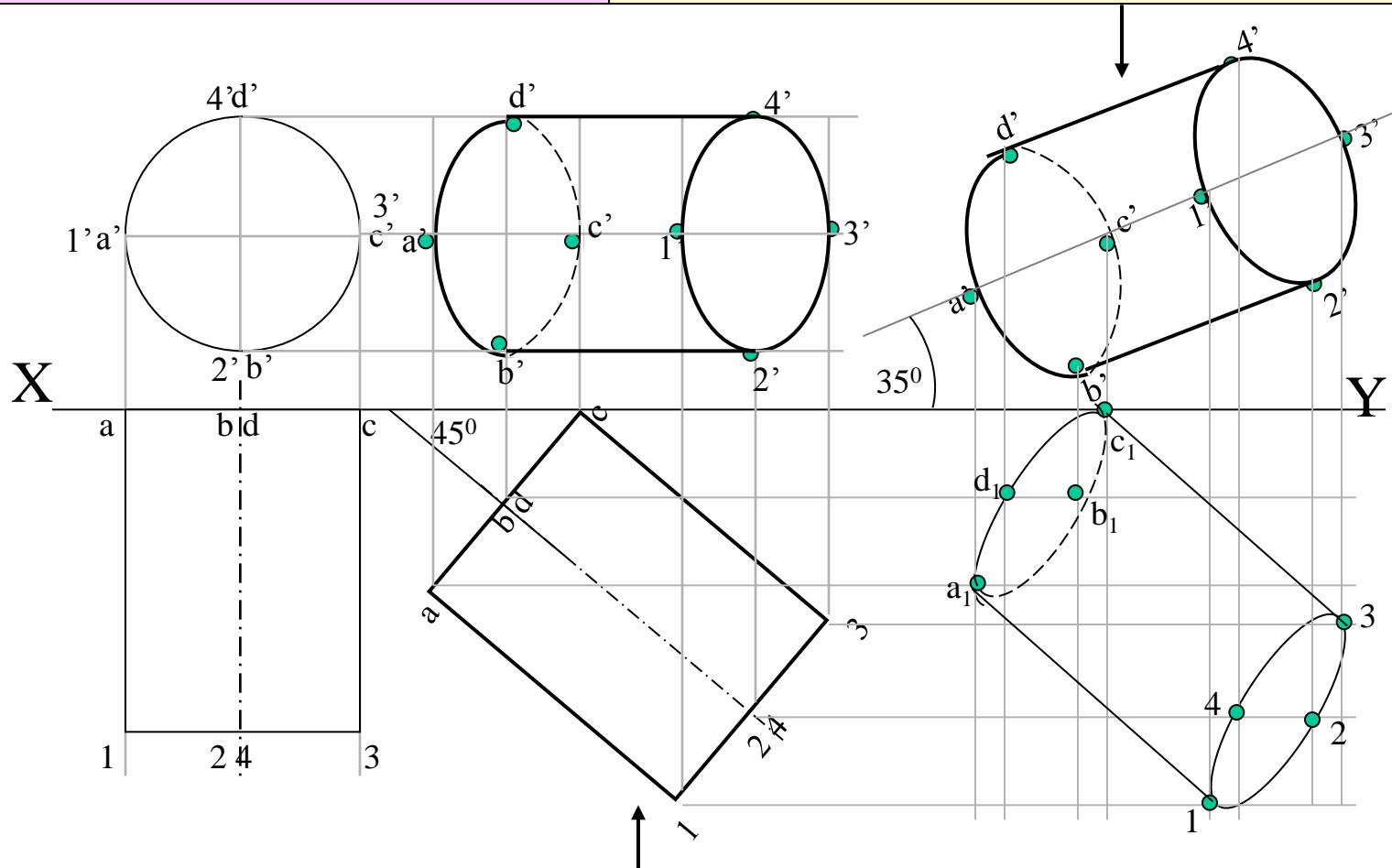
Problem 3:

A cylinder 40 mm diameter and 50 mm axis is resting on one point of a base circle on Vp while it's axis makes 45° with Vp and Fv of the axis 35° with Hp. Draw projections..

Solution Steps:

Resting on Vp on one point of base, means inclined to Vp:

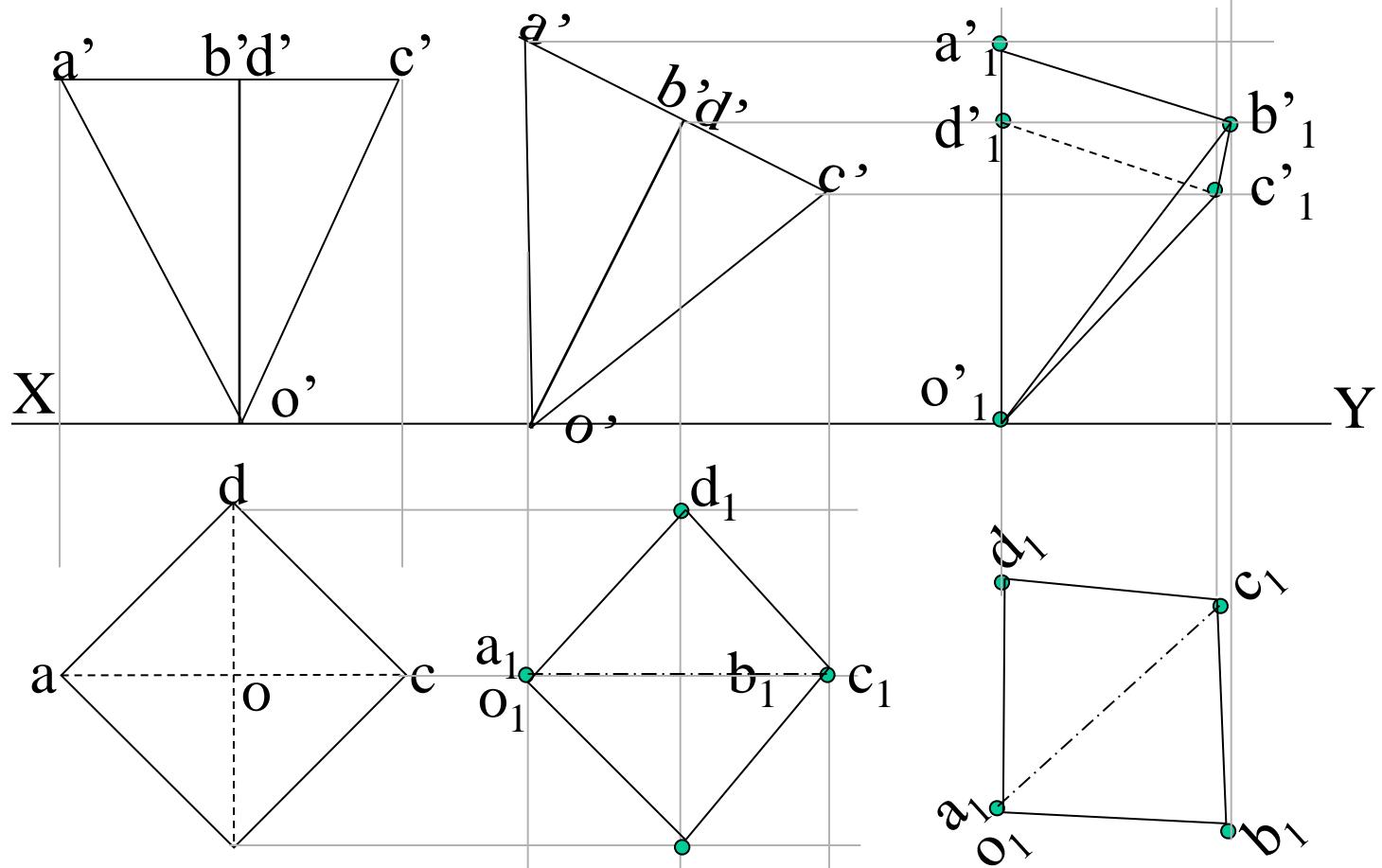
1. Assume it standing on Vp
2. It's Fv will show True Shape of base & top(circle)
3. Draw 40mm dia. Circle as Fv & taking 50 mm axis project Tv. (a Rectangle)
4. Name all points as shown in illustration.
5. Draw 2nd Tv making axis 45° to xy And project it's Fv above xy.
6. Make visible lines dark and hidden dotted, as per the procedure.
7. Then construct remaining inclination with Hp (Fv of axis i.e. center line of view to xy as shown) & project final Tv.



Problem 4: A square pyramid 30 mm base side and 50 mm long axis is resting on its apex on Hp, such that its one slant edge is vertical and a triangular face through it is perpendicular to Vp. Draw its projections.

Solution Steps :

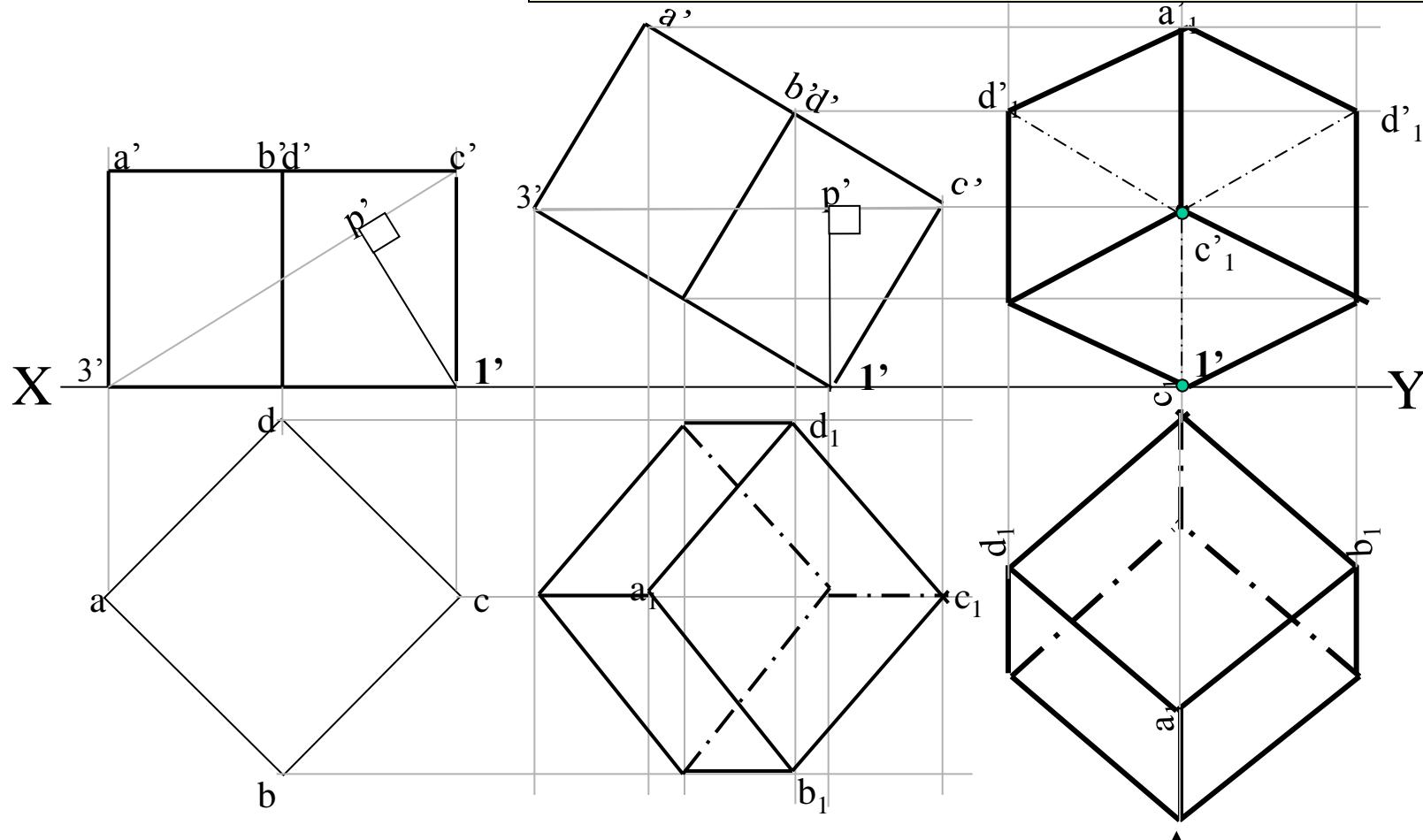
1. Assume it standing on Hp but as said on apex. (inverted).
2. It's Tv will show True Shape of base(square)
3. Draw a corner case square of 30 mm sides as Tv (as shown) Showing all slant edges dotted, as those will not be visible from top.
4. taking 50 mm axis project Fv. (a triangle)
5. Name all points as shown in illustration.
6. Draw 2nd Fv keeping o'a' slant edge vertical & project its Tv
7. Make visible lines dark and hidden dotted, as per the procedure.
8. Then redrew 2nd Tv as final Tv keeping a₁o₁d₁ triangular face perpendicular to Vp i.e. xy. Then as usual project final Fv.



Problem 5: A cube of 50 mm long edges is so placed on Hp on one corner that a body diagonal is parallel to Hp and perpendicular to Vp. Draw its projections.

Solution Steps:

1. Assuming standing on Hp, begin with Tv, a square with all sides equally inclined to xy. Project Fv and name all points of FV & TV.
2. Draw a body-diagonal joining c' with 3' (This can become // to xy)
3. From 1' drop a perpendicular on this and name it p'
4. Draw 2nd Fv in which 1'-p' line is vertical **means** c'-3' diagonal must be horizontal. Now as usual project Tv..
6. In final Tv draw same diagonal is perpendicular to Vp as said in problem. Then as usual project final FV.



Problem 6: A tetrahedron of 50 mm long edges is resting on one edge on Hp while one triangular face containing this edge is vertical and 45° inclined to Vp. Draw projections.

IMPORTANT:

Tetrahedron is a special type of triangular pyramid in which base sides & slant edges are equal in length. Solid of four faces. Like cube it is also described by One dimension only.. Axis length generally not given.

Solution Steps

As it is resting assume it standing on Hp.

Begin with Tv , an equilateral triangle as side case as shown:

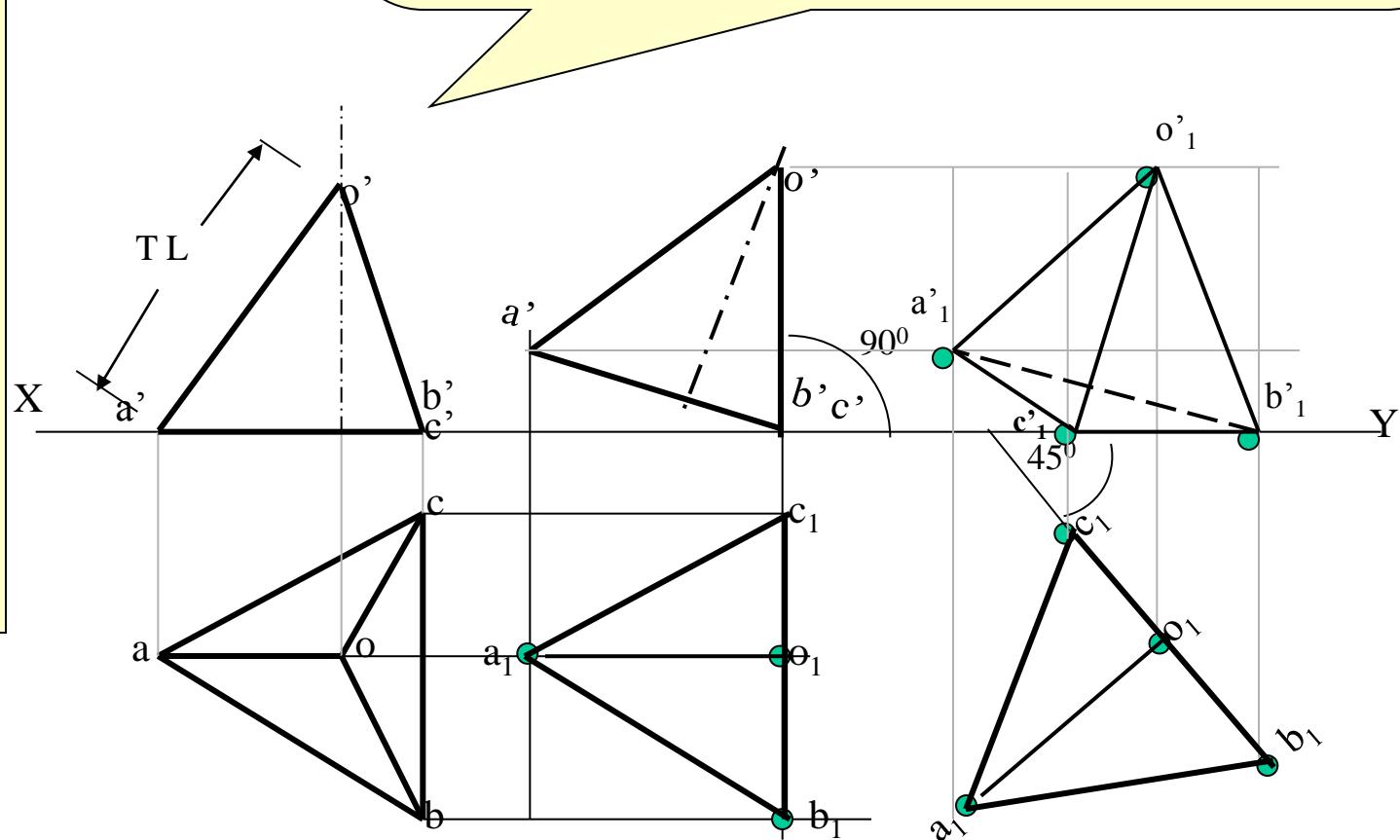
First project base points of Fv on xy, name those & axis line.

From a' with TL of edge, 50 mm, cut on axis line & mark o' (as axis is not known, o' is finalized by slant edge length)

Then complete Fv.

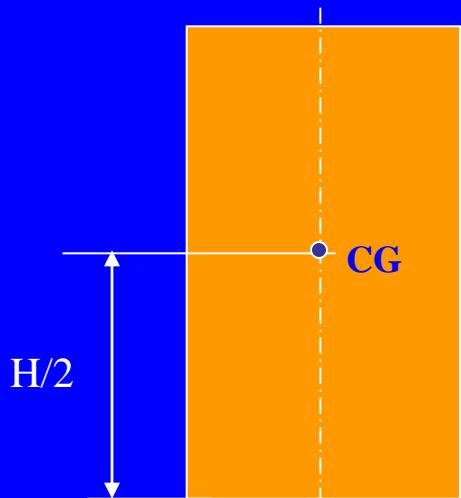
In 2nd Fv make face o'b'c' vertical as said in problem.

And like all previous problems solve completely.

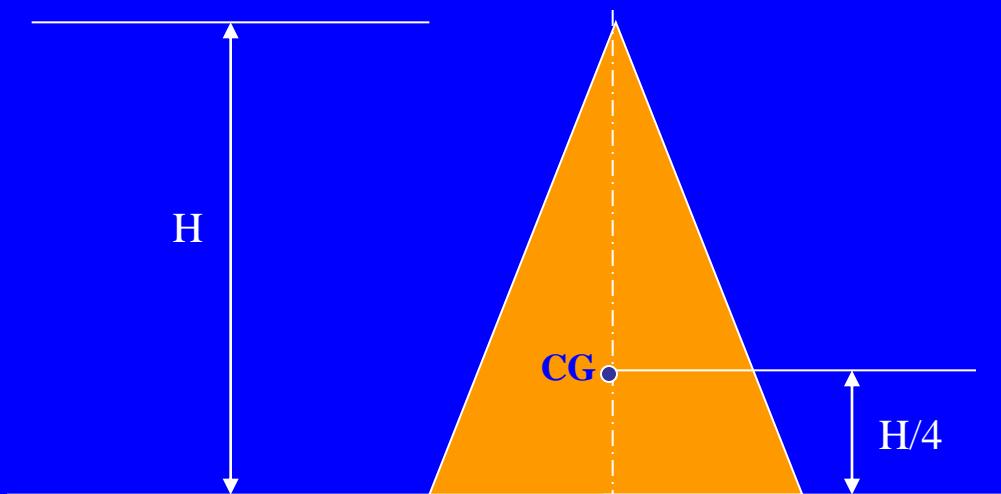


FREELY SUSPENDED SOLIDS:

Positions of CG, on axis, from base, for different solids are shown below.



GROUP A SOLIDS
(Cylinder & Prisms)



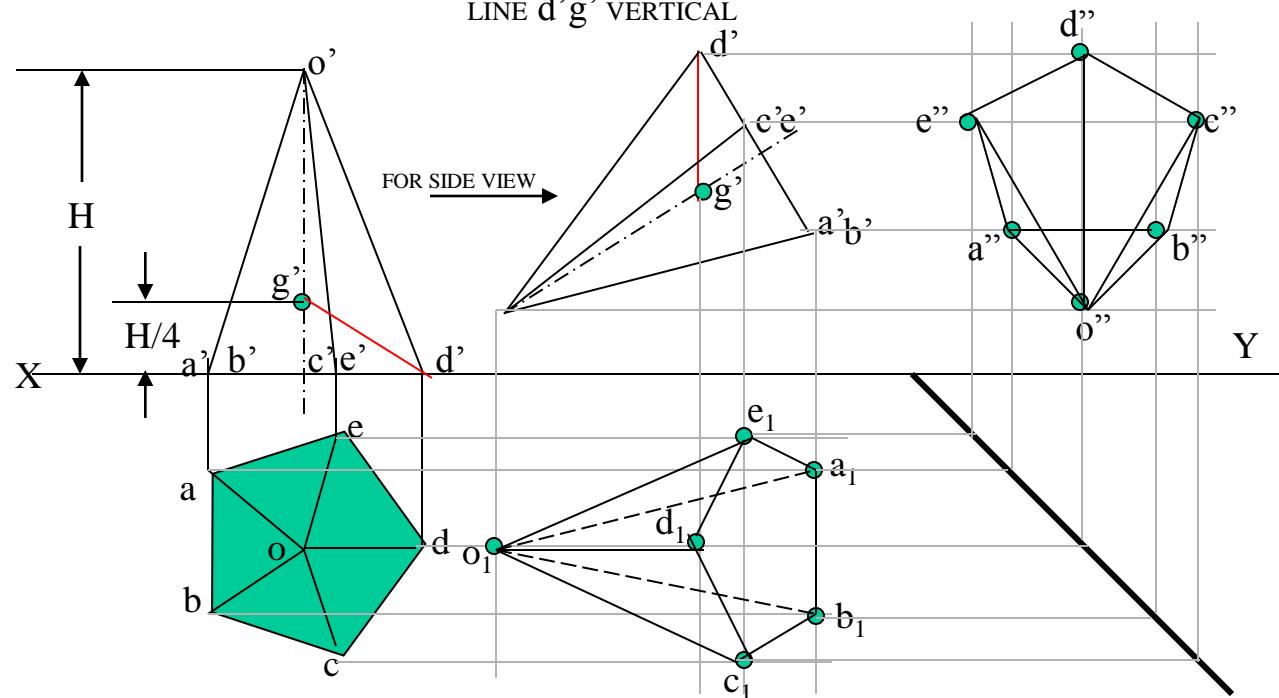
GROUP B SOLIDS
(Cone & Pyramids)

Problem 7: A pentagonal pyramid
30 mm base sides & 60 mm long axis,
is freely suspended from one corner of
base so that a plane containing it's axis
remains parallel to Vp.
Draw it's three views.

Solution Steps:

In all suspended cases axis shows inclination with Hp.

- 1.Hence assuming it standing on Hp, drew Tv - a regular pentagon,corner case.
- 2.Project Fv & locate CG position on axis – ($\frac{1}{4} H$ from base.) and name g' and Join it with corner d'
- 3.As 2nd Fv, redraw first keeping line $g'd'$ vertical.
- 4.As usual project corresponding Tv and then Side View looking from.



IMPORTANT:
When a solid is freely suspended from a corner, then line joining point of contact & C.G. remains vertical.
(Here axis shows inclination with Hp.) So in all such cases, assume solid standing on Hp initially.)

Solution Steps:

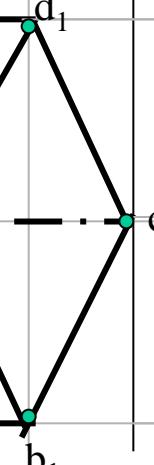
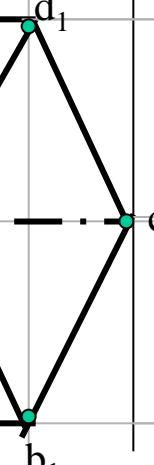
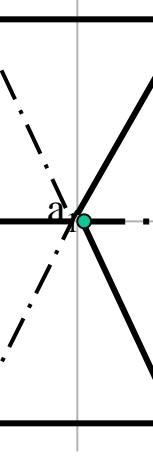
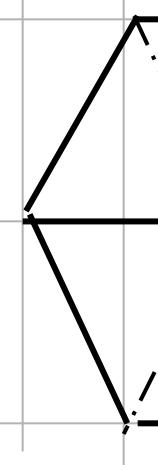
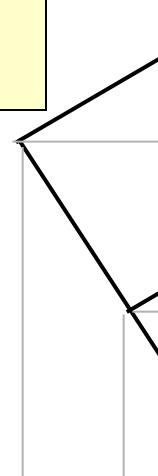
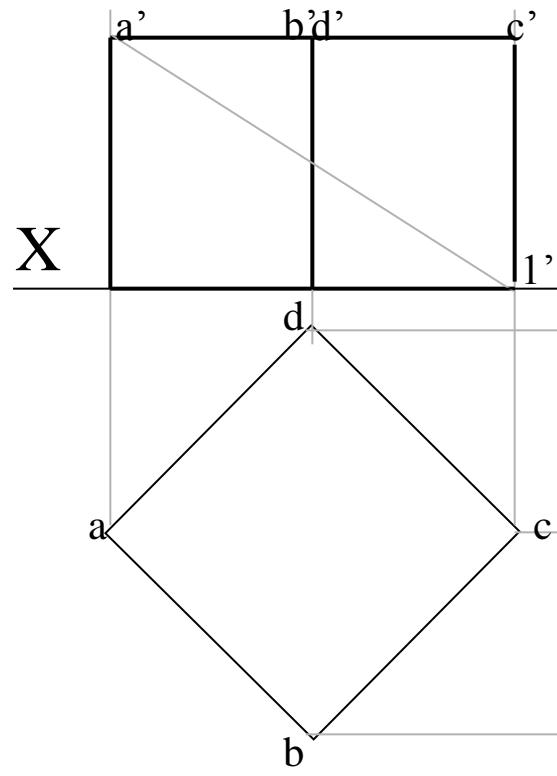
1. Assuming it standing on Hp begin with Tv, a square of corner case.
2. Project corresponding Fv. & name all points as usual in both views.
3. Join $a'1'$ as body diagonal and draw 2nd Fv making it vertical (I' on xy)
4. Project it's Tv drawing dark and dotted lines as per the procedure.
5. With standard method construct Left-hand side view.

(Draw a 45° inclined Line in Tv region (below xy).

Project horizontally all points of Tv on this line and reflect vertically upward, above xy. After this, draw horizontal lines, from all points of Fv, to meet these lines. Name points of intersections and join properly.

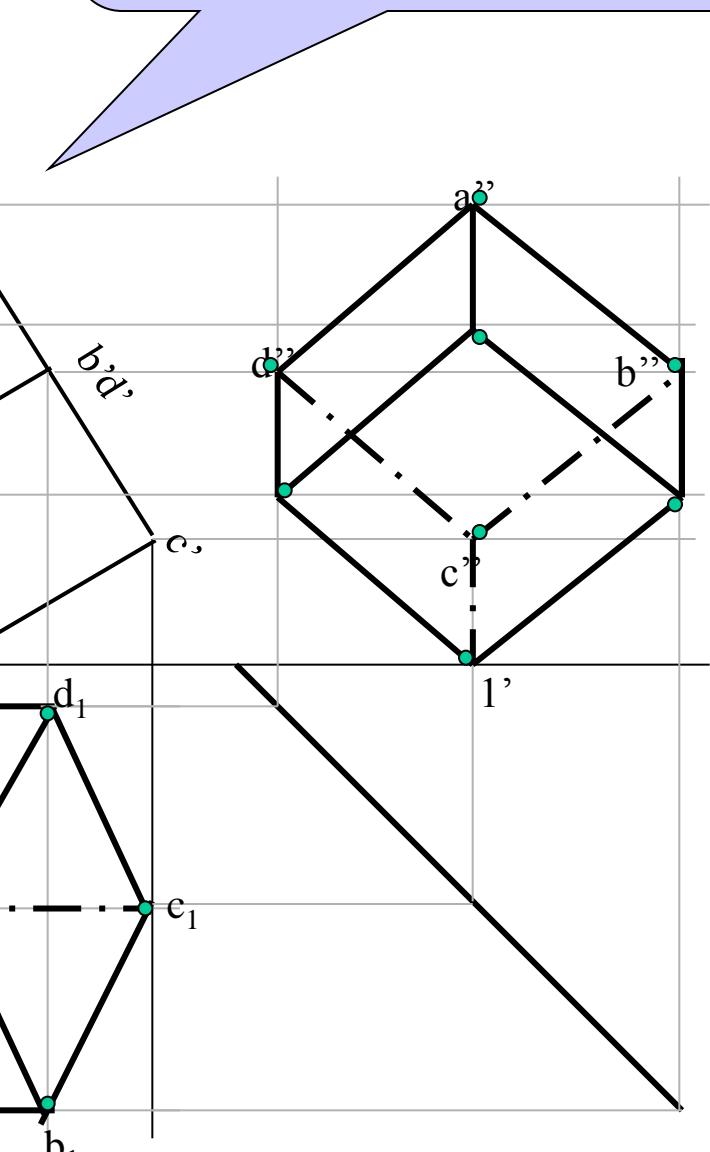
For dark & dotted lines

locate observer on left side of Fv as shown.)



Problem 8:

A cube of 50 mm long edges is so placed on Hp on one corner that a body diagonal through this corner is perpendicular to Hp and parallel to Vp. Draw its three views.



Y

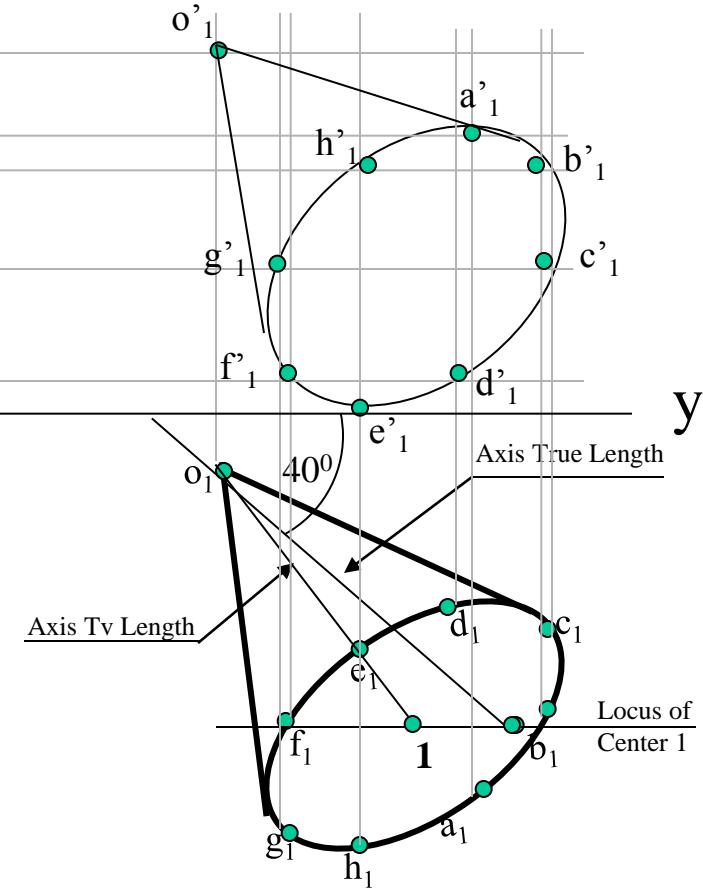
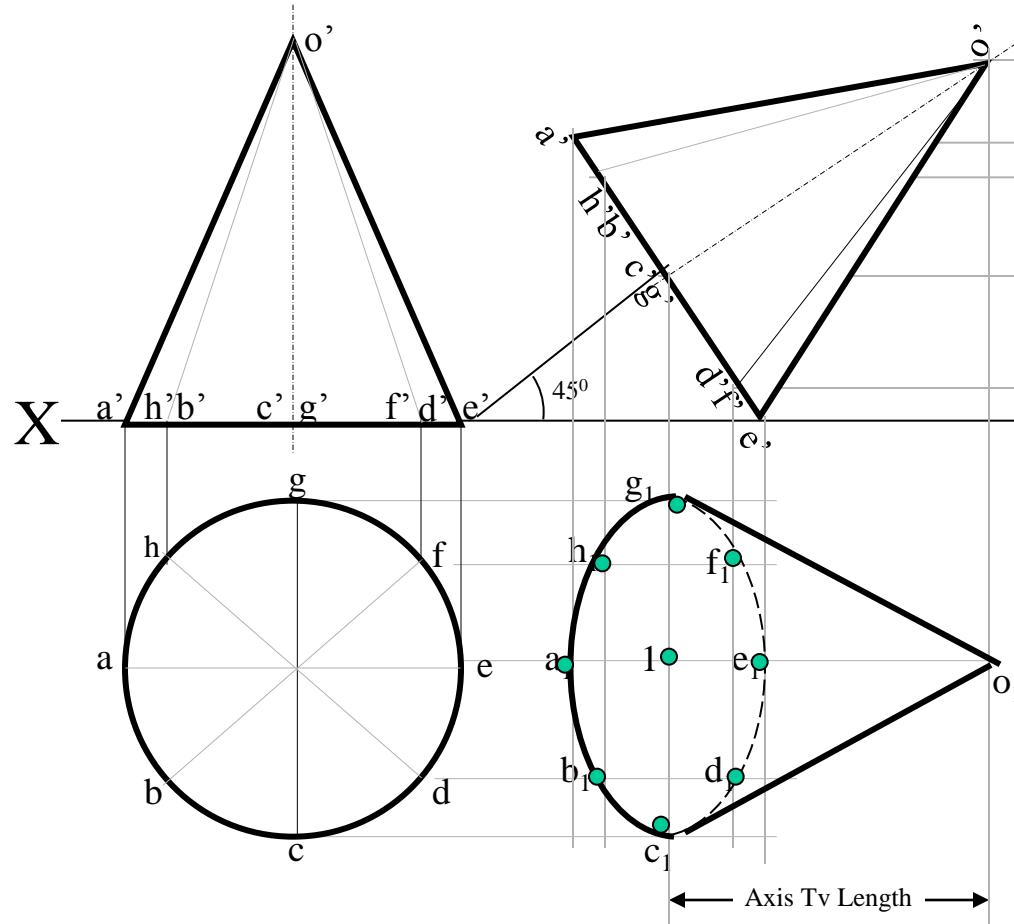
X

Problem 9: A right circular cone, 40 mm base diameter and 60 mm long axis is resting on Hp on one point of base circle such that it's axis makes 45^0 inclination with Hp and 40^0 inclination with Vp. Draw it's projections.

This case resembles to problem no.7 & 9 from projections of planes topic.

In previous all cases 2nd inclination was done by a parameter not showing TL. Like Tv of axis is inclined to Vp etc. But here it is clearly said that the axis is 40^0 inclined to Vp. Means here TL inclination is expected. So the same construction done in those Problems is done here also. See carefully the final Tv and inclination taken there.

So assuming it standing on HP begin as usual.

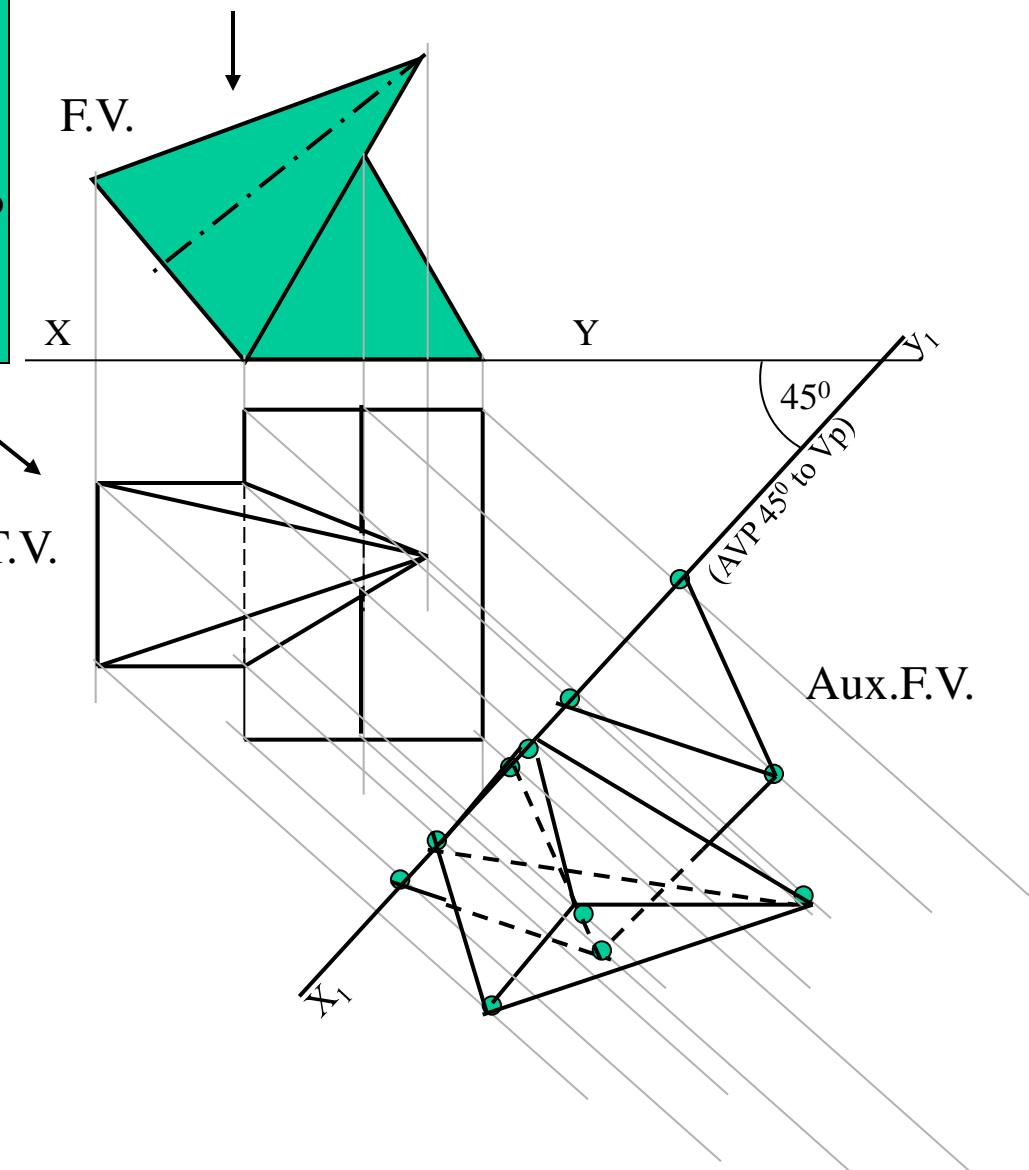


Problem 10:

A triangular prism,
40 mm base side 60 mm axis
is lying on Hp on one rectangular face
with axis perpendicular to Vp.
One square pyramid is leaning on it's face
centrally with axis // to vp. It's base side is
30 mm & axis is 60 mm long resting on Hp
on one edge of base. Draw FV & TV of
both solids. Project another FV
on an AVP 45^0 inclined to VP.

Steps :

Draw Fv of lying prism
(an equilateral Triangle)
And Fv of a leaning pyramid.
Project Tv of both solids.
Draw x_1y_1 45^0 inclined to xy
and project aux.Fv on it.
Mark the distances of first FV
from first xy for the distances
of aux. Fv from x_1y_1 line.
Note the observer's directions
Shown by arrows and further
steps carefully.



Problem 11:

A hexagonal prism of base side 30 mm long and axis 40 mm long, is standing on Hp on its base with one base edge // to Vp.

A tetrahedron is placed centrally on the top of it. The base of tetrahedron is a triangle formed by joining alternate corners of top of prism..Draw projections of both solids. Project an auxiliary Tv on AIP 45° inclined to Hp.

STEPS:

Draw a regular hexagon as Tv of standing prism With one side // to xy and name the top points. Project it's Fv – a rectangle and name it's top.

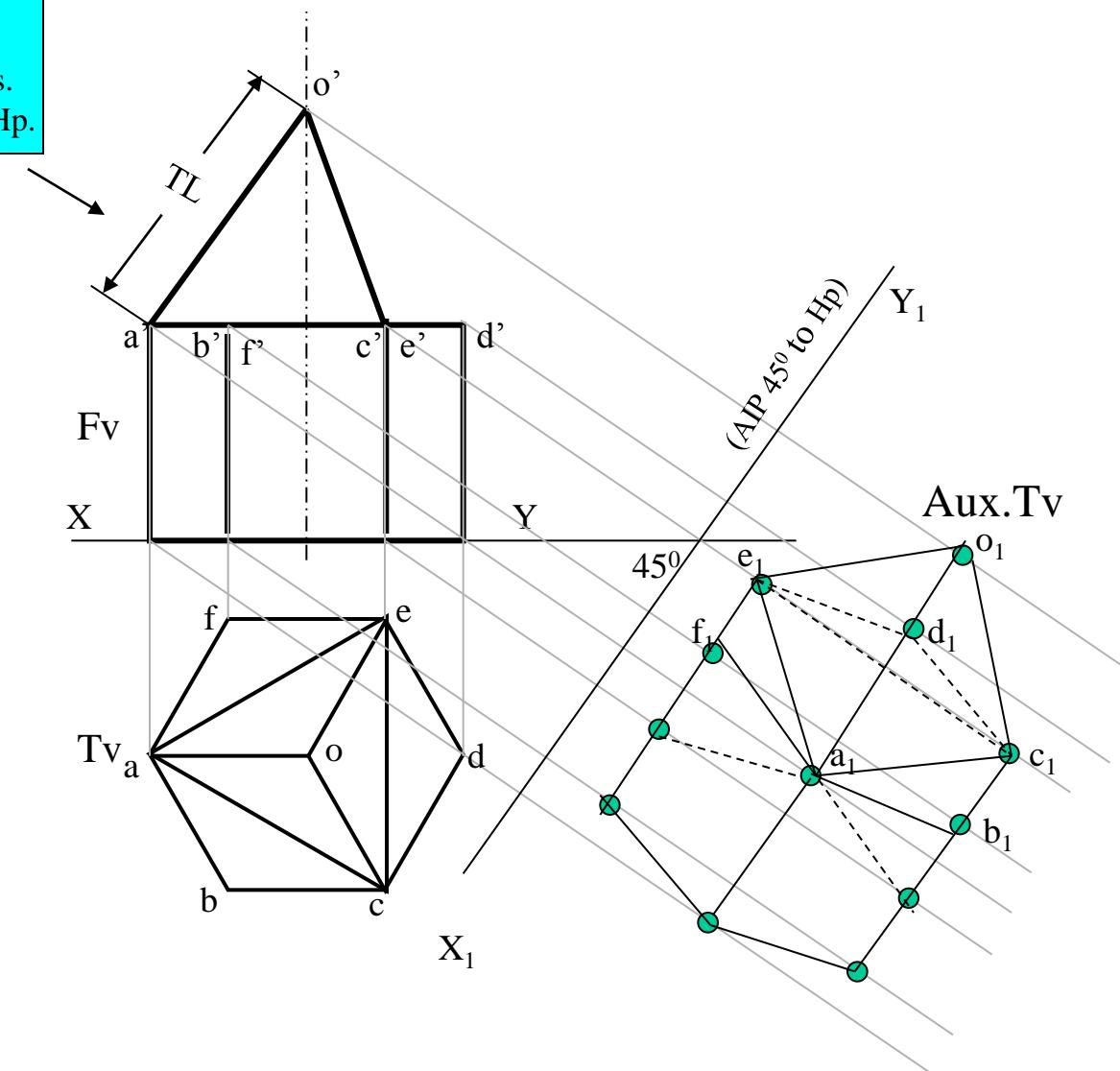
Now join it's alternate corners a-c-e and the triangle formed is base of a tetrahedron as said.

Locate center of this triangle & locate apex o

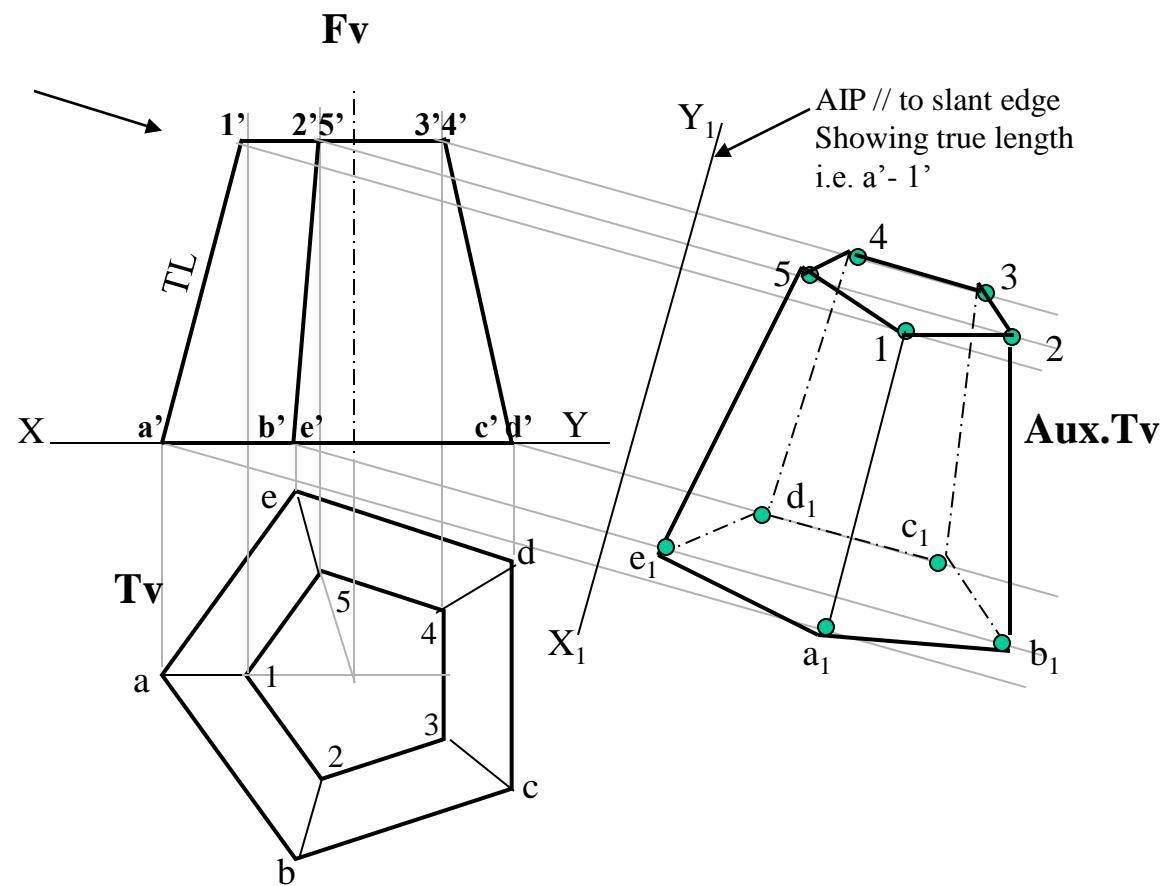
Extending it's axis line upward mark apex o'

By cutting TL of edge of tetrahedron equal to a-c. and complete Fv of tetrahedron.

Draw an AIP (x_1y_1) 45° inclined to xy And project Aux.Tv on it by using similar Steps like previous problem.



Problem 12: A frustum of regular hexagonal pyramid is standing on it's larger base On Hp with one base side perpendicular to Vp. Draw it's Fv & Tv.
 Project it's Aux.Tv on an AIP parallel to one of the slant edges showing TL.
 Base side is 50 mm long , top side is 30 mm long and 50 mm is height of frustum.



ENGINEERING APPLICATIONS OF THE PRINCIPLES OF PROJECTIONS OF SOLIDES.

- 1. SECTIONS OF SOLIDS.**
- 2. DEVELOPMENT.**
- 3. INTERSECTIONS.**

**STUDY CAREFULLY
THE ILLUSTRATIONS GIVEN ON
NEXT *SIX* PAGES !**

SECTIONING A SOLID.

An object (here a solid) is cut by some imaginary cutting plane to understand internal details of that object.

The action of cutting is called **SECTIONING** a solid

&

The plane of cutting is called **SECTION PLANE**.

Two cutting actions means section planes are recommended.

- A) Section Plane perpendicular to Vp and inclined to Hp.
(This is a definition of an Aux. Inclined Plane i.e. A.I.P.)

NOTE:- This section plane appears as a straight line in FV.

- B) Section Plane perpendicular to Hp and inclined to Vp.
(This is a definition of an Aux. Vertical Plane i.e. A.V.P.)

NOTE:- This section plane appears as a straight line in TV.

Remember:-

1. After launching a section plane either in FV or TV, the part towards observer is assumed to be removed.
2. As far as possible the smaller part is assumed to be removed.

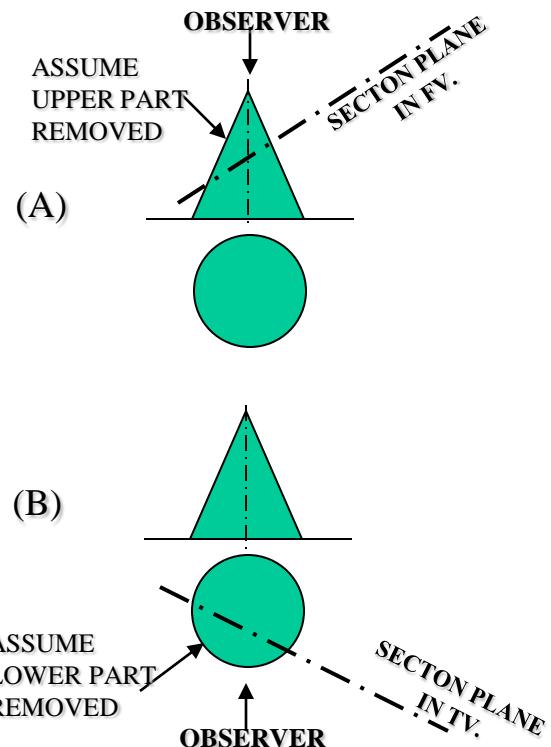
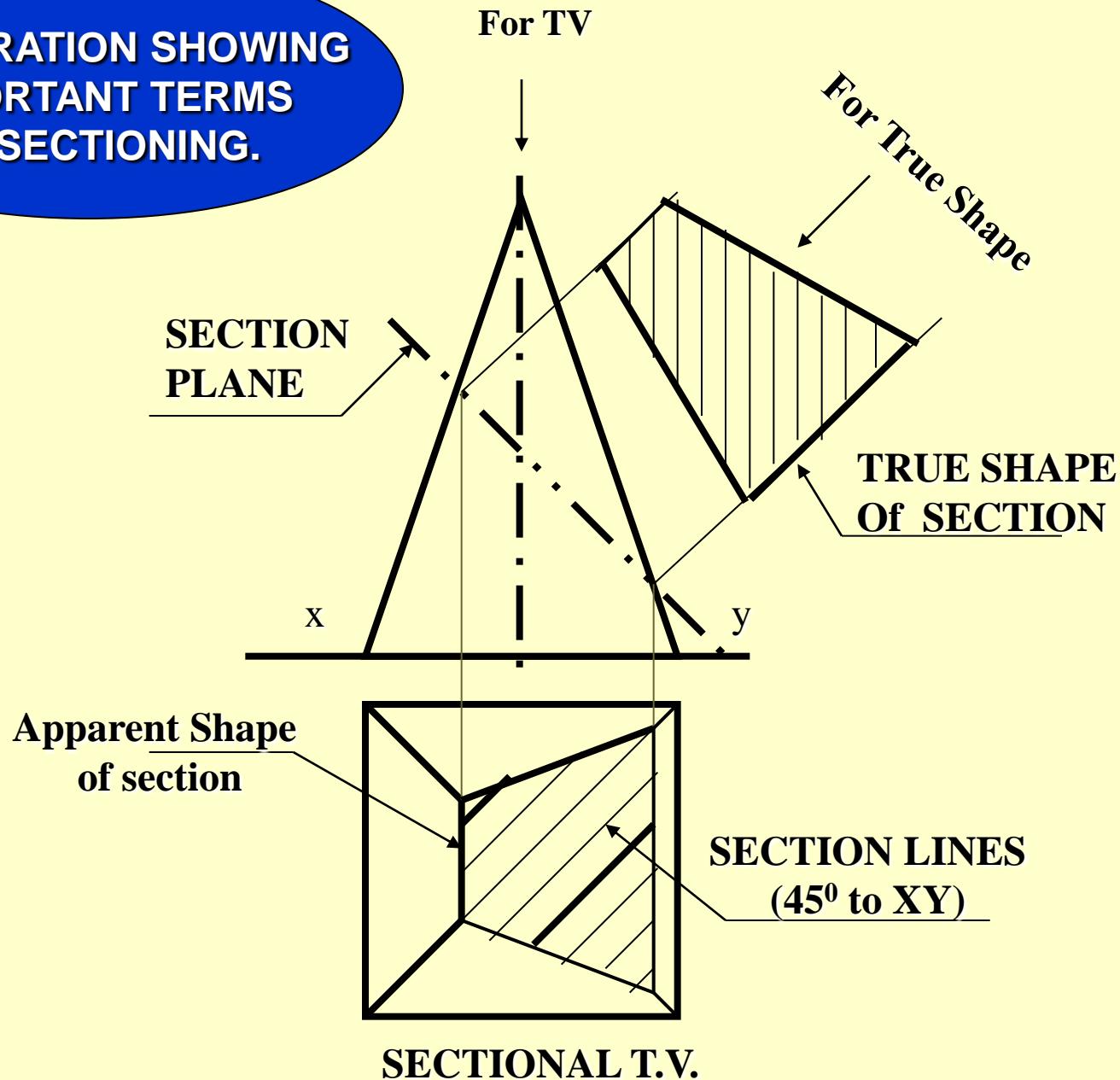
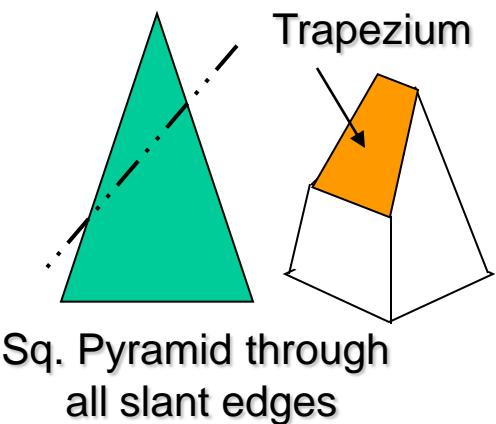
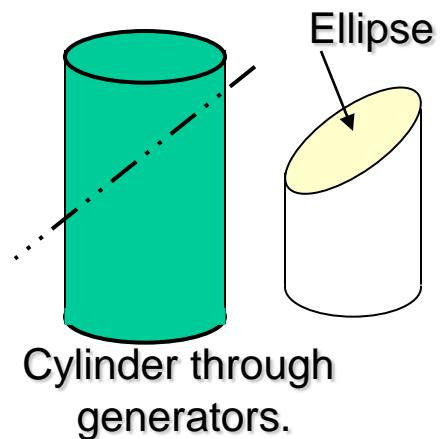
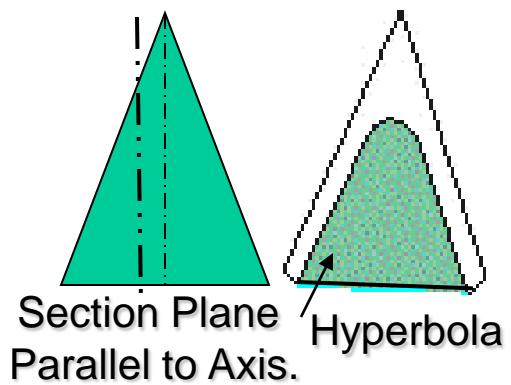
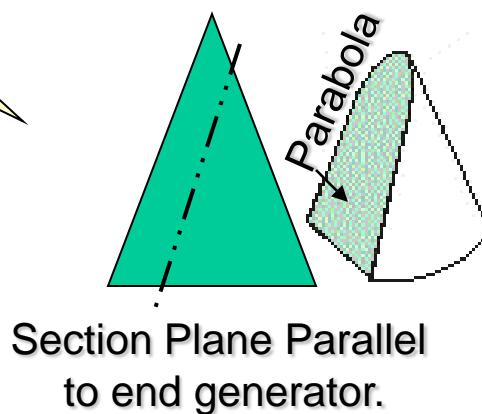
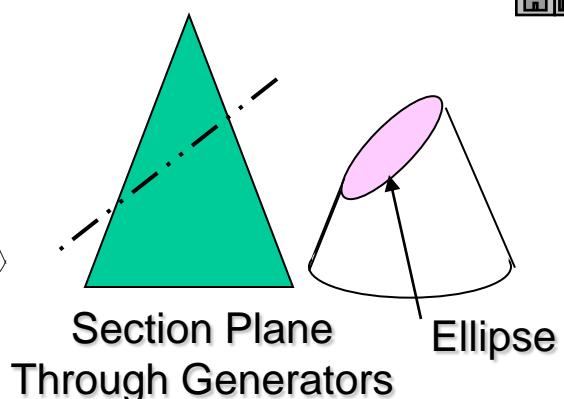
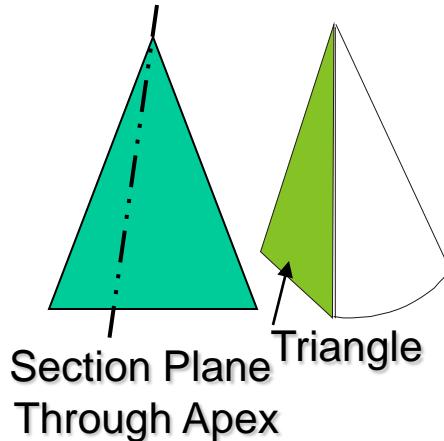


ILLUSTRATION SHOWING IMPORTANT TERMS IN SECTIONING.



Typical Section Planes & Typical Shapes Of Sections.



DEVELOPMENT OF SURFACES OF SOLIDS.

MEANING:-

ASSUME OBJECT HOLLOW AND MADE-UP OF THIN SHEET. CUT OPEN IT FROM ONE SIDE AND UNFOLD THE SHEET COMPLETELY. THEN THE **SHAPE OF THAT UNFOLDED SHEET IS CALLED DEVELOPMENT OF LATERAL SURFACES** OF THAT OBJECT OR SOLID.

LATERAL SURFACE IS THE SURFACE EXCLUDING SOLID'S TOP & BASE.

ENGINEERING APPLICATION:

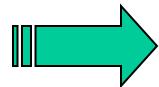
THERE ARE SO MANY PRODUCTS OR OBJECTS WHICH ARE DIFFICULT TO MANUFACTURE BY CONVENTIONAL MANUFACTURING PROCESSES, BECAUSE OF THEIR SHAPES AND SIZES.

THOSE ARE FABRICATED IN SHEET METAL INDUSTRY BY USING DEVELOPMENT TECHNIQUE. THERE IS A VAST RANGE OF SUCH OBJECTS.

EXAMPLES:-

Boiler Shells & chimneys, Pressure Vessels, Shovels, Trays, Boxes & Cartons, Feeding Hoppers, Large Pipe sections, Body & Parts of automotives, Ships, Aeroplanes and many more.

**WHAT IS
OUR OBJECTIVE
IN THIS TOPIC ?**



To learn methods of development of surfaces of different solids, their sections and frustums.

*But before going ahead,
note following
Important points.*

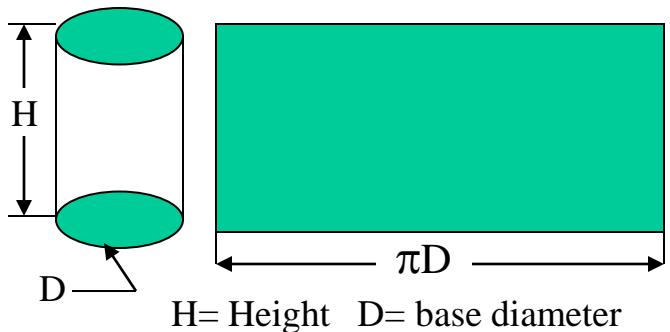
1. Development is different drawing than PROJECTIONS.
2. It is a shape showing AREA, means it's a 2-D plain drawing.
3. Hence all dimensions of it must be TRUE dimensions.
4. As it is representing shape of an un-folded sheet, no edges can remain hidden
And hence DOTTED LINES are never shown on development.

Study illustrations given on next page carefully.

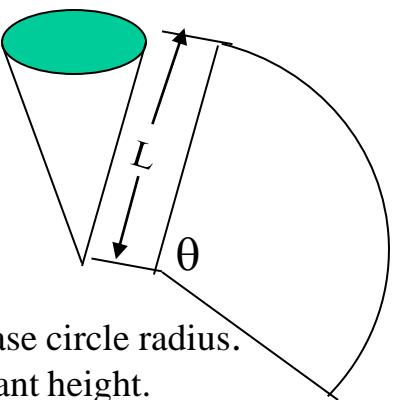
Development of lateral surfaces of different solids.

(Lateral surface is the surface excluding top & base)

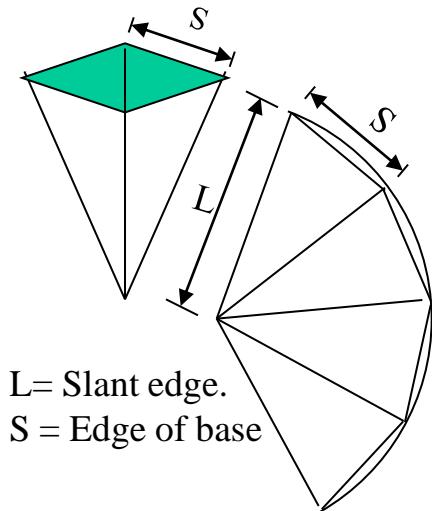
Cylinder: A Rectangle



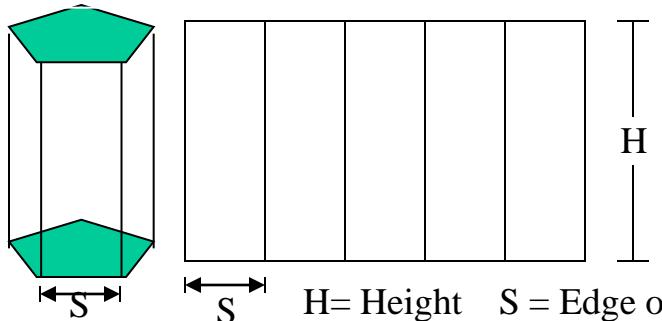
Cone: (Sector of circle)



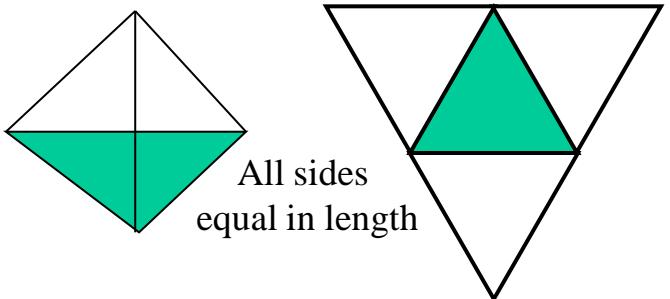
Pyramids: (No.of triangles)



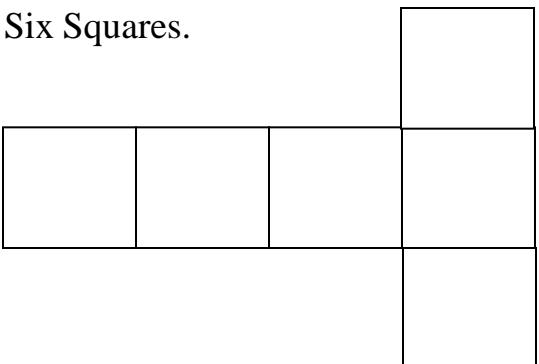
Prisms: No.of Rectangles



Tetrahedron: Four Equilateral Triangles

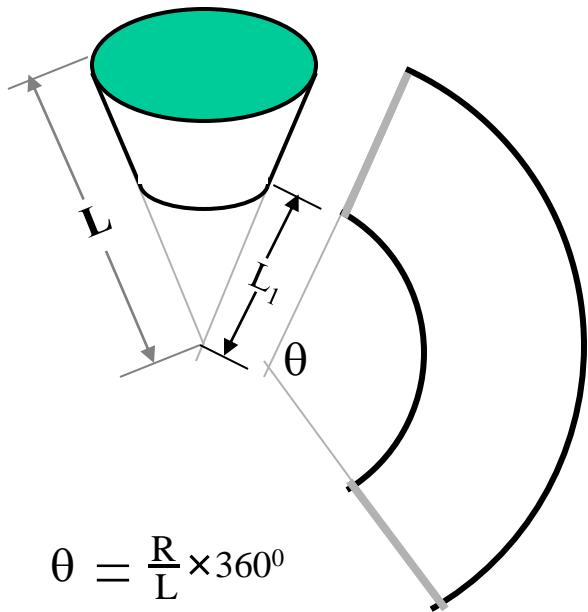


Cube: Six Squares.



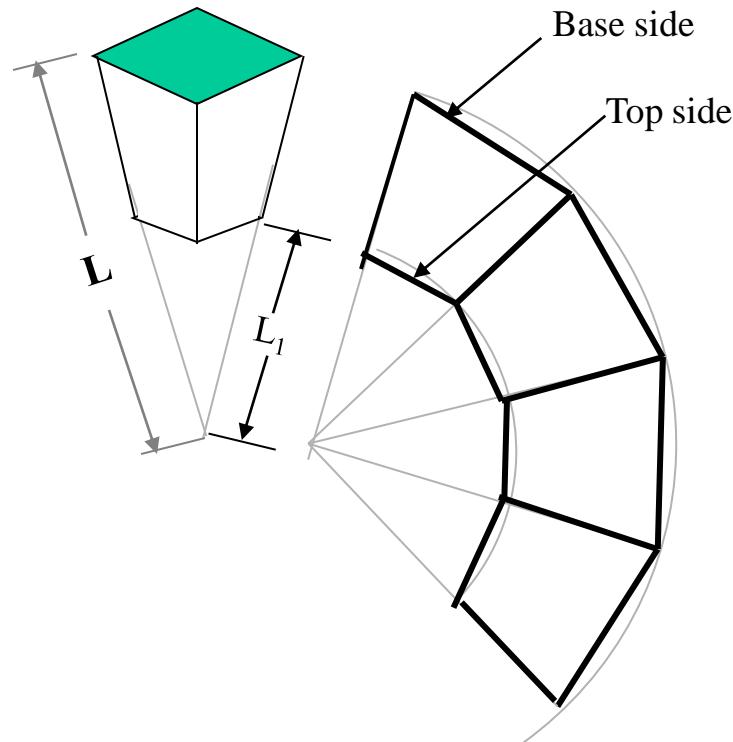
FRUSTUMS

DEVELOPMENT OF FRUSTUM OF CONE



R= Base circle radius of cone
 L= Slant height of cone
 L_1 = Slant height of cut part.

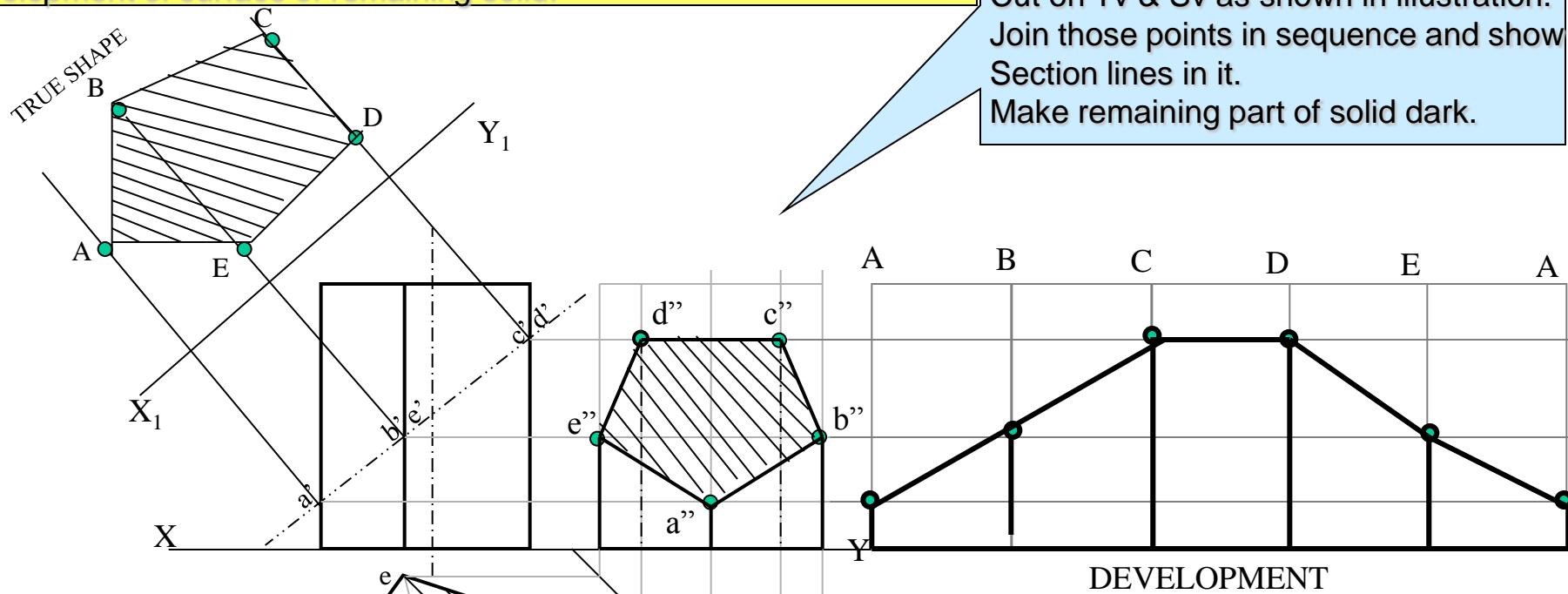
DEVELOPMENT OF FRUSTUM OF SQUARE PYRAMID



L= Slant edge of pyramid
 L_1 = Slant edge of cut part.

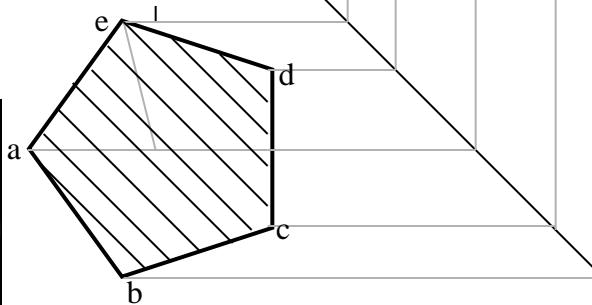
**STUDY NEXT *NINE* PROBLEMS OF
SECTIONS & DEVELOPMENT**

Problem 1: A pentagonal prism , 30 mm base side & 50 mm axis is standing on Hp on it's base whose one side is perpendicular to Vp. It is cut by a section plane 45^0 inclined to Hp, through mid point of axis. Draw Fv, sec.Tv & sec. Side view. Also draw true shape of section and Development of surface of remaining solid.



For True Shape:

Draw $x_1y_1 \parallel$ to sec. plane
Draw projectors on it from cut points.
Mark distances of points of Sectioned part from Tv, on above projectors from x_1y_1 and join in sequence.
Draw section lines in it.
It is required true shape.



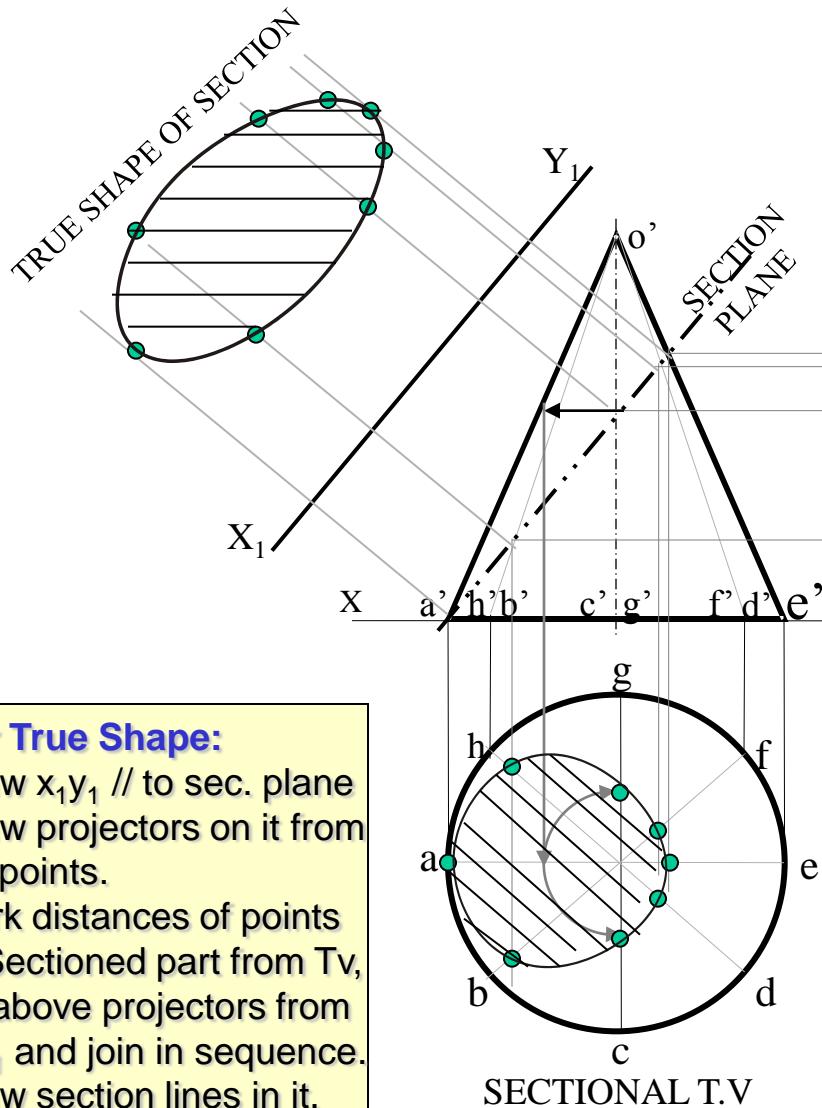
For Development:

Draw development of entire solid. Name from cut-open edge i.e. A. in sequence as shown.
Mark the cut points on respective edges.
Join them in sequence in st. lines.
Make existing parts dev.dark.

Solution Steps:for sectional views:

Draw three views of standing prism.
Locate sec. plane in Fv as described.
Project points where edges are getting Cut on Tv & Sv as shown in illustration.
Join those points in sequence and show Section lines in it.
Make remaining part of solid dark.

Problem 2: A cone, 50 mm base diameter and 70 mm axis is standing on its base on Hp. It is cut by a section plane 45° inclined to Hp through base end of end generator. Draw projections, sectional views, true shape of section and development of surfaces of remaining solid.

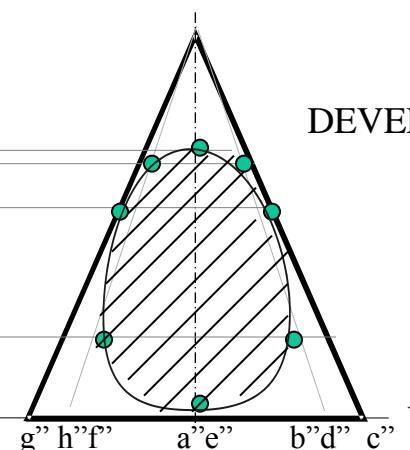


For True Shape:

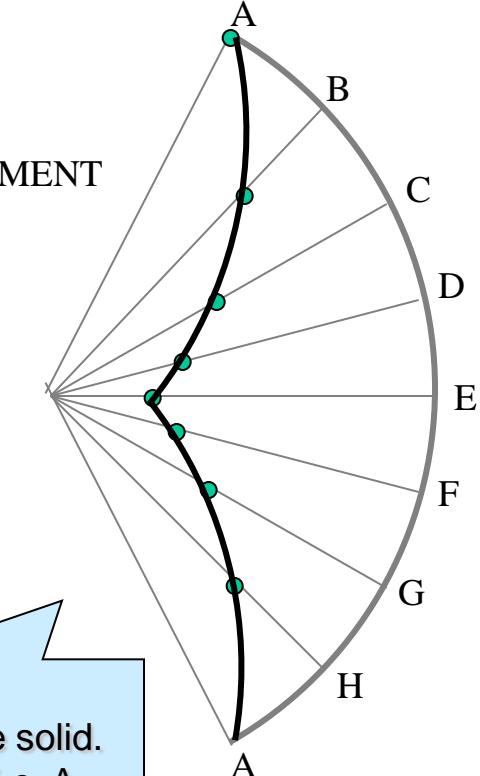
Draw $x_1y_1 \parallel$ to sec. plane
Draw projectors on it from cut points.
Mark distances of points of Sectioned part from Tv, on above projectors from x_1y_1 and join in sequence.
Draw section lines in it.
It is required true shape.

Solution Steps: for sectional views:
Draw three views of standing cone.
Locate sec. plane in Fv as described.
Project points where generators are getting Cut on Tv & Sv as shown in illustration. Join those points in sequence and show Section lines in it.
Make remaining part of solid dark.

SECTIONAL S.V



DEVELOPMENT

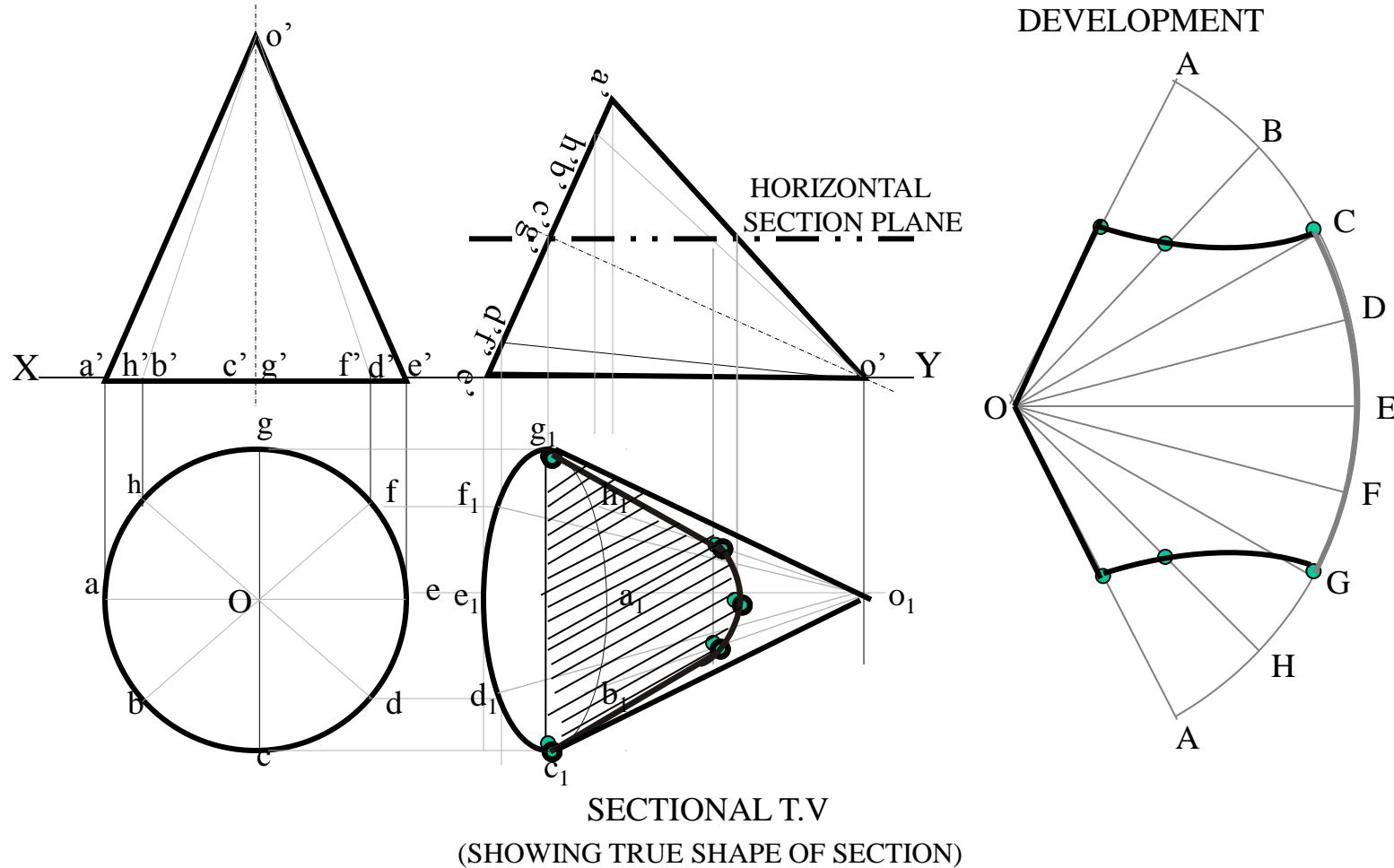


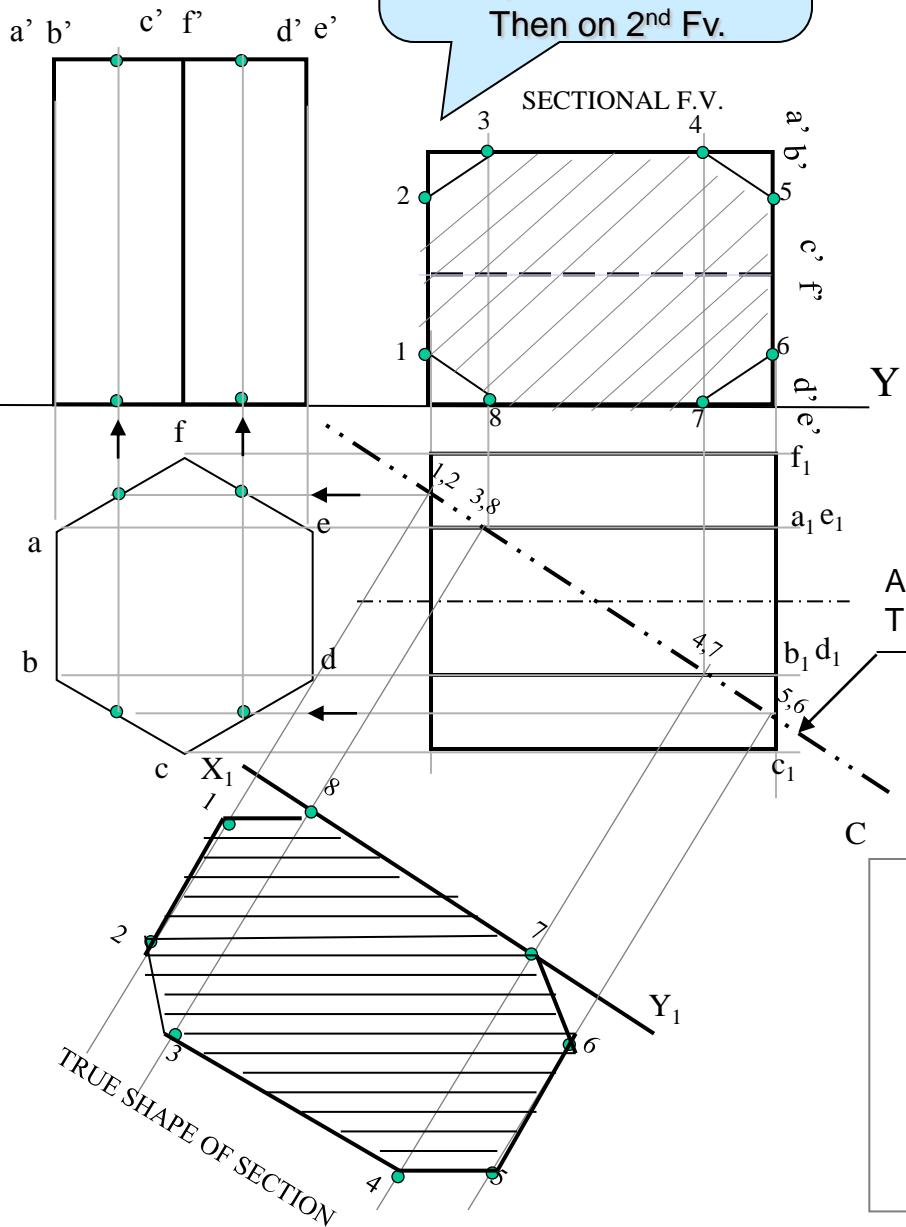
For Development:

Draw development of entire solid.
Name from cut-open edge i.e. A in sequence as shown. Mark the cut points on respective edges.
Join them in sequence in curvature.
Make existing parts dev.dark.

Problem 3: A cone 40mm diameter and 50 mm axis is resting on one generator on Hp(lying on Hp) which is // to Vp.. Draw it's projections. It is cut by a horizontal section plane through it's base center. Draw sectional TV, development of the surface of the remaining part of cone.

Follow similar solution steps for Sec.views - True shape – Development as per previous problem!



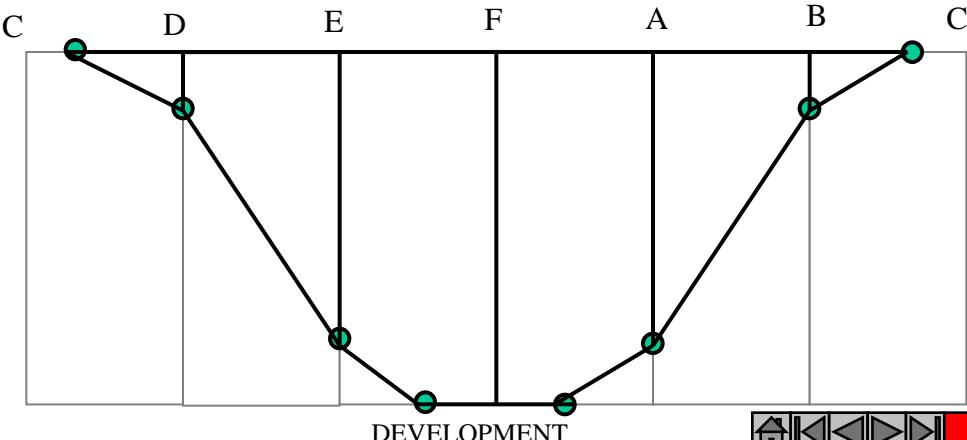


Problem 4: A hexagonal prism. 30 mm base side & 55 mm axis is lying on Hp on its rect.face with axis // to Vp. It is cut by a section plane normal to Hp and 30° inclined to Vp bisecting axis.
Draw sec. Views, true shape & development.

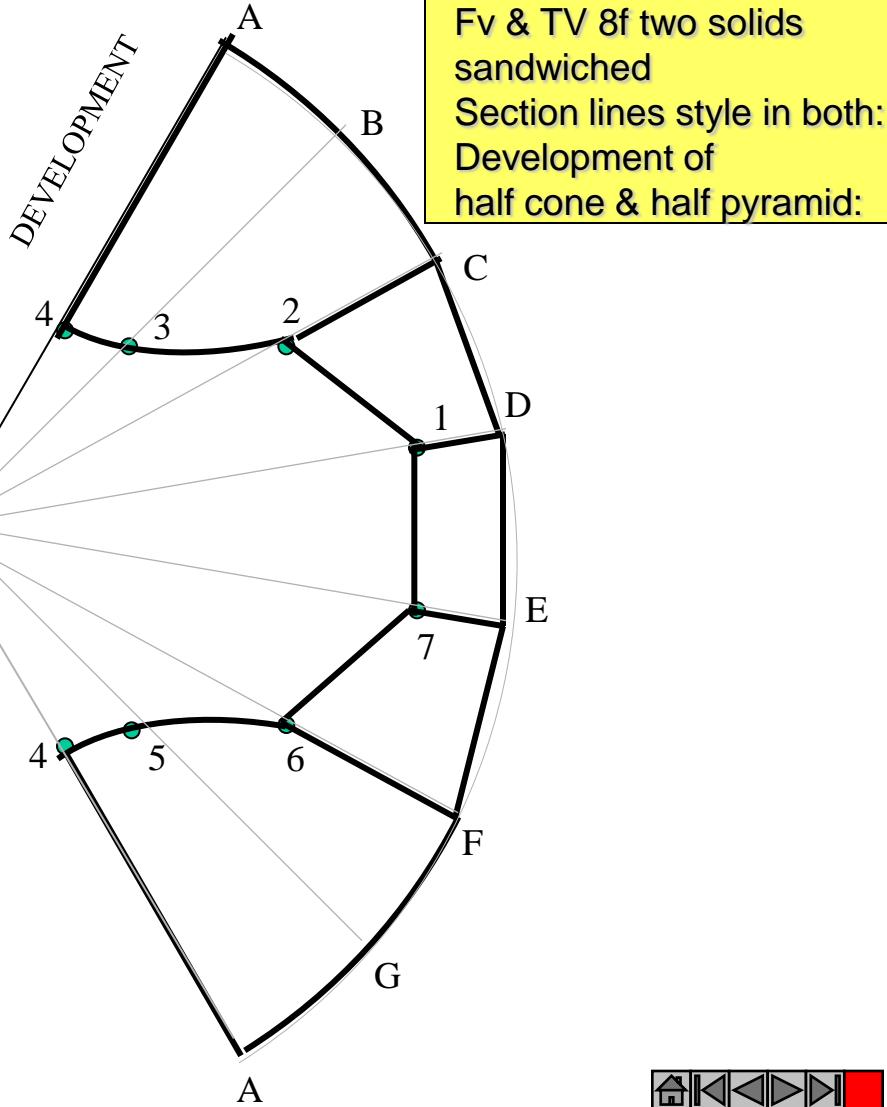
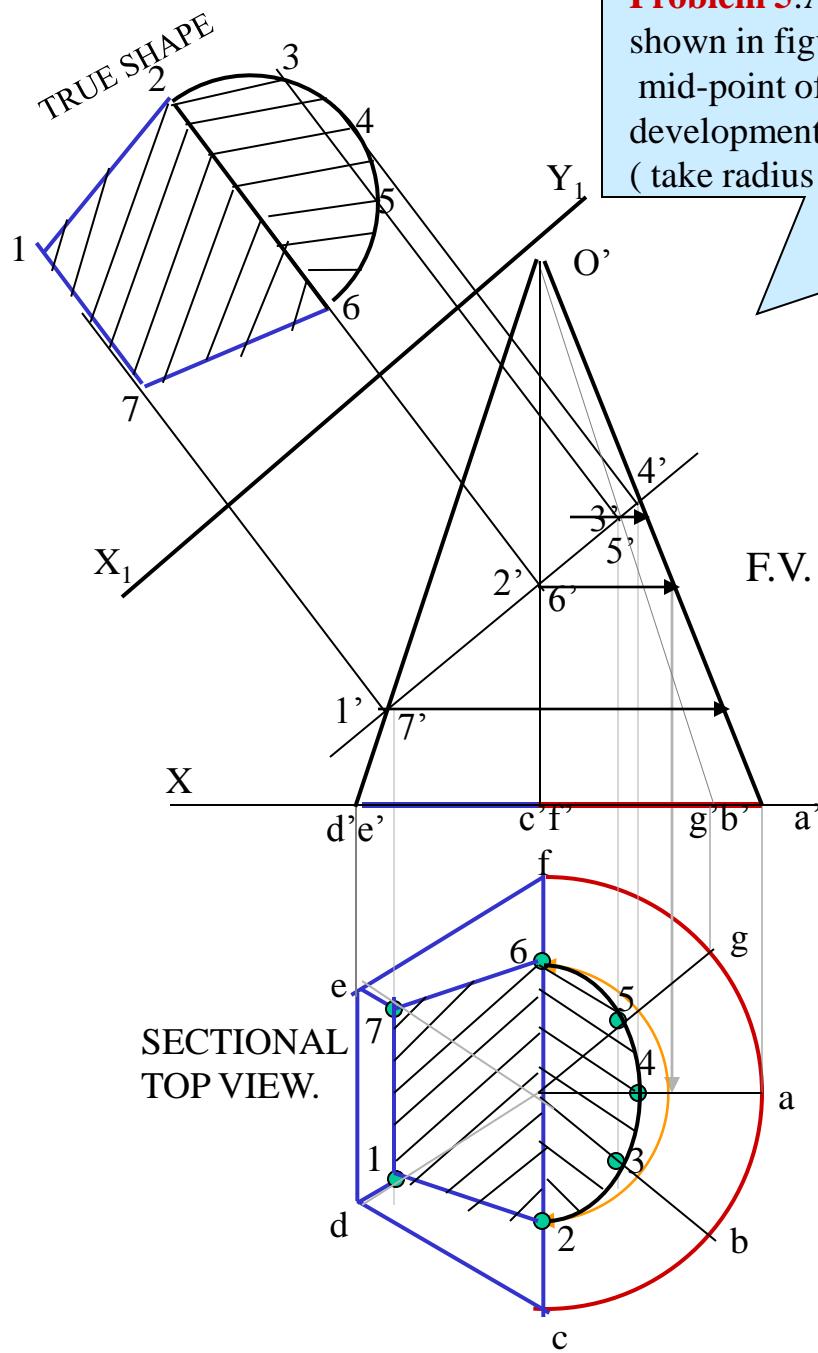
Use similar steps for sec.views & true shape.
NOTE: for development, always cut open object from From an edge in the boundary of the view in which sec.plane appears as a line.
Here it is Tv and in boundary, there is c1 edge.Hence it is opened from c and named C,D,E,F,A,B,C.

A.V.P30° inclined to Vp
Through mid-point of axis.

AS SECTION PLANE IS IN T.V.,
CUT OPEN FROM BOUNDARY EDGE C_l FOR DEVELOPMENT.

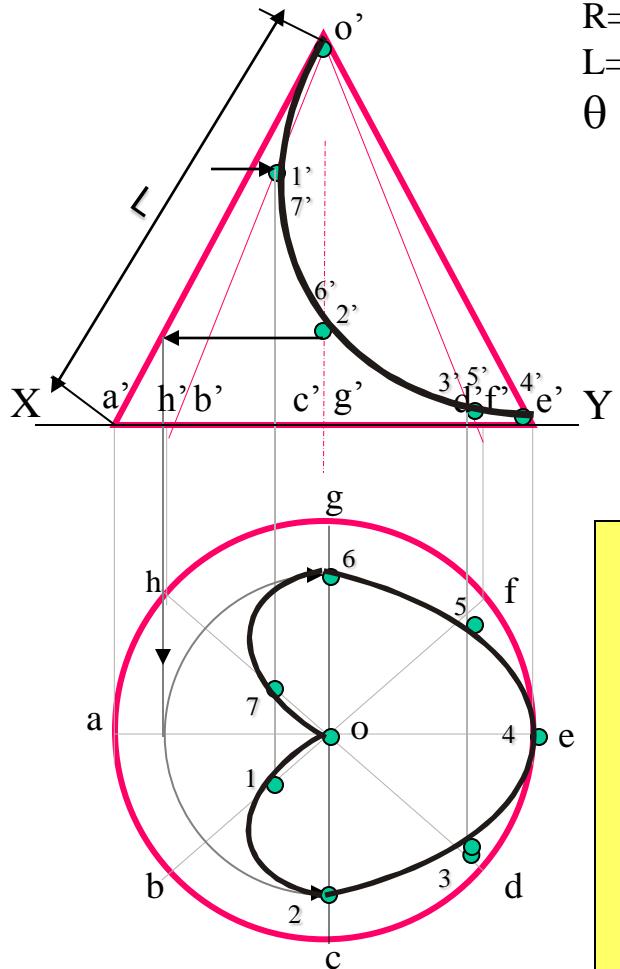


Problem 5: A solid composed of a half-cone and half-hexagonal pyramid is shown in figure. It is cut by a section plane 45^0 inclined to Hp, passing through mid-point of axis. Draw F.v., sectional T.v., true shape of section and development of remaining part of the solid.
(take radius of cone and each side of hexagon 30mm long and axis 70mm.)



Problem 6: Draw a semicircle of 100 mm diameter and inscribe in it a largest circle. If the semicircle is development of a cone and inscribed circle is some curve on it, then draw the projections of cone showing that curve.

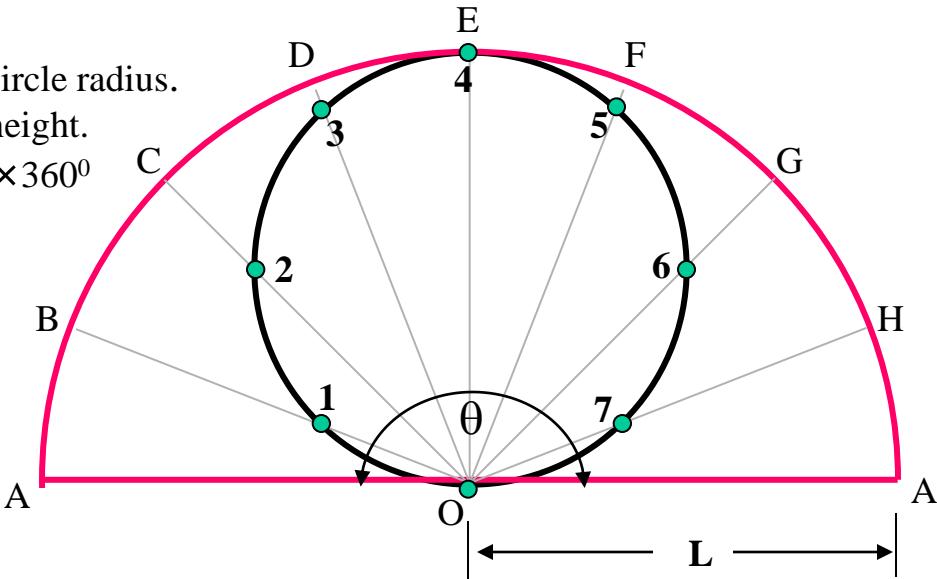
TO DRAW PRINCIPAL VIEWS FROM GIVEN DEVELOPMENT.



R=Base circle radius.

L=Slant height.

$$\theta = \frac{R}{L} \times 360^\circ$$

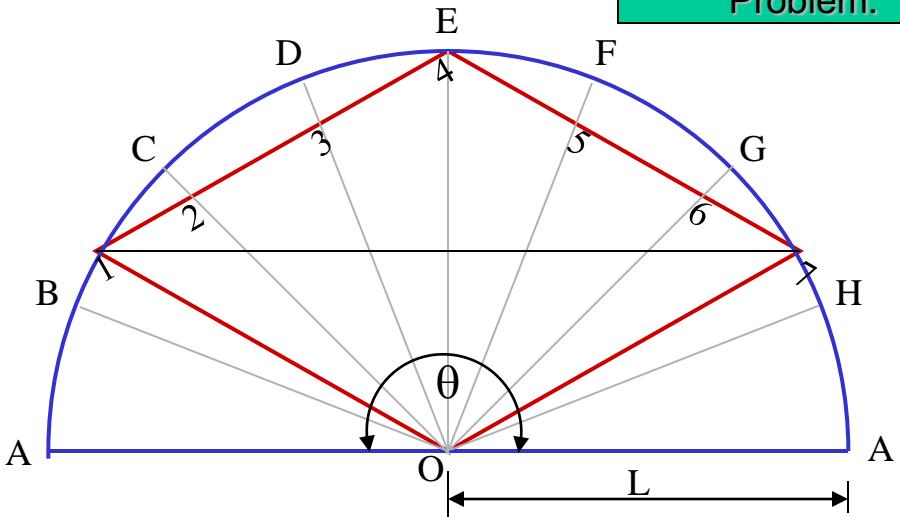
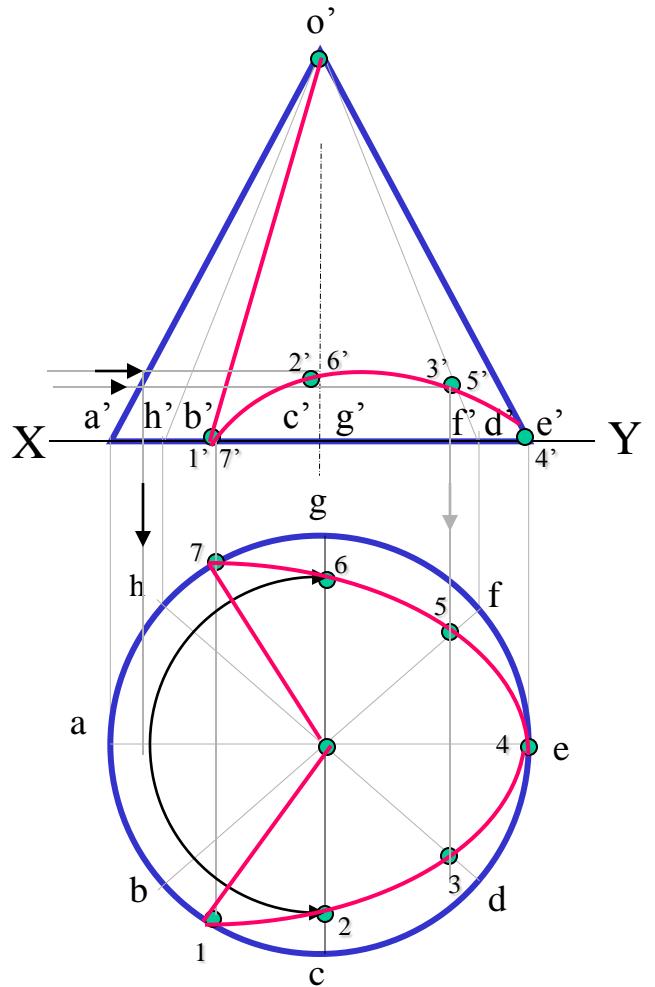


Solution Steps:

Draw semicircle of given diameter, divide it in 8 Parts and inscribe in it a largest circle as shown. Name intersecting points 1, 2, 3 etc. Semicircle being dev.of a cone it's radius is slant height of cone. (L) Then using above formula find R of base of cone. Using this data draw Fv & Tv of cone and form 8 generators and name. Take o -1 distance from dev., mark on TL i.e. o'a' on Fv & bring on o'b' and name 1' Similarly locate all points on Fv. Then project all on Tv on respective generators and join by smooth curve.

TO DRAW PRINCIPAL VIEWS FROM GIVEN DEVELOPMENT.

Problem 7: Draw a semicircle of 100 mm diameter and inscribe in it a largest rhombus. If the semicircle is development of a cone and rhombus is some curve on it, then draw the projections of cone showing that curve.



R=Base circle radius.

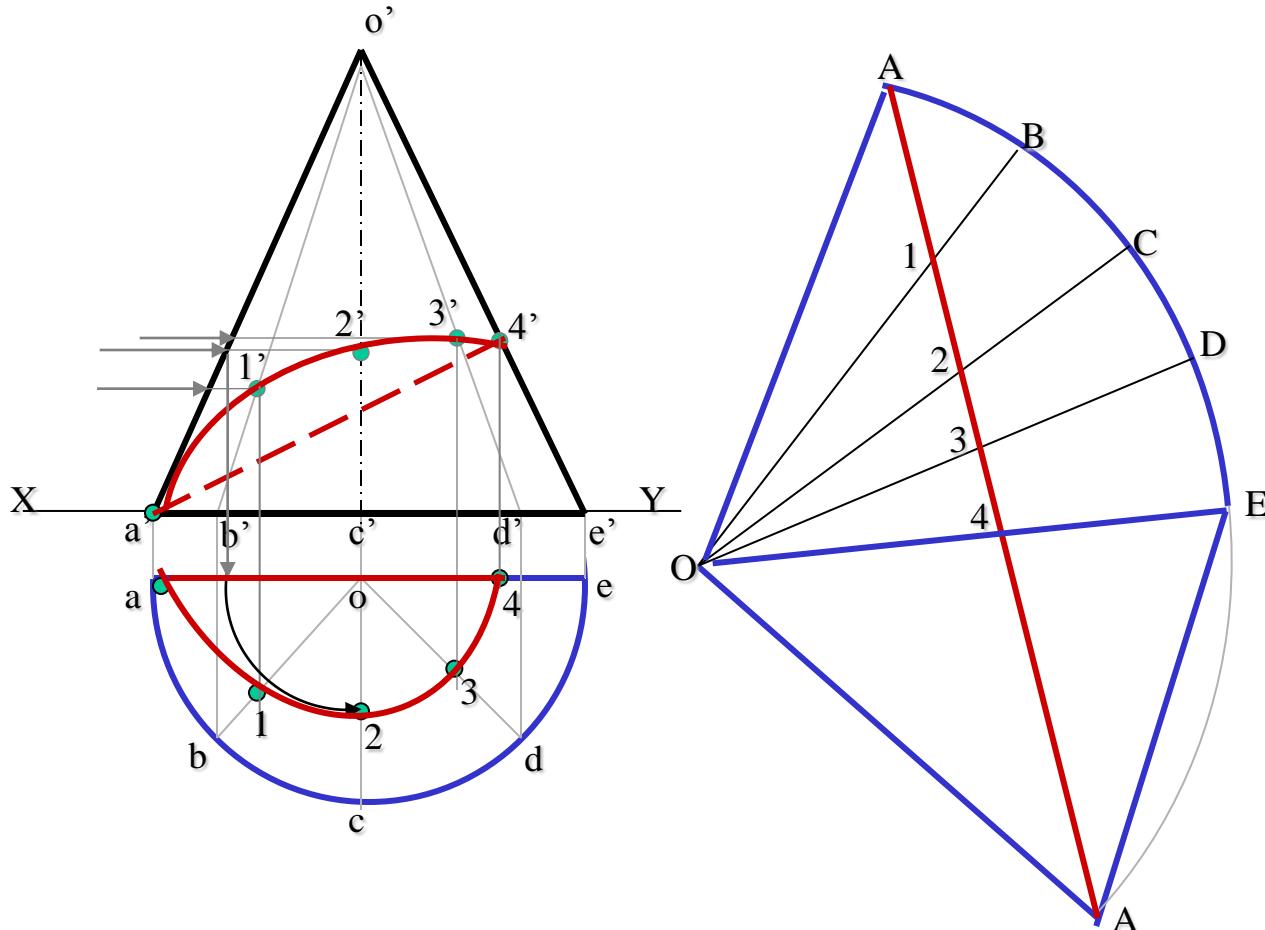
L=Slant height.

$$\theta = \frac{R}{L} \times 360^\circ$$

Solution Steps:
Similar to previous Problem:

Problem 8: A half cone of 50 mm base diameter, 70 mm axis, is standing on it's half base on HP with it's flat face parallel and nearer to VP. An inextensible string is wound round it's surface from one point of base circle and brought back to the same point. If the string is of **shortest length**, find it and show it on the projections of the cone.

TO DRAW A CURVE ON PRINCIPAL VIEWS FROM DEVELOPMENT.

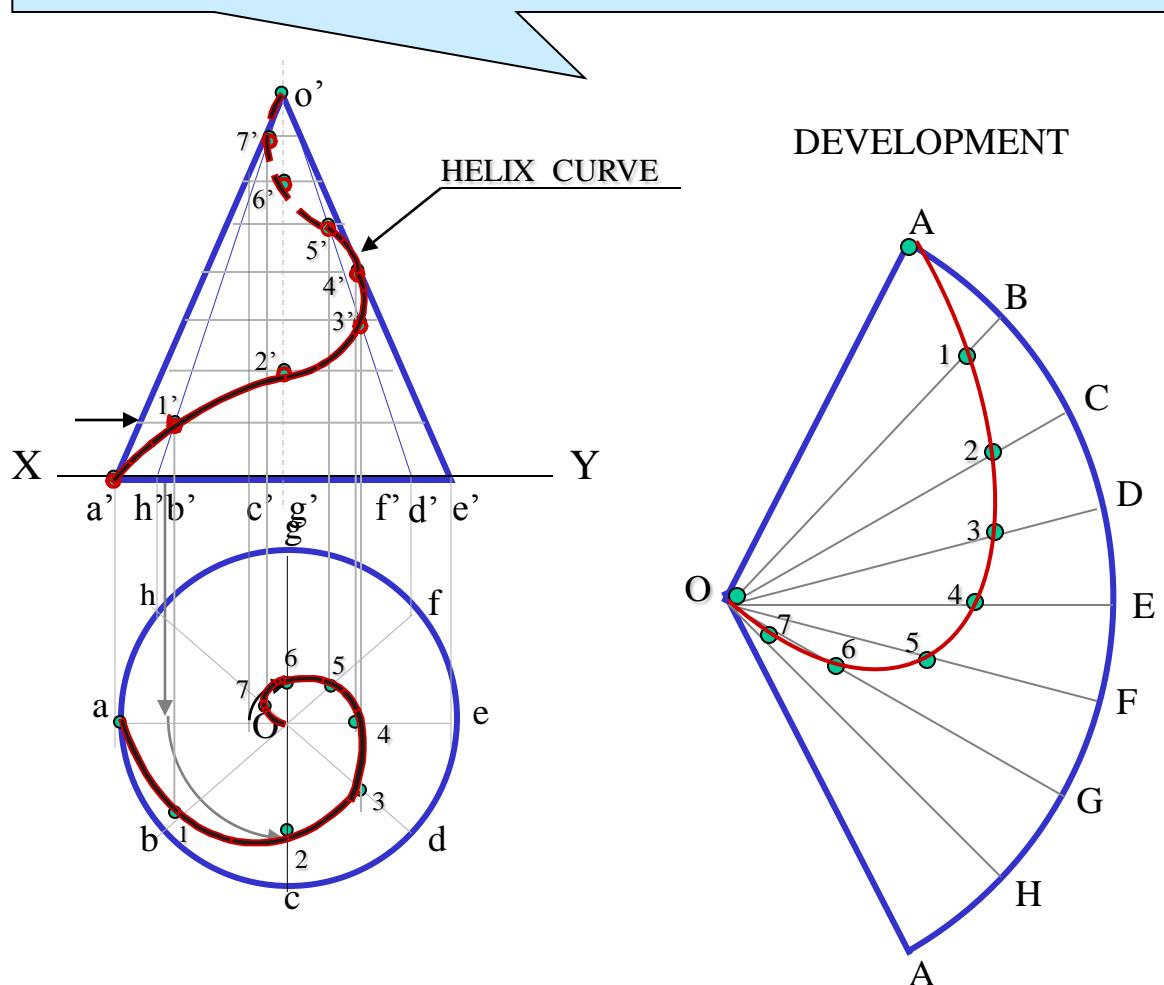


Concept: A string wound from a point up to the same Point, of shortest length Must appear st. line on it's Development.

Solution steps:
Hence draw development, Name it as usual and join A to A This is shortest Length of that string.
Further steps are as usual. On dev. Name the points of Intersections of this line with Different generators.Bring Those on Fv & Tv and join by smooth curves.
Draw 4' a' part of string dotted As it is on back side of cone.

Problem 9: A particle which is initially on base circle of a cone, standing on Hp, moves upwards and reaches apex in one complete turn around the cone. Draw it's path on projections of cone as well as on its development.

Take base circle diameter 50 mm and axis 70 mm long.



It's a construction of curve Helix of one turn on cone:

Draw Fv & Tv & dev.as usual
On all form generators & name.

Construction of curve Helix::

Show 8 generators on both views
Divide axis also in same parts.
Draw horizontal lines from those
points on both end generators.

1' is a point where first horizontal
Line & gen. b'o' intersect.

2' is a point where second horiz.
Line & gen. c'o' intersect.

In this way locate all points on Fv.
Project all on Tv.Join in curvature.

For Development:

Then taking each points true
Distance From resp.generator
from apex, Mark on development
& join.

INTERPENETRATION OF SOLIDS

WHEN ONE SOLID PENETRATES ANOTHER SOLID THEN THEIR SURFACES INTERSECT AND AT THE JUNCTION OF INTERSECTION A TYPICAL CURVE IS FORMED, WHICH REMAINS COMMON TO BOTH SOLIDS.

THIS CURVE IS CALLED **CURVE OF INTERSECTION** AND IT IS A RESULT OF INTERPENETRATION OF SOLIDS.

PURPOSE OF DRAWING THESE CURVES:-

WHEN TWO OBJECTS ARE TO BE JOINED TOGETHER, MAXIMUM SURFACE CONTACT BETWEEN BOTH BECOMES A BASIC REQUIREMENT FOR STRONGEST & LEAK-PROOF JOINT.

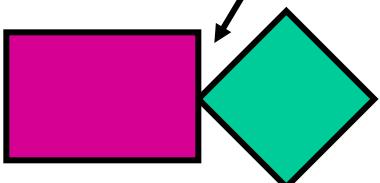
Curves of Intersections being common to both Intersecting solids, show exact & maximum surface contact of both solids.

Study Following Illustrations Carefully.

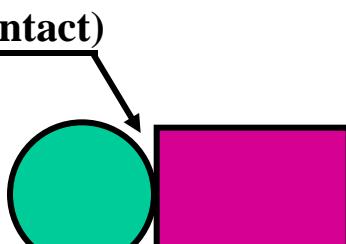


Minimum Surface Contact.

(Point Contact)



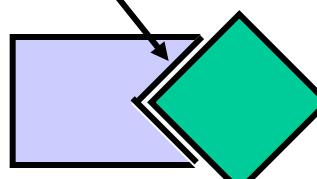
Square Pipes.



Circular Pipes.

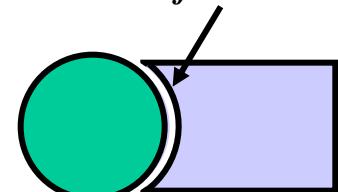
(Maximum Surface Contact)

Lines of Intersections.



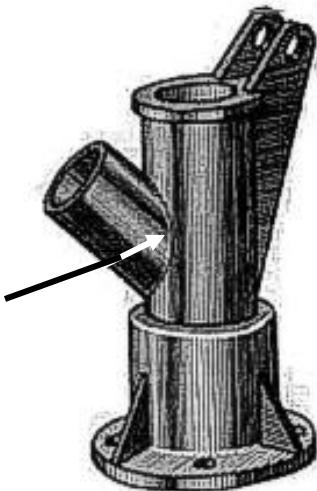
Square Pipes.

Curves of Intersections.

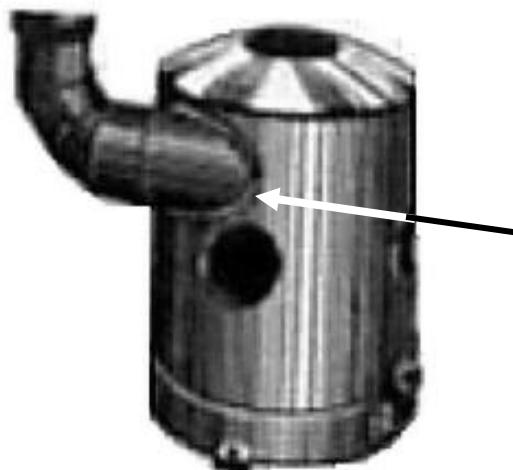


Circular Pipes.

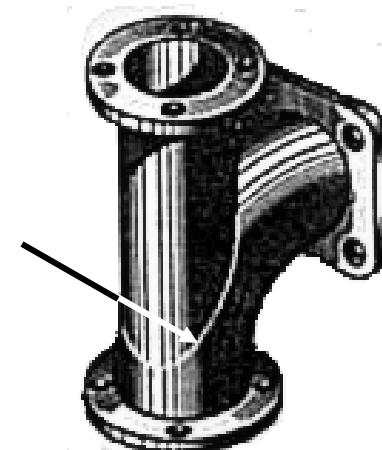
SOME ACTUAL OBJECTS ARE SHOWN, SHOWING CURVES OF INTERSECTIONS. BY WHITE ARROWS.



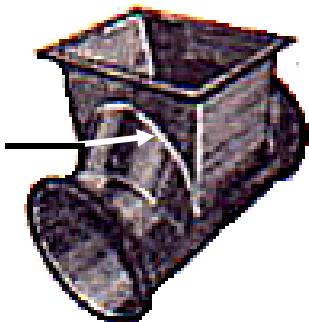
A machine component having two intersecting cylindrical surfaces with the axis at acute angle to each other.



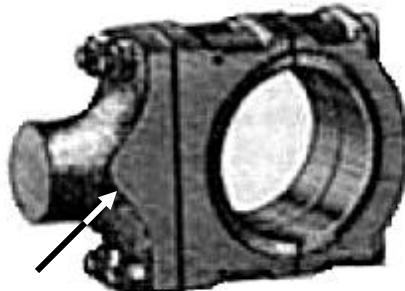
An Industrial Dust collector.
Intersection of two cylinders.



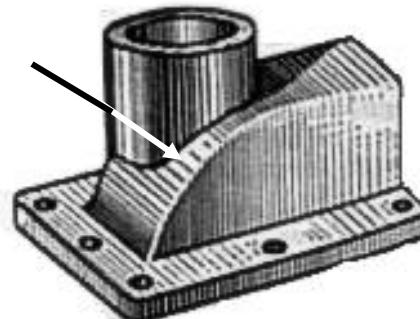
Intersection of a Cylindrical main and Branch Pipe.



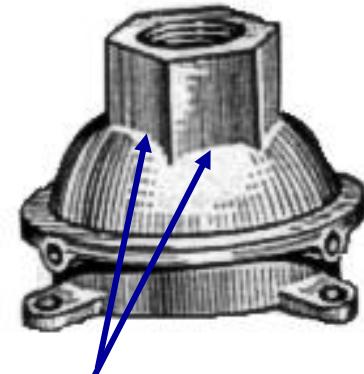
A Feeding Hopper
In industry.



Forged End of a
Connecting Rod.



Two Cylindrical
surfaces.



Pump lid having shape of a hexagonal Prism and Hemi-sphere intersecting each other.

FOLLOWING CASES ARE SOLVED.
REFER ILLUSTRATIONS
AND
NOTE THE COMMON
CONSTRUCTION
FOR ALL

- 1.CYLINDER TO CYLINDER2.
- 2.SQ.PRISM TO CYLINDER
- 3.CONE TO CYLINDER
- 4.TRIANGULAR PRISM TO CYLINDER
- 5.SQ.PRISM TO SQ.PRISM
- 6.SQ.PRISM TO SQ.PRISM
(SKEW POSITION)
- 7.SQUARE PRISM TO CONE (*from top*)
- 8.CYLINDER TO CONE

COMMON SOLUTION STEPS

One solid will be standing on HP
Other will penetrate horizontally.
Draw three views of standing solid.
Name views as per the illustrations.
Beginning with side view draw three
Views of penetrating solids also.
On it's S.V. mark number of points
And name those(either letters or nos.)
The points which are on standard
generators or edges of standing solid,
(in S.V.) can be marked on respective
generators in Fv and Tv. And other
points from SV should be brought to
Tv first and then projecting upward
To Fv.

Dark and dotted line's decision should
be taken by observing side view from
it's right side as shown by arrow.
Accordingly those should be joined
by curvature or straight lines.

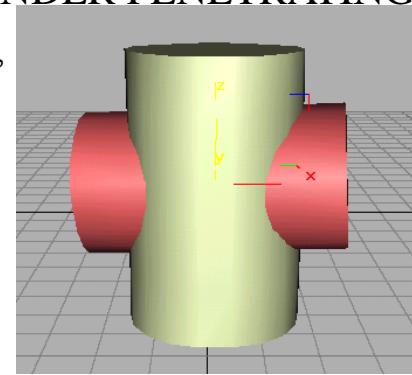
Note:

Incase cone is penetrating solid Side view is not necessary.
Similarly in case of penetration from top it is not required.

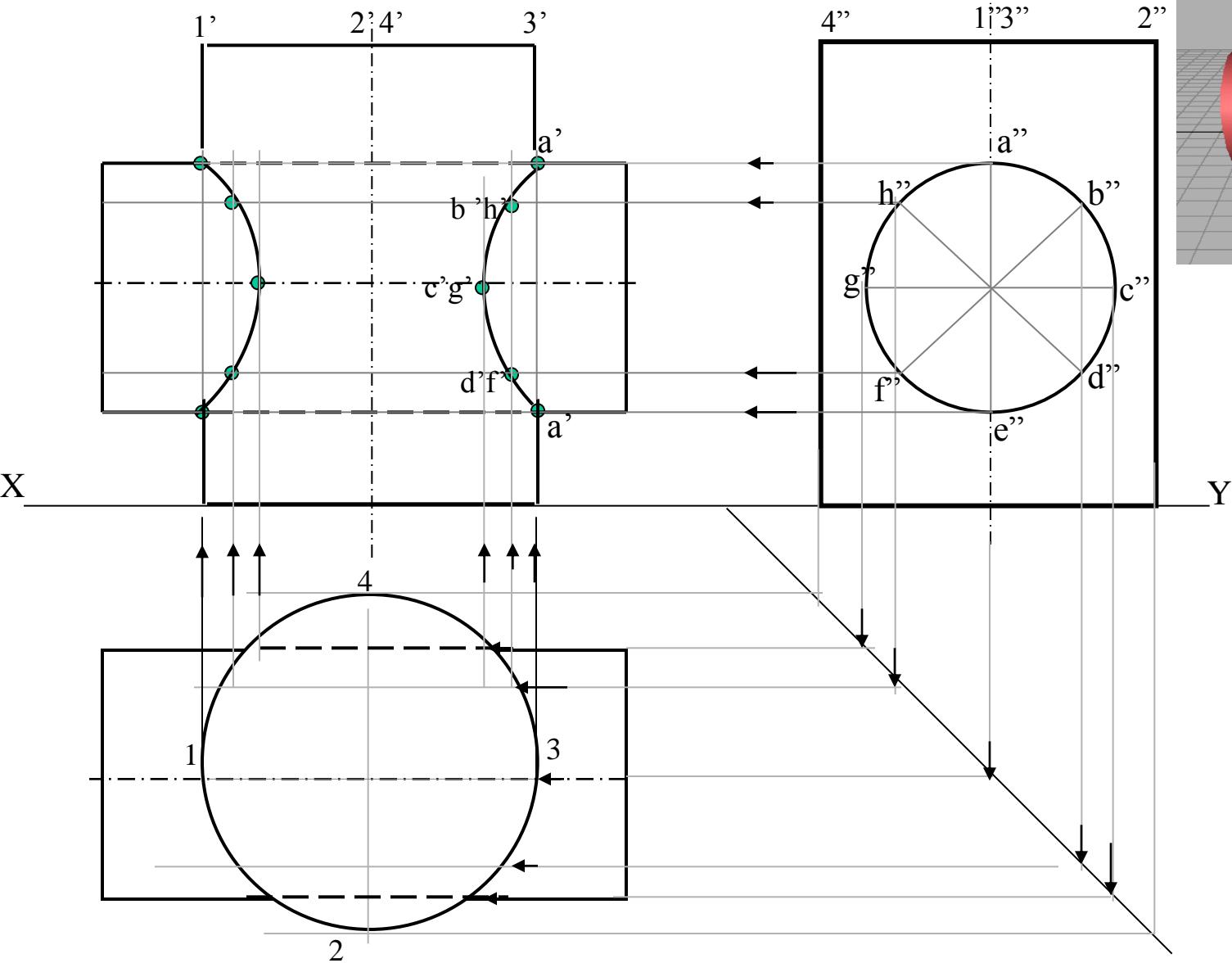
CYLINDER STANDING

&

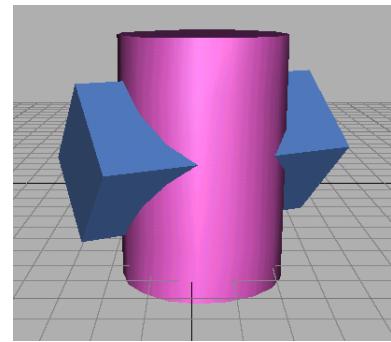
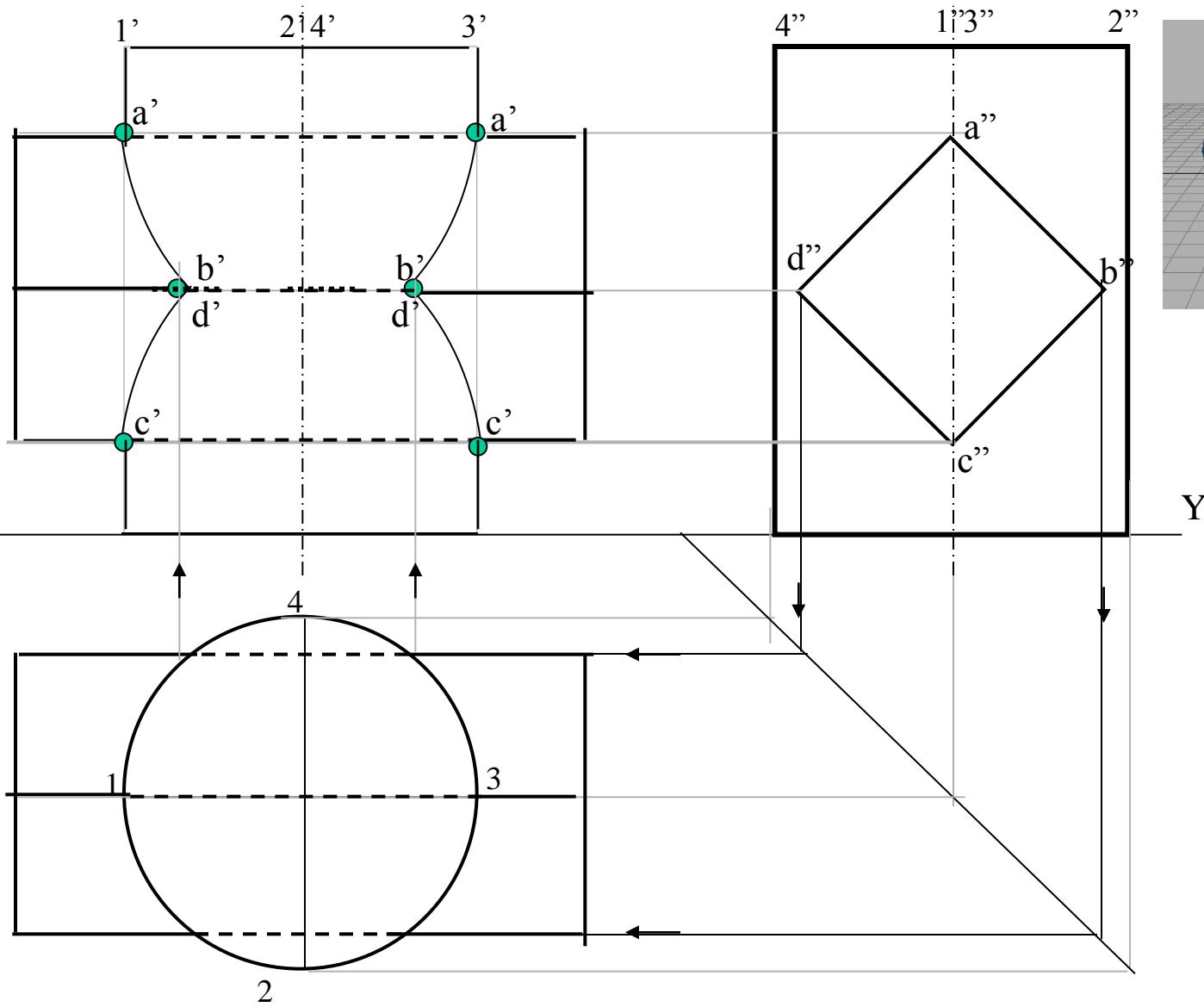
CYLINDER PENETRATING



Problem: A cylinder 50mm dia. and 70mm axis is completely penetrated by another of 40 mm dia. and 70 mm axis horizontally Both axes intersect & bisect each other. Draw projections showing curves of intersections.

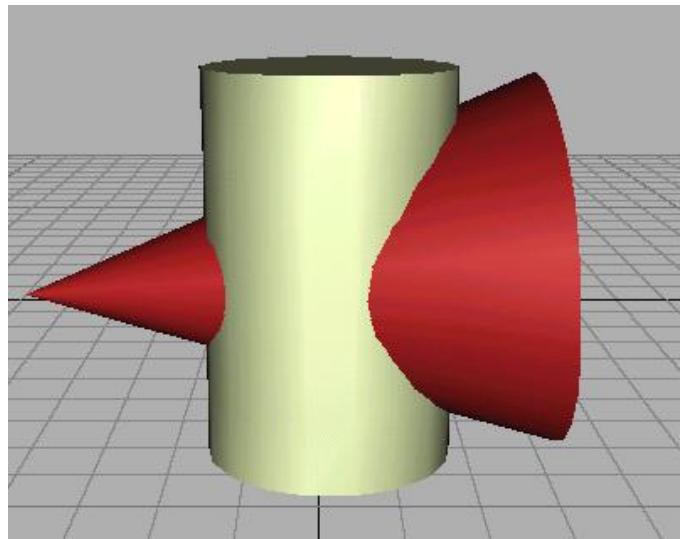
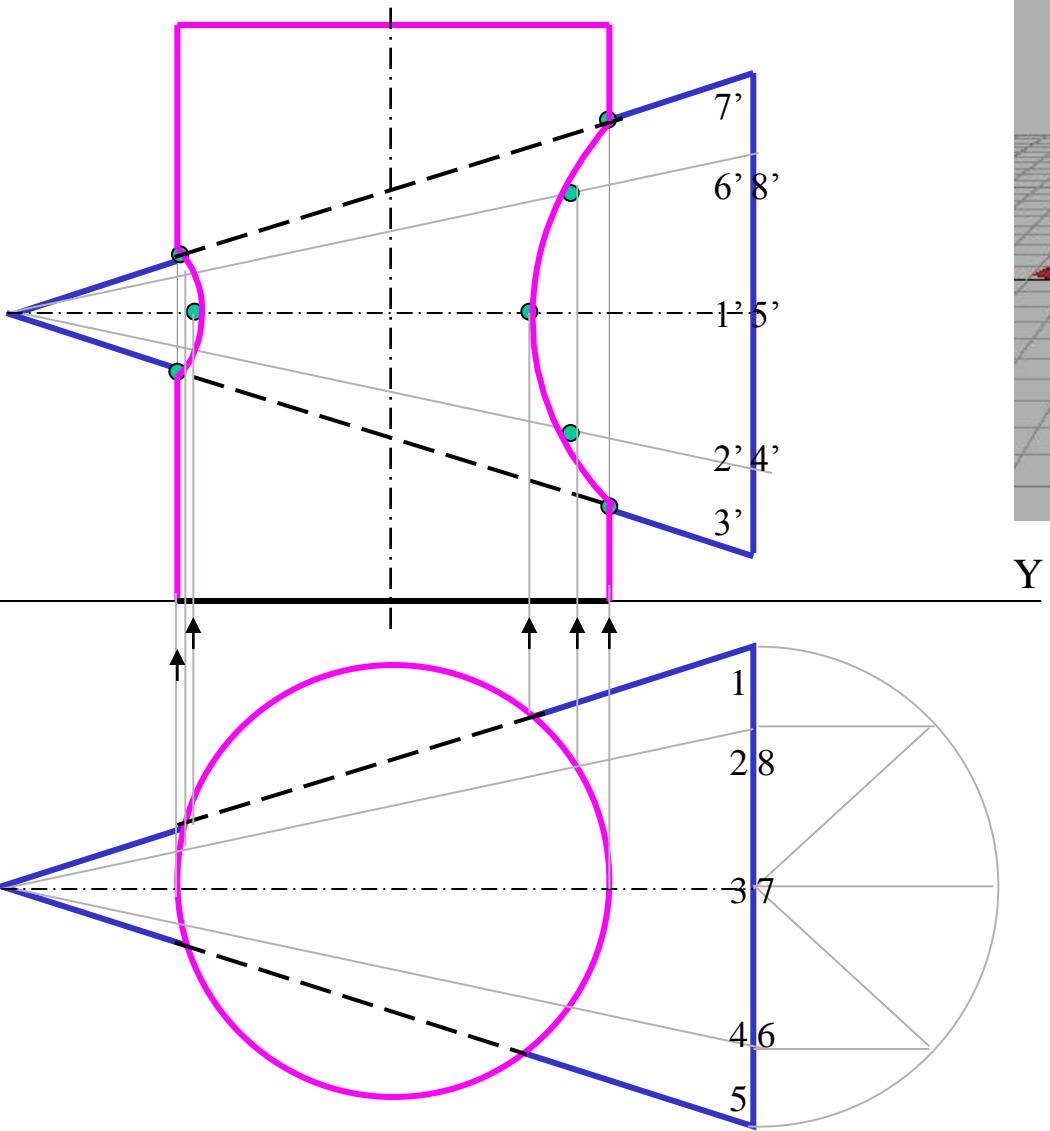


Problem: A cylinder 50mm dia. and 70mm axis is completely penetrated by a square prism of 25 mm sides. and 70 mm axis, horizontally. Both axes Intersect & bisect each other. All faces of prism are equally inclined to Hp. Draw projections showing curves of intersections.



CASE 3.
CYLINDER STANDING
&
CONE PENETRATING

Problem: A cylinder of 80 mm diameter and 100 mm axis is completely penetrated by a cone of 80 mm diameter and 120 mm long axis horizontally. Both axes intersect & bisect each other. Draw projections showing curve of intersections.

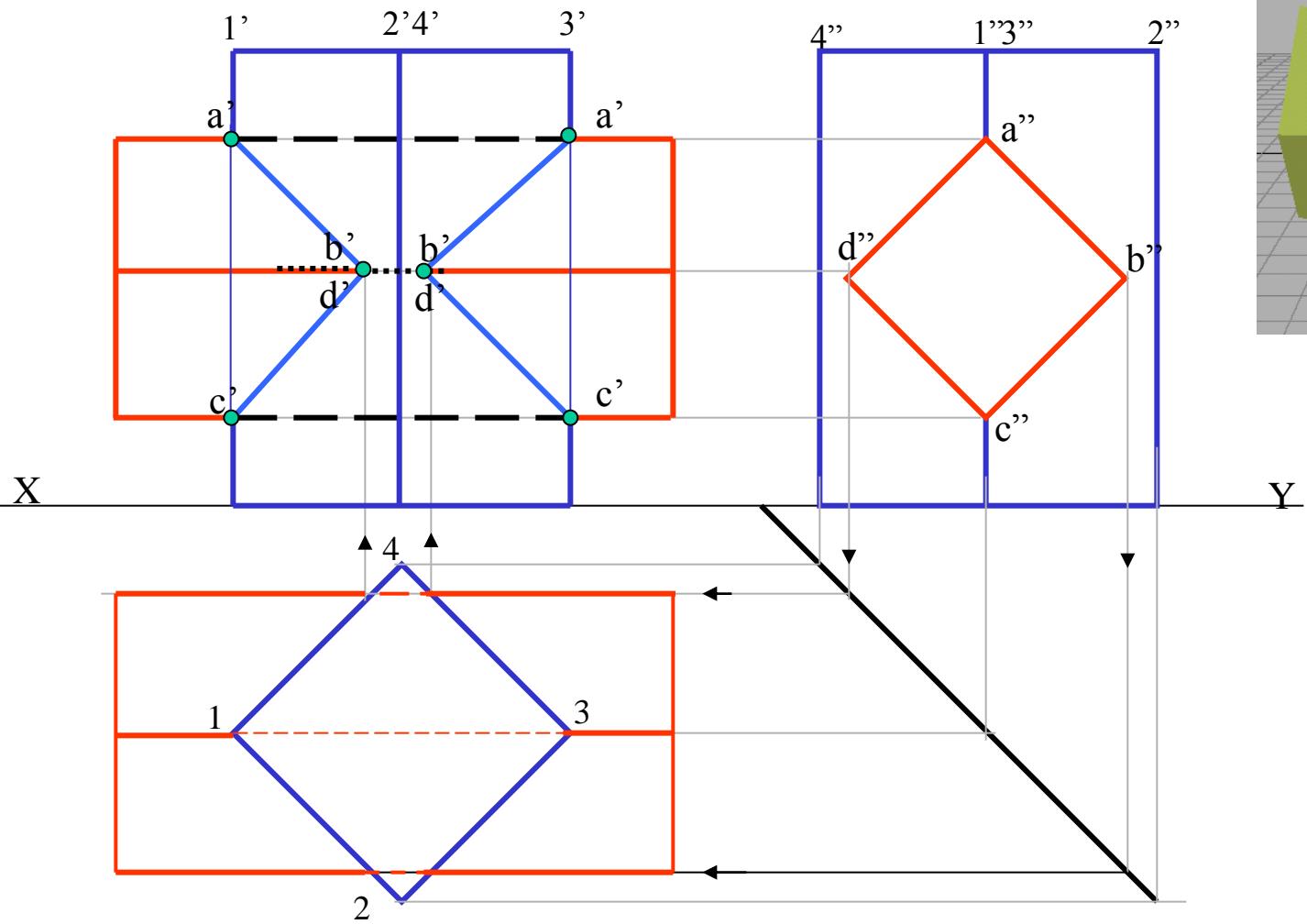
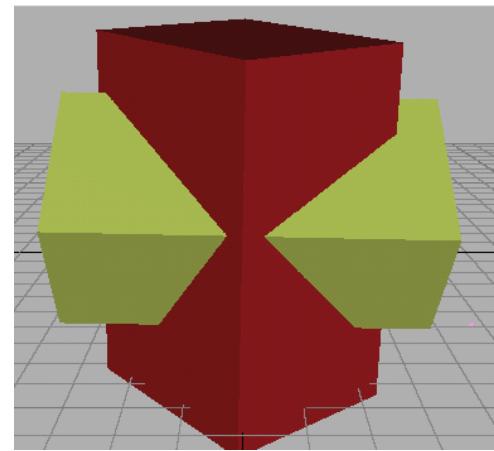


Problem: A sq.prism 30 mm base sides.and 70mm axis is completely penetrated

by another square prism of 25 mm sides.and 70 mm axis, horizontally. Both axes \$Q\$. PRISM STANDING
Intersects & bisect each other. All faces of prisms are equally inclined to Vp.

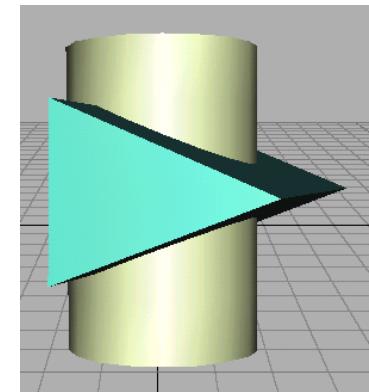
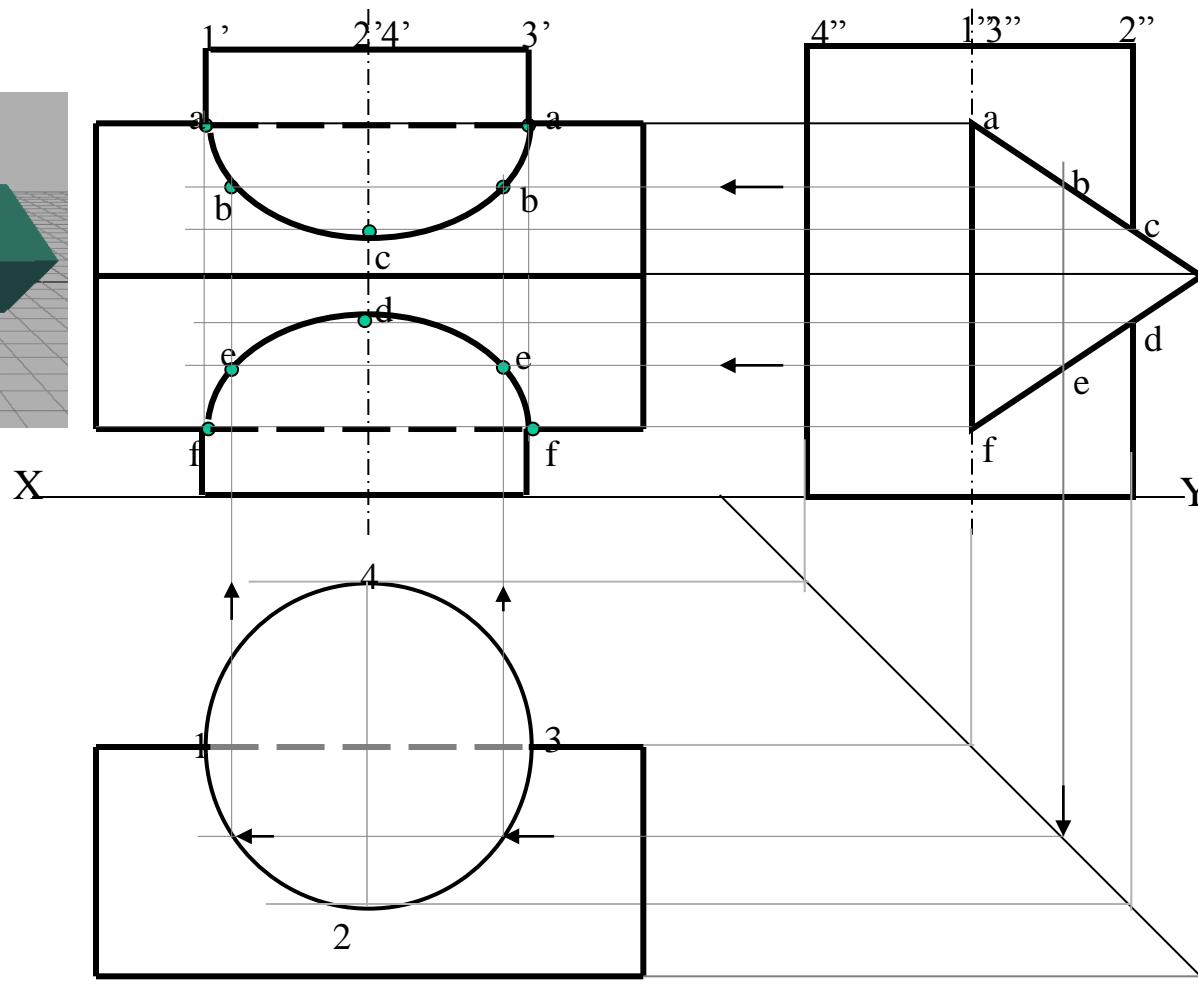
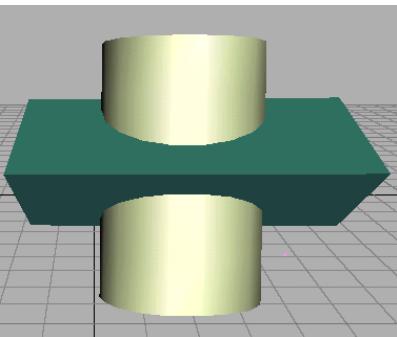
Draw projections showing curves of intersections.

PRISM STANDING &
SQ.PRISM PENETRATING



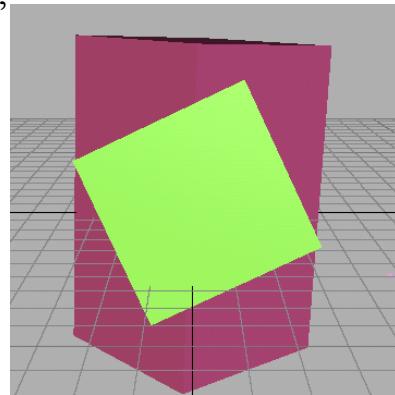
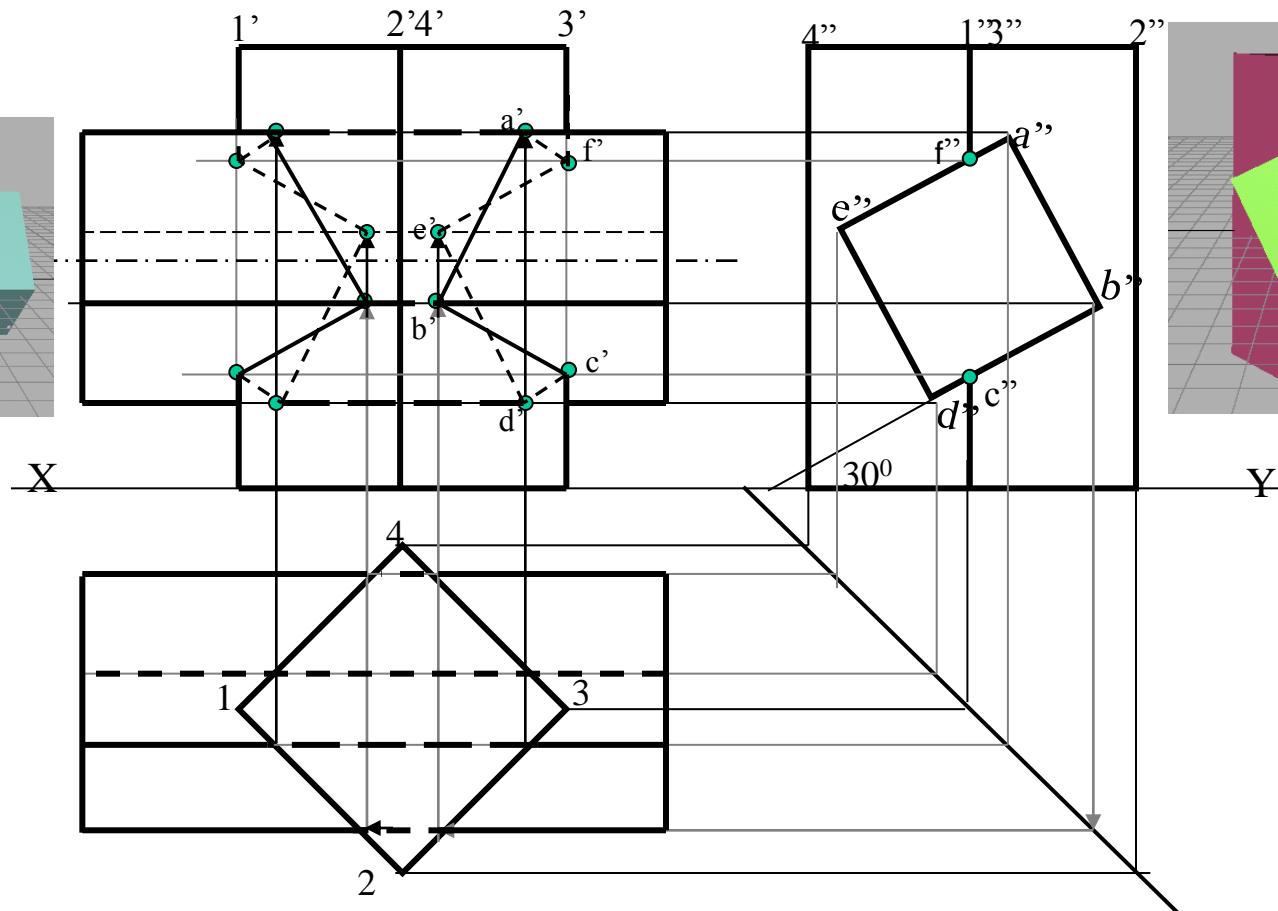
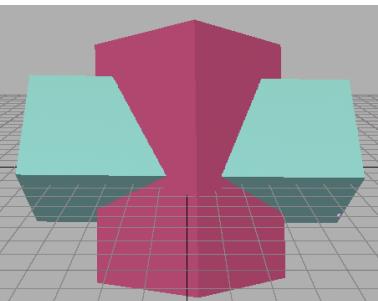
Problem: A cylinder 50mm dia. and 70mm axis is completely penetrated by a triangular prism of 45 mm sides and 70 mm axis, horizontally. One flat face of prism is parallel to Vp and Contains axis of cylinder. Draw projections showing curves of intersections.

CASE 5. CYLINDER STANDING & TRIANGULAR PRISM PENETRATING

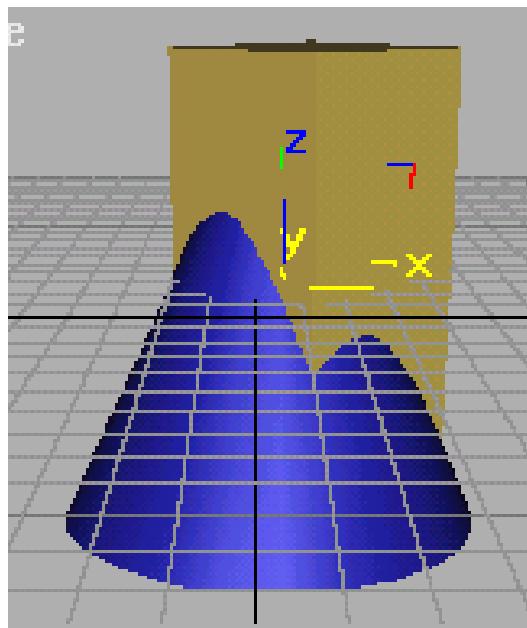
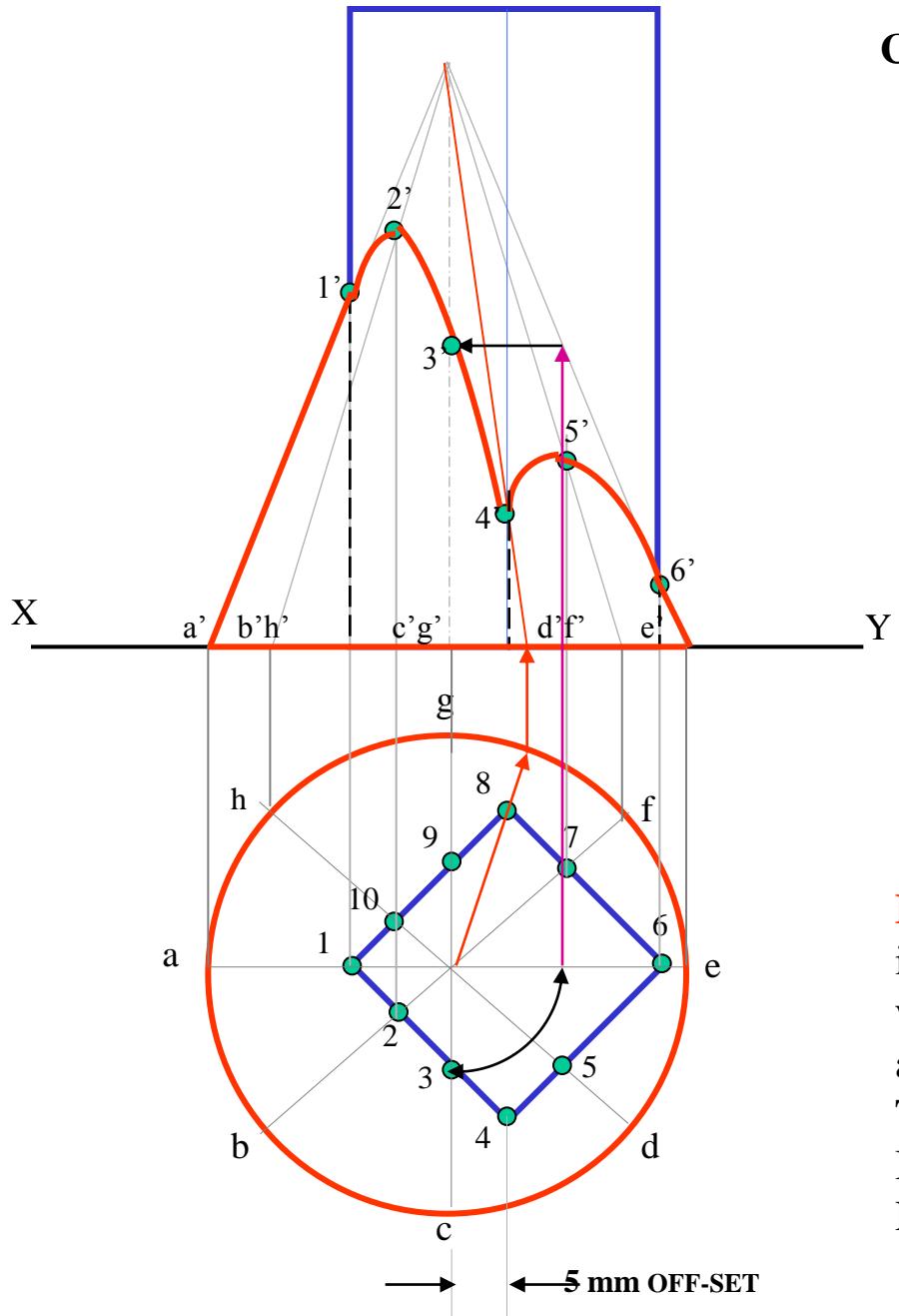


SQ.PRISM STANDING
&SQ.PRISM PENETRATING
(30° SKEW POSITION)

Problem: A sq.prism 30 mm base sides.and 70mm axis is completely penetrated by another square prism of 25 mm side s.and 70 mm axis, horizontally. Both axes Intersect & bisect each other.Two faces of penetrating prism are 30° inclined to Hp. Draw projections showing curves of intersections.



CASE 7.
CONE STANDING & SQ.PRISM PENETRATING
(BOTH AXES VERTICAL)

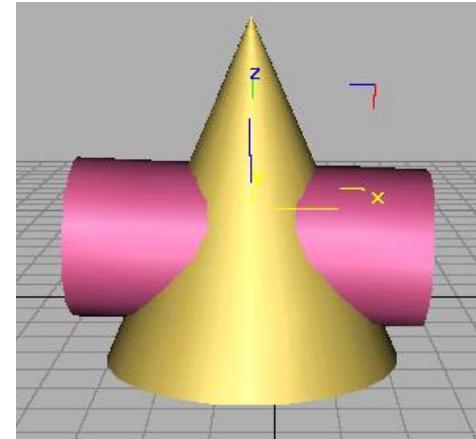


Problem: A cone 70 mm base diameter and 90 mm axis is completely penetrated by a square prism from top with its axis // to cone's axis and 5 mm away from it. a vertical plane containing both axes is parallel to Vp. Take all faces of sq.prism equally inclined to Vp. Base Side of prism is 0 mm and axis is 100 mm long. Draw projections showing curves of intersections.

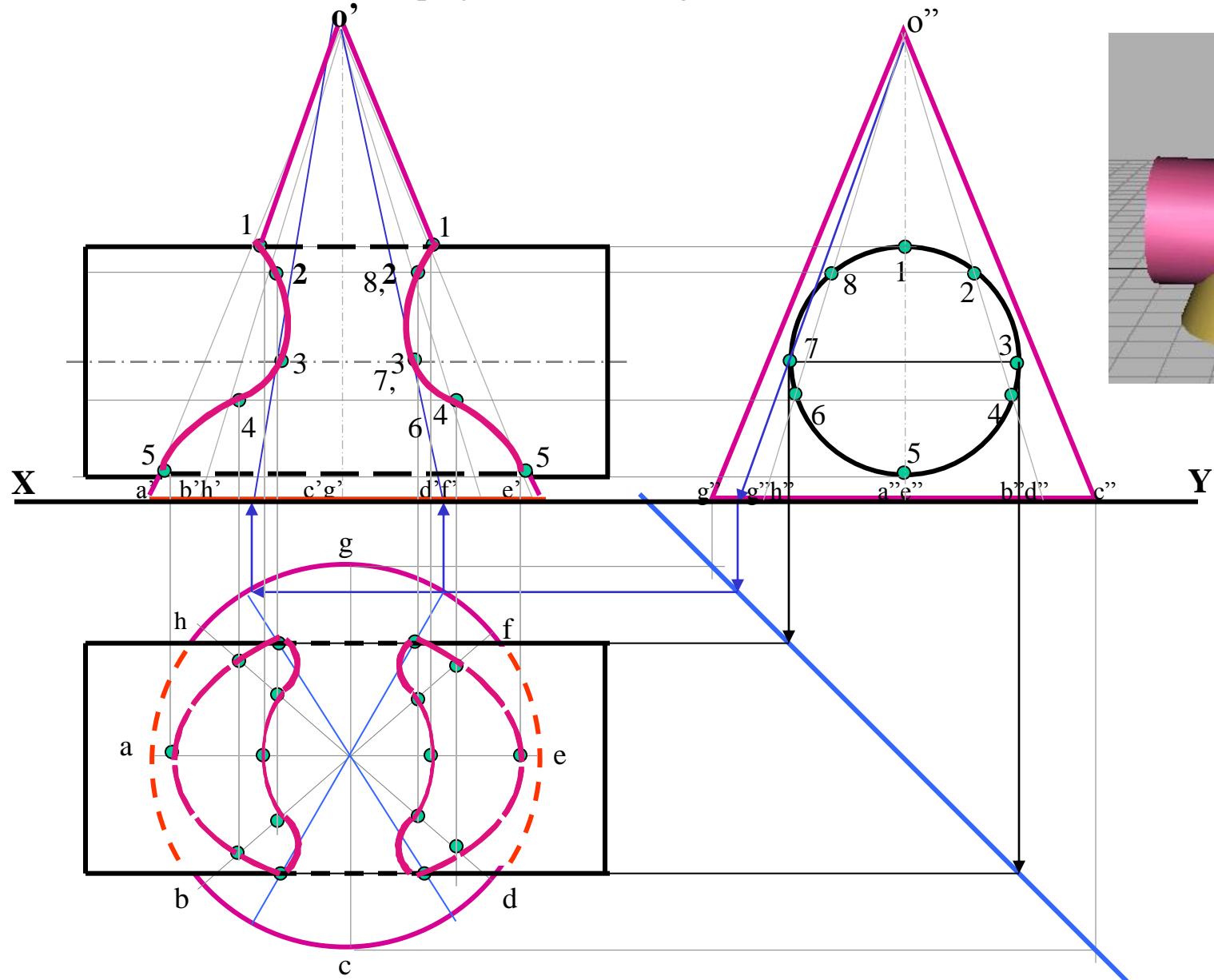
CONE STANDING

&

CYLINDER PENETRATING



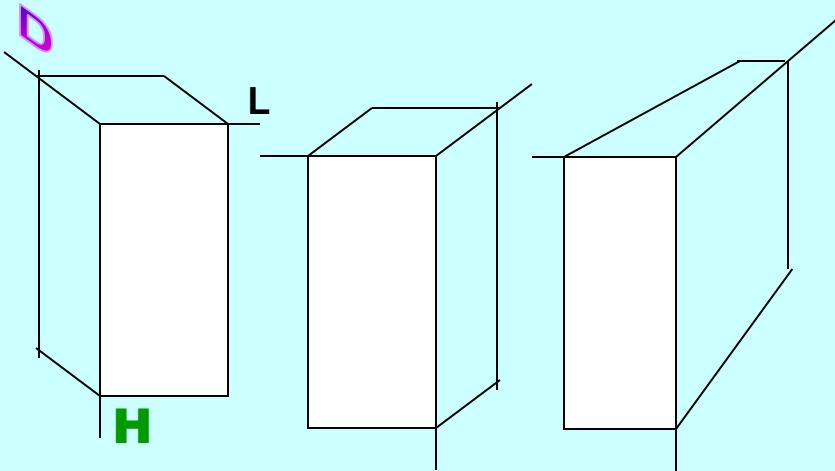
Problem: A vertical cone, base diameter 75 mm and axis 100 mm long, is completely penetrated by a cylinder of 45 mm diameter. The axis of the cylinder is parallel to Hp and Vp and intersects axis of the cone at a point 28 mm above the base. Draw projections showing curves of intersection.



ISOMETRIC DRAWING

IT IS A TYPE OF PICTORIAL PROJECTION IN WHICH ALL THREE DIMENSIONS OF AN OBJECT ARE SHOWN IN ONE VIEW AND IF REQUIRED, THEIR ACTUAL SIZES CAN BE MEASURED DIRECTLY FROM IT.

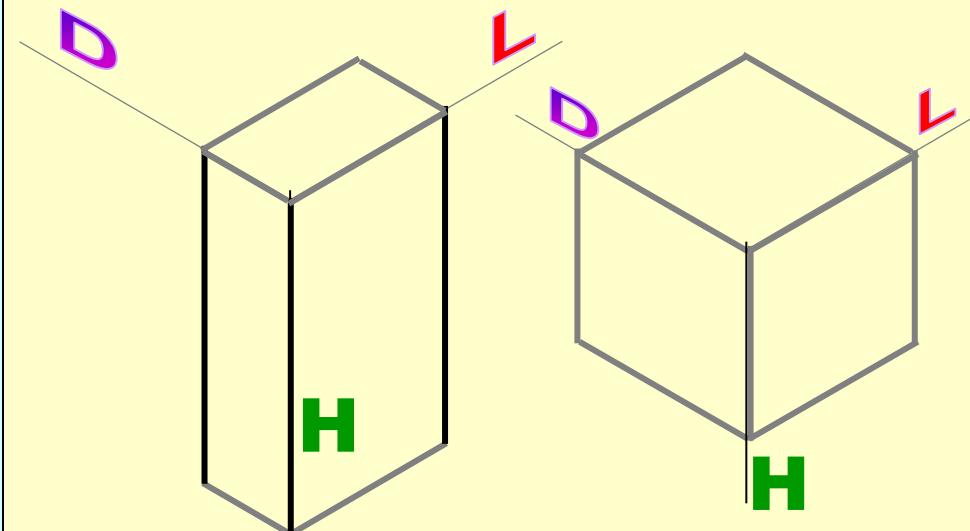
3-D DRAWINGS CAN BE DRAWN IN NUMEROUS WAYS AS SHOWN BELOW. ALL THESE DRAWINGS MAY BE CALLED 3-DIMENSIONAL DRAWINGS, OR PHOTOGRAPHIC OR PICTORIAL DRAWINGS. HERE NO SPECIFIC RELATION AMONG H, L & D AXES IS MAINTAINED.



TYPICAL CONDITION.

IN THIS 3-D DRAWING OF AN OBJECT, ALL THREE DIMENSIONAL AXES ARE MAINTAINED AT EQUAL INCLINATIONS WITH EACH OTHER. (120°)

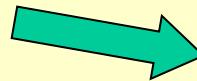
NOW OBSERVE BELOW GIVEN DRAWINGS. ONE CAN NOTE SPECIFIC INCLINATION AMONG H, L & D AXES. ISO MEANS SAME, SIMILAR OR EQUAL. HERE ONE CAN FIND EQUAL INCLINATION AMONG H, L & D AXES. EACH IS 120° INCLINED WITH OTHER TWO. HENCE IT IS CALLED ISOMETRIC DRAWING



PURPOSE OF ISOMETRIC DRAWING IS TO UNDERSTAND OVERALL SHAPE, SIZE & APPEARANCE OF AN OBJECT PRIOR TO ITS PRODUCTION.

SOME IMPORTANT TERMS:

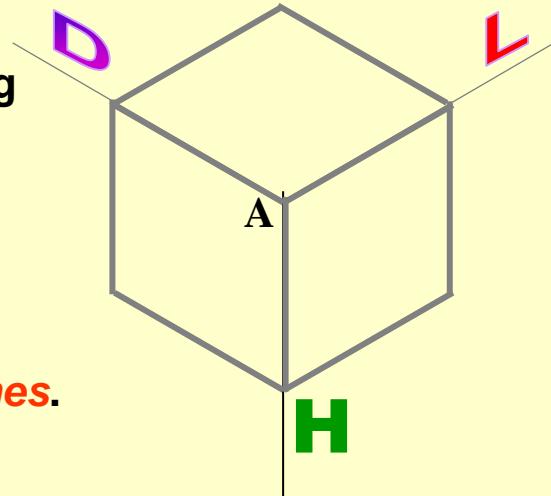
ISOMETRIC AXES, LINES AND PLANES:



The three lines AL, AD and AH, meeting at point A and making 120° angles with each other are termed **Isometric Axes**.

The lines parallel to these axes are called **Isometric Lines**.

The planes representing the faces of the cube as well as other planes parallel to these planes are called **Isometric Planes**.



ISOMETRIC SCALE:

When one holds the object in such a way that all three dimensions are visible then in the process all dimensions become proportionally inclined to observer's eye sight and hence appear apparent in lengths.

This reduction is 0.815 or 9 / 11 (approx.) It forms a reducing scale which is used to draw isometric drawings and is called **Isometric scale**.

In practice, while drawing isometric projection, it is necessary to convert true lengths into isometric lengths for measuring and marking the sizes. This is conveniently done by constructing an isometric scale as described on next page.

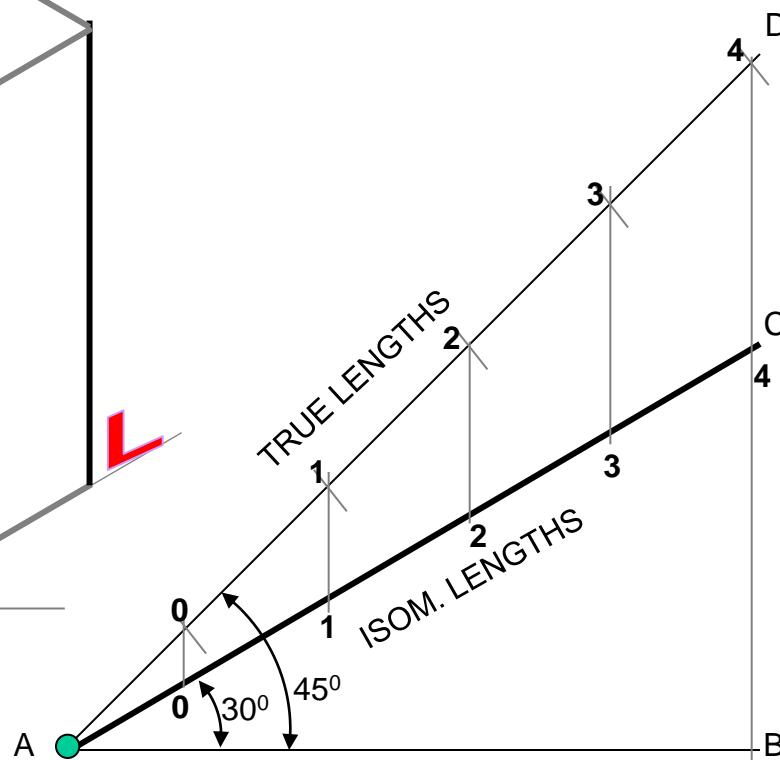
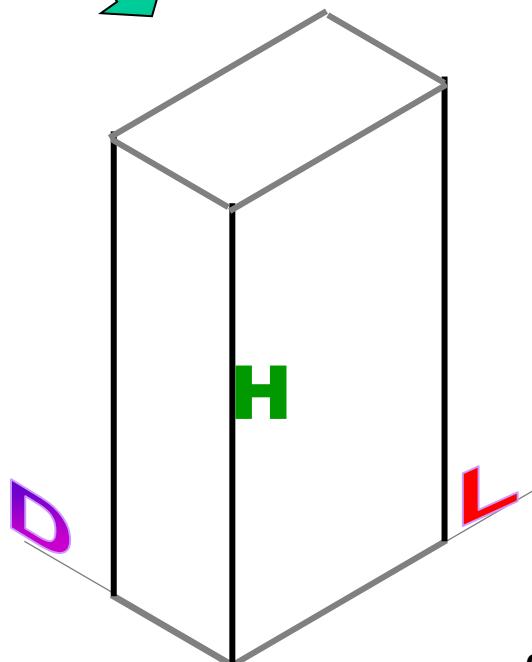
TYPES OF ISOMETRIC DRAWINGS

ISOMETRIC VIEW

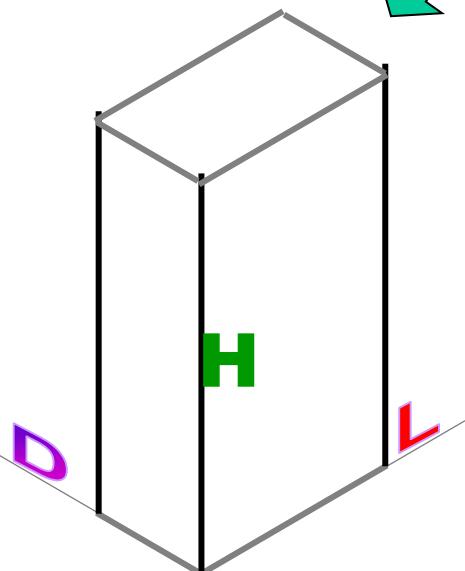
Drawn by using True scale
(True dimensions)

ISOMETRIC PROJECTION

Drawn by using Isometric scale
(Reduced dimensions)



Isometric scale [Line AC]
required for Isometric Projection



CONSTRUCTION OF ISOM. SCALE.
From point A, with line AB draw 30° and 45° inclined lines AC & AD resp on AD. Mark divisions of true length and from each division-point draw vertical lines upto AC line. The divisions thus obtained on AC give lengths on isometric scale.

ISOMETRIC OF PLANE FIGURES

AS THESE ALL ARE
2-D FIGURES
WE REQUIRE ONLY TWO
ISOMETRIC AXES.

IF THE FIGURE IS
FRONT VIEW, H & L
AXES ARE REQUIRED.

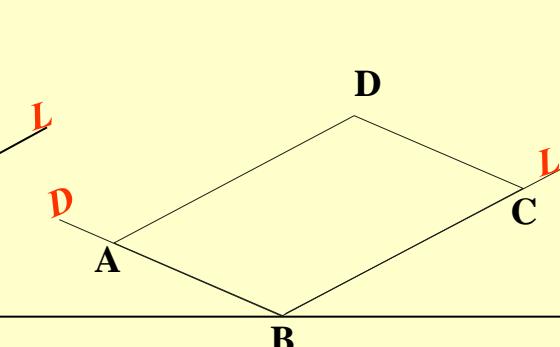
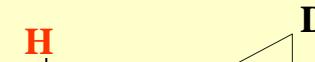
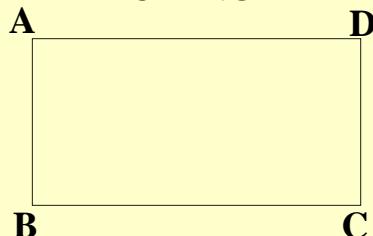
IF THE FIGURE IS TOP
VIEW, D & L AXES ARE
REQUIRED.

Shapes containing
Inclined lines should
be enclosed in a
rectangle as shown.
Then first draw isom.
of that rectangle and
then inscribe that
shape as it is.

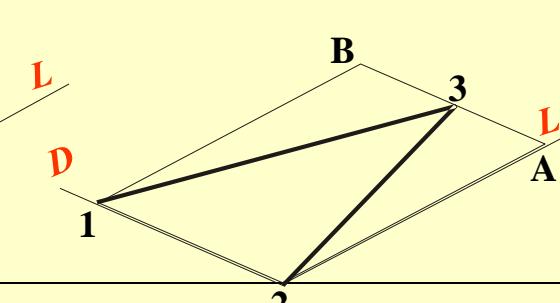
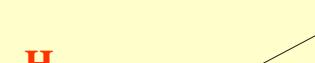
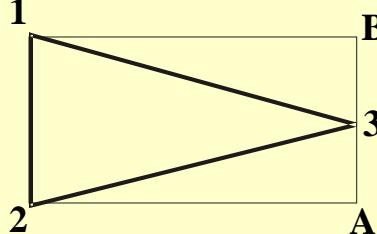
SHAPE

Isometric view if the Shape is
F.V. or T.V.

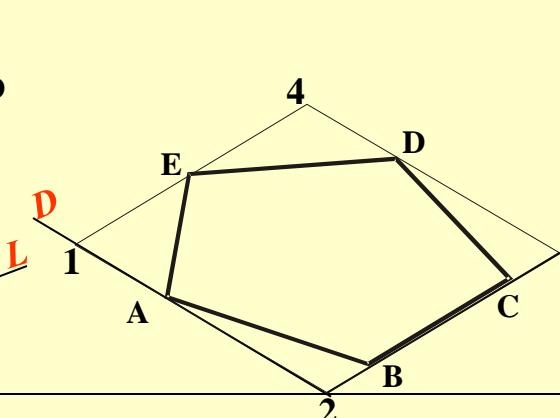
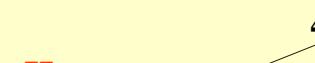
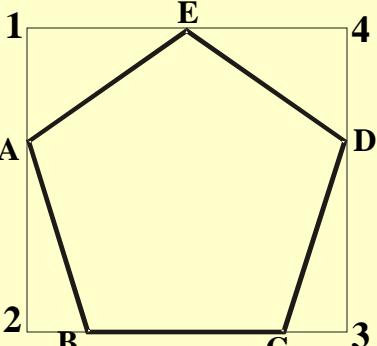
RECTANGLE



TRIANGLE

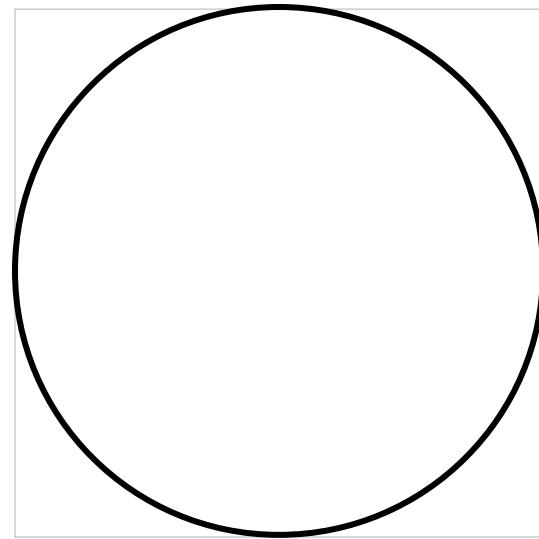


PENTAGON

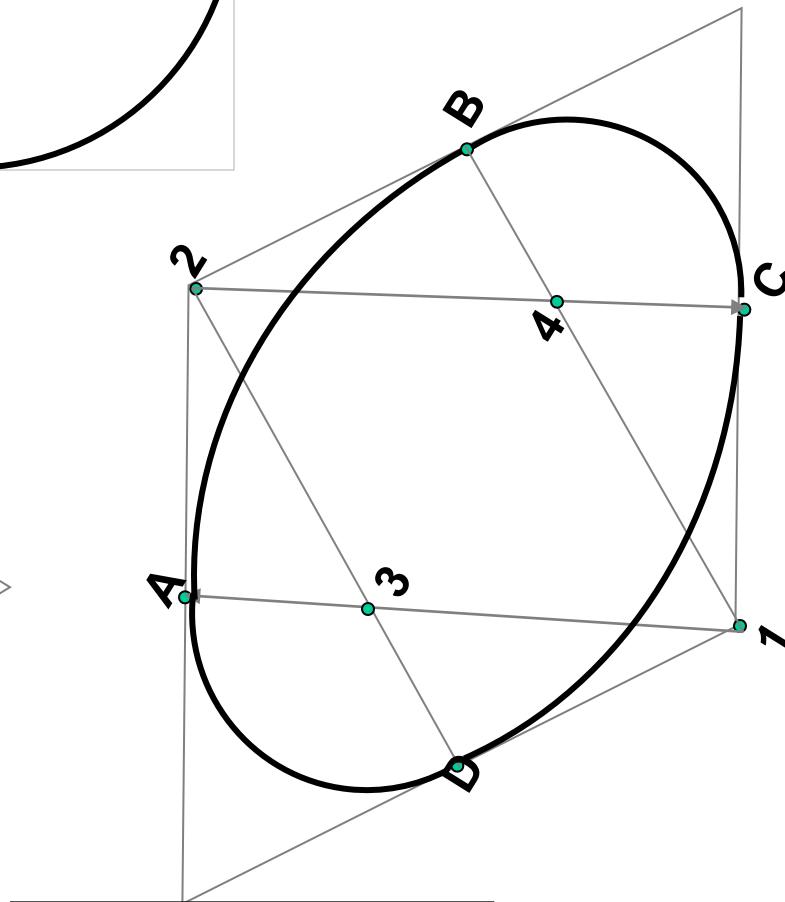
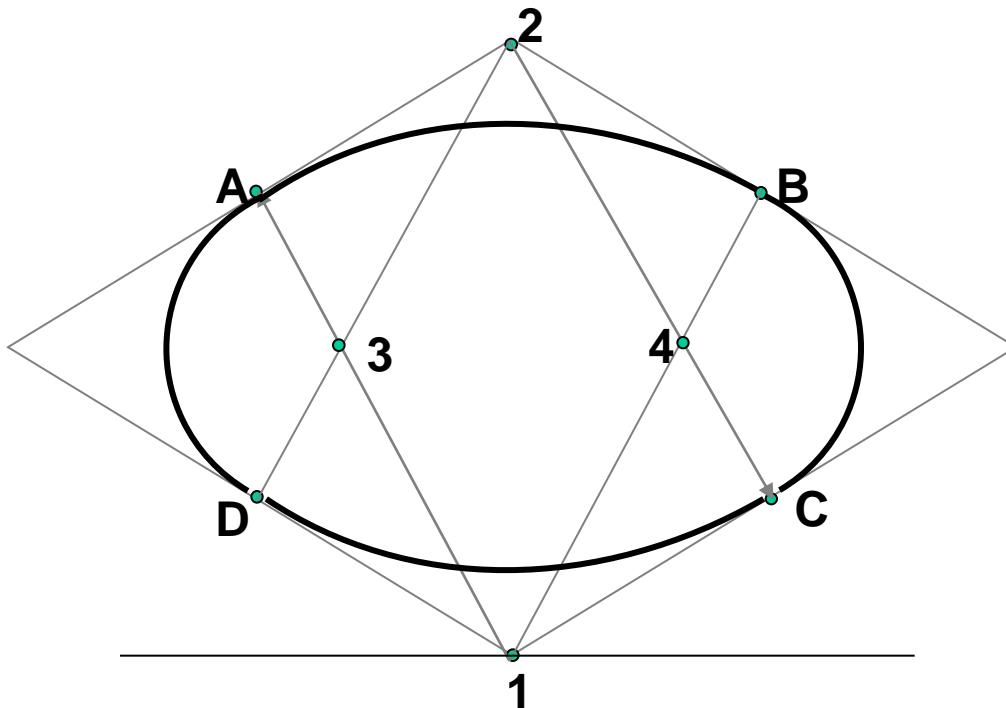


STUDY ILLUSTRATIONS

DRAW ISOMETRIC VIEW OF A CIRCLE IF IT IS A TV OR FV.



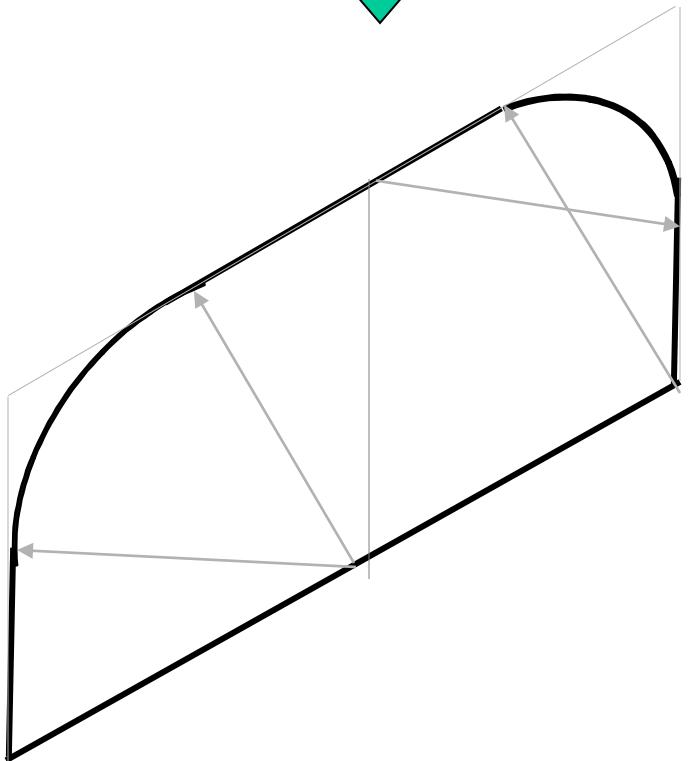
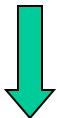
FIRST ENCLOSE IT IN A SQUARE.
IT'S ISOMETRIC IS A RHOMBUS WITH D & L AXES FOR TOP VIEW.
THEN USE H & L AXES FOR ISOMETRIC WHEN IT IS FRONT VIEW.
FOR CONSTRUCTION USE RHOMBUS METHOD SHOWN HERE. STUDY IT.



STUDY ILLUSTRATIONS

DRAW ISOMETRIC VIEW OF THE FIGURE
SHOWN WITH DIMENTIONS (ON RIGHT SIDE)
CONSIDERING IT FIRST AS F.V. AND THEN T.V.

IF FRONT VIEW

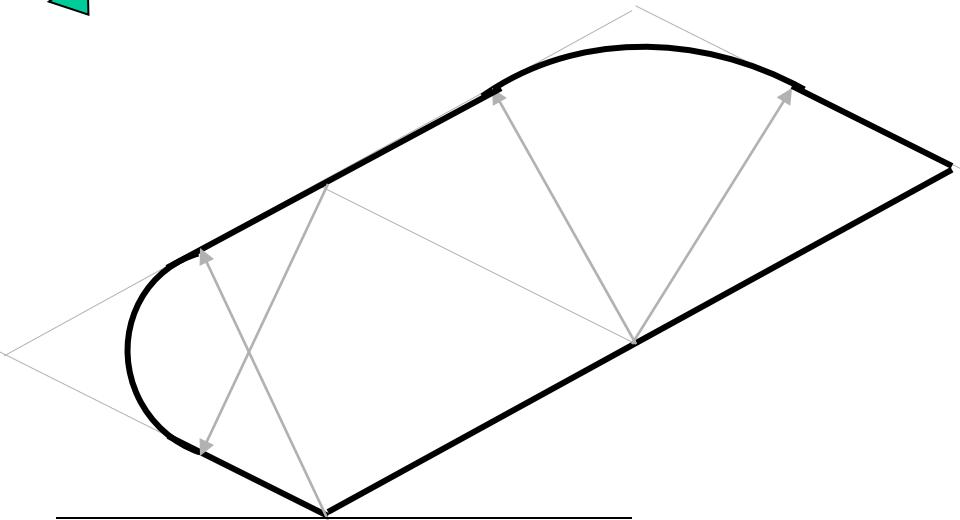


25 R

50 MM

100 MM

IF TOP VIEW



ISOMETRIC OF PLANE FIGURES

AS THESE ALL ARE
2-D FIGURES
WE REQUIRE ONLY
TWO ISOMETRIC
AXES.

**IF THE FIGURE IS
FRONT VIEW, H & L
AXES ARE REQUIRED.**

**IF THE FIGURE IS
TOP VIEW, D & L
AXES ARE REQUIRED.**

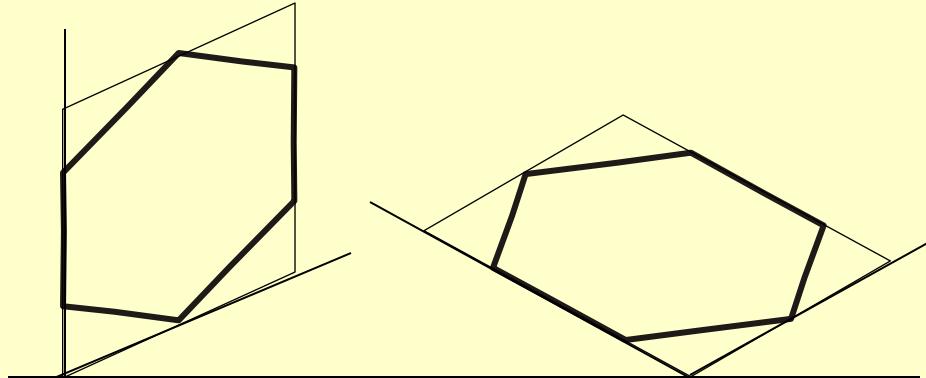
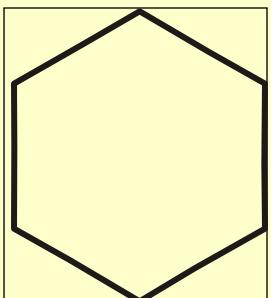
For Isometric of
Circle/Semicircle
use Rhombus method.
Construct it of sides equal
to diameter of circle always.
(Ref. Previous two pages.)

SHAPE

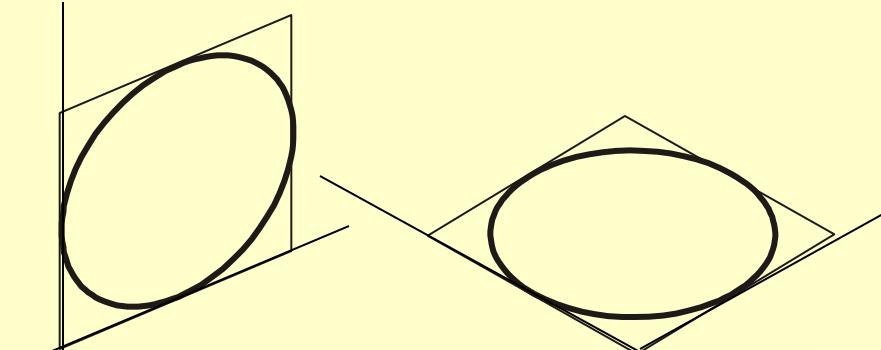
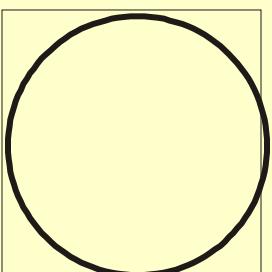
IF F.V.

IF T.V.

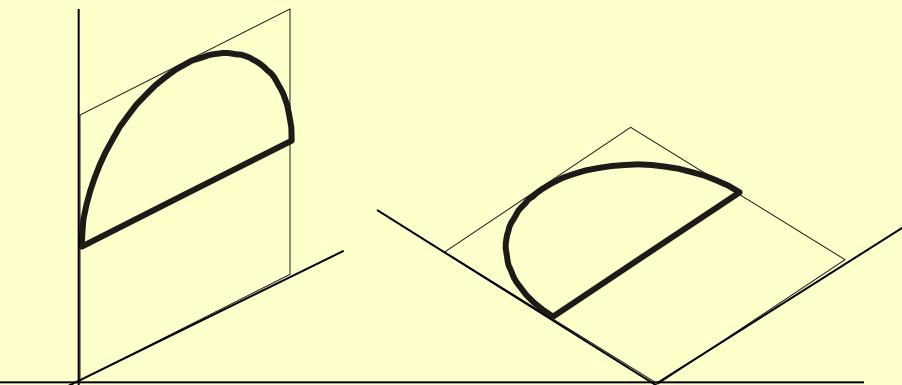
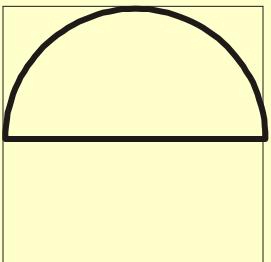
HEXAGON



CIRCLE



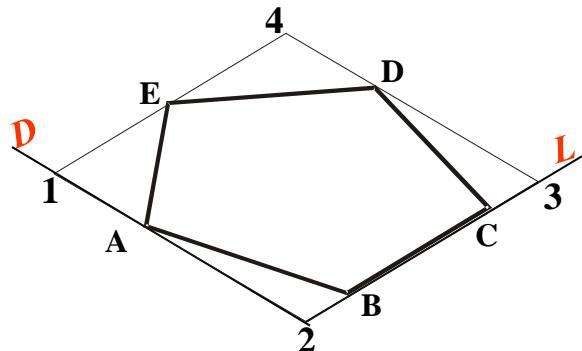
SEMI CIRCLE



For Isometric of Circle/Semicircle use Rhombus method. Construct Rhombus of sides equal to Diameter of circle always. (Ref. topic ENGG. CURVES.)

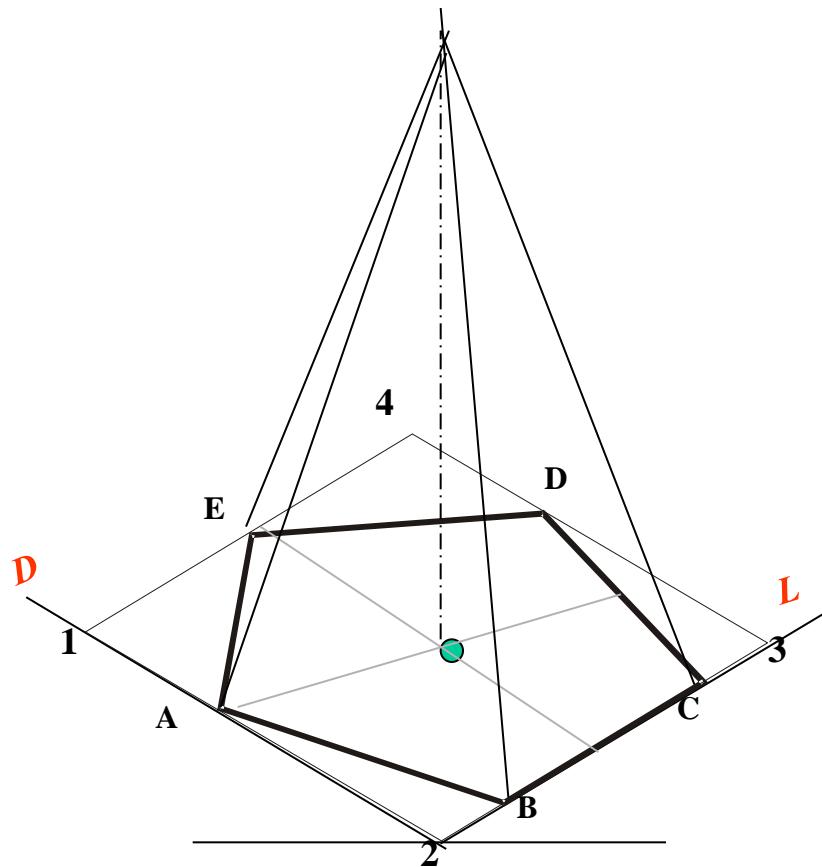
STUDY ILLUSTRATIONS

ISOMETRIC VIEW OF BASE OF PENTAGONAL PYRAMID STANDING ON H.P.

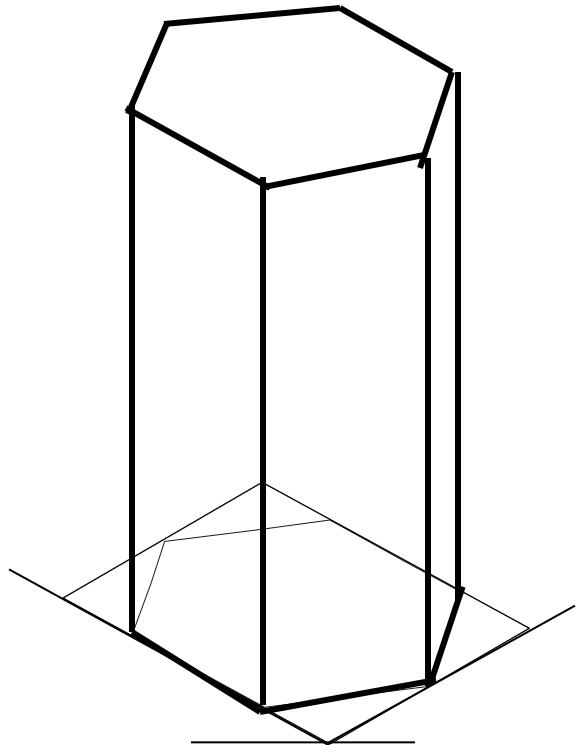


ISOMETRIC VIEW OF PENTAGONAL PYRAMID STANDING ON H.P.

(Height is added from center of pentagon)

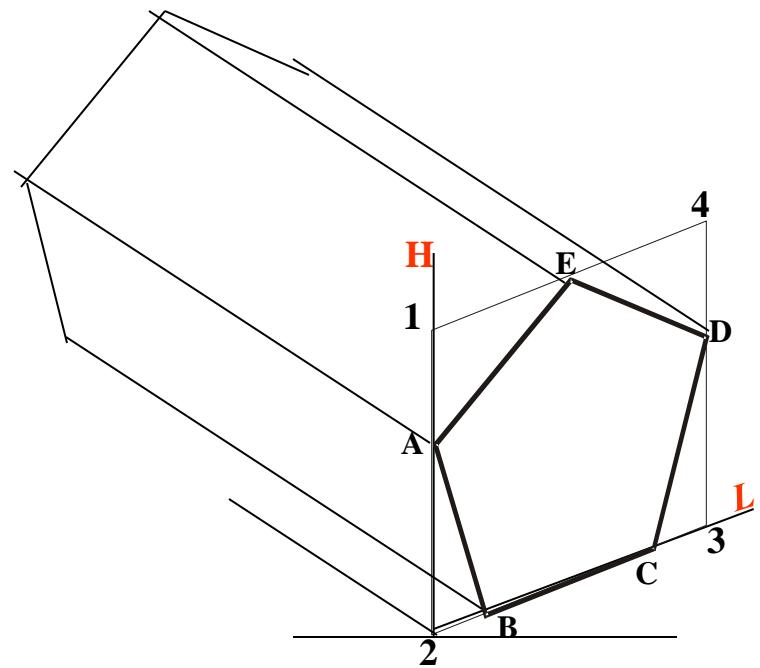


STUDY ILLUSTRATIONS



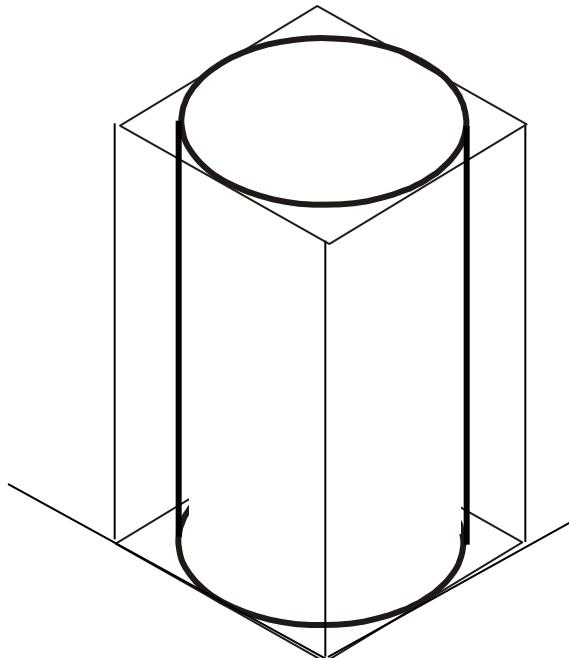
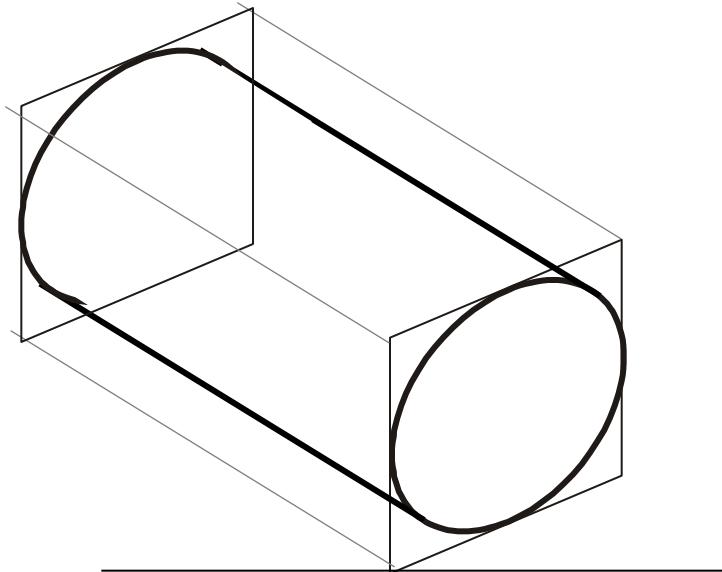
ISOMETRIC VIEW OF
HEXAGONAL PRISM
STANDING ON H.P.

ISOMETRIC VIEW OF PENTAGONAL PRISM LYING ON H.P.



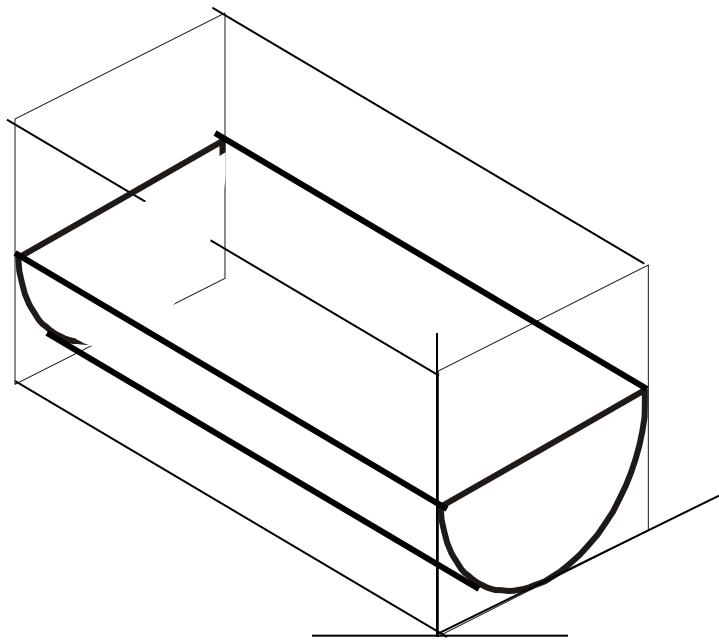
STUDY ILLUSTRATIONS

CYLINDER STANDING ON H.P.

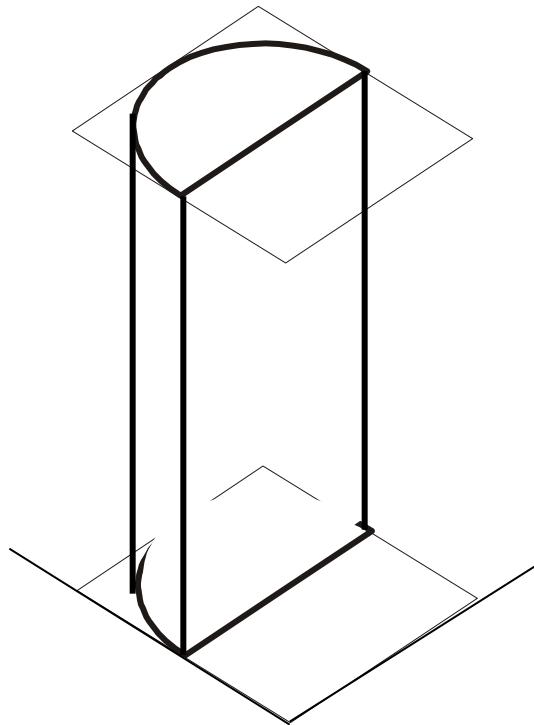


CYLINDER LYING ON H.P.

**STUDY
ILLUSTRATIONS**

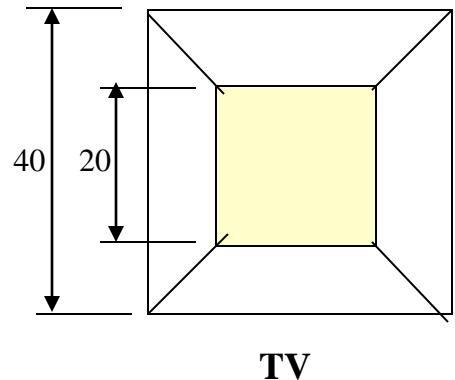
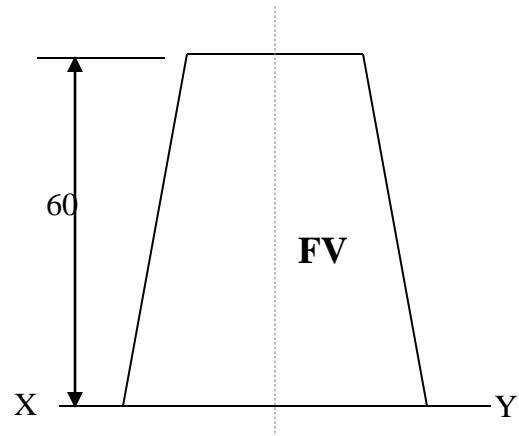


**HALF CYLINDER
STANDING ON H.P.
(ON IT'S SEMICIRCULAR BASE)**

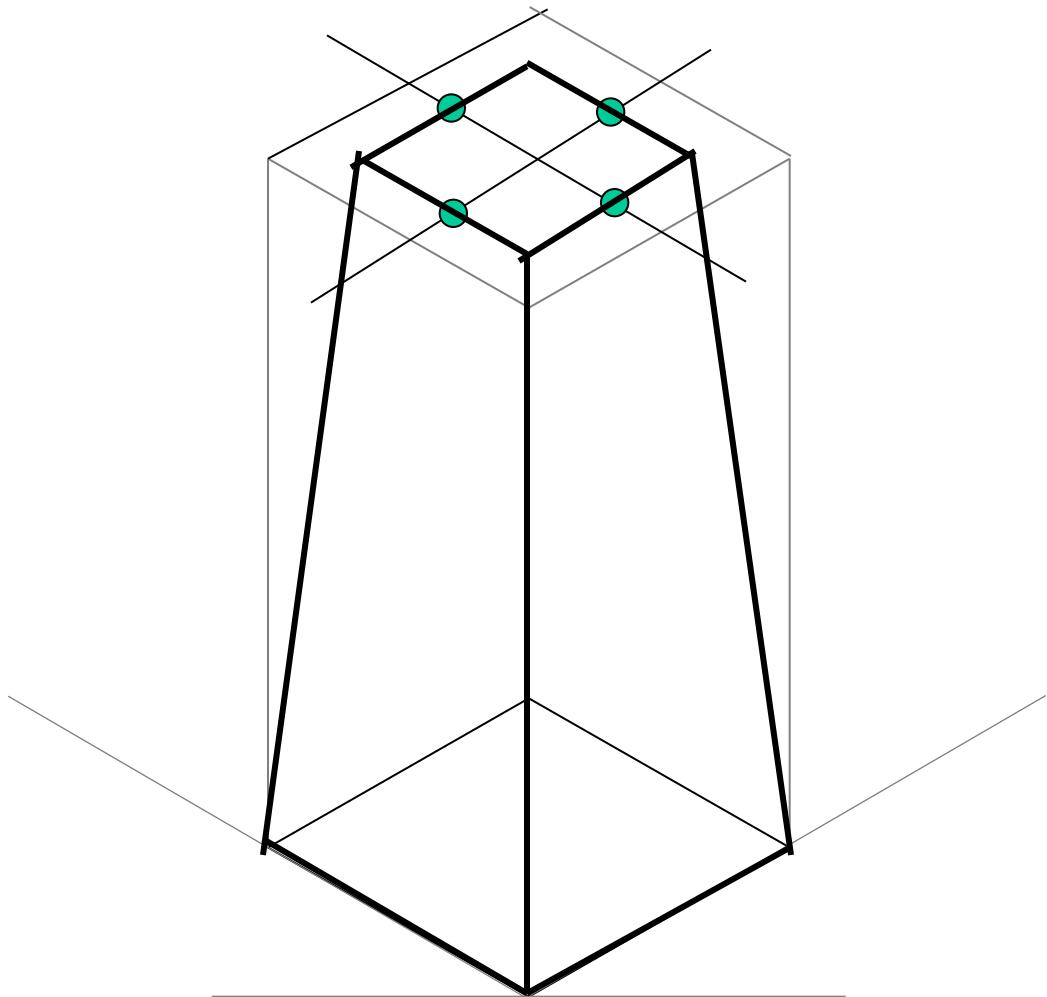


**HALF CYLINDER
LYING ON H.P.
(with flat face // to H.P.)**

STUDY ILLUSTRATIONS

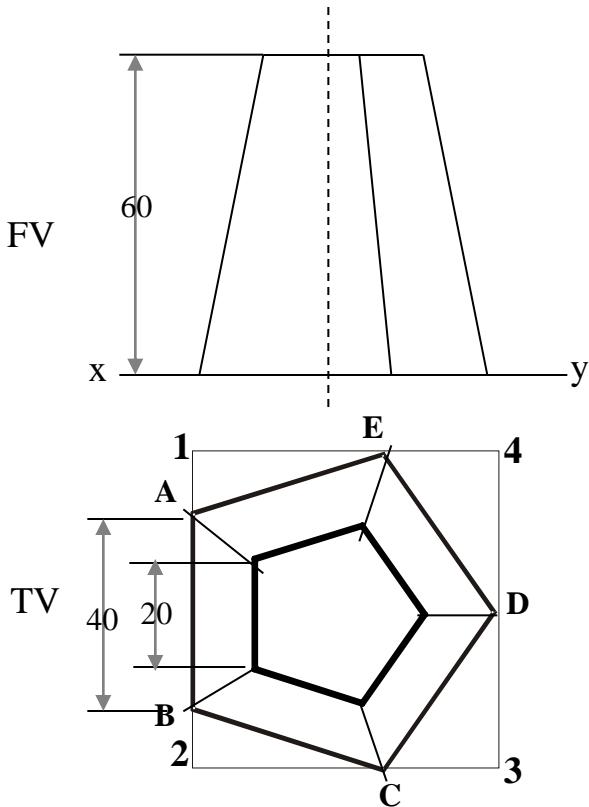


ISOMETRIC VIEW OF A FRUSTOM OF SQUARE PYRAMID STANDING ON H.P. ON IT'S LARGER BASE.

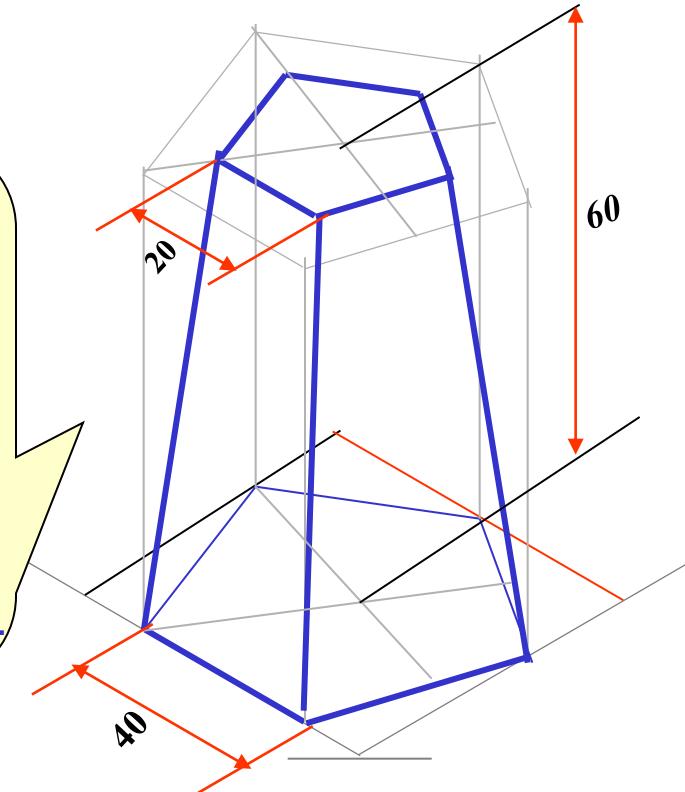


STUDY ILLUSTRATION

PROJECTIONS OF FRUSTOM OF PENTAGONAL PYRAMID ARE GIVEN.
DRAW IT'S ISOMETRIC VIEW.



ISOMETRIC VIEW
OF
FRUSTOM OF PENTAGONAL PYRAMID



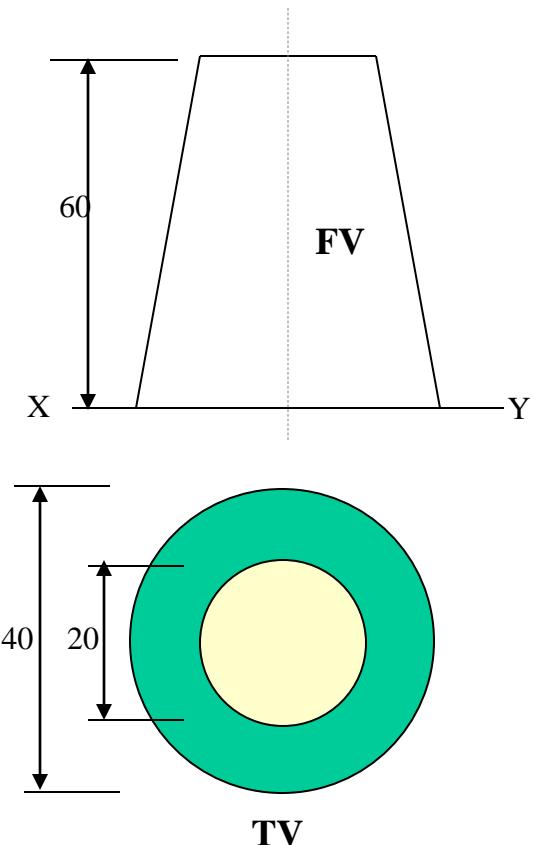
SOLUTION STEPS:

FIRST DRAW ISOMETRIC OF IT'S BASE.

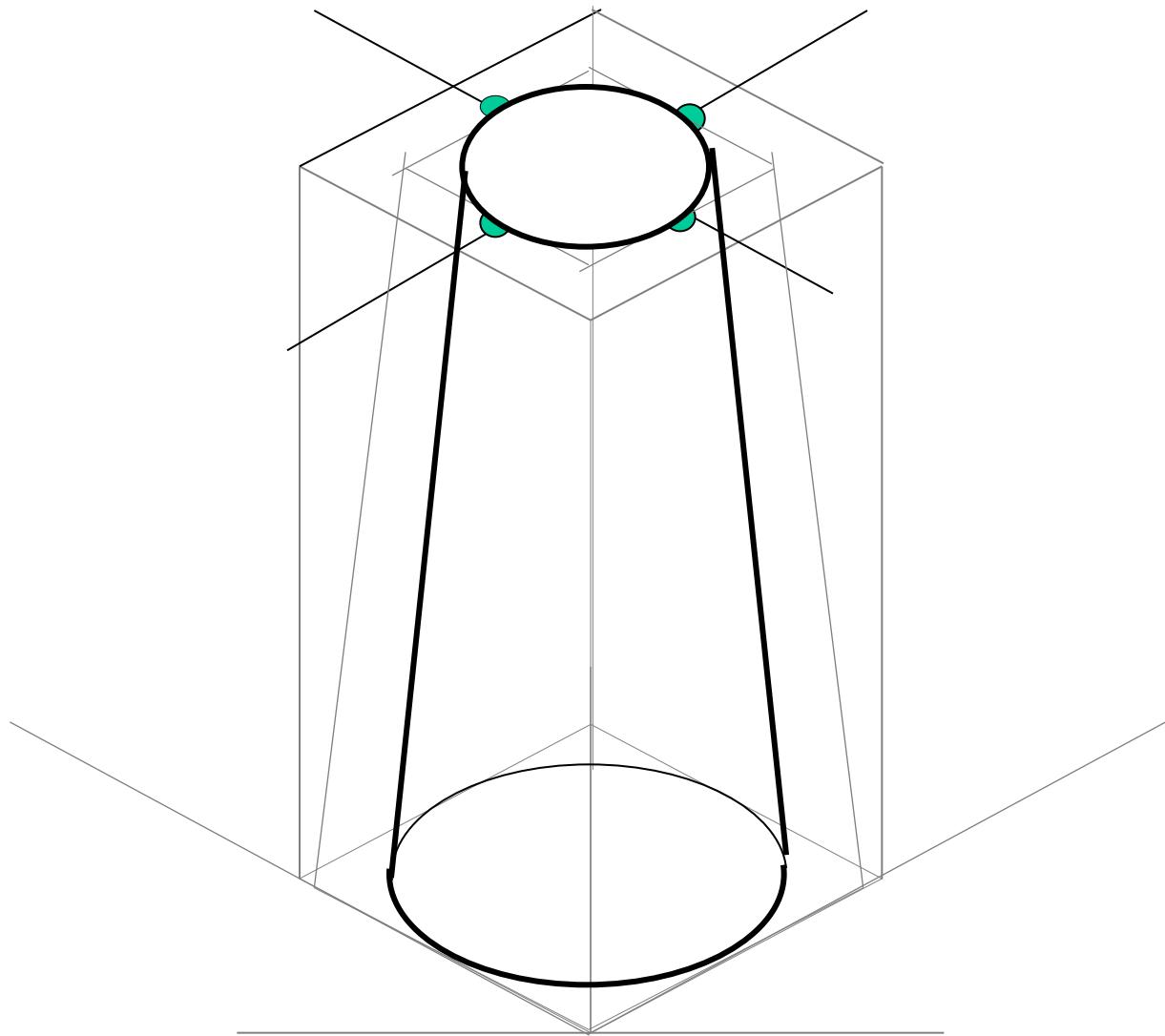
THEN DRAW SAME SHAPE AS TOP, 60 MM ABOVE THE BASE PENTAGON CENTER.

THEN REDUCE THE TOP TO 20 MM SIDES AND JOIN WITH THE PROPER BASE CORNERS.

STUDY ILLUSTRATIONS



ISOMETRIC VIEW OF A FRUSTOM OF CONE STANDING ON H.P. ON IT'S LARGER BASE.



STUDY ILLUSTRATIONS

PROBLEM: A SQUARE PYRAMID OF 30 MM BASE SIDES AND 50 MM LONG AXIS, IS CENTRALLY PLACED ON THE TOP OF A CUBE OF 50 MM LONG EDGES.DRAW ISOMETRIC VIEW OF THE PAIR.

