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# MEEN 432 –Automotive Engineering

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# Lecture : Vehicle Controls

# Smoothing Desired Quantities

- Desired Speed:
- The desired speed command can be determined based on a logic that looks at the current location and a knowledge of the race track:  $v_{d,c}(X, Y)$
- This command is filtered through a 1<sup>st</sup> order filter so that we can (i) smoothen the desired speed profile, and (ii) calculate the rate of change of desired speed:
  - $v_d(t + 1) = v_d(t) + \Delta t \lambda (v_{d,c}(t) - v_d(t))$
  - and  $\dot{v}_d(t + 1) = \frac{(v_d(t+1) - v_d(t))}{\Delta t}$

# Feed forward Control – 1

- While feedback is a good way to fix any deviation between desired and actual, it is also useful to consider a “feed forward” term that anticipates the desired quantity
- Consider that we are given  $\dot{v}_d(t)$  and  $v_d(t)$  at any time instant  $t$
- The tractive force at the vehicle required to achieve this is:
  - $F_{xd} = m \dot{v}_d + (c_0 + c_1 v_d + c_2 v_d^2) + mg \sin \theta$
- This tractive force can be cascaded through the powertrain to arrive at the desired final drive input (or transmission output) torque:
  - $\tau_{fd,d} = F_{xd} r_w / G_{FD}$
- Corresponding to this tractive force, there is also the desired angular speed and net power desired:
  - $\omega_{fd,d} = \frac{v_d}{r_w} G_{FD}$
  - $p_{fd,d} = F_{xd} v_d$ 
    - (Note that for this cascade of torque and power, we assume no inertia effects and no losses)

# Feed Forward Control – 2

- Assume a gear with gear ratio  $G$  is chosen
- Then the motor torque and speed requirement is given by:
  - $\tau_{md} = \frac{\tau_{FD,d}}{G} = \frac{F_{xd}r_w}{G_{FD}G}$  and  $\omega_{md} = \omega_{FD,d}G = \frac{v_d}{r_w}G_{FD}G$
- Then the driver control will have two components:
  - Feed Forward:
    - $\alpha_{FF} = \frac{\tau_{md}}{\tau_{m,max}}$
  - Feed Back:
    - $\alpha_{FB} = PID(v_d - v)$
  - $\alpha = \alpha_{FF} + \alpha_{FB}$

# Gear Selection

- Let there be  $n$  Gear choices available, with the gear ratios defined as  $G_i$   $1 \leq i \leq n$
- The (feed forward) motor operating point is defined for each gear  $G_i$ :
  - $\tau_{md,i} = \frac{F_{xd} r_w}{G_{FD} G_i}$  and  $\omega_{md,i} = \frac{v_d}{r_w} G_{FD} G_i$
- Corresponding to the operating point, there is an efficiency  $\eta_i(\tau_{md,i}, \omega_{md,i})$
- The choice of the gear  $G^*$  is then done through a simple optimization:
  - $G^* = \operatorname{argmax}_{1 \leq i \leq n} \eta_i(\tau_{md,i}, \omega_{md,i})$  such that
  - $\omega_{min} \leq \omega_{md,i} \leq \omega_{max}; \tau_{min} \leq \tau_{md,i} \leq \tau_{max}$
- Additionally, some practical constraints are added: (examples)
  - Shift Business: Do not shift within x seconds of a shift
  - Shift magnitude: Do not shift by more than x gears when in gear y

# Desired psi\_d: 1/2

- Find Look Ahead Point  $(x_l, y_l)$ , vehicle at  $(x, y)$  with look ahead  $l$ 
  - Vehicle on Straightaways:
    - Bottom:
      - if  $x + l < 900$ :  $x_l = x + l$ ;  $y_l = 0$
      - Else  $x_l = 900 + R \sin(\frac{l_1}{R})$ ;  $y_l = R \cos(\frac{l_1}{R})$ , with  $l_1 = x + l - 900$
    - Top
      - if  $x - l > 0$ :  $x_l = x - l$ ;  $y_l = 400$
      - Else  $x_l = -R \sin(\frac{l_1}{R})$ ;  $y_l = 400 - R \cos(\frac{l_1}{R})$ , with  $l_1 = l - x$
  - Vehicle on Curves:
    - Right Curve:
      - $x_l = 900 + R \sin(\frac{l+l_2}{R})$ ;  $y_l = R \cos(\frac{l+l_2}{R})$ , with  $l_2 = R \tan^{-1}(\frac{200-y}{x-900})$
    - Left Curve
      - $x_l = -R \sin(\frac{l+l_2}{R})$ ;  $y_l = 400 - R \cos(\frac{l+l_2}{R})$ , with  $l_2 = R \tan^{-1}(\frac{200-y}{x})$

# Desired psi\_d: 2/2

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- Once you find the look ahead point, the desired heading angle can be calculated as below:
- $\psi_d = \tan^{-1} \frac{y_l - y}{x_l - x}$