

AI 6102: Machine Learning Methodologies & Applications


L13: Transfer Learning

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Outline

- What is transfer learning?
 - Transfer learning methodologies
 - Instance-based
 - Feature-based
 - Parameter-based
 - Relational
- 
- A decorative graphic consisting of several overlapping, wavy, curved lines in shades of light pink and peach, located in the bottom right corner of the slide.

Transfer of Learning

Psychological point of view

- Inspired by human's transfer of learning ability
- The study of dependency of human conduct, learning or performance on prior experience.
 - [Thorndike and Woodworth, 1901] explored how individuals would transfer in one context to another context that share similar characteristics.



Transfer Learning

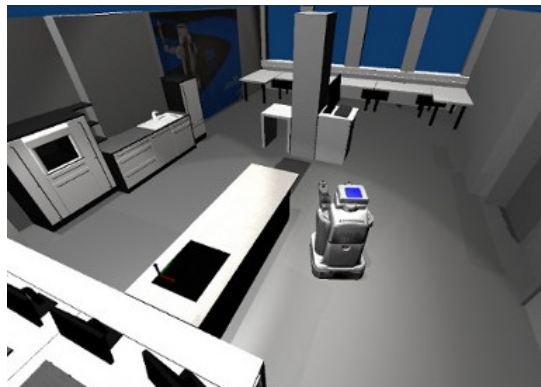
Machine learning community

- The ability of a system to recognize and apply knowledge and skills learned in previous domains/tasks to novel tasks/domains, which share some commonality



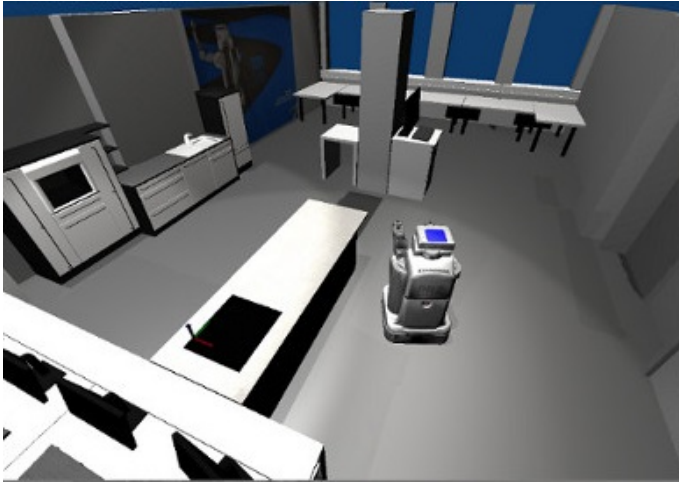
Motivating Example I

- Goal: to train a robot to accomplish Task T_1 in an indoor environment E_1 using machine learning techniques:
 - Sufficient training data required: sensor readings to measure the environment as well as supervision, i.e. labels by human or feedback from environment
 - A policy or predictive model can be learned, and used in the same environment



Task T_1 in environment E_1

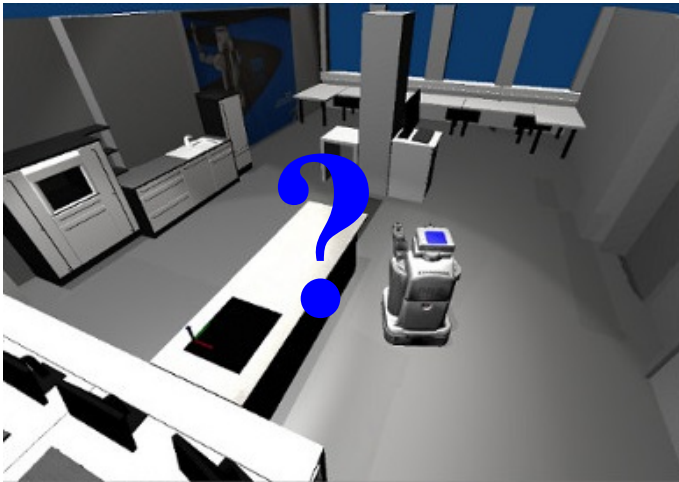
To train the robot from scratch?
Expensive & time consuming!



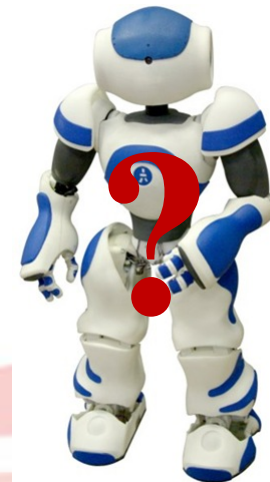
Task T_1



Environment changes E_2

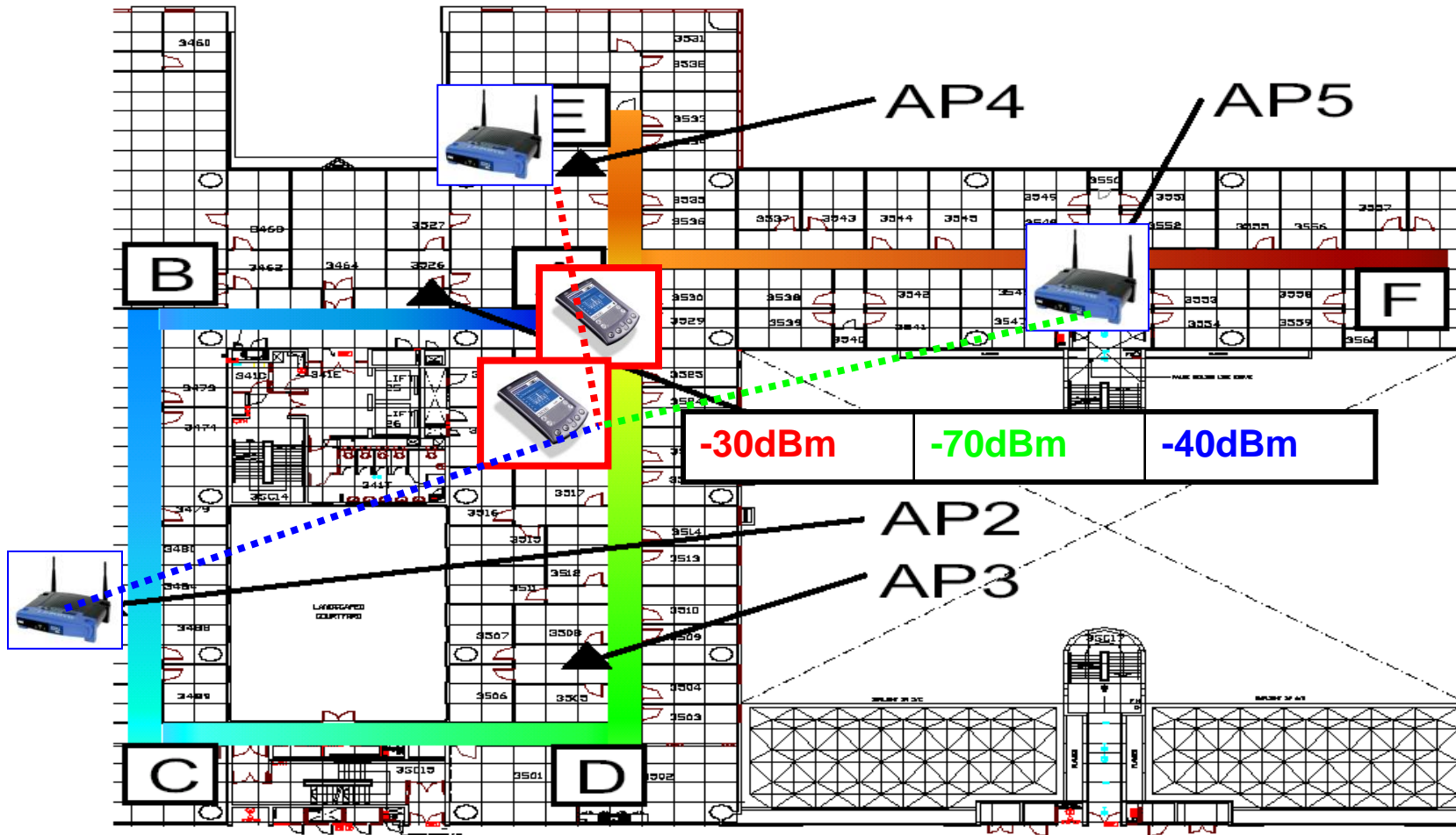


Task T_2



New robot

Motivating Example I I



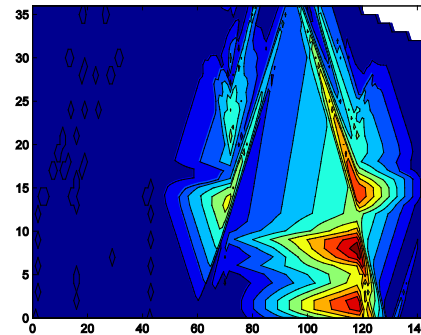
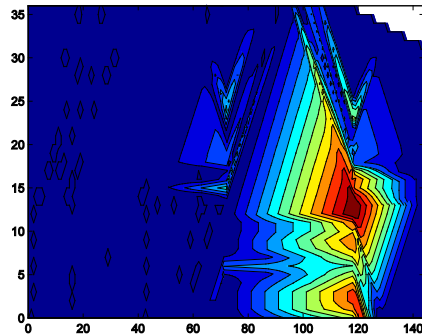
Motivating Example II (cont.)

- WiFi localization: signal strength changes a lot over different time periods, or across different mobile devices.

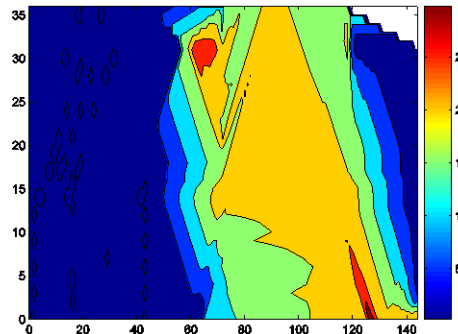
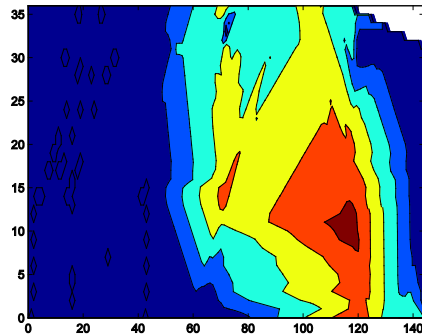
Time Period A

Time Period B

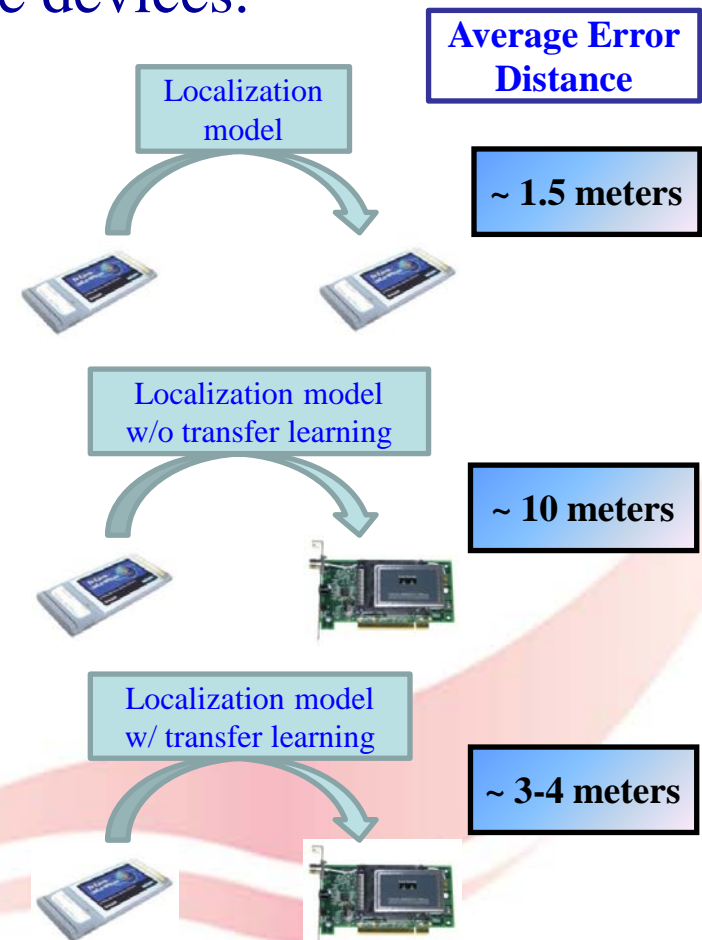
Device A



Device B



Contour of signal strength values

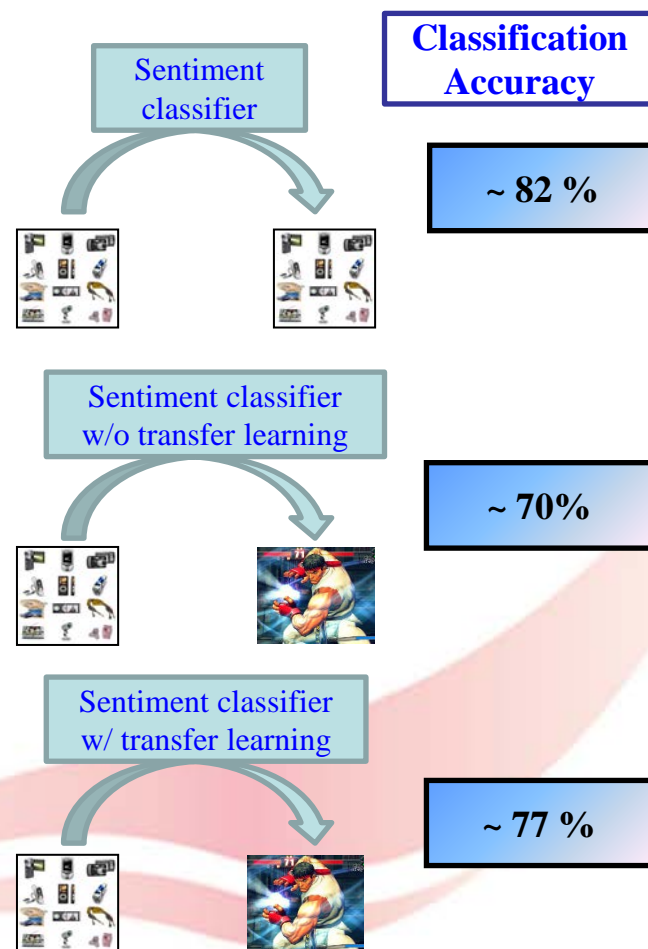


Motivating Examples III

- Sentiment analysis: users may use different sentiment words across different domains.

Electronics	Video Games
(1) Compact ; easy to operate; very good picture quality; looks sharp !	(2) A very good game! It is action packed and full of excitement. I am very much hooked on this game.
(3) I purchased this unit from Circuit City and I was very excited about the quality of the picture. It is really nice and sharp .	(4) Very realistic shooting action and good plots. We played this and were hooked .
(5) It is also quite blurry in very dark settings. I will never buy HP again.	(6) The game is so boring . I am extremely unhappy and will probably never buy UbiSoft again.

Product reviews on different domains



A Strong Assumption

- **Assumption:** training and test data are assumed to be
 - Represented in the same feature space, AND
 - Follow the same data distribution
- If the assumption holds, then there is theoretical guarantee on the performance of the model learned with training data on the test data



A Strong Assumption (cont.)

- Consider the learning framework of empirical risk minimization

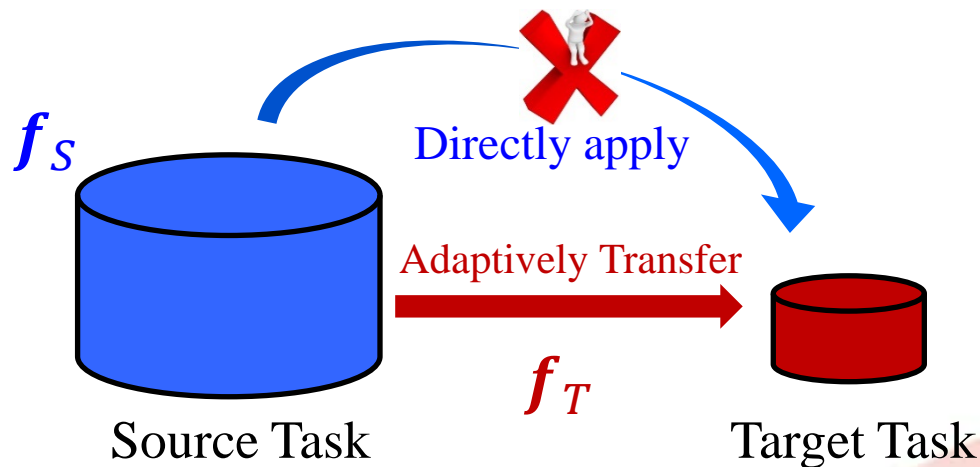
$$\begin{aligned}\theta^* &= \arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{tst}} [\ell(x, y; \theta)] \\&= \arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{tst}} \left[\frac{P_{trn}(x, y)}{P_{trn}(x, y)} \ell(x, y; \theta) \right] \\&= \arg \min_{\theta} \int_y \int_x P_{tst}(x, y) \left(\frac{P_{trn}(x, y)}{P_{trn}(x, y)} \ell(x, y; \theta) \right) dx dy \\&= \arg \min_{\theta} \int_y \int_x P_{trn}(x, y) \left(\frac{P_{tst}(x, y)}{P_{trn}(x, y)} \ell(x, y; \theta) \right) dx dy \\&= \arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{trn}} \left[\frac{P_{tst}(x, y)}{P_{trn}(x, y)} \ell(x, y; \theta) \right]\end{aligned}$$

If $P_{tst}(x, y) = P_{trn}(x, y)$

$$= \arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{trn}} [\ell(x, y; \theta)]$$

Transfer Learning

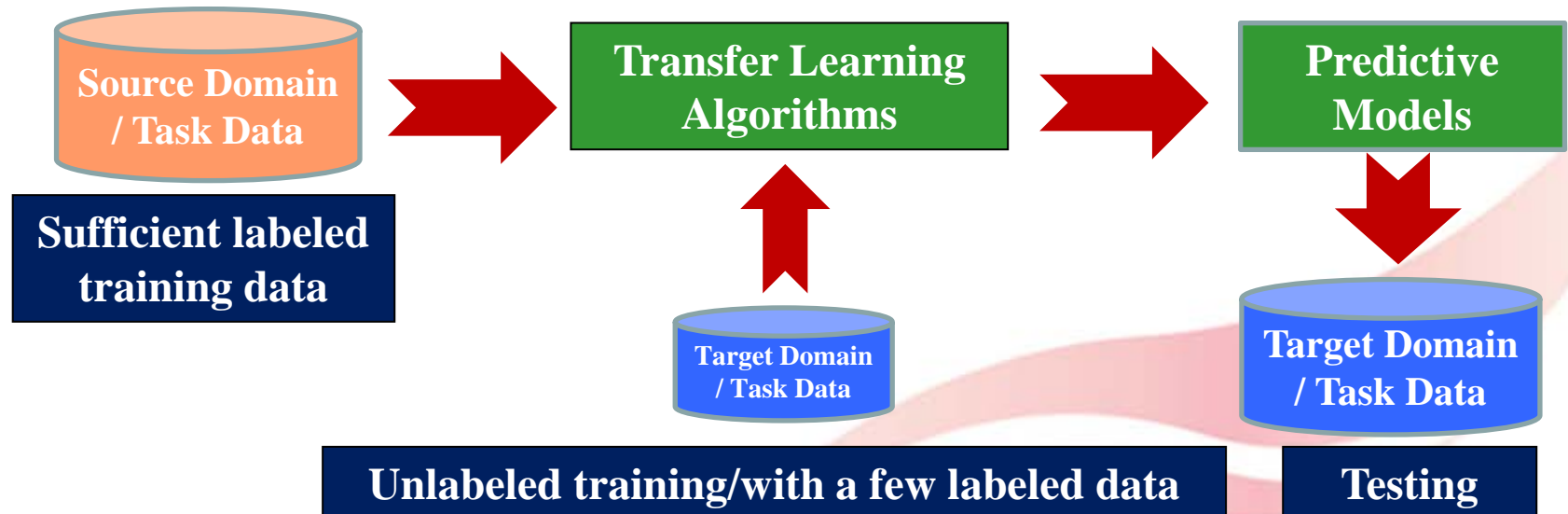
- In practice: training and test data come from different domains
 - Represented in different feature spaces, OR
 - Follow different data distributions
- $\arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{tst}} [\ell(x, y; \theta)] \neq \arg \min_{\theta} \mathbb{E}_{(x,y) \sim P_{trn}} [\ell(x, y; \theta)]$



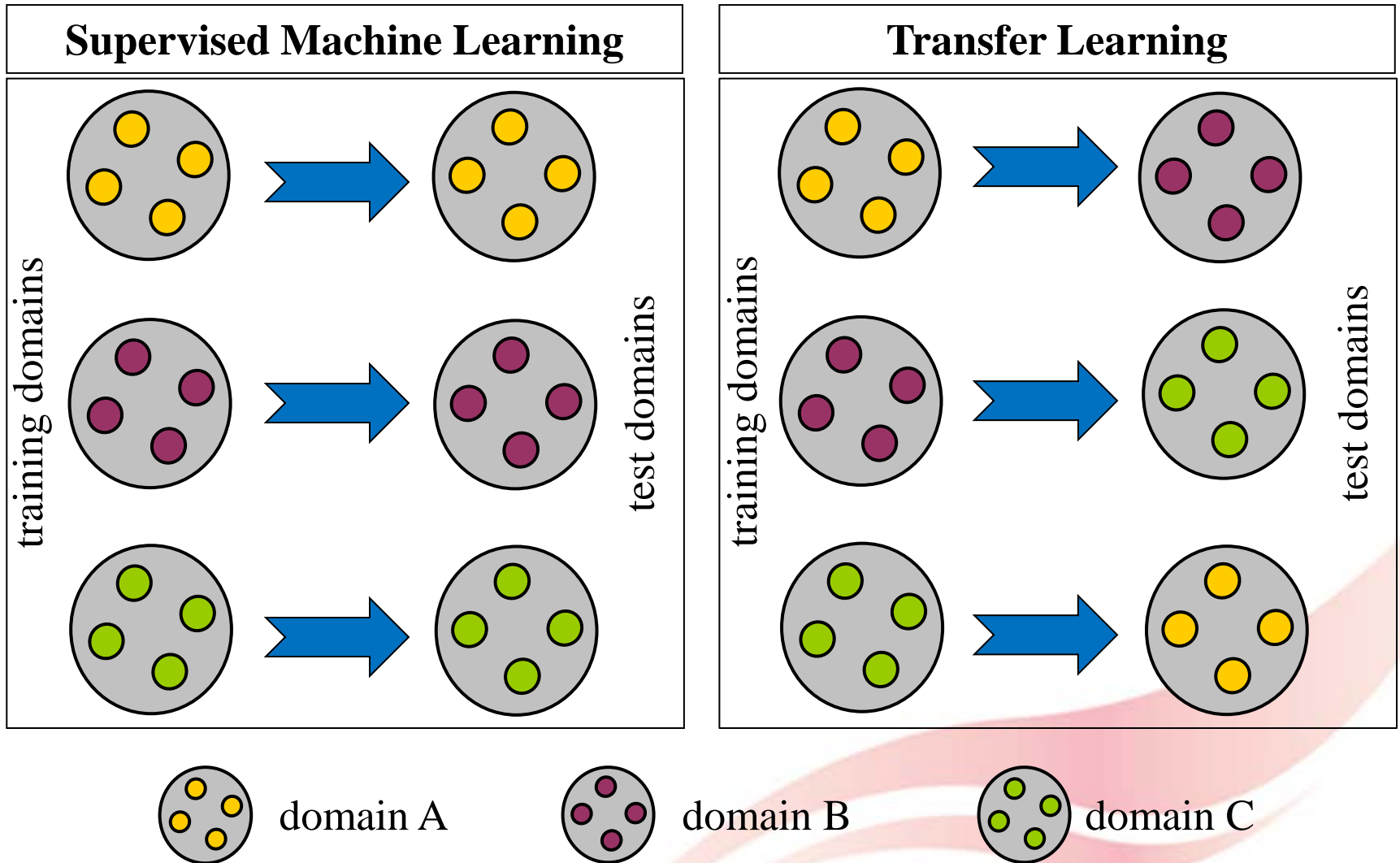
What if machines have transfer learning ability?

Transfer Learning (cont.)

- Given a target domain/task, transfer learning aims to
 - identify the commonality between the target domain/task and previous domains/tasks
 - transfer knowledge from the previous domains/tasks to the target one such that human supervision on the target domain/task can be dramatically reduced.

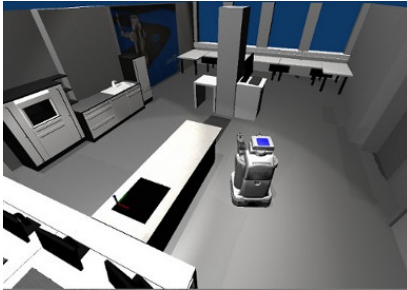


TL v.s. Supervised ML



TL for Different ML Problems

- Transfer learning for reinforcement learning



[Taylor and Stone, Transfer Learning for Reinforcement Learning Domains: A Survey, JMLR 2009]

- Transfer learning for classification/regression




[**Pan** and Yang, A Survey on Transfer Learning, IEEE TKDE 2010]

[**Pan**, Transfer Learning, Chapter 21, Data Classification: Algorithms and Applications 2014]

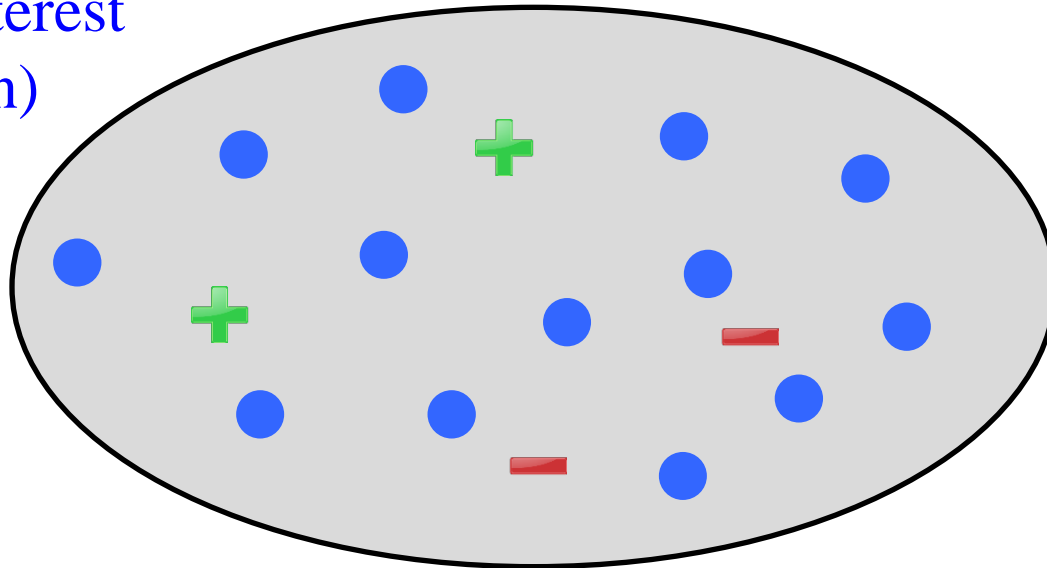
[Yang, Zhang, Dai and **Pan**, Transfer Learning, Cambridge University Press 2020]

TL v.s. Active Learning & Semi-supervised Learning

- They are all proposed to address the labeled data sparsity issue on the learning domain of interest
 - The strategies used or the assumptions made are quite different
 - They can be combined to further boost the performance of the learning problems with sparse labeled data
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Semi-supervised Learning

Domain of interest
(target domain)

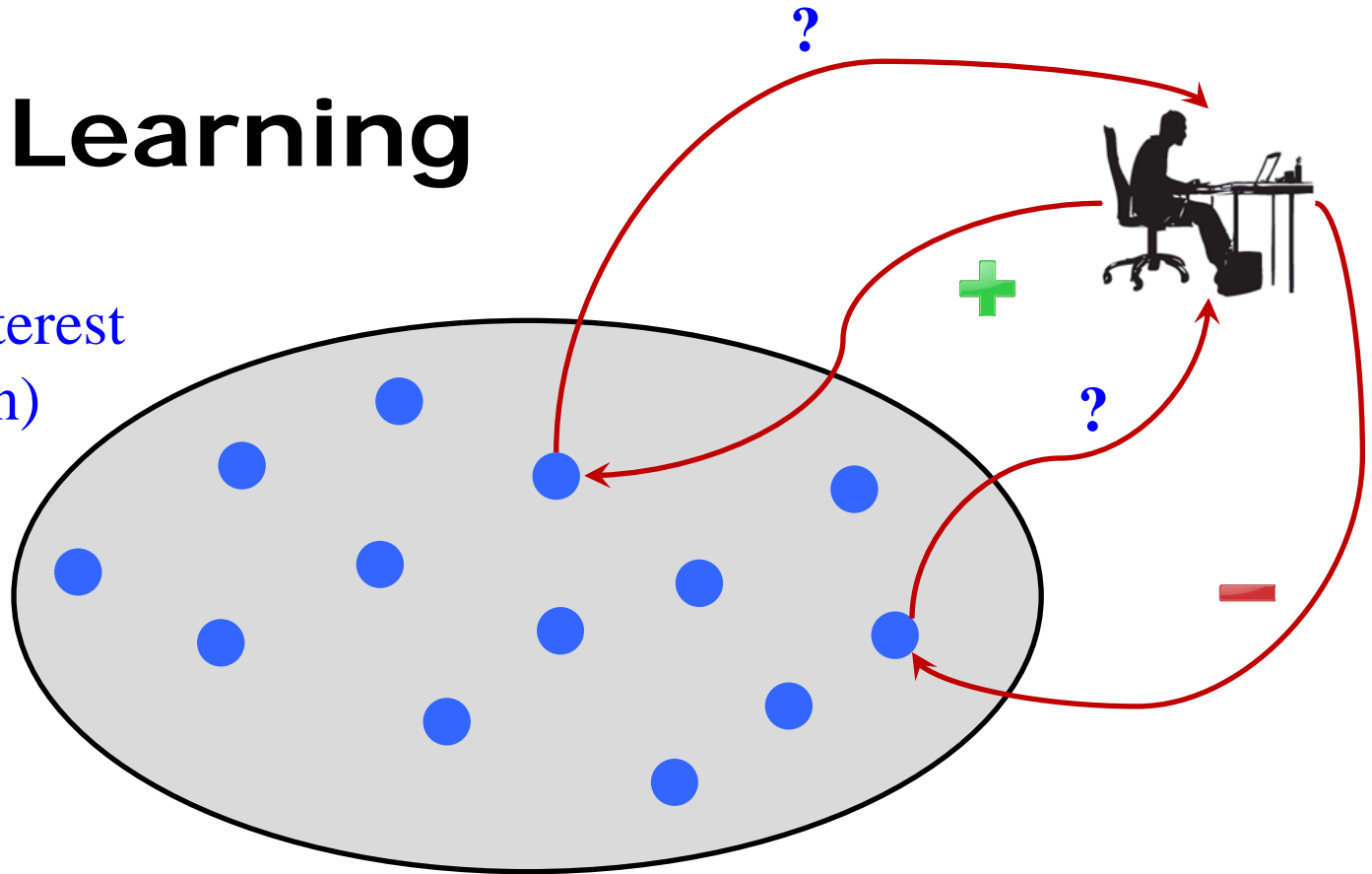


Assumption:

1. A little labeled data is available
2. Plenty of unlabeled data is cheap to collect
3. Underlying cluster or manifold structure can be discovered by using unlabeled data, and is useful for label propagation

Active Learning

Domain of interest
(target domain)

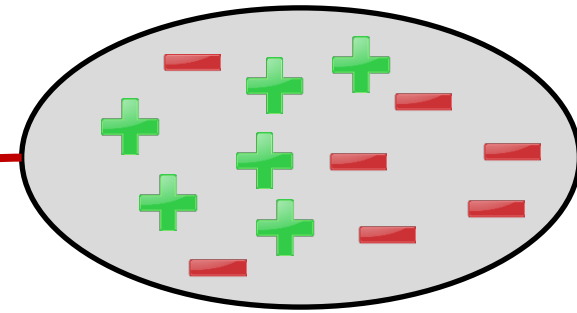
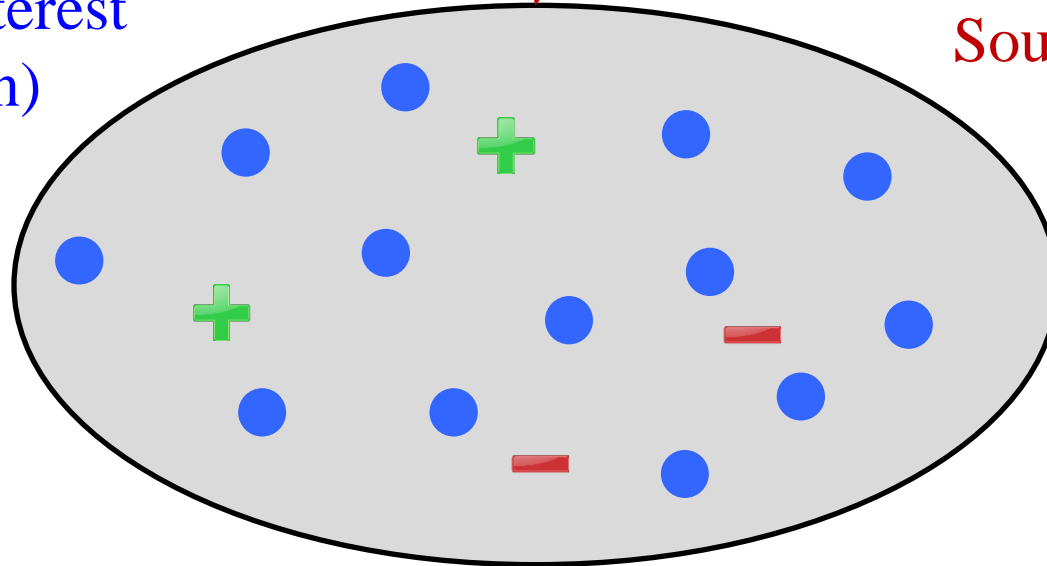


Assumption:

1. A pool of unlabeled data is available
2. An oracle is able to provide labels via querying with cost
3. The budget for querying labels is limited

Transfer Learning

Domain of interest
(target domain)

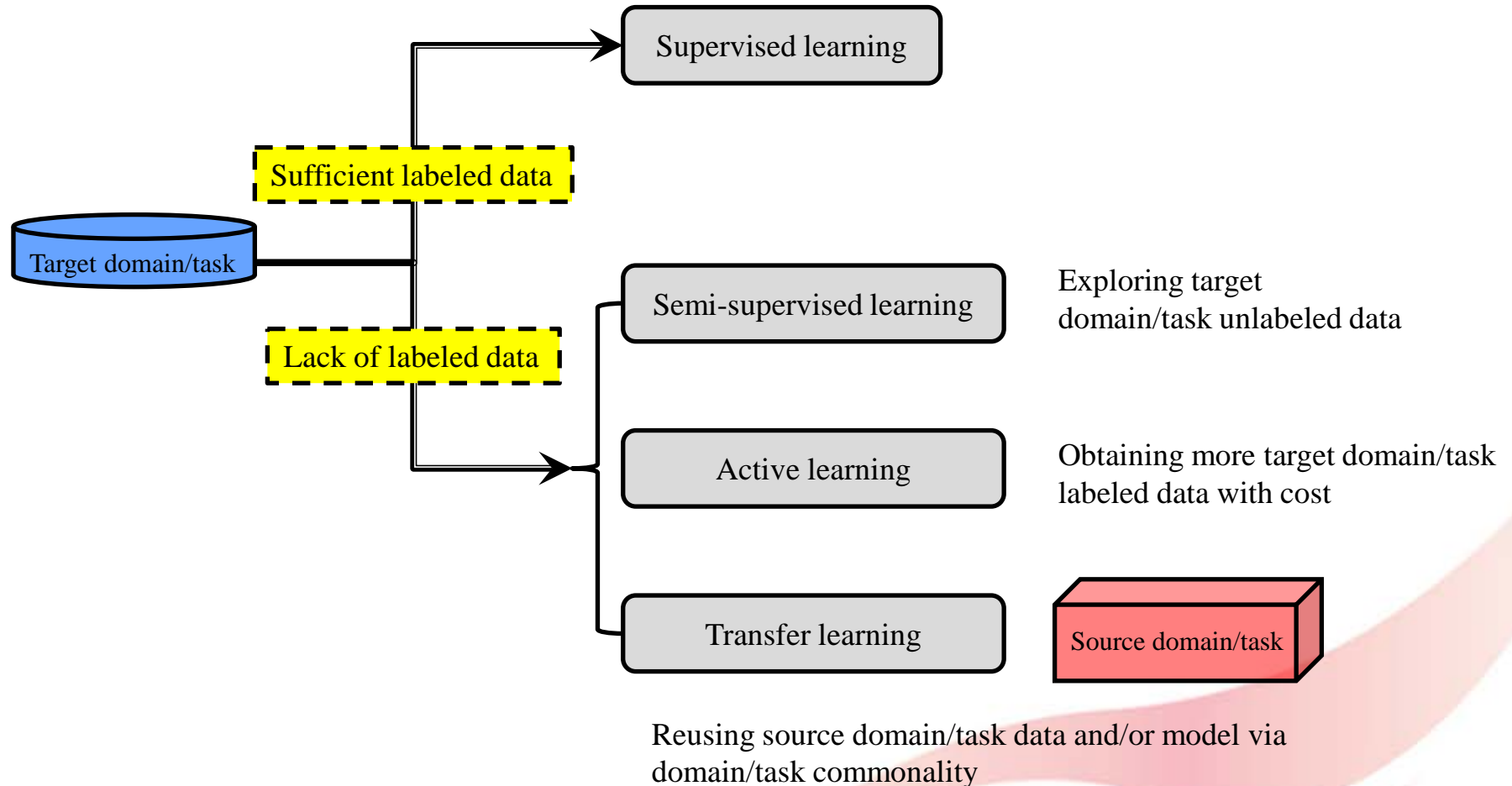


Source domain

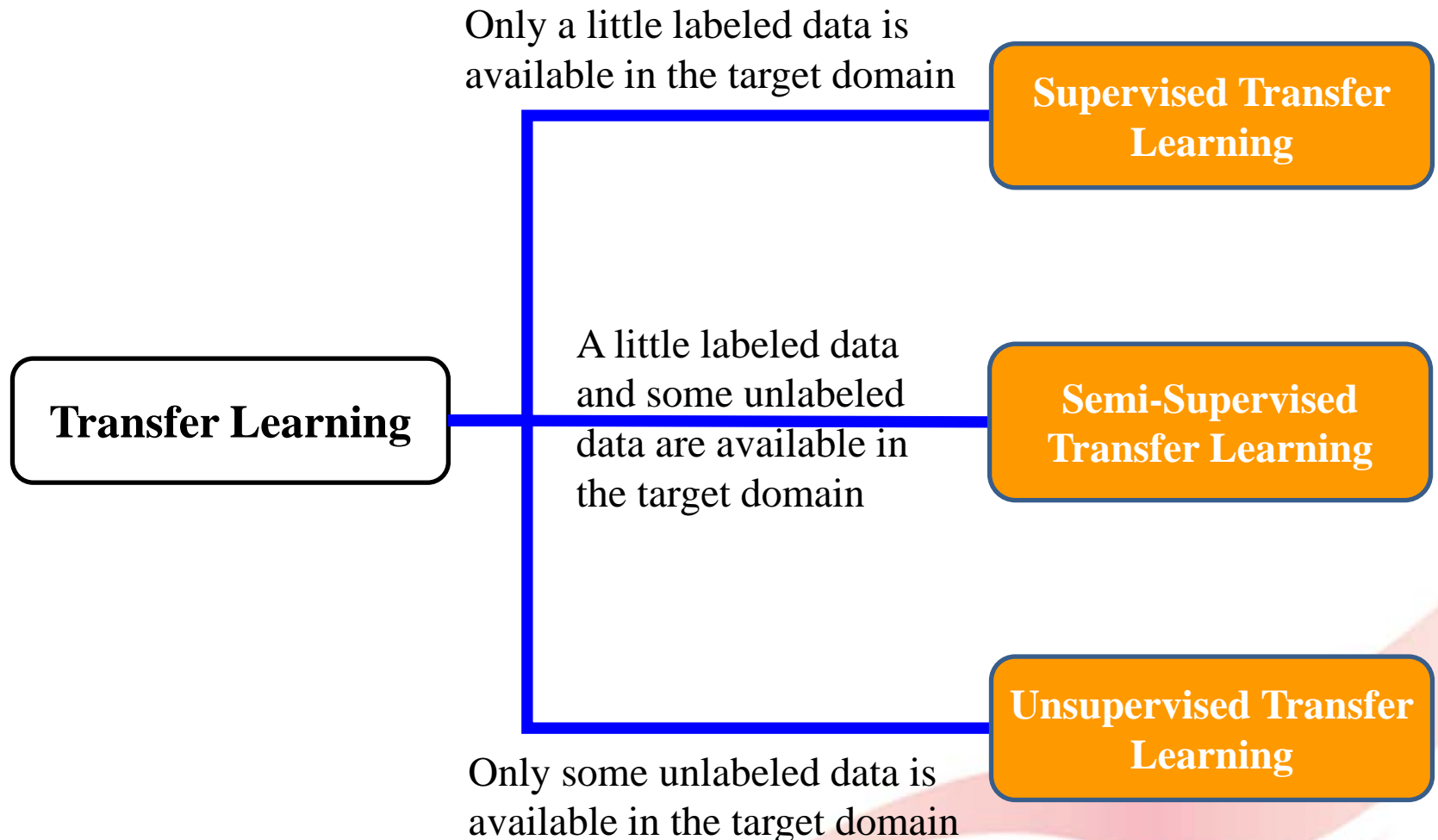
Assumption:

1. A little labeled or/and some unlabeled data is available on the target domain
2. Plenty labeled data is available on related source domain(s)
3. Source-domain data can be borrowed to learn a target classifier after some adaptation

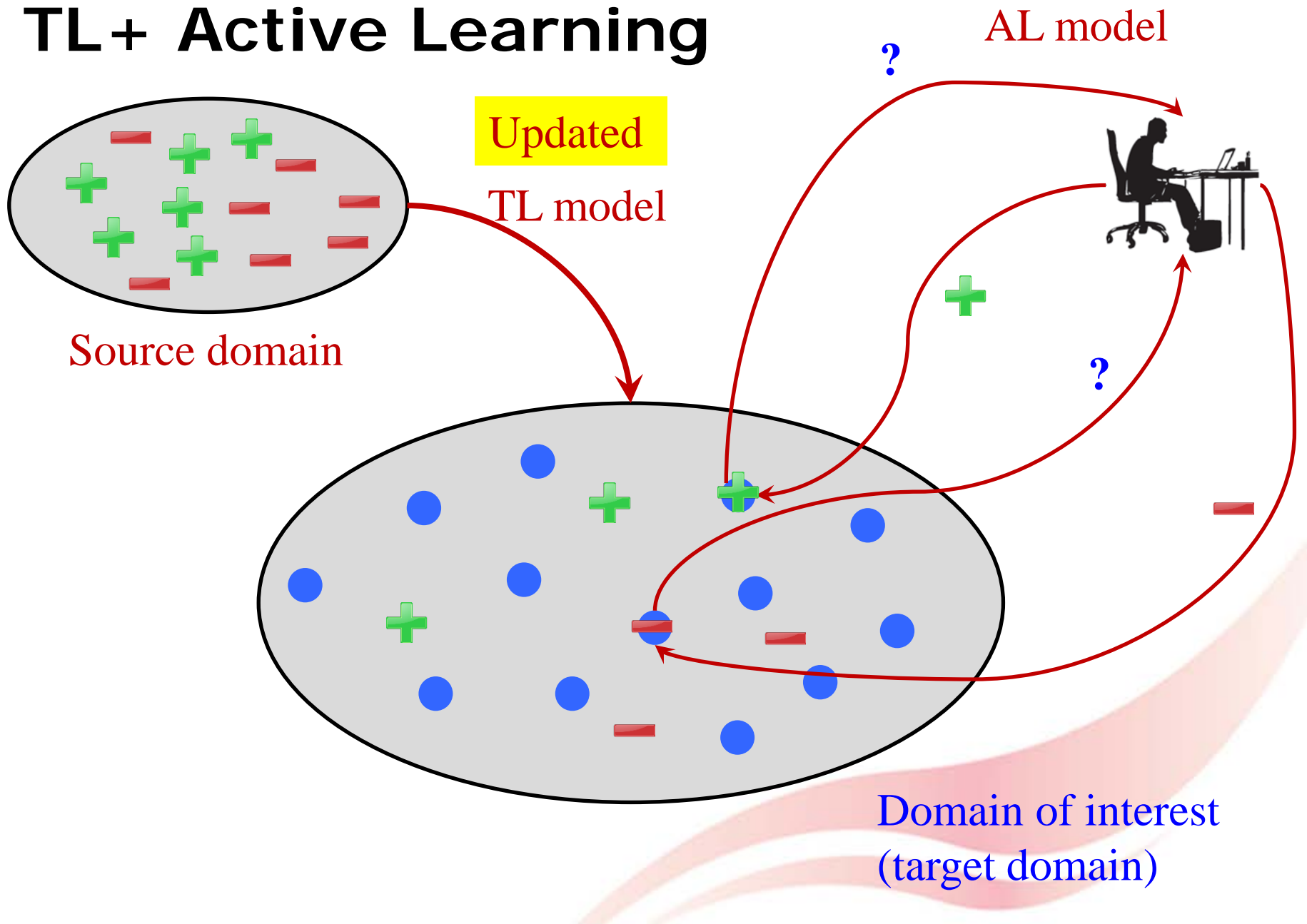
TL v.s. Active Learning & Semi-supervised Learning (cont.)



TL+ Semi-supervised Learning

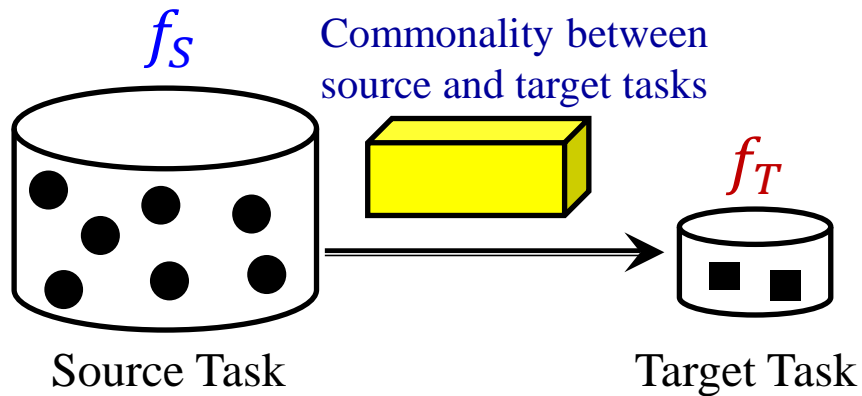


TL+ Active Learning

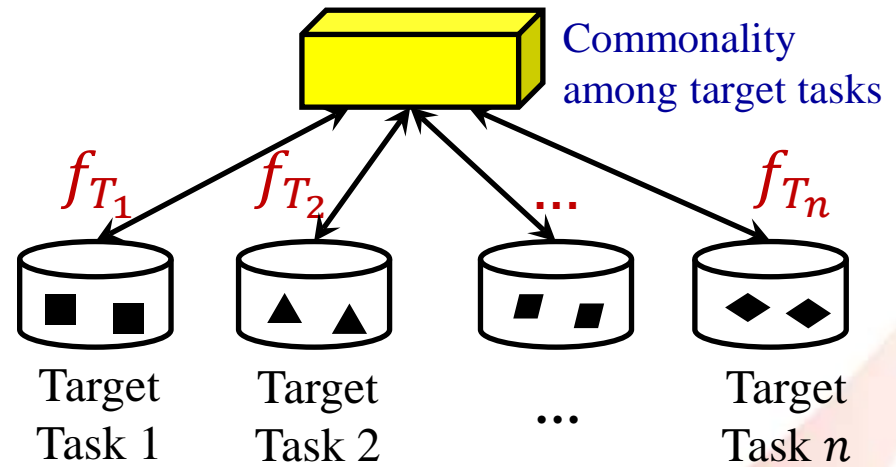


TL v.s. Multi-task Learning

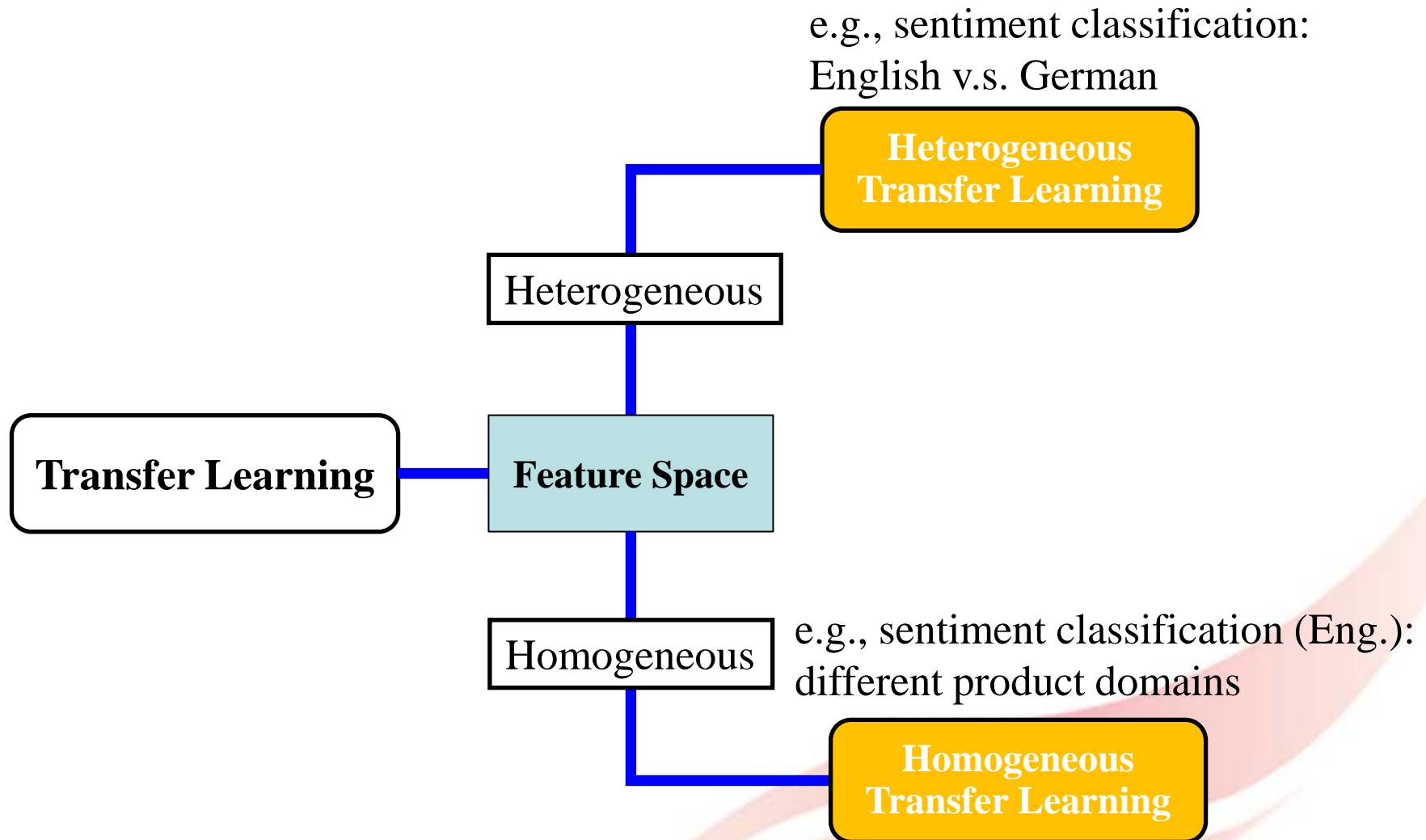
Transfer Learning



Multi-task Learning



Different TL Settings



Research Issues in TL

What to transfer

What knowledge across domains/tasks can be transferred

How to transfer

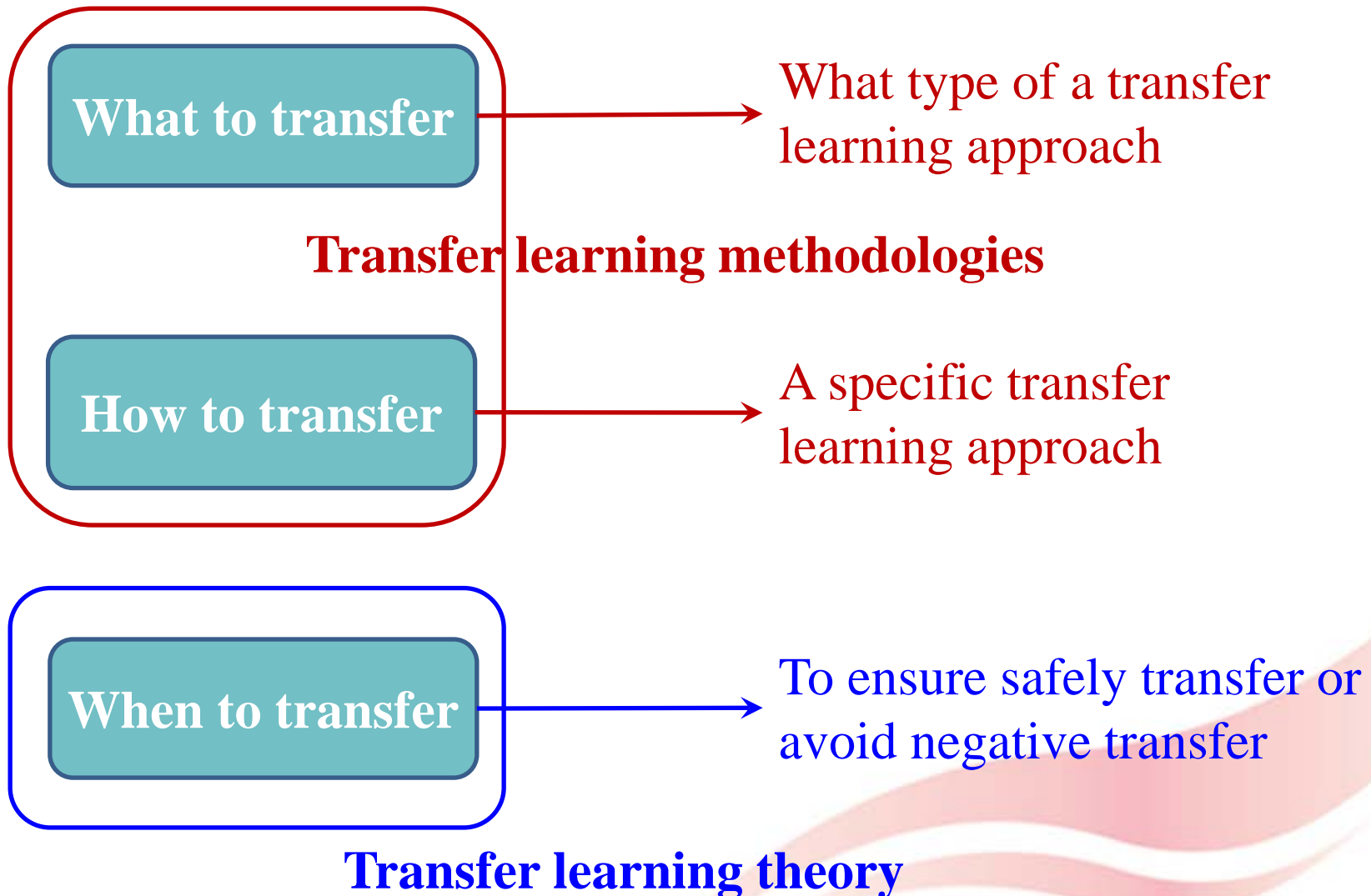
Once what knowledge to be transferred is identified, how to encode the knowledge into a learning algorithm to transfer

When to transfer

In which situations, transfer learning can be safely performed



Research Issues in TL (cont.)



Transfer Learning Approaches

Based on “what to transfer”

**Instance-based
Approaches**

**Feature-based
Approaches**

**Parameter-based
Approaches**

**Relational
Approaches**

TL Approaches (cont.)

Instance-based Approaches

Knowledge to be transferred corresponds to the weights attached to source instances

Feature-based Approaches

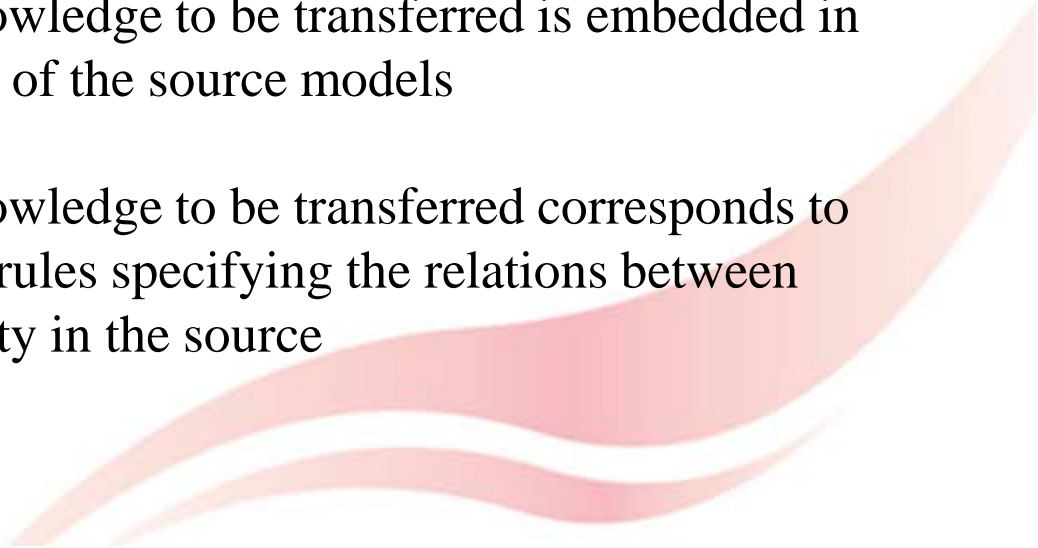
Knowledge to be transferred corresponds to be the learned features across domains

Parameter-based Approaches

Knowledge to be transferred is embedded in part of the source models

Relational Approaches

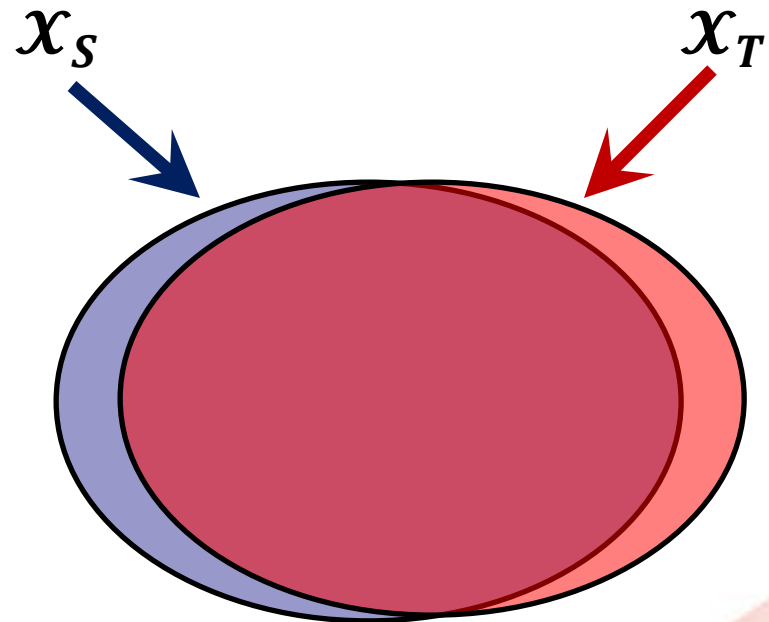
Knowledge to be transferred corresponds to the rules specifying the relations between entity in the source



Instance-based TL Approaches

General Assumption

Source and target domains have a lot of overlapping features (domains share the same/similar support)



Instance-based TL Approaches

Case I

Problem Setting

Given $\mathbf{D}_S = \{x_{S_i}, y_{S_i}\}_{i=1}^{n_S}$, $\mathbf{D}_T = \{x_{T_i}\}_{i=1}^{n_T}$,

Learn f_T , s.t. $\sum_i \epsilon(f_T(x_{T_i}), y_{T_i})$ is small,

where y_{T_i} is unknown.

Assumption

$$P_S(y|x) = P_T(y|x)$$

$$P_S(x) \neq P_T(x)$$

Case II

Problem Setting

Given $\mathbf{D}_S = \{x_{S_i}, y_{S_i}\}_{i=1}^{n_S}$,

$\mathbf{D}_T = \{x_{T_i}, y_{T_i}\}_{i=1}^{n_T}$, $n_T \ll n_S$,

Learn f_T , s.t. $\epsilon(f_T(x_{T_i}), y_{T_i})$ is small, and

f_T has good generalization on unseen x_T^* .

Assumption

$$P_S(y|x) \neq P_T(y|x)$$

Instance-based Approaches: Case I

Given a target task, based on the learning framework of empirical risk minimization

$$\theta^* = \arg \min \mathbb{E}_{(x,y) \sim P_T} [l(x, y, \theta)]$$

$$= \arg \min \mathbb{E}_{(x,y) \sim P_T} \left[\frac{P_S(x, y)}{P_S(x, y)} l(x, y, \theta) \right]$$

$$= \arg \min \int_y \int_x P_T(x, y) \left(\frac{P_S(x, y)}{P_S(x, y)} l(x, y, \theta) \right) dx dy$$

$$= \arg \min \int_y \int_x P_S(x, y) \left(\frac{P_T(x, y)}{P_S(x, y)} l(x, y, \theta) \right) dx dy$$

$$= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x, y)}{P_S(x, y)} l(x, y, \theta) \right]$$

Instance-based Approaches: Case I (cont.)

Assumption: $\{P_S(x) \neq P_T(x), P_S(y|x) = P_T(y|x)\} \Rightarrow P_S(x, y) \neq P_T(x, y)$

$$\begin{aligned}\theta^* &= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x, y)}{P_S(x, y)} l(x, y, \theta) \right] \\ &= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x) \cancel{P_T(y|x)}}{P_S(x) \cancel{P_S(y|x)}} l(x, y, \theta) \right] \\ &= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x)}{P_S(x)} l(x, y, \theta) \right]\end{aligned}$$


Denote $\beta(x) = \frac{P_T(x)}{P_S(x)},$


$$\theta^* = \arg \min \sum_{i=1}^{n_S} \beta(x_{S_i}) l(x_{S_i}, y_{S_i}, \theta) + \lambda \Omega(\theta)$$

Instance-based Approaches: Case I (cont.)

How to estimate $\beta(x) = \frac{P_T(x)}{P_S(x)}$?

A simple solution is to first estimate $P_T(x)$, $P_S(x)$, respectively,

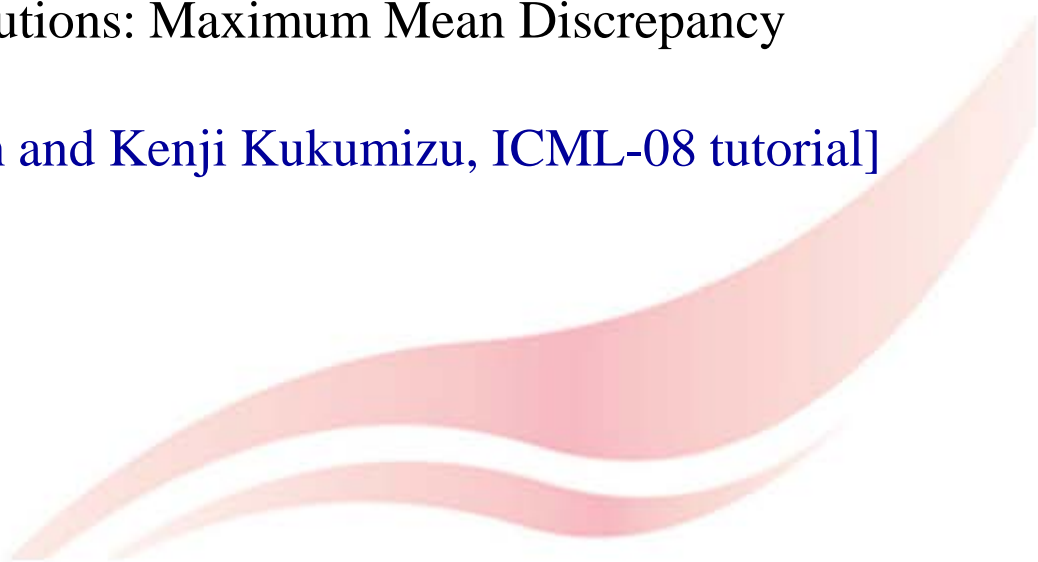
and calculate $\frac{P_T(x)}{P_S(x)}$. 

An alternative solution is to estimate $\frac{P_T(x)}{P_S(x)}$ directly. 

Correcting Sample Selection Bias / Covariate Shift

[Quionero-Candela, *etal*, Data Shift in Machine Learning, MIT Press 2009]

Classic Approaches

- Modeling a sampling selection biased process [Zadrozny, ICML-04]
 - Assume the difference between $P_S(x)$ and $P_T(x)$ is caused by a biased sample selection process
 - Approximate $\beta(x)$ by a linear combination of some base functions [Sugiyama *etal.*, NIPS-07, Kanamori *etal.*, JMLR-09]
 - $\beta(x) = \sum_{\ell=1}^b \alpha_{\ell} \psi_{\ell}(x)$, where the coefficients α'_{ℓ} s are to be learned
 - Kernel mean matching (KMM) [Huang *etal.*, NIPS-06]
 - Kernel embedding of distributions: Maximum Mean Discrepancy (MMD)
[Alex Smola, Arthur Gretton and Kenji Kukumizu, ICML-08 tutorial]
- 


Instance-based Approaches: Case II

- Assumption: $P_S(y|x) \neq P_T(y|x)$

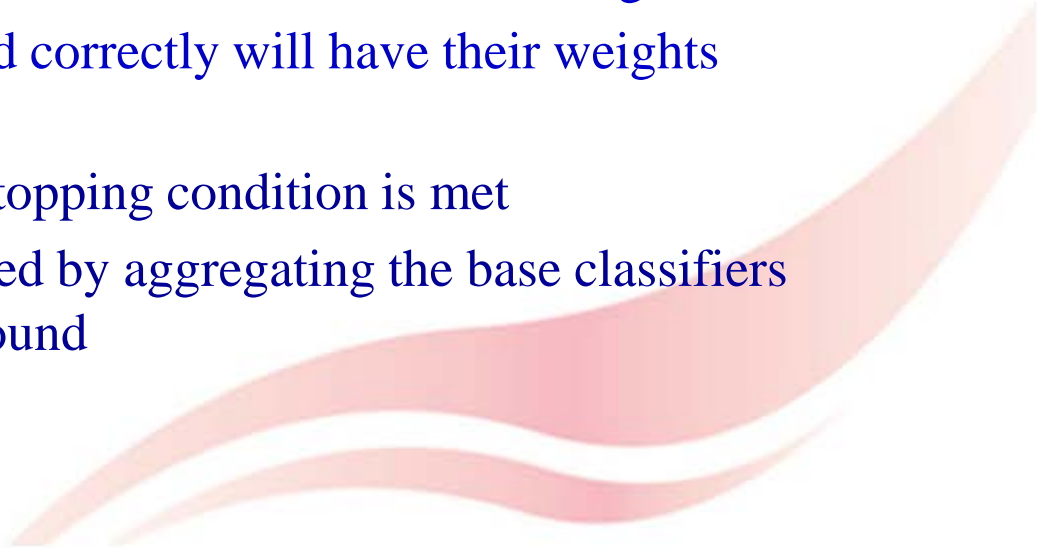
- Recall:
$$\begin{aligned}\theta^* &= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x,y)}{P_S(x,y)} l(x,y,\theta) \right] \\ &= \arg \min \mathbb{E}_{(x,y) \sim P_S} \left[\frac{P_T(x)P_T(y|x)}{P_S(x)P_S(y|x)} l(x,y,\theta) \right] \\ &\quad \not\propto \frac{P_T(x)}{P_S(x)}\end{aligned}$$

- Intuitive idea: Part of the labeled data in the source domain can be reused in the target domain after re-weighting based on their contributions to the classification accuracy of the learning problem in the target domain

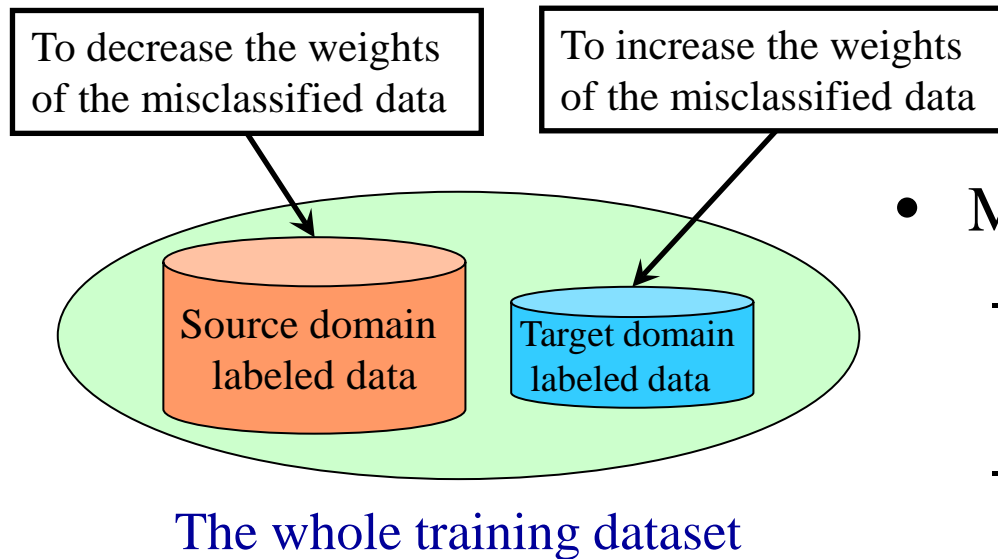
TraAdaBoost [Dai *etal* ICML-07]

- A boosting style approach to transfer learning
 - High-level idea:
 - Use the same strategy as a standard boosting approach to update the weights of target domain data
 - Use a new mechanism to decrease the weights of misclassified source domain data
- 

Boosting Procedure: Review

1. Initially, all training examples are assigned equal weights, so that they are equally likely to be chosen for training. A sample is drawn uniformly to obtain a new training set.
 2. A classifier is induced from the training set, and used to classify all the examples in the original training set
 3. The weights of the training examples are updated at the end of each boosting round
 - Records that are wrongly classified will have their weights increased
 - Records that are classified correctly will have their weights decreased
 4. Repeat Step 2 and 3 until the stopping condition is met
 5. Finally, the ensemble is obtained by aggregating the base classifiers obtained from each boosting round
- 

TrAdaBoost

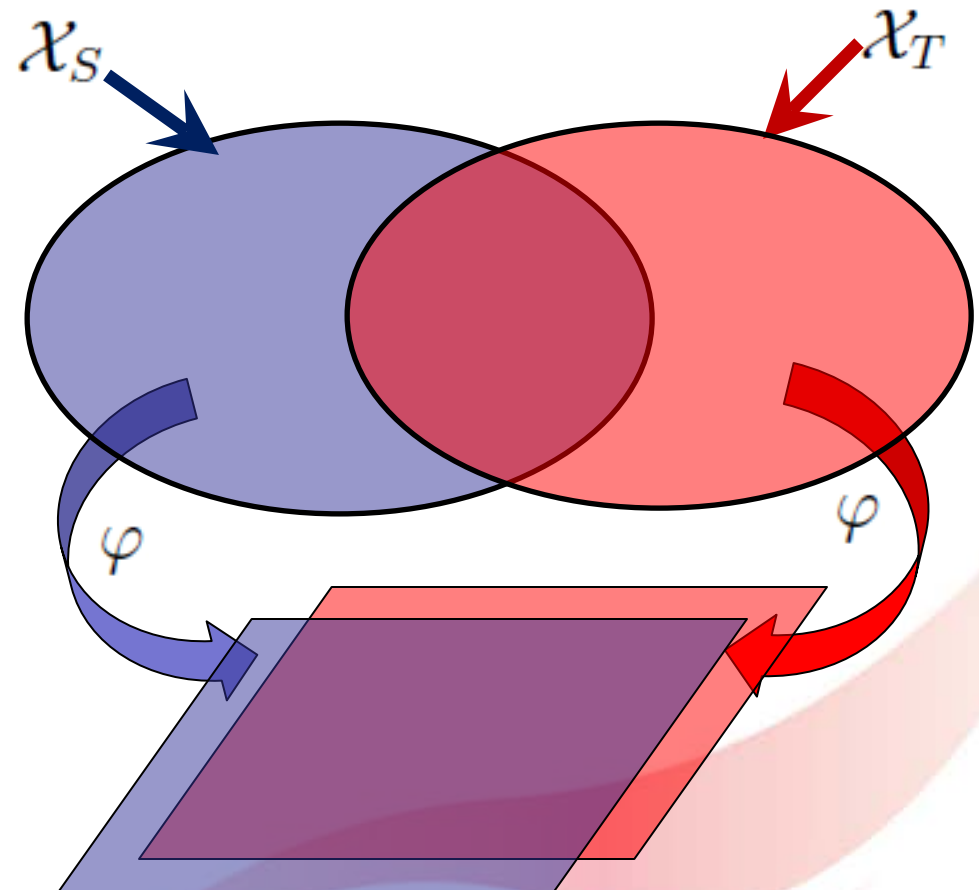


- Misclassified instances:
 - increase the weights of the misclassified **target** data
 - decrease the weights of the misclassified **source** data

TrAdaBoost is build on top of AdaBoost

Feature-based TL Approaches

When source and target domains only have some overlapping features. (lots of features only have support in either the source or the target domain)



General Feature-based TL Approaches

- General approaches to learning the transformation
 - Learning features by minimizing distance between distributions
 - Learning universal features via self-taught learning

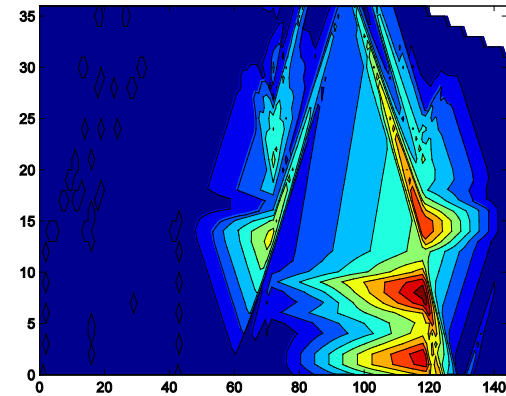
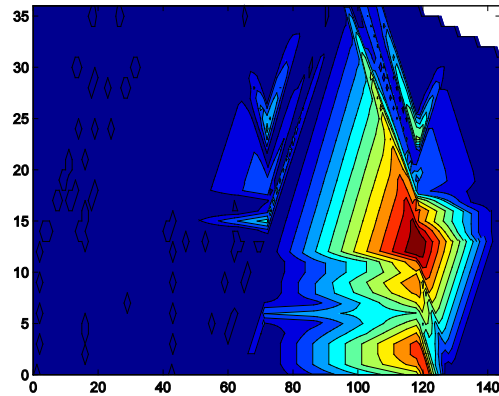


An Example

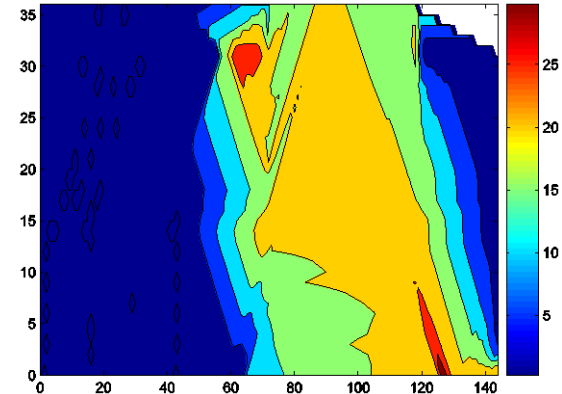
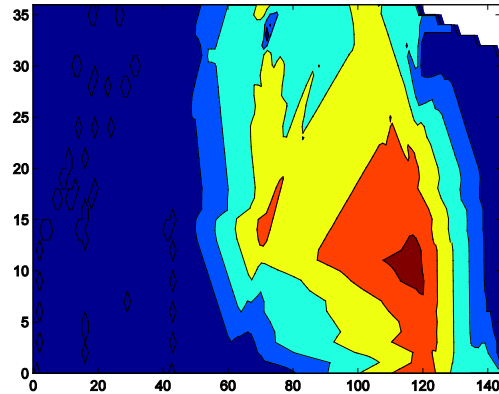
Time Period A

Time Period B

Device A



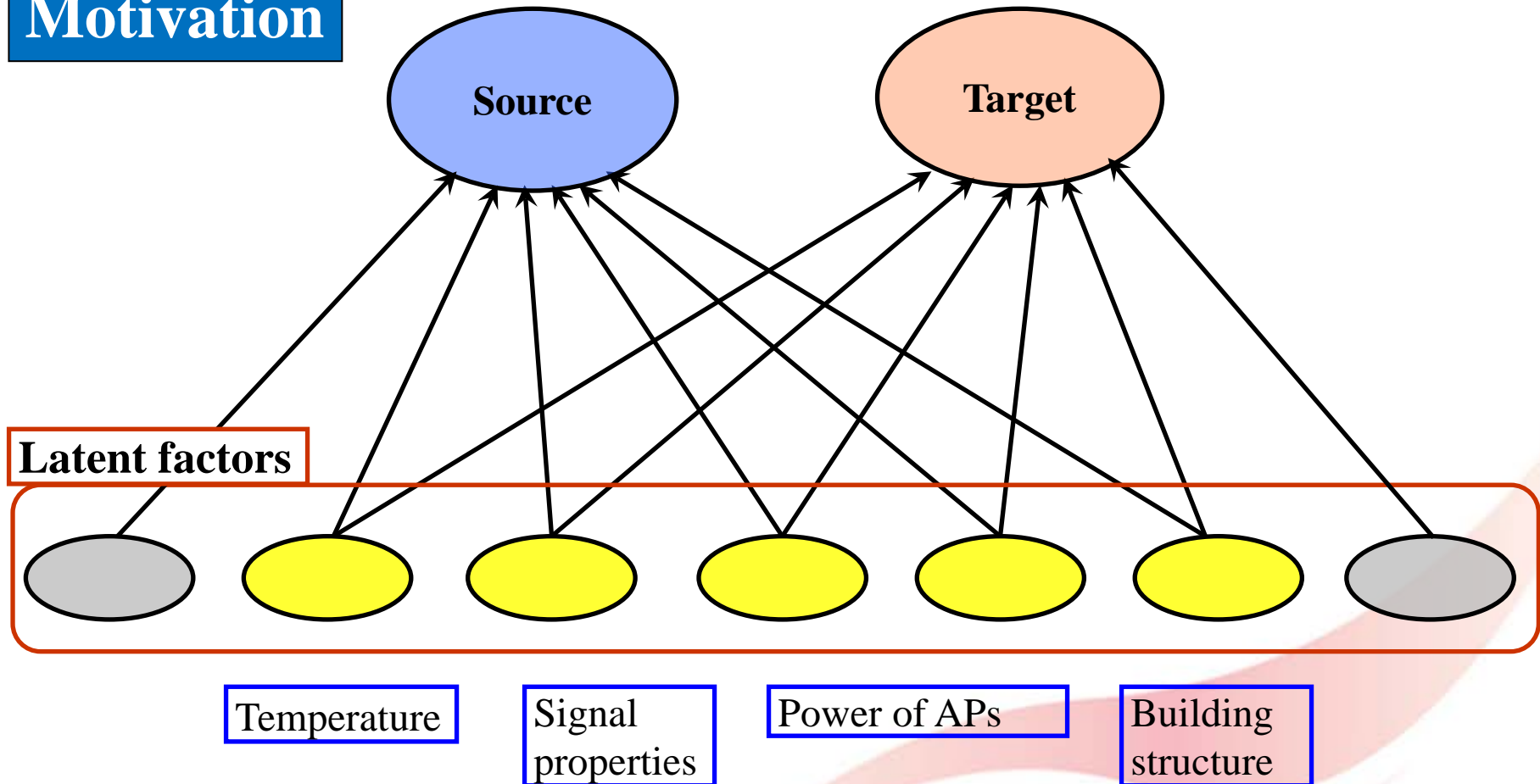
Device B



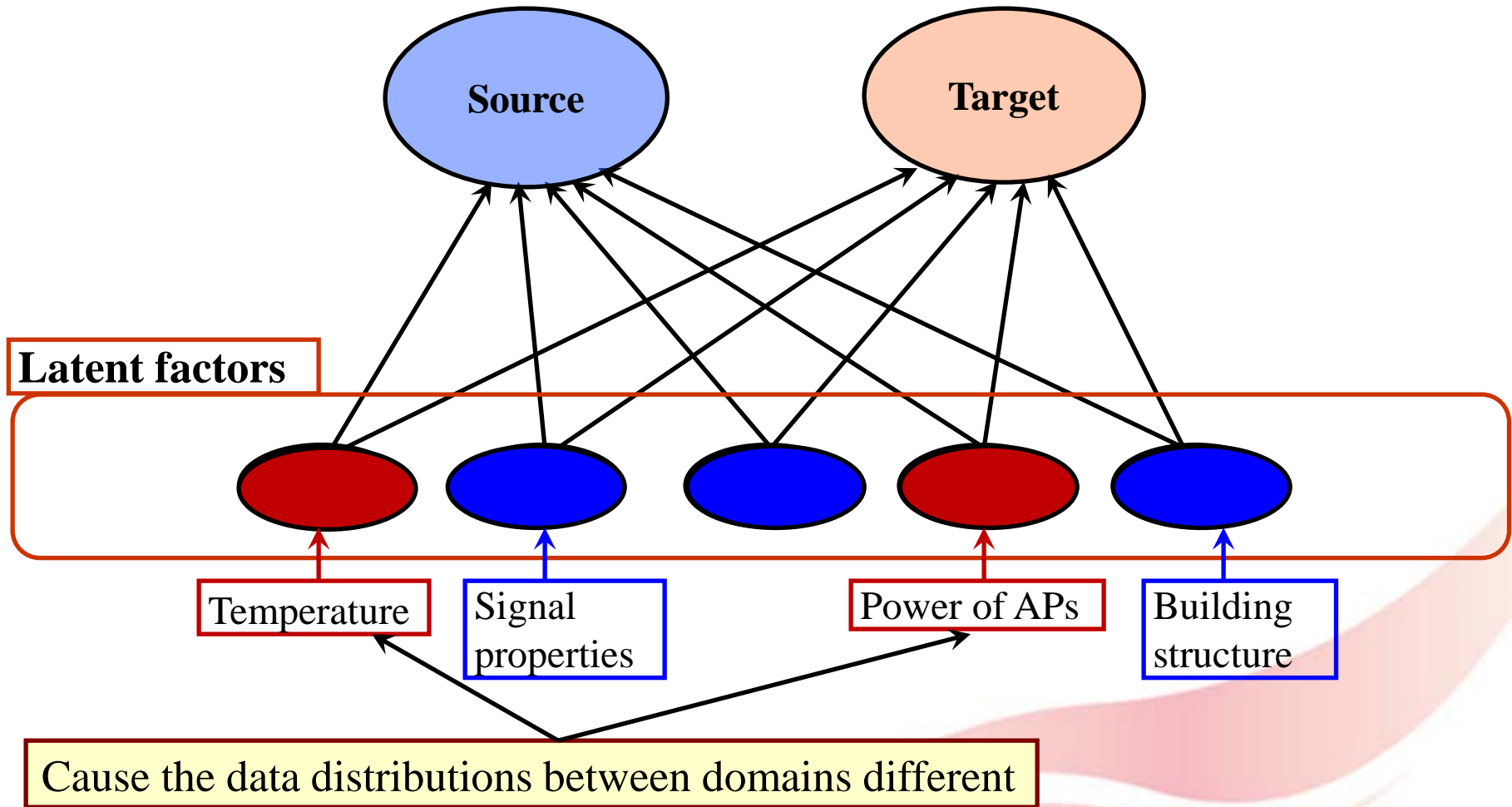
Transfer Component Analysis (TCA)

[Pan *et al.*, IJCAI-09, TNN-11]

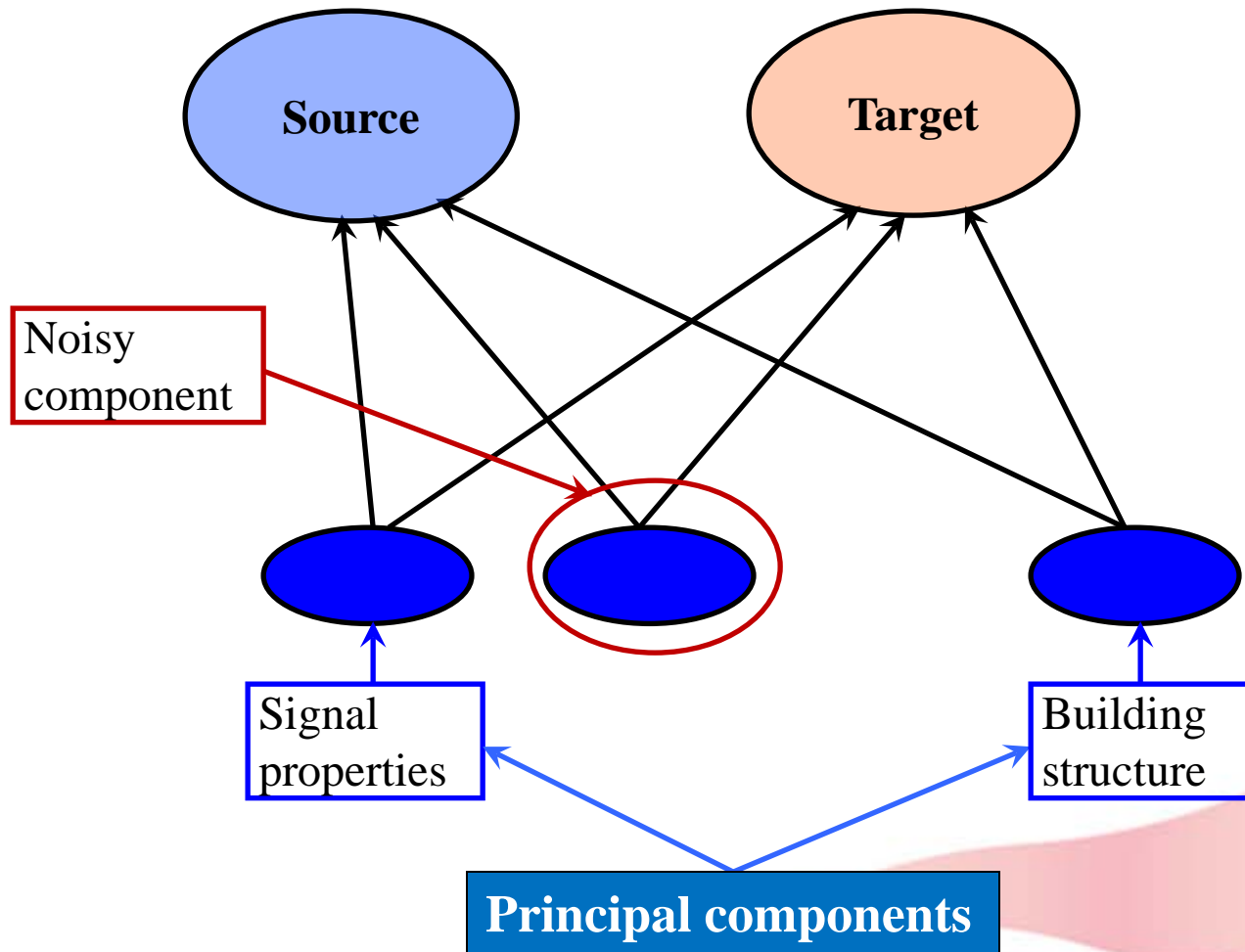
Motivation



TCA (cont.)

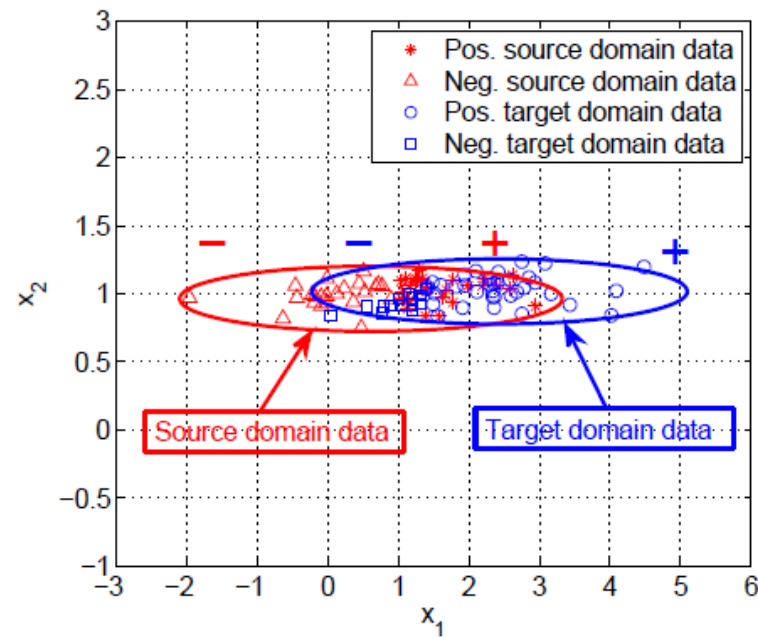


TCA (cont.)



TCA (cont.)

Learning φ by only minimizing distance between distributions may map the data onto noisy factors.



TCA (cont.)

- Main idea: the learned φ should map the source domain and target domain data to a latent space spanned by the factors that reduce domain distance as well as preserve data structure
- High level optimization problem

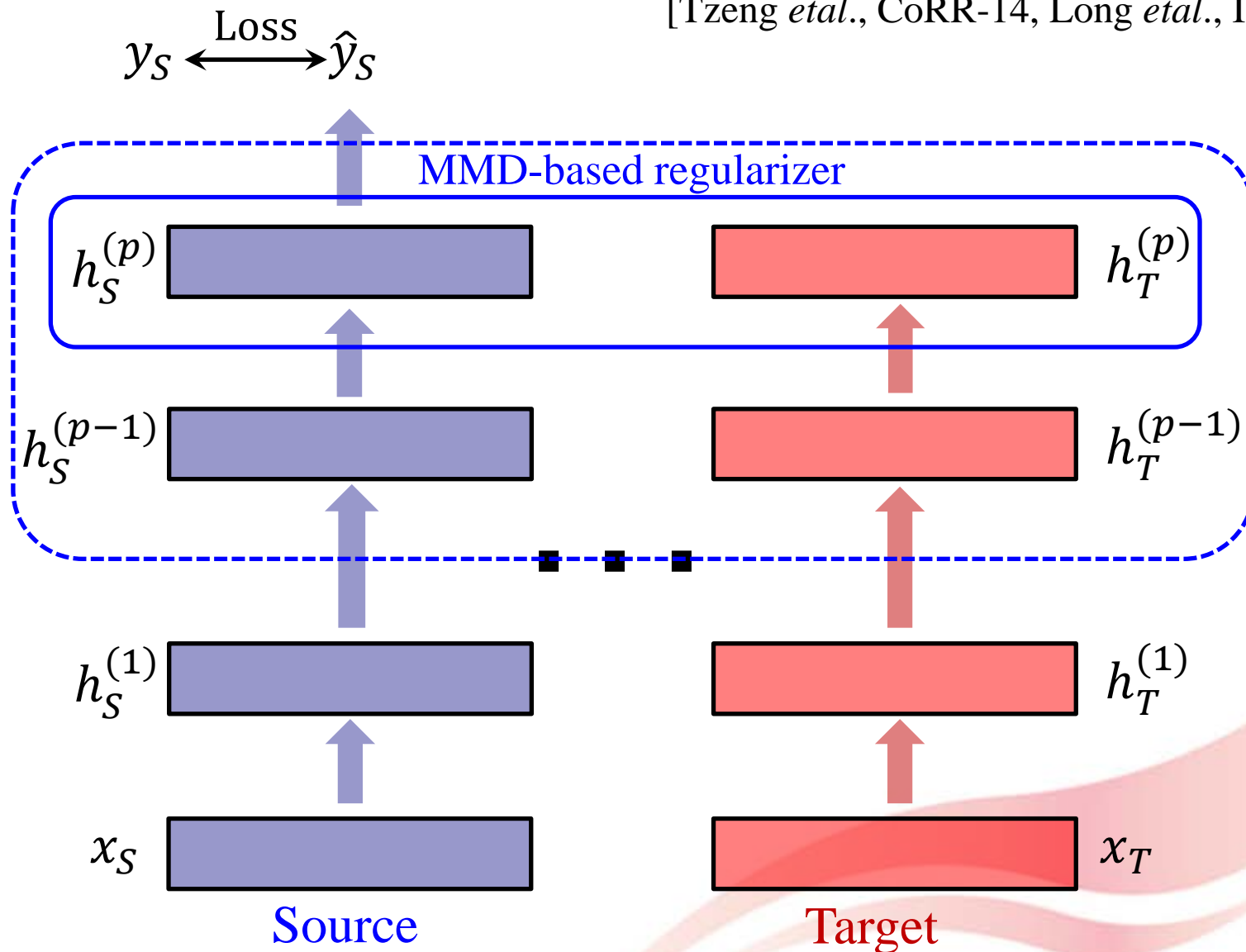
$$\begin{array}{ll} \min_{\varphi} & \text{Dist}(\varphi(X_S), \varphi(X_T)) + \lambda \Omega(\varphi) \\ \text{s.t.} & \text{constraints on } \varphi(X_S) \text{ and } \varphi(X_T) \end{array}$$

Preserve data variance

Maximum Mean Discrepancy (MMD)

Extension to Deep Architecture

[Tzeng *et al.*, CoRR-14, Long *et al.*, ICML-15]



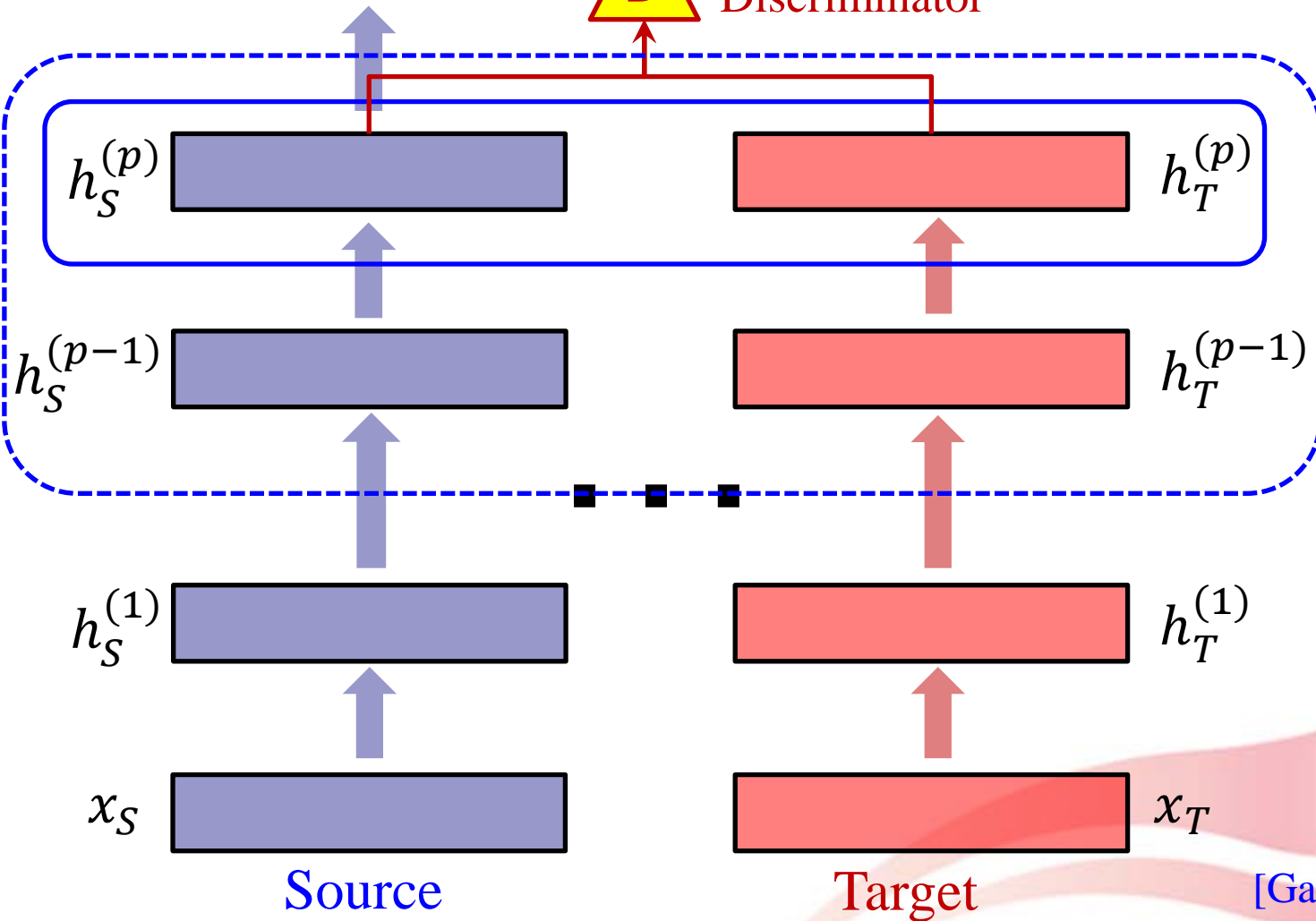
Domain Adversarial Training

$y_S \xleftrightarrow{\text{Loss}} \hat{y}_S$

D Domain Discriminator

Objective 1: learn hidden features to obtain low loss: **minimization**

Objective 2: learn hidden features to confuse domain discriminator: **maximization**



General Feature-based TL Approaches

- General approaches to learning the transformation
 - Learning features by minimizing distance between distributions
 - Learning universal features via self-taught learning

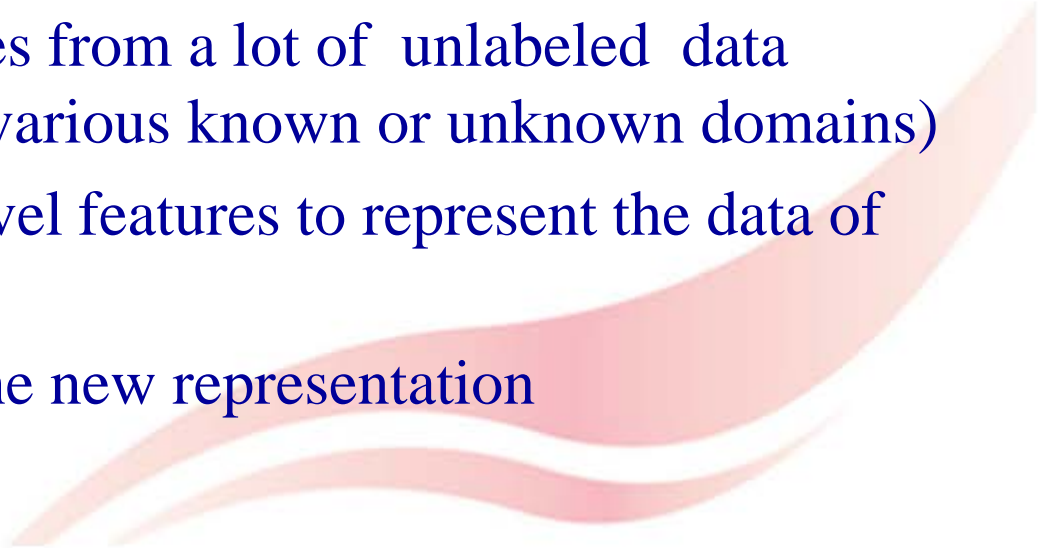


Self-taught Feature Learning

- **Motivation:**

- There exist some high-level features that can help the target learning task even only a few labeled data are given
- High-level features can be learned in advance from auxiliary tasks or domains

- **General steps:**

- Learn high-level features from a lot of unlabeled data (which can come from various known or unknown domains)
 - Use the learned high-level features to represent the data of the target task
 - Training models with the new representation
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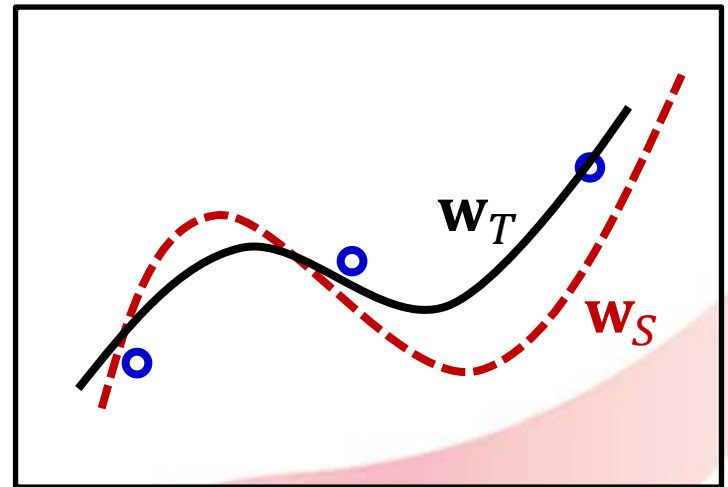
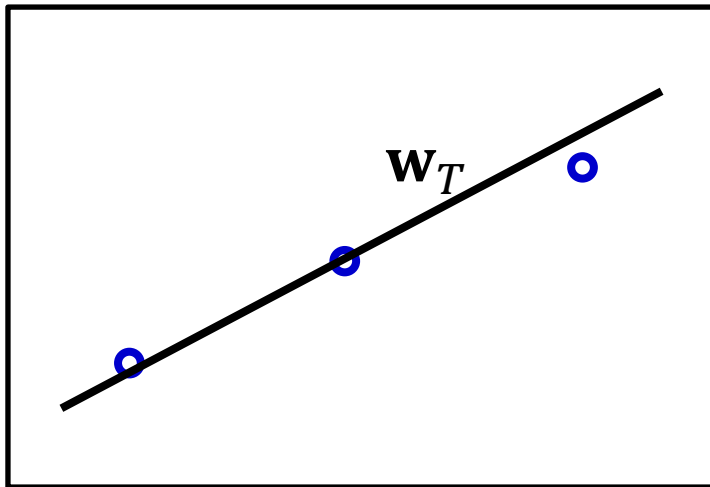
Self-taught Feature Learning (cont.)

- How to learn universal high-level features
 - Sparse Coding [Raina et al., 2007]
 - Autoencoder [Glorot *et al.*, 2011]
 - Other deep learning models, e.g., CNNs



Parameter-based Approaches

- **Motivation:** A well-trained source model \mathbf{w}_S has captured a lot of structure from data. If two tasks are related, this structure can be transferred to learn a more precise target model \mathbf{w}_T with a few labeled data in the target domain



Parameter-based TL Approaches (cont.)

- Assumption: if tasks are related, they may share similar parameter vectors

$$\begin{aligned} \mathbf{w}_S &= \mathbf{w}_0 + \mathbf{v}_S \\ \mathbf{w}_T &= \mathbf{w}_0 + \mathbf{v}_T \end{aligned}$$

Common part

Specific part for individual task

The diagram illustrates the decomposition of task-specific parameters. Two equations are shown: $\mathbf{w}_S = \mathbf{w}_0 + \mathbf{v}_S$ and $\mathbf{w}_T = \mathbf{w}_0 + \mathbf{v}_T$. A black box encloses the \mathbf{w}_0 terms in both equations, with an arrow pointing to the text 'Common part'. Red circles enclose the \mathbf{v}_S and \mathbf{v}_T terms, with arrows pointing to the text 'Specific part for individual task'.

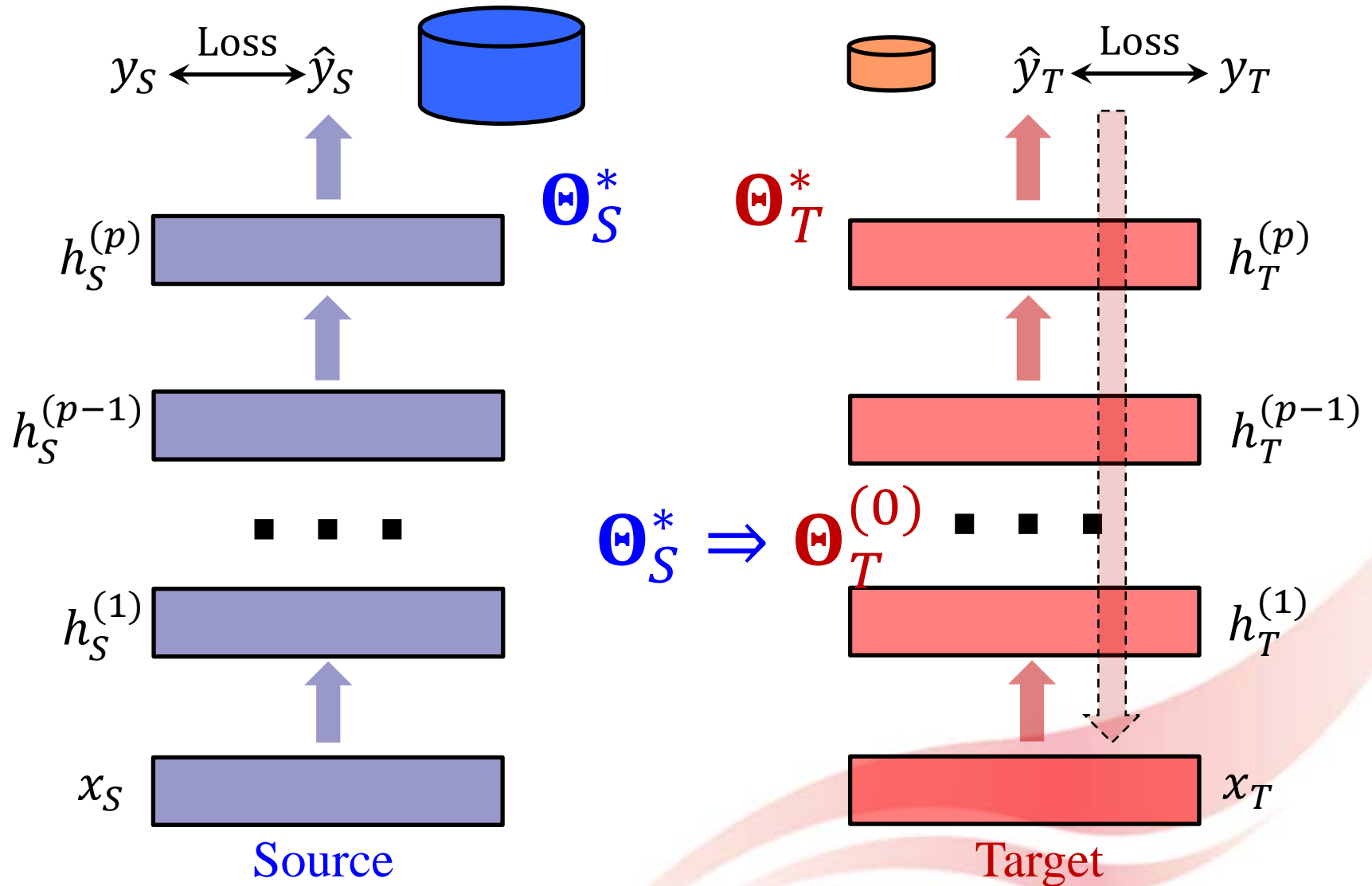
$$\min_{\mathbf{v}_S, \mathbf{v}_T, \mathbf{w}_0} \sum_{t \in \{S, T\}} \frac{\gamma_t}{n_t} \sum_{i=1}^{n_t} l(x_{t_i}, y_{t_i}; \mathbf{w}_t) + \lambda_1 (\|\mathbf{v}_S\|_2^2 + \|\mathbf{v}_T\|_2^2) + \lambda_2 \|\mathbf{w}_0\|_2^2$$

Optimized by using all the data

Optimized by using the data of individual task, respectively

The diagram shows the optimization of the parameters in the loss function. A red box encloses the regularization terms $\lambda_1 (\|\mathbf{v}_S\|_2^2 + \|\mathbf{v}_T\|_2^2)$, with an arrow pointing to the text 'Optimized by using the data of individual task, respectively'. A black box encloses the $\lambda_2 \|\mathbf{w}_0\|_2^2$ term, with an arrow pointing to the text 'Optimized by using all the data'.

In the Context of Deep Learning



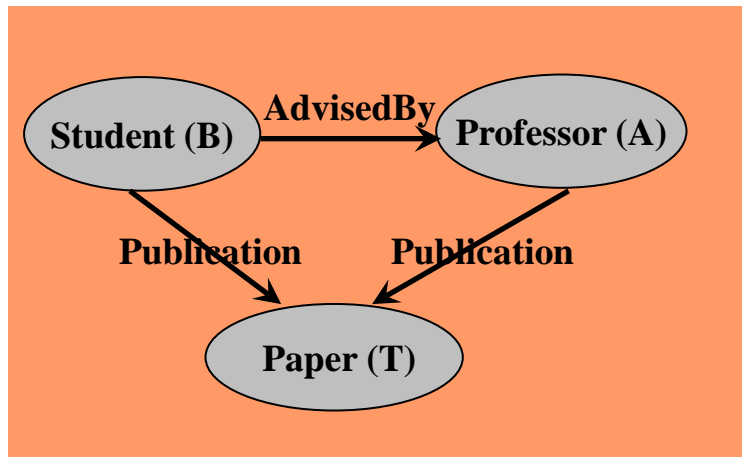
Relational TL Approaches

- **Motivation:** If two relational domains (non-i.i.d) are related, they may share some similar relations among objects. These relations can be used for knowledge transfer across domains



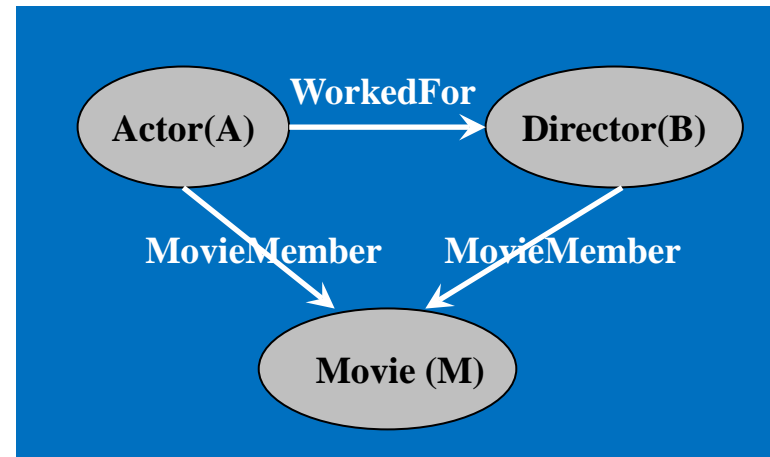
Motivating Example

Academic domain (source)



$\text{AdvisedBy}(B, A) \wedge \text{Publication}(B, T) \Rightarrow \text{Publication}(A, T)$

Movie domain (target)



$\text{WorkedFor}(A, B) \wedge \text{MovieMember}(A, M) \Rightarrow \text{MovieMember}(B, M)$

$P1(x, y) \wedge P2(x, z) \Rightarrow P2(y, z)$

Summary

In data level

Instance-based Approaches

Knowledge to be transferred corresponds to the weights attached to source instances

Feature-based Approaches

Knowledge to be transferred corresponds to be the learned features across domains

Parameter-based Approaches

Knowledge to be transferred is embedded in part of the source models

In model level

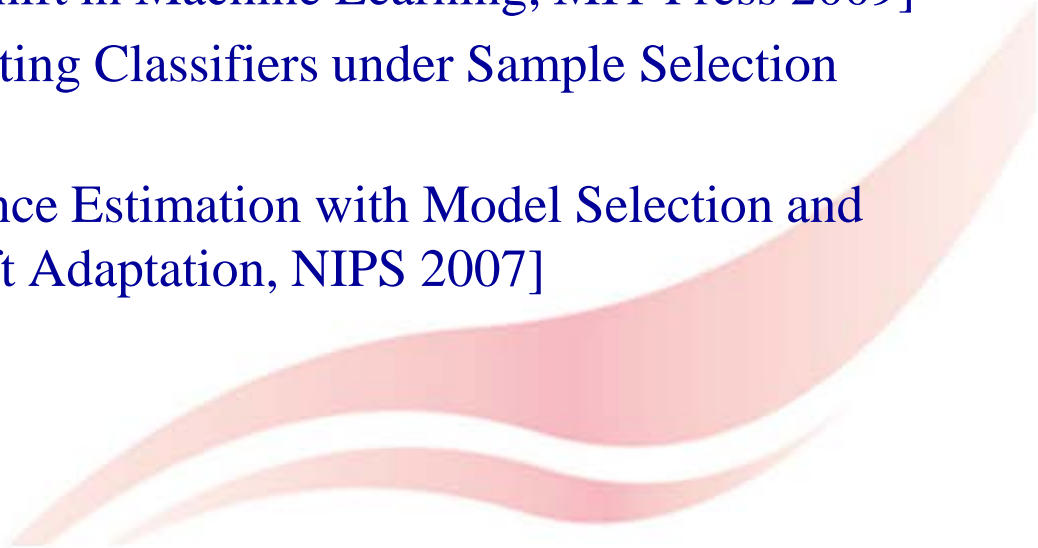
Relational Approaches

Knowledge to be transferred corresponds to the rules specifying the relations between entity in the source

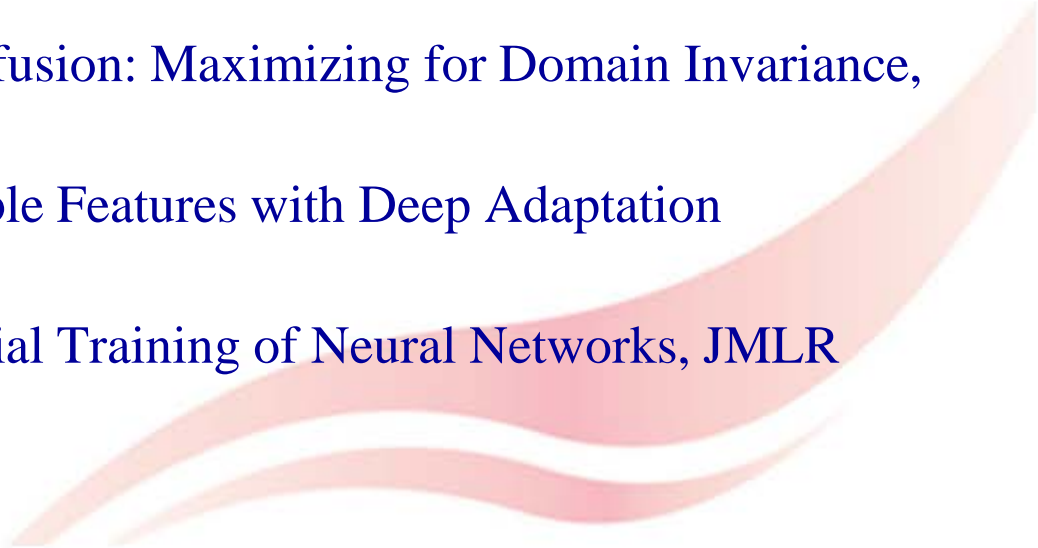
Thank You!




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 - [Davis and Domingos, Deep Transfer via Second-order Markov Logic, ICML 2009]
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- A decorative graphic consisting of several overlapping, wavy, curved lines in shades of light pink and peach, located in the bottom right corner of the slide.