

AI6122 Text Data Management & Analysis

Topic: Parsing



Syntax

- **The way words are arranged together**
 - Implicit knowledge of your native language that you had mastered by the time you were young without explicit instruction
 - Not the kind of stuff you were later taught in “grammar” school
- Why should we care?
 - Syntax is the key concept for many NLP tasks
 - E.g. information extraction, grammar checking
 - An **approximation** would be still useful



Key notions

- Constituency
 - Groups of words that behave as **a single unit** or **phrase**
 - E.g., a few words form a noun phrase
- Grammatical relations
 - Syntactic relations between constituents
 - E.g., Subject – verb, verb – object
- Subcategorization
 - Certain kinds of relation between words and phrases
 - transitive words, which can take a direct object
 - intransitive words which cannot take a direct object



Constituent

- Groups of words that behave as a single unit or phrase
 - Can all appear in similar syntactic environments
- Example: Noun phrases (NPs) can occur before verbs
 - Three example sentences starting with NPs
 - three parties from Brooklyn *arrive* ...
 - a high-class spot such as Mindy's *attracts* ...
 - the Broadway coppers *love* ...
 - While the whole noun phrase can occur before a verb, it is not true of each of the individual words that make up a noun phrase



Constituent

- Evidence for constituency
 - Stick together through pre-/post-posed constructions (example using a prepositional phrase)
 - On September seventeenth, I'd like to fly from Atlanta to Denver.
 - I'd like to fly on September seventeenth from Atlanta to Denver.
 - I'd like to fly from Atlanta to Denver on September seventeenth.
 - Individual words making of the phrase cannot be placed differently.
 - *On, I'd like to fly from Atlanta to Denver September seventeenth.
- Non-standard constructions (or constituents)
 - I gave John a watch and Mary a doll.
 - *I gave John a watch Mary and a doll.



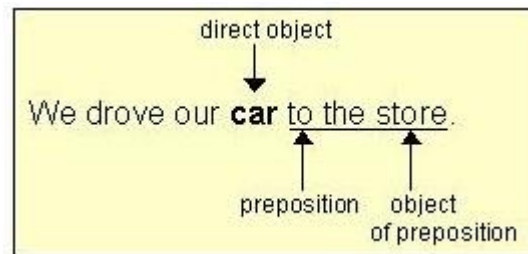
For your information only (details in textbook)

- Noun phrase (NP), verb phrase (VP), prepositional phrase (PP), adjective phrase
- Declarative, imperative, clause
 - Declarative sentences have a subject noun phrase followed by a verb phrase. “I prefer a morning flight”
 - Imperative sentences begin with a verb and have no subject. “Show me the code”.
- Determiner, nominal, quantifier
 - Noun phrases can begin with determiners or quantifier. “a bus stop” “a non-stop flight”
- Auxiliaries, passive, perfect, progressive
 - Auxiliaries include modal verb can could shall, perfect auxiliary have, progressive auxiliary be and passive auxiliary be
- Coordination, conjunction
 - A coordinate noun phrase can consist of two noun phrases by a conjunction: “course code and course title”



Grammatical relations

- Syntactic relations **between constituents**
 - Subject-verb: I love him.
 - Verb-object: I love him.
 - Verb-PrepositionalPhrase: I study at the library.
 - Noun-PrepositionalPhrase: The history of Singapore
 - Preposition-object



<https://webapps.towson.edu/ows/prepositions.htm>

Verb phrases (VPs): Sample patterns

- Verb
 - disappear
 - *prefer
- Verb Object
 - prefer a morning flight
 - *disappear a morning flight
- Verb IObject DObject (indirect object, direct object)
 - give John a watch
 - *prefer John a watch
- Verb Object PrepositionalPhrase(PP)
 - leave Boston in the morning
- Verb PP
 - leave on Thursday



Subcategorization

- ‘Subcategories’ of different types of verbs, by the constituents complement them
 - Verb “disappear”
 - Verb NP “prefer a morning flight”
 - Verb NP NP “give John a watch”
 - Verb NP PP “leave Boston in the morning”
 - Verb PP “leave on Thursday”
- Subcategorization frame
 - A possible set of complements for a verb
 - e.g. ‘give’: {}, {NP}, {NP, NP}, {NP, PPto}, {PP}
 - Verb: function, complements: arguments
 - e.g. `def buy(Person: buyer, Thing: product)`

Syntactic structure

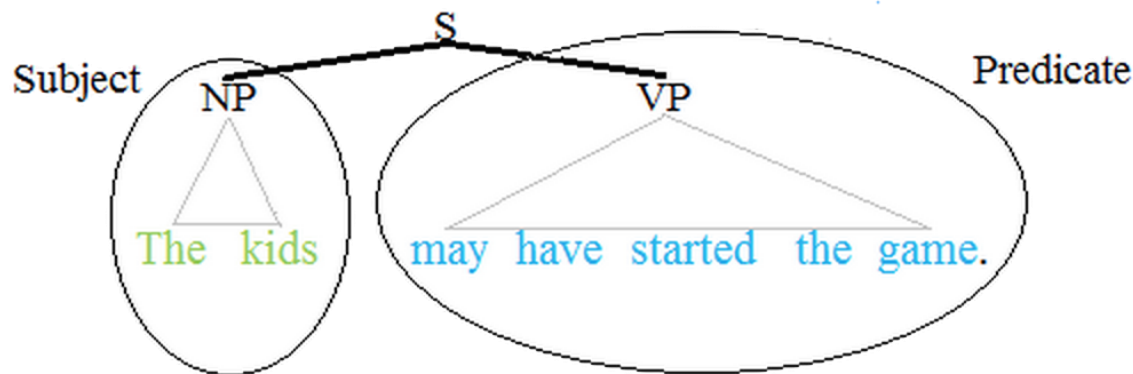
- Why do we learn about syntax in NLP course?
 - To identify and understand the syntactic structures of sentences
- **Parse tree**
 - Structural representation of grammatical relations expressed in a string
- Representations
 - Phrase structure
 - Dependency structure
 - Predicate-argument structure

Syntactic \neq Semantic

- iPhone7 is nice but expensive
- iPhone7 is expensive but nice

Phrase Structure

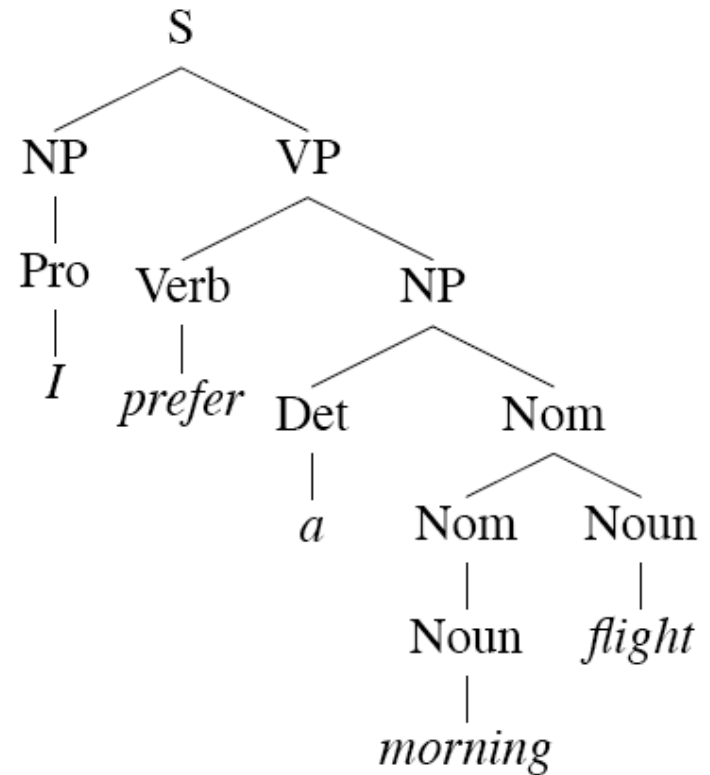
- Phrase structure rules are used to break down a natural language sentence into its constituent parts (also known as syntactic categories), including both lexical categories (parts of speech) and phrasal categories
 - Split a sentence (S) into subject (NP) and predicate (VP)
 - Split subject and predicate into smaller parts
 - Continue until terminal nodes are reached



Phrase Structure

- Organizes words into nested constituents
 - Example sentence: “I prefer a morning flight”

(S
 (NP (Pro I))
 (VP (Verb **prefer**)
 (NP (Det **a**)
 (Nom
 (Nom (Noun **morning**))
 (Noun **flight**))))))



Nominal: (i) noun phrase without determiner; and
(ii) the noun that modifies the head noun in a noun phrase.

Exercise: Phrase structure

- Give the phrase structures of the two sentences:
 - (S1) John gives a present to Mary.
 - (S2) John gives Mary a present.
- POS tags:
 - E.g. ProperNoun: John, Mary
 - E.g. Verb, Det, Noun, Prep
- Example syntactic tags
 - E.g. S, NP, VP, PP_{xx}



Exercise: Phrase structure

- Give the phrase structures of the two sentences:

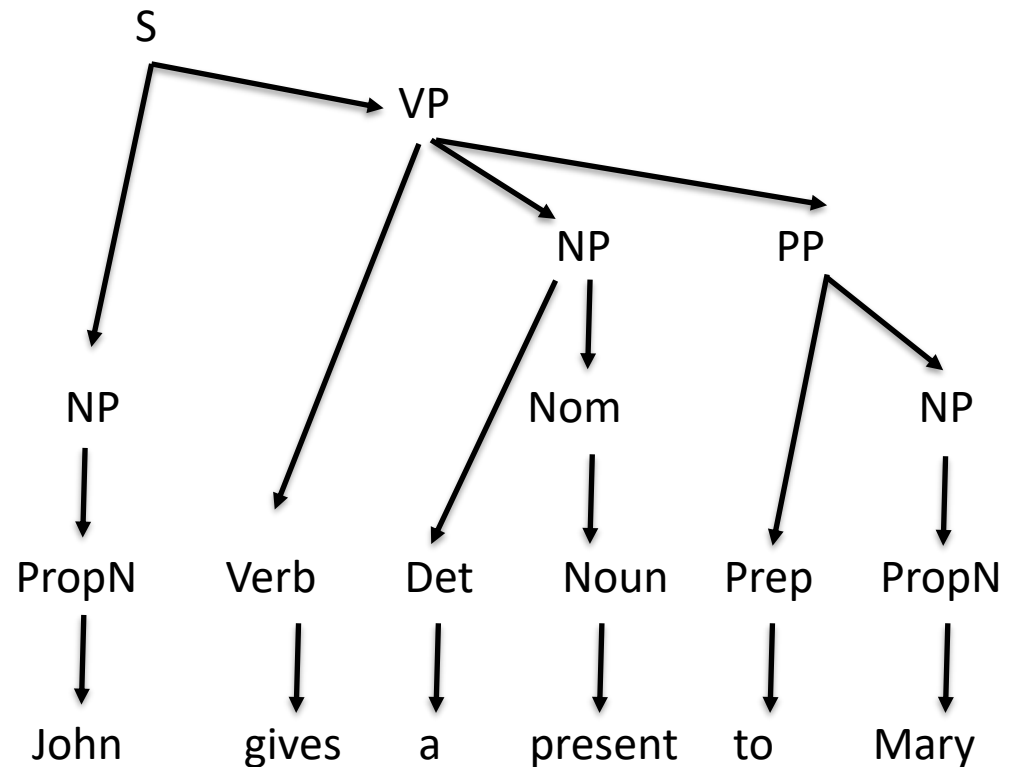
- (S1) John gives a present to Mary.
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- POS tags:

- E.g. ProperNoun: John, Mary
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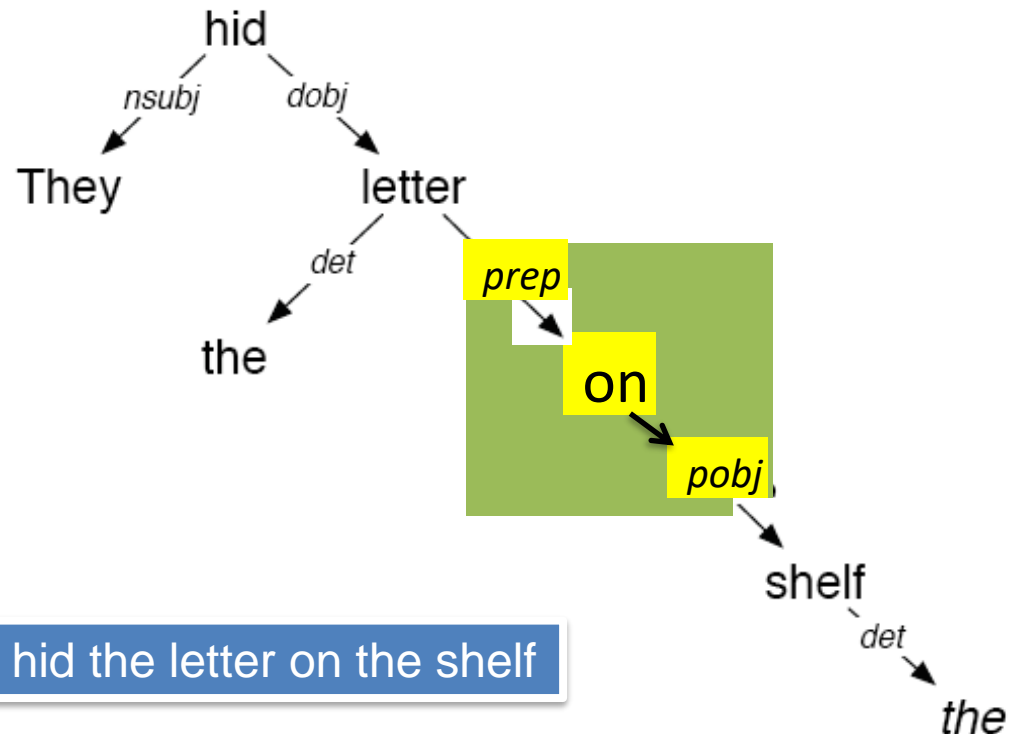
- Example syntactic tags

- E.g. S, NP, VP, PP_{xx}



Dependency structure

- Represents grammatical (dependency) relations between pairs of words: head, dependent
- Head: Grammatically most important word in a phrase
 - Verb of VP
 - Noun of NP
 - Prep of PP
 - Adj of AdjP
 - ...



They hid the letter on the shelf

Dependency Relations

Argument Dependencies	Description
nsubj	nominal subject
csbj	clausal subject
dobj	direct object
iobj	indirect object
pobj	object of preposition
Modifier Dependencies	Description
tmod	temporal modifier
appos	appositional modifier
det	determiner
prep	prepositional modifier

<http://universaldependencies.org/u/dep/index.html>



Phrase structure vs. Dependency structure

(S

(NP (Pro **They**))

(VP

(Verb **hid**)

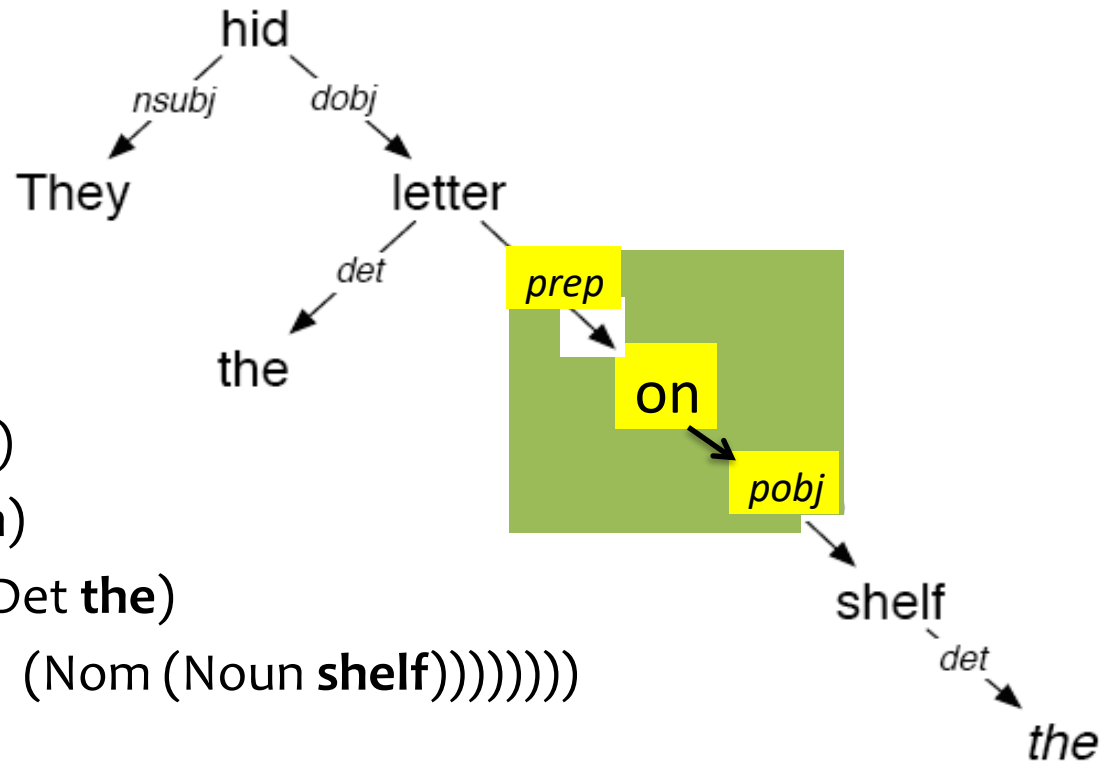
(NP (Det **the**)

(Nom (Noun **letter**)

(PP (Prep **on**)

(NP (Det **the**)

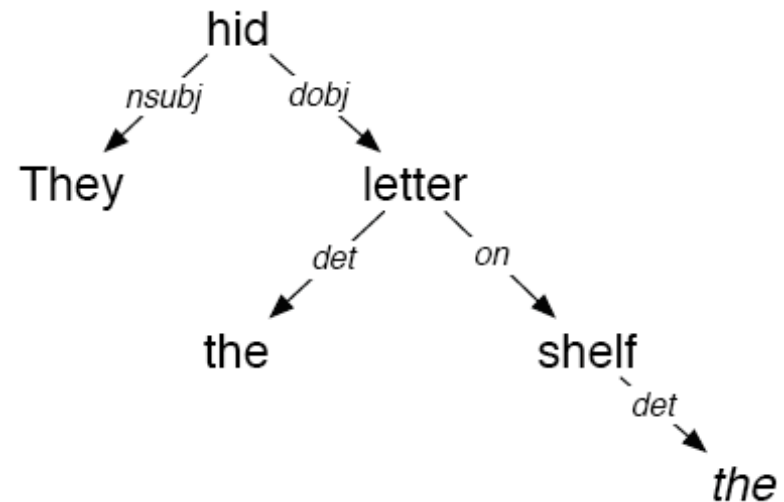
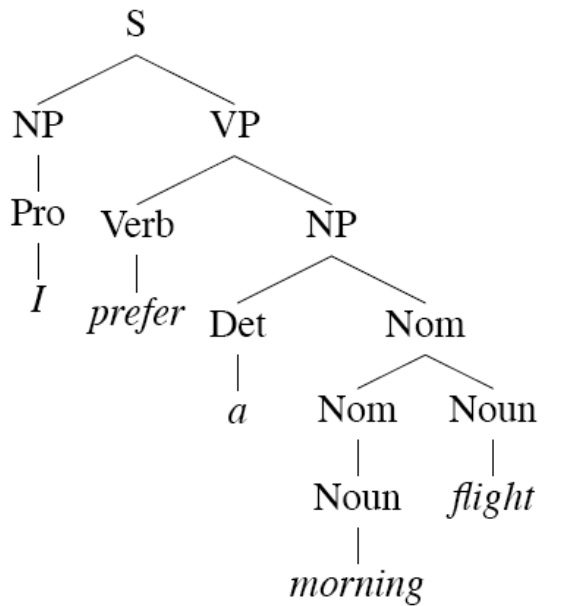
(Nom (Noun **shelf**)))))))))



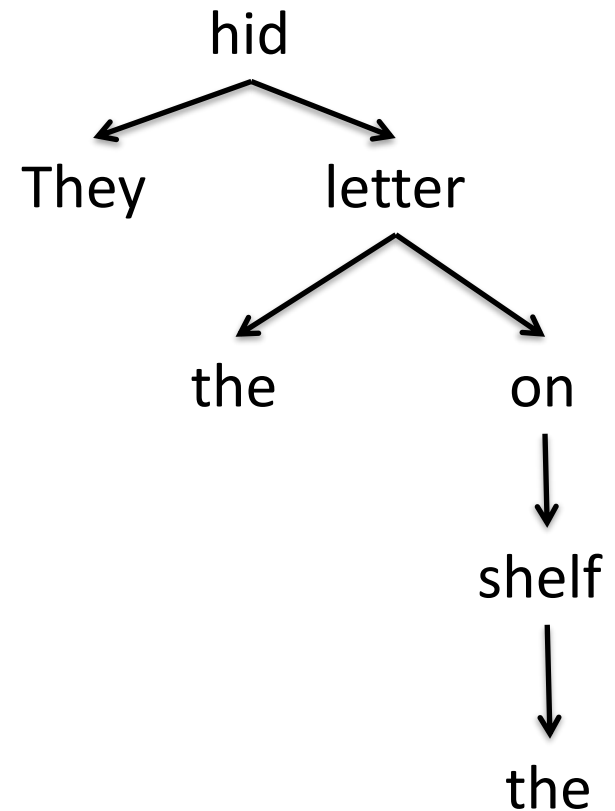
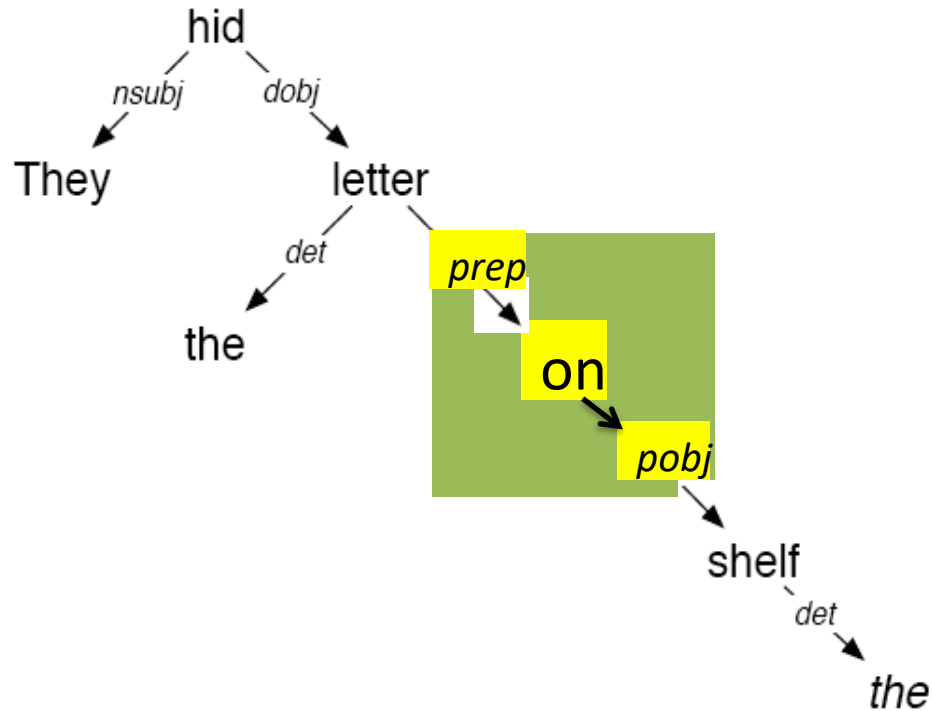
They hid the letter on the shelf

Phrase vs. dependency structure

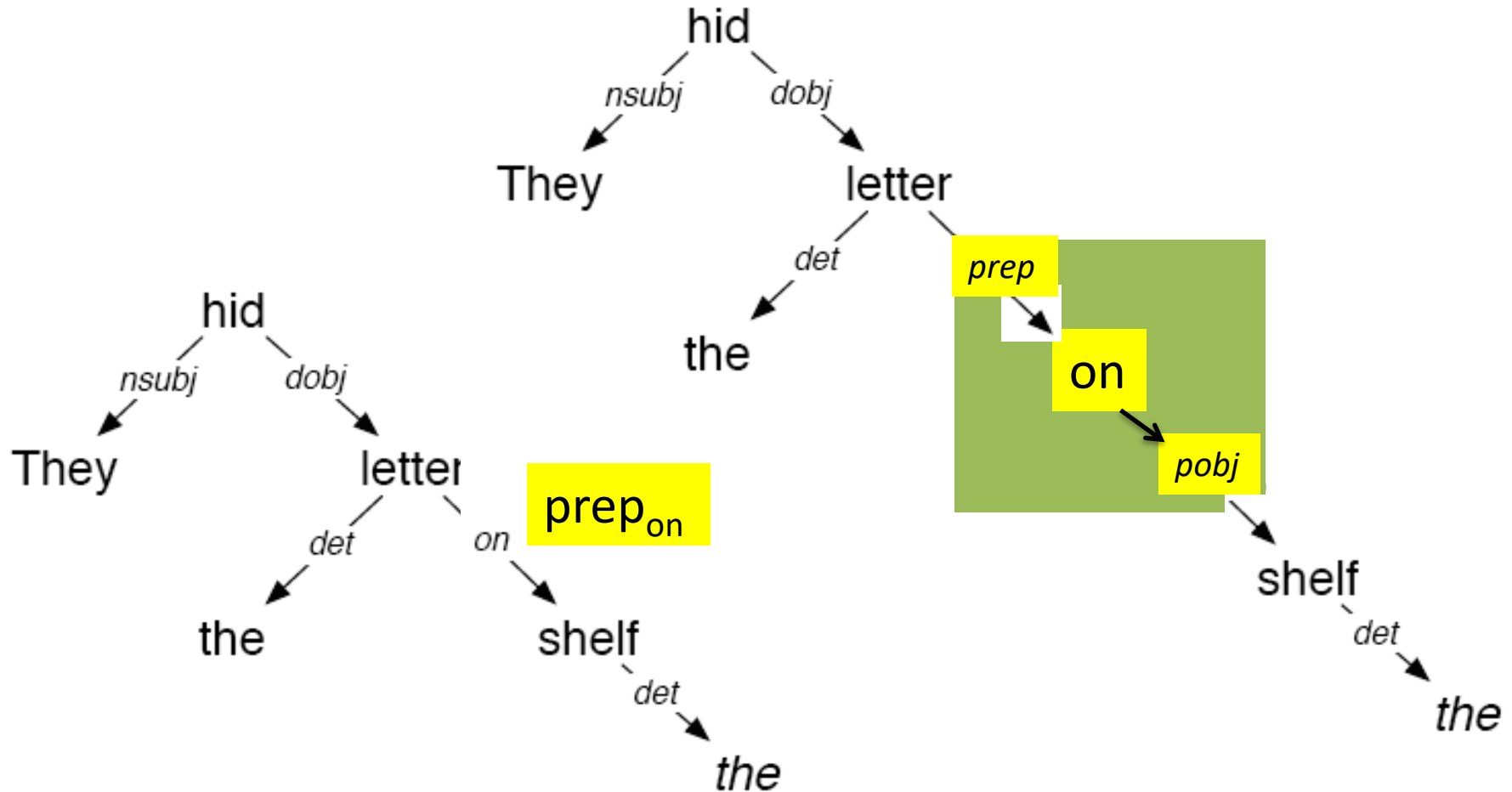
- Constituents are specified
- Grammatical relations are implied
 - Can be deduced from phrase structure
- Grammatical relations are specified
- A subtree corresponds to a constituent
 - Syntactic tag is implied by the root of subtree



Typed dependency vs. untyped dependency



Typed dependency vs. Collapsed typed dependency



Preposition word followed by its object

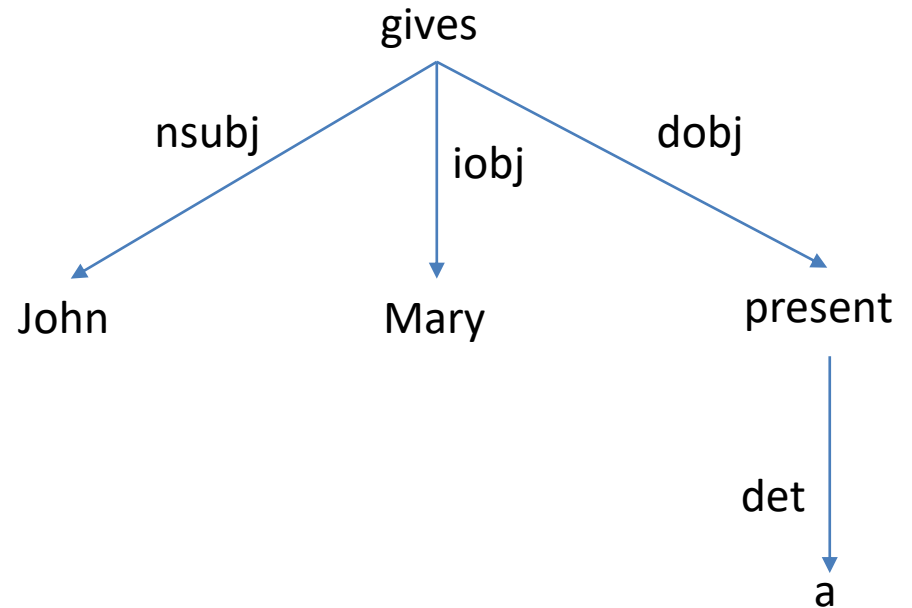
Exercise: Dependency structure

- Give the dependency structures of the two sentences:
 - (S1) John gives a present to Mary.
 - (S2) John gives Mary a present.
- Example dependency relations
 - E.g. nsubj, iobj, dobj, det, prep_{xx}



Exercise: Dependency structure

- Give the dependency structures of the two sentences:
 - (S1) John gives a present to Mary.
 - (S2) John gives Mary a present.
- Example dependency relations
 - E.g. nsubj, iobj, dobj, det, prep_{xx}



Predicate-argument structure

- Review: Subcategorization frame
 - Verb: function/predicate, complements: arguments
- Generalize to all types of words that have complements
 - E.g. Preposition: predicate, object: argument
 - E.g. They hid **the**₁ letter on **the**₂ shelf.

Relation type	Predicate	Argument 1	Argument 2
verb_arg12	hid	They	letter
det_arg1	the ₁	letter	
prep_arg12	on	letter	shelf
det_arg1	the ₂	shelf	

Dependency structure vs. Predicate-argument structure

- Sentence: They hid the letter on the shelf

Dependency structure

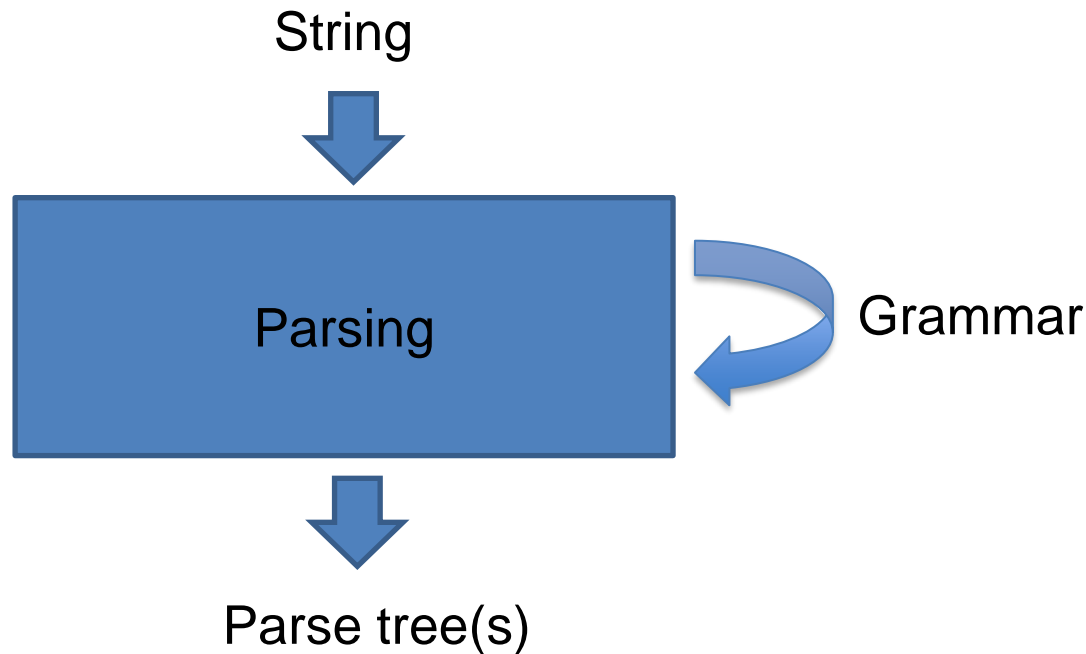
root(ROOT-0, hid-2)
nsubj(hid-2, They-1)
dobj(hid-2, letter-4)
det(letter-4, the-3)
prep_on(letter-4, shelf-7)
det(shelf-7, the-6)

Predicate-argument structure

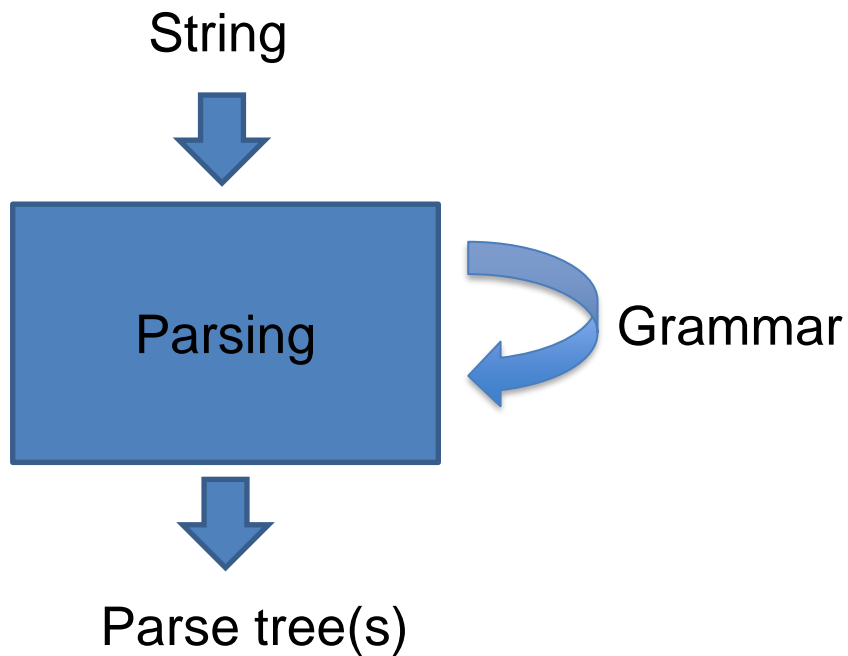
verb_arg12(hid-2, They-1, letter-4)
det_arg1(the-3, letter-4)
prep_arg12(on-6, letter-4, shelf-7)
det_arg1(the-6, shelf-7)

Syntactic parsing

- The process of taking a string and a grammar and returning parse tree(s) for that string



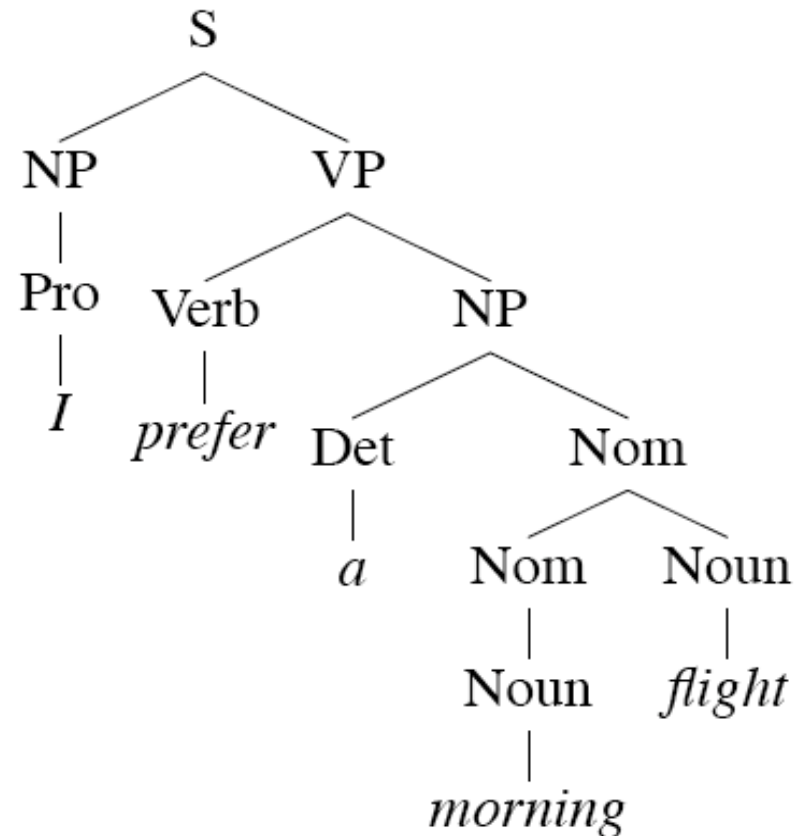
Syntactic parsing in the course



- $G = (T, N, S, R)$
 - T: a set of terminals (e.g. 'flight')
 - N: a set of non-terminals (e.g. Noun)
 - S: the start symbol, a non-terminal
 - R: rules of the form $X \rightarrow \gamma$
 - X: a non-terminal
 - γ : a sequence of terminals and non-terminals
- Examples on next slide

Context-free grammar (1/2)

- $G = (T, N, S, R)$
 - T: a set of terminals (e.g. 'flight')
 - N: a set of non-terminals (e.g. Noun)
 - S: the start symbol, a non-terminal
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 - γ : a sequence of terminals and non-terminals

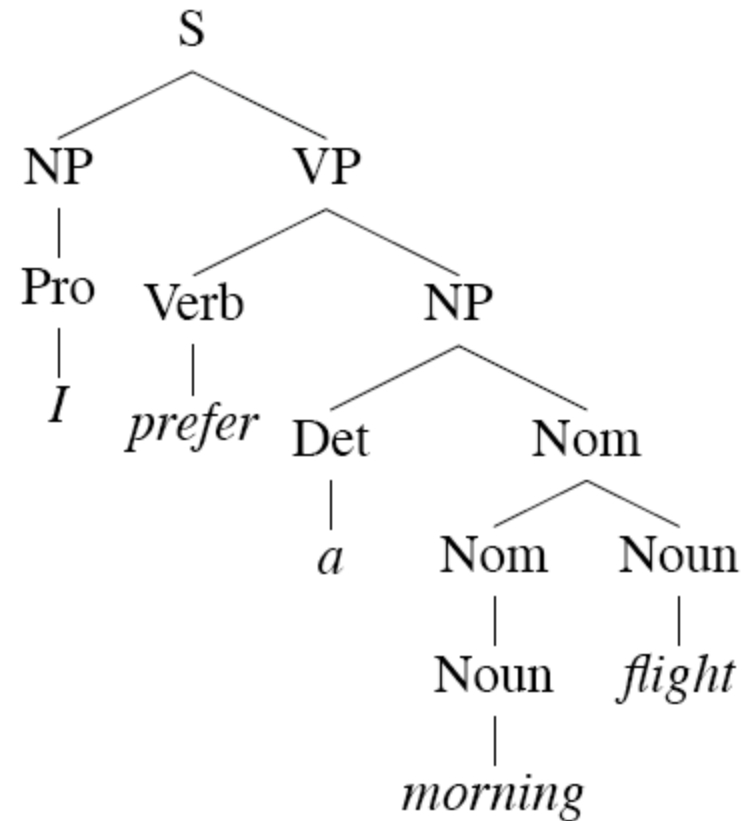


$NP \rightarrow Det\ Nominal$
$NP \rightarrow ProperNoun$
$Nominal \rightarrow Noun \mid Nominal\ Noun$

Context-free grammar (2/2)

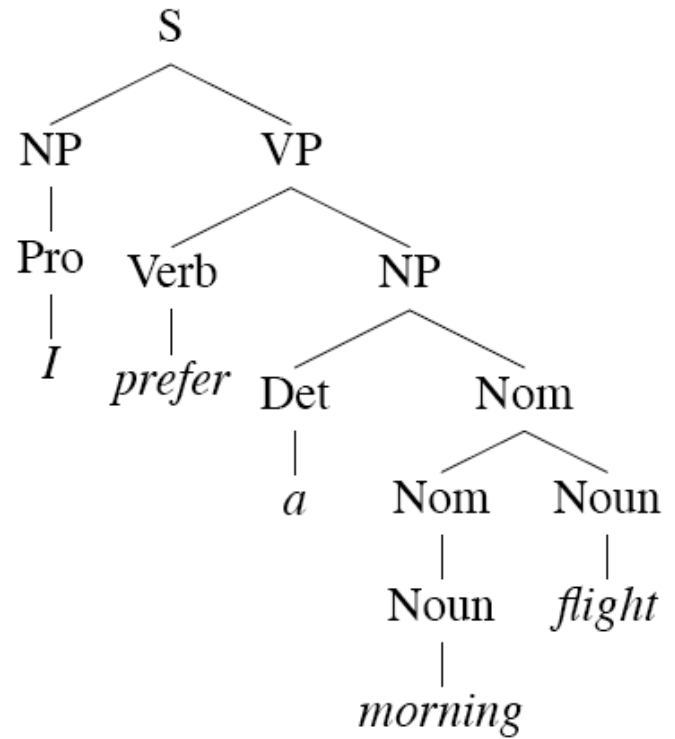
- A grammar G **generates** a language L
 - A language is a set of sentences
- $G = (T, N, S, R)$
 - T : **words or tokens**
 - N : **POS tags, syntactic tags**
 - S : the start symbol
 - R : rules of the form $X \rightarrow \gamma$
 - X : a non-terminal
 - γ : the sequence of X 's children

$NP \rightarrow Det\ Nominal$
$NP \rightarrow ProperNoun$
$Nominal \rightarrow Noun \mid Nominal\ Noun$



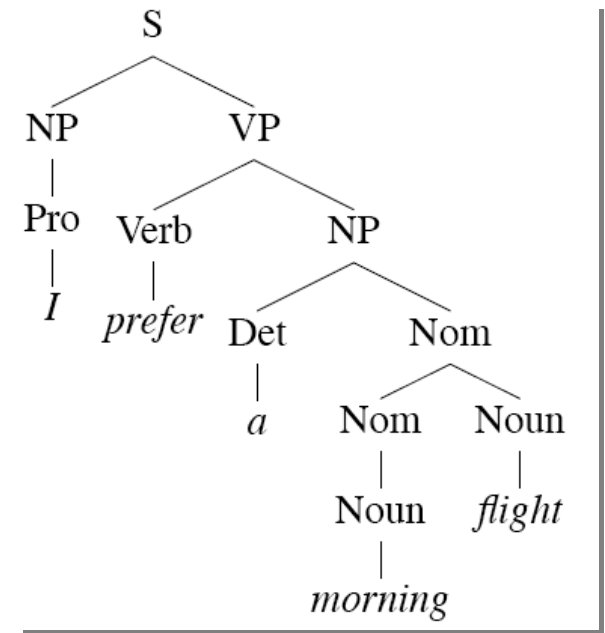
Exercise: Context free grammar

- Give a context free grammar to generate the parse tree



Exercise: Context free grammar

- Give a context free grammar to generate the parse tree
 - T: {I, prefer, a, morning, flight}
 - N: {VP, VP, Pro, Verb, Det, Nom, Noun}
 - S: S
 - R:
 - S → NP VP
 - NP → Pro
 - VP → Verb NP
 - Verb → prefer
 - NP → Det Nom
 - Nom → Nom Noun | Noun
 - Noun → morning | flight
 - Det → a
 - Pro → I



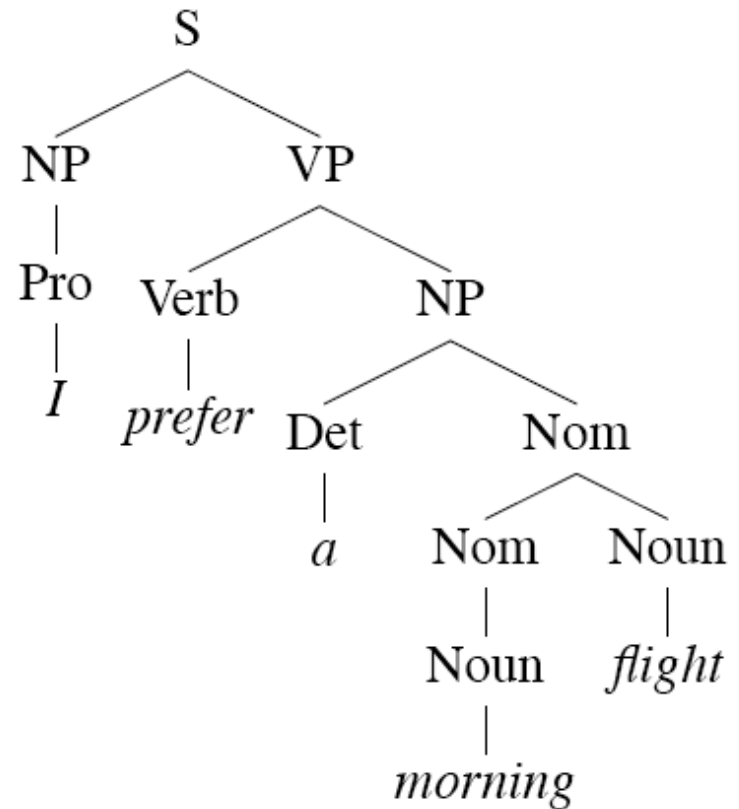
L0 grammar

Grammar Rules	Examples
$S \rightarrow NP VP$	I + want a morning flight
$NP \rightarrow$ <ul style="list-style-type: none">$Pronoun$$Proper-Noun$$Det Nominal$	<ul style="list-style-type: none">ILos Angelesa + flight
$Nominal \rightarrow$ <ul style="list-style-type: none">$Nominal Noun$$Noun$	<ul style="list-style-type: none">morning + flightflights
$VP \rightarrow$ <ul style="list-style-type: none">$Verb$$Verb NP$$Verb NP PP$$Verb PP$	<ul style="list-style-type: none">dowant + a flightleave + Boston + in the morningleaving + on Thursday
$PP \rightarrow Preposition NP$	from + Los Angeles

Derivation

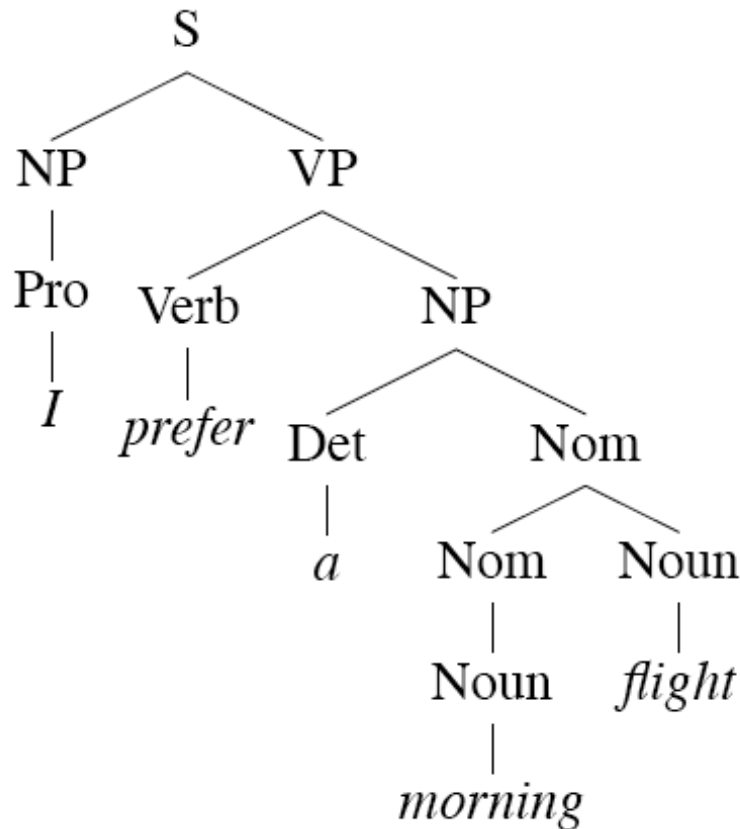
- A sequence of rules applied to a string that accounts for that string

S	\rightarrow	$NP VP$
NP	\rightarrow	$Pronoun$
		$Proper-Noun$
		$Det Nominal$
$Nominal$	\rightarrow	$Nominal Noun$
		$Noun$
VP	\rightarrow	$Verb$
		$Verb NP$
		$Verb NP PP$
		$Verb PP$
PP	\rightarrow	$Preposition NP$



I prefer a morning flight.

Derivation (2)



$S \rightarrow NP VP$

$NP \rightarrow Pro$

$Pro \rightarrow I$

$VP \rightarrow Verb NP$

$Verb \rightarrow \textit{prefer}$

$NP \rightarrow Det Nom$

$Det \rightarrow a$

$Nom \rightarrow Nom Noun$

$Nom \rightarrow Noun$

$Noun \rightarrow \textit{morning}$

$Noun \rightarrow \textit{flight}$

Summary: CFG & phrase structure

- $G = (T, N, S, R)$
 - Terminals: words
 - Non-terminals: constituent names (e.g. NP, VP)
 - Start symbol: S (sentence) or NP (noun phrase)
 - Rules: e.g. subcategorization frames for verbs
- Derivation will generate the phrase structure of an input



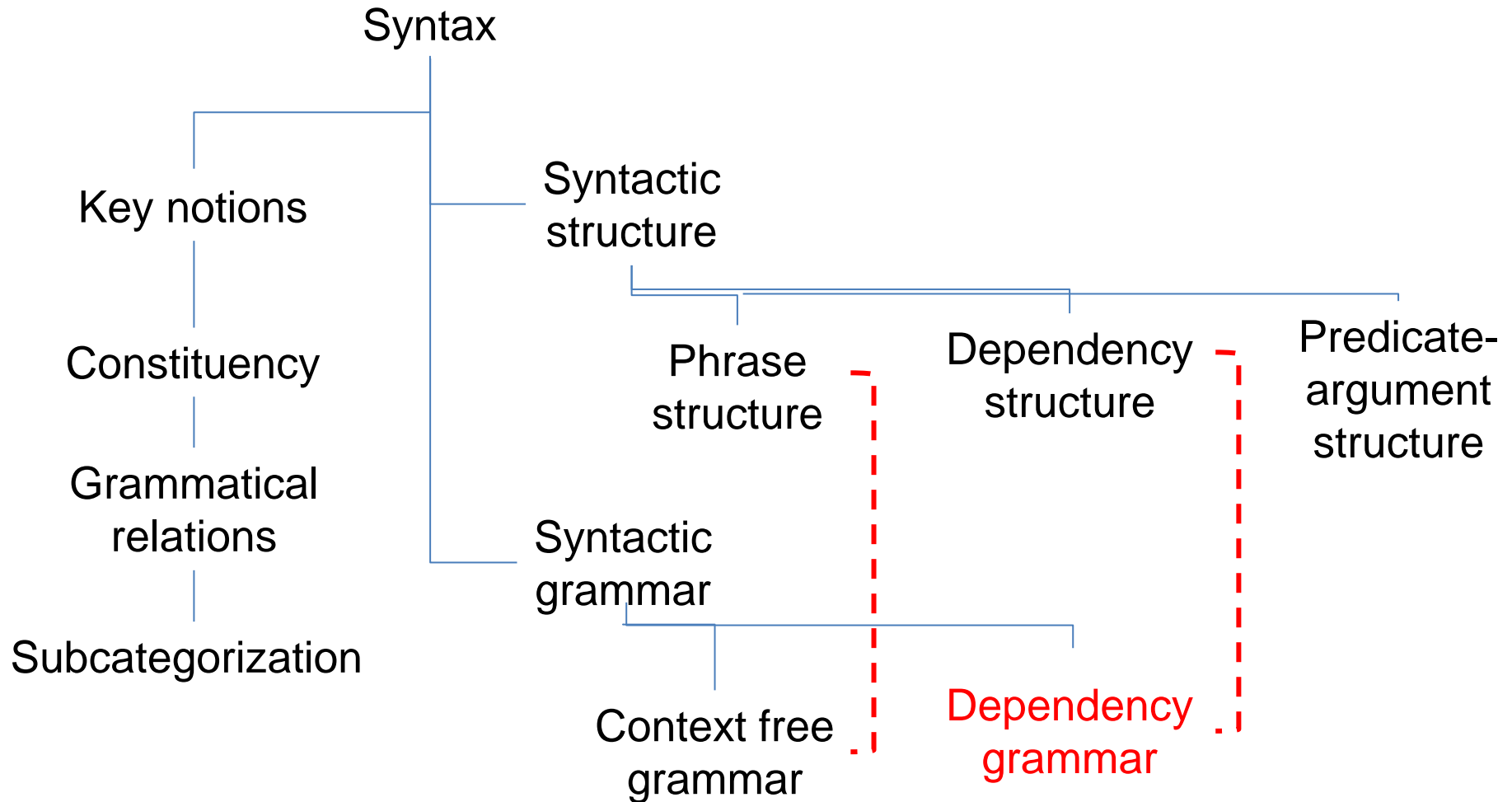
Example grammar formalisms

- Context free grammar (CFG)
- Combinatory categorial grammar (CCG)
- Dependency grammar (DG)

- HPSG: head-driven phrase structure grammar
- LFG: lexical functional grammar
- TAG: tree-adjoining grammar



Summary

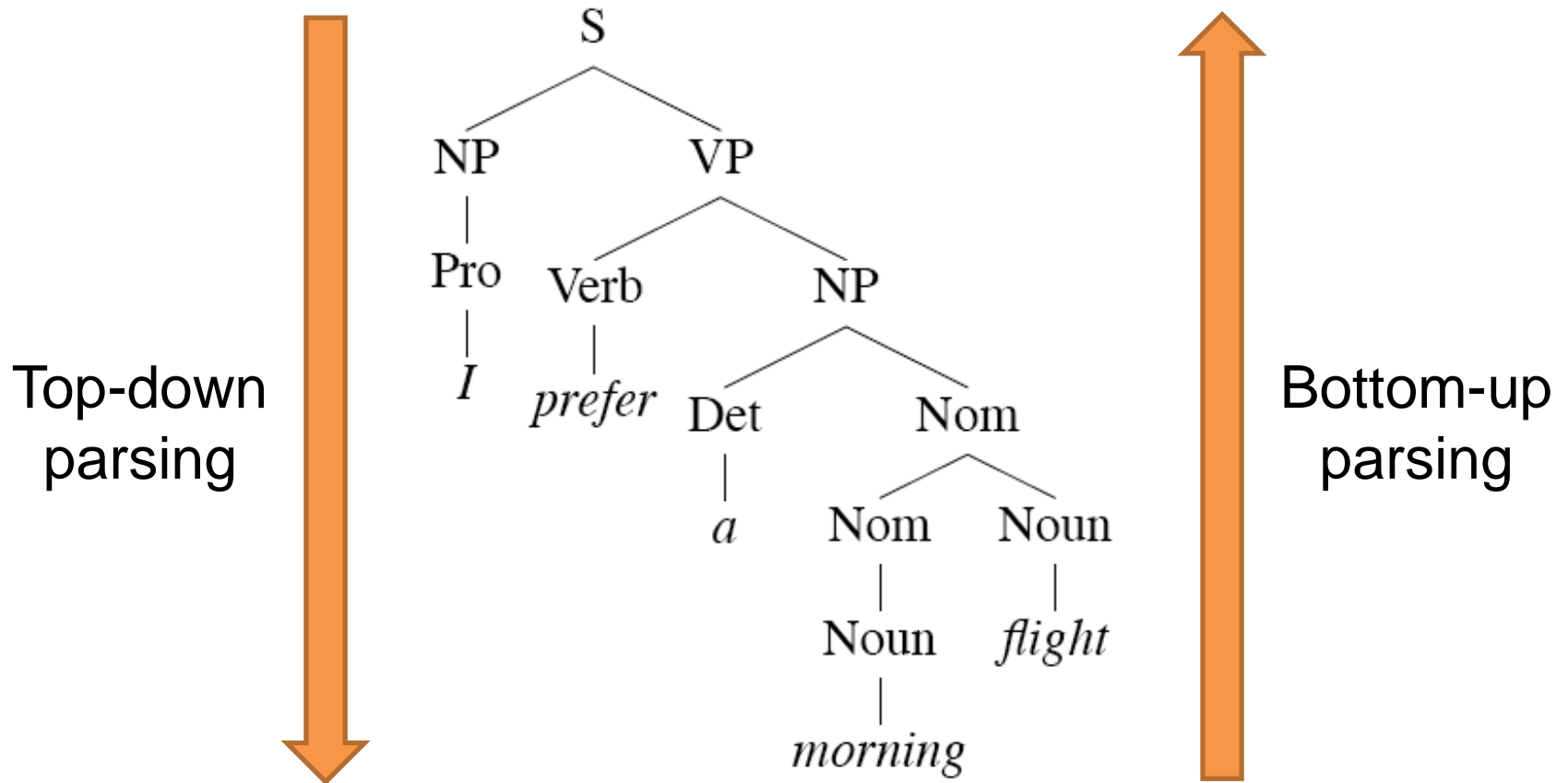


We focus on CFG!

- Classic approach
 - Still widely used for practical parsing systems
- Theoretically well-studied
 - Equivalent to Backus-Naur Form (BNF)
 - SQL is formally defined in BNF

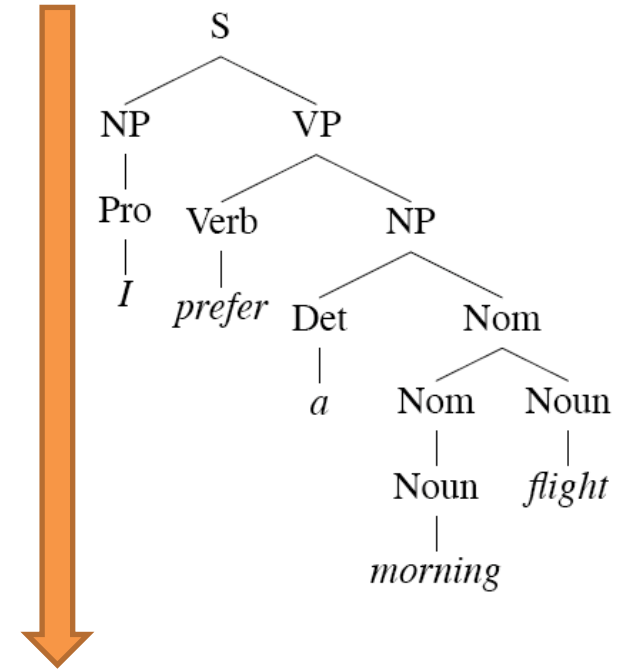


Parsing strategies



Top-down parsing

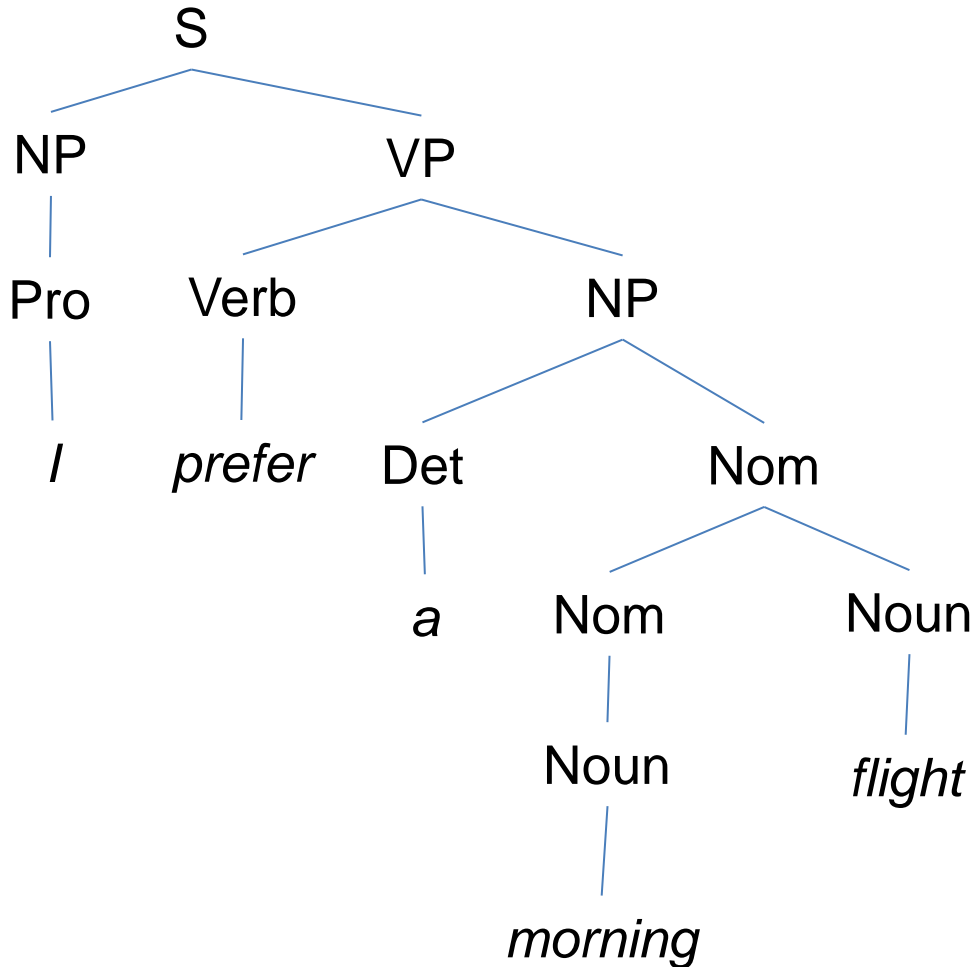
- Goal-directed
 - Start from 'S'
- Rewrite the goal(s) with the RHS of relevant rules, e.g.,
 - $S \rightarrow NP VP$,
 - $VP \rightarrow Verb NP$
- Parsing is finished when the rewriting generates the whole string



Top-down
parsing

Top-down parsing: Example

I prefer a morning flight.



1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$

5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$

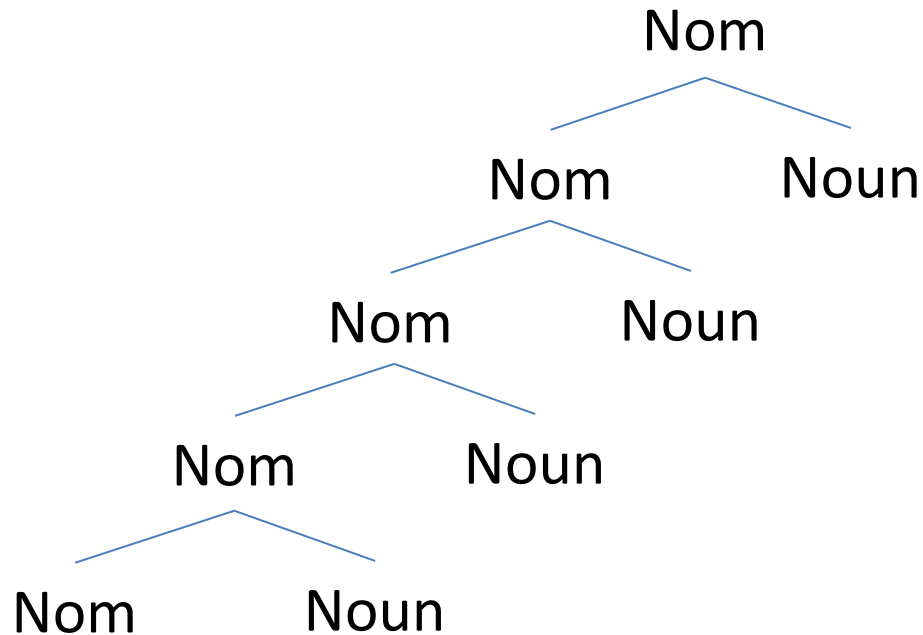
6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

Top-down parsing: Issues (1/2)

- If a goal can be written in several ways, there is a choice of which rule to apply
 - Example: $NP \rightarrow Pro$, $NP \rightarrow Det\ Nom$
- Search problem
 - Search methods: Depth-first, breadth-first, goal-ordering, etc.
- Need grammar-driven control for optimization
 - May waste lots of time in trying rules that are inconsistent with the input string
 - Example: left recursive rules (e.g. $Nom \rightarrow Nom\ Noun$)



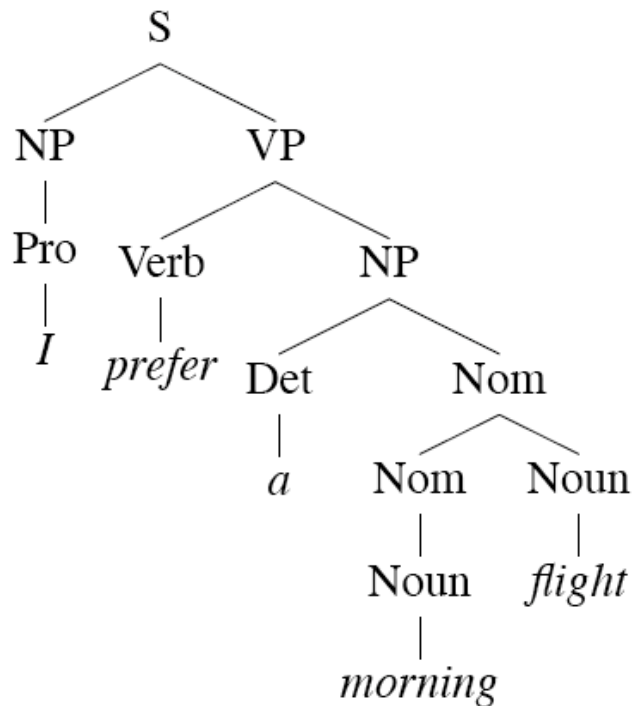
Top-down parsing: left recursive rules



Example: Southeast Asia Public Interest Research Group

Top-down parsing: Issues (2/2)

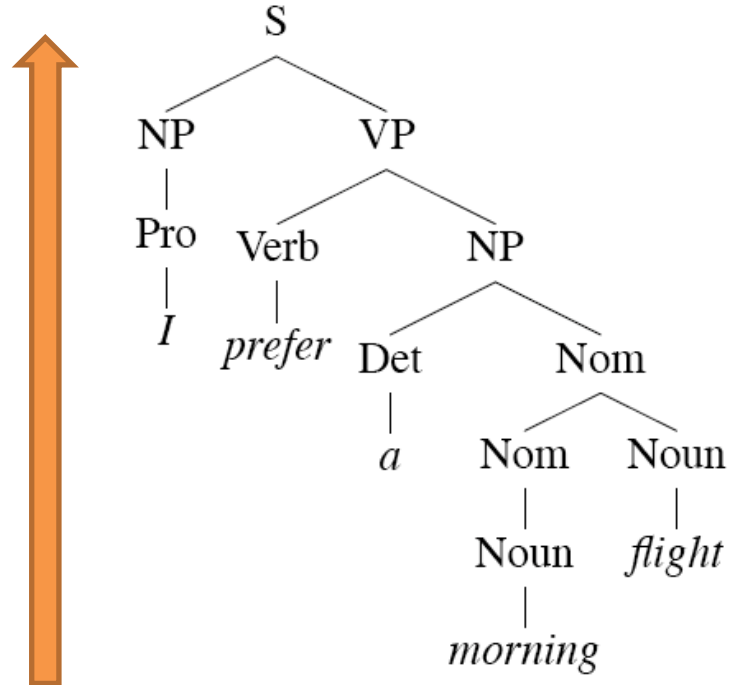
- A part-of-speech like Noun can be replaced with any noun; trying out all rules of a part-of-speech is time consuming
- In practice, **part-of-speech tags are predetermined**



1. $S \rightarrow NP VP$
2. $NP \rightarrow Pro$
 $Pro \rightarrow I$
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$
4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$
5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$
6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

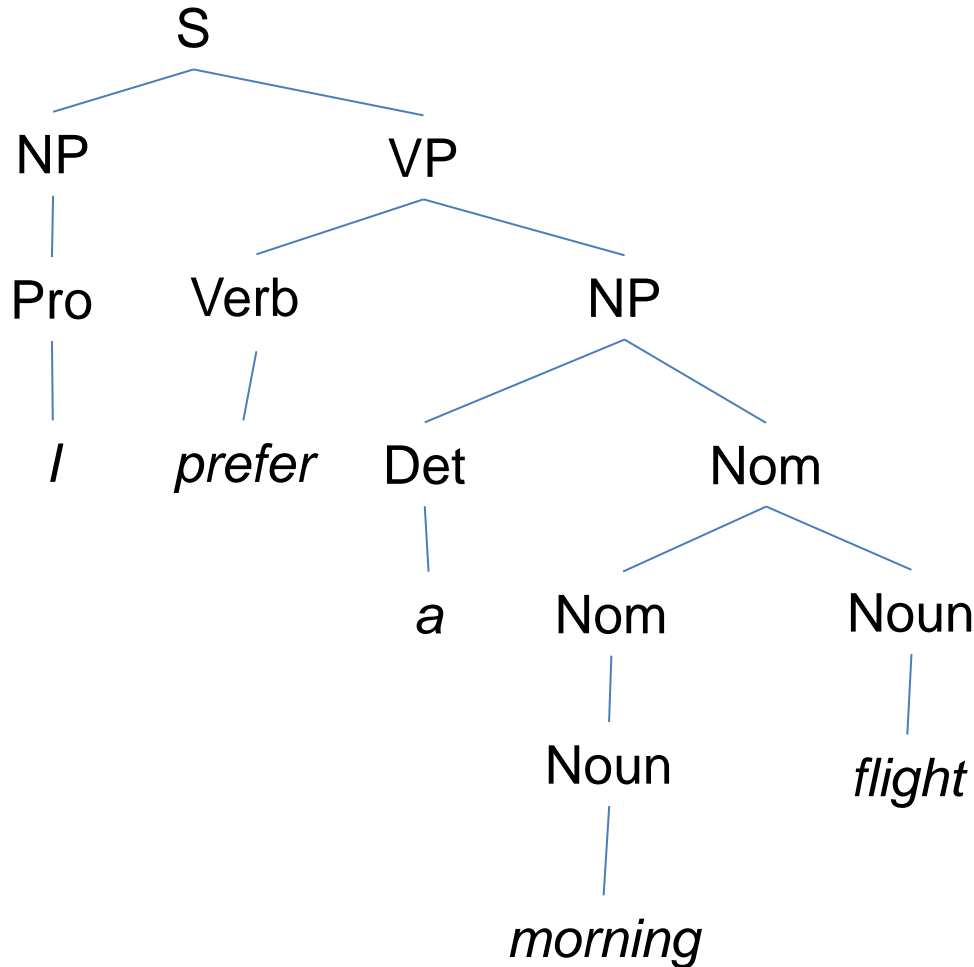
Bottom-up parsing

- Data-directed
 - Start with words
- If a substring matches the RHS of a rule, replace the substring with the LHS
 - Example: Nom \rightarrow Noun (“morning”)
 - Example: Nom \rightarrow Nom Noun
 (“*morning flight*”)
- Parsing is finished when the whole string is replaced with a goal



Bottom-up approach: Example

I prefer a morning flight.



6. $S \rightarrow NP VP$

5. $Pro \rightarrow I$
 $NP \rightarrow Pro$

4. $Verb \rightarrow prefer$
 $VP \rightarrow Verb NP$

3. $Det \rightarrow a$
 $NP \rightarrow Det Nom$

2. $Noun \rightarrow flight$
 $Nom \rightarrow Nom Noun$

1. $Noun \rightarrow morning$
 $Nom \rightarrow Noun$

Parsing strategies

Top-down parsing

- Goal-directed
 - Start from 'S'
- Rewrite the goal(s) with the RHS of relevant rules
 - Example: $S \rightarrow NP VP$
- Parsing is finished when the rewriting generates the whole string

Bottom-up parsing

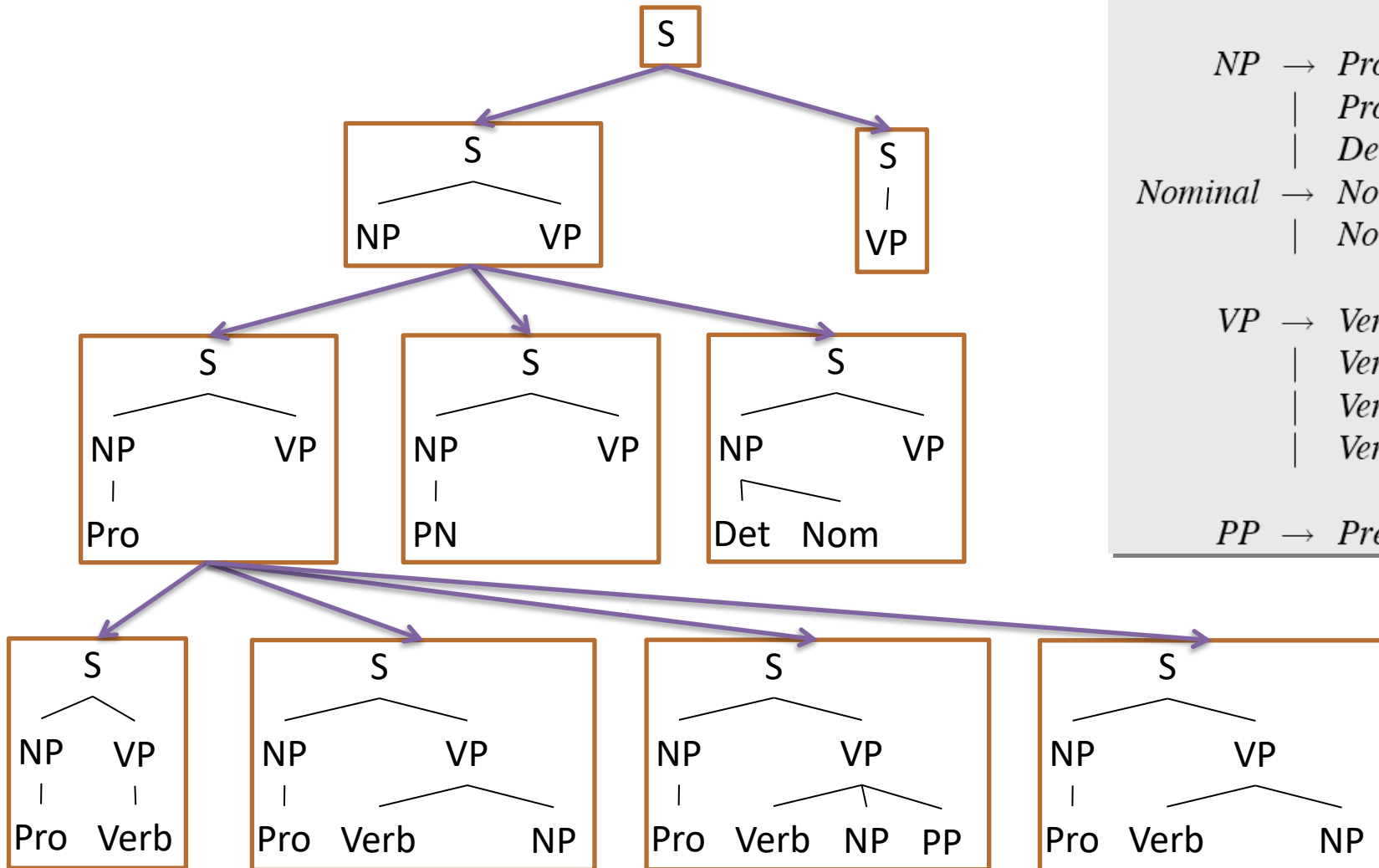
- Data-directed
 - Start with words
- If a substring matches the RHS of a rule, replace the substring with the LHS
 - Example: $Nom \rightarrow Noun$
 - $Nom \rightarrow Nom Noun$
(*“morning flight”*)
- Parsing is finished when the whole string is replaced with a goal

Top-down vs. Bottom-up parsing

- Top-down
 - Waste lots of time in trying inconsistent rule applications. The application of the rules does not lead the generation of the given string
 - Never explore subtrees that cannot find a place in some S-rooted tree. All trees are generated starting with S.
- Bottom-up
 - Never suggest trees that are not grounded in the input string; All trees are generated based on input string
 - Trees that have no hope of leading to an S are generated; Some trees cannot proceed further to reach S



Parsing as search (e.g. I prefer a morning flight)



Grammar Rules

$S \rightarrow NP VP / VP$

$NP \rightarrow$

- $Pronoun$
- $Proper-Noun$
- $Det Nominal$

$Nominal \rightarrow$

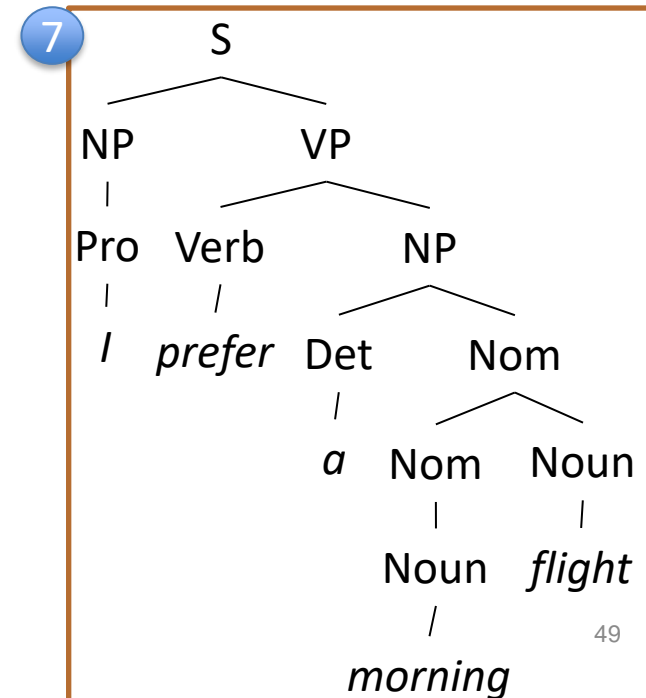
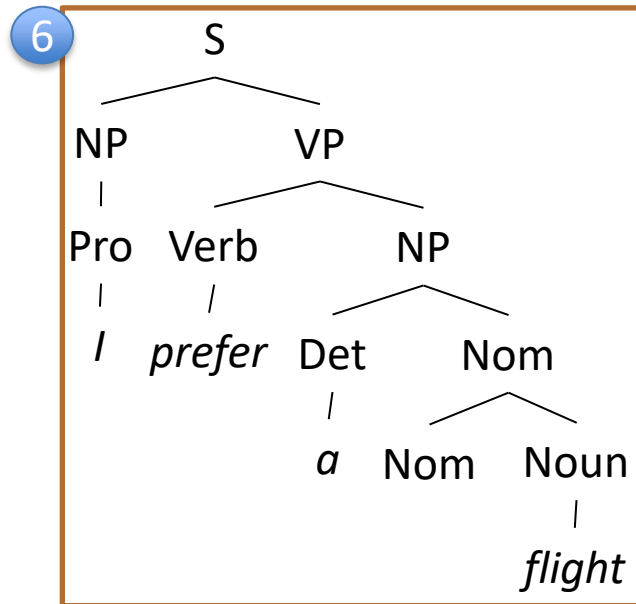
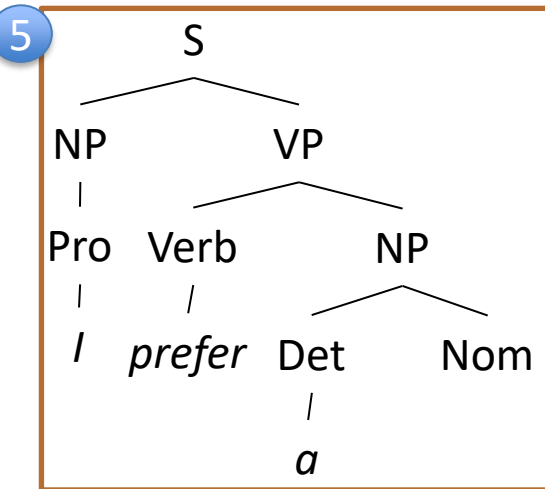
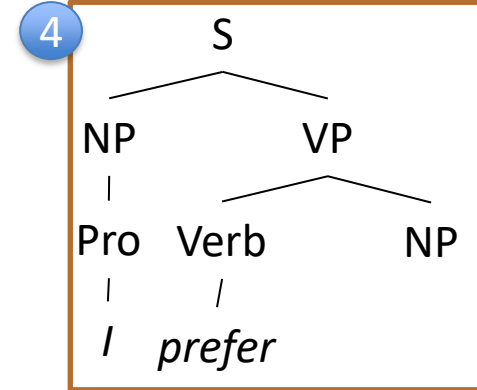
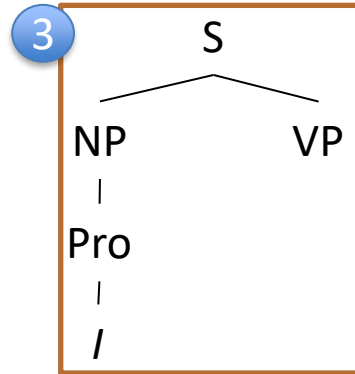
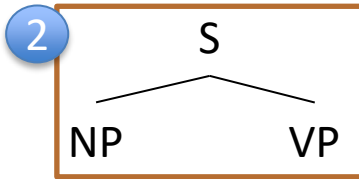
- $Nominal Noun$
- $Noun$

$VP \rightarrow$

- $Verb$
- $Verb NP$
- $Verb NP PP$
- $Verb PP$

$PP \rightarrow Preposition NP$

Parsing as search



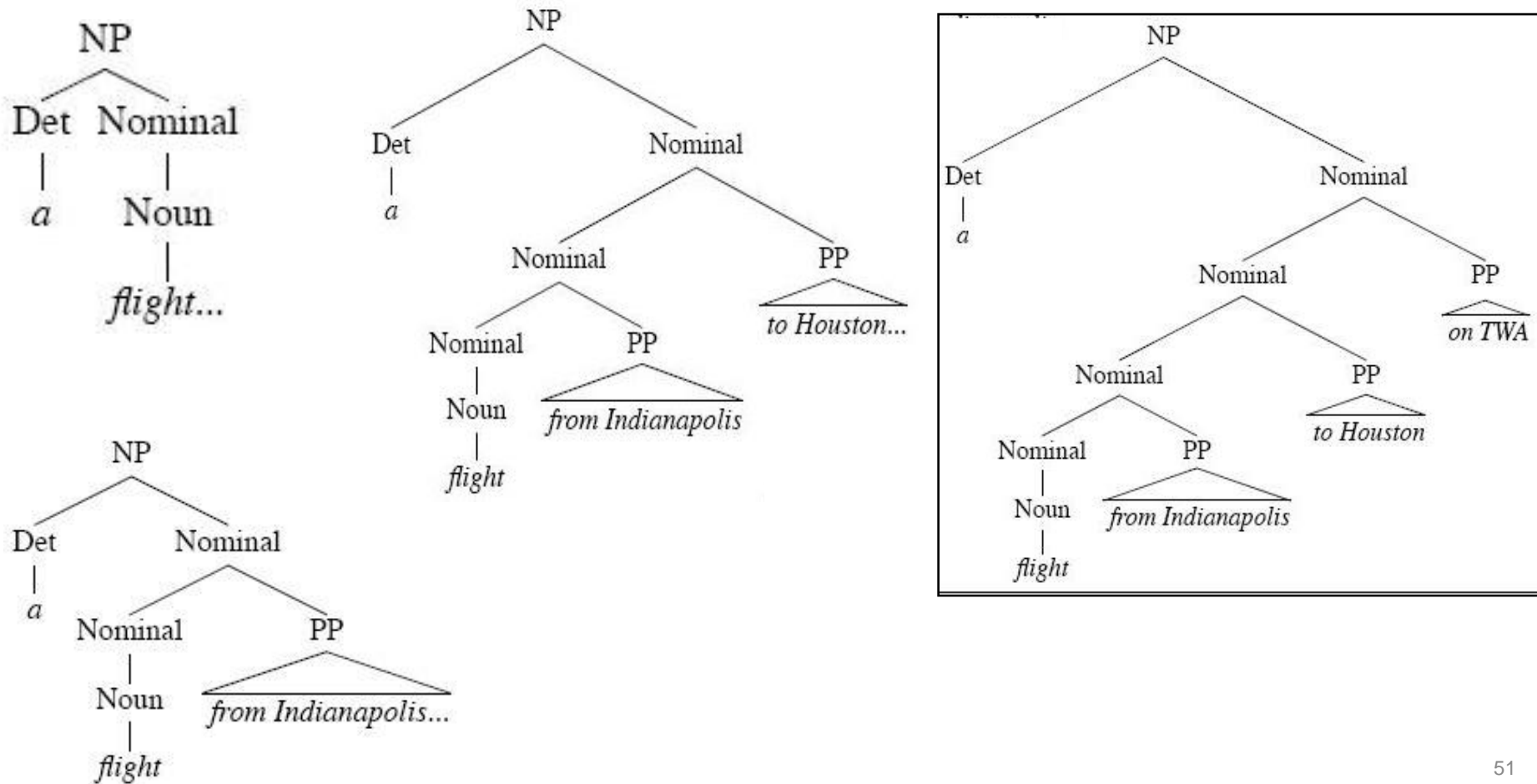
Exercise: Parsing as search

- Draw a search space for parsing “I sleep” in a top-down parsing based on L0 grammar

Grammar Rules	
S	$\rightarrow NP VP$
NP	\rightarrow $\begin{array}{l} \textit{Pronoun} \\ \textit{Proper-Noun} \\ \textit{Det Nominal} \end{array}$
$Nominal$	\rightarrow $\begin{array}{l} \textit{Nominal Noun} \\ \textit{Noun} \end{array}$
VP	\rightarrow $\begin{array}{l} \textit{Verb} \\ \textit{Verb NP} \\ \textit{Verb NP PP} \\ \textit{Verb PP} \end{array}$
PP	$\rightarrow \textit{Preposition NP}$

Repeated work in parsing-as-search

- Parsing: “a flight from Indianapolis to Houston on TWA” (Figure 13.7)



Dynamic programming parsing methods

- Parsing-as-search may have exponentially many parse states
- Dynamic programming solves the problem of doing repeated work
 - Memorization (remembering solved subproblems)
- Bottom-up approach: CKY parsing
 - Parse table
- Top-down approach: Earley parsing
 - Dotted rules



Parse table

- Cell $[i, j]$ contains the syntactic structures of the substring from the $(i + 1)$ -th word to the j -th word

\mathcal{L}_1 Grammar
$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$
$S \rightarrow VP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

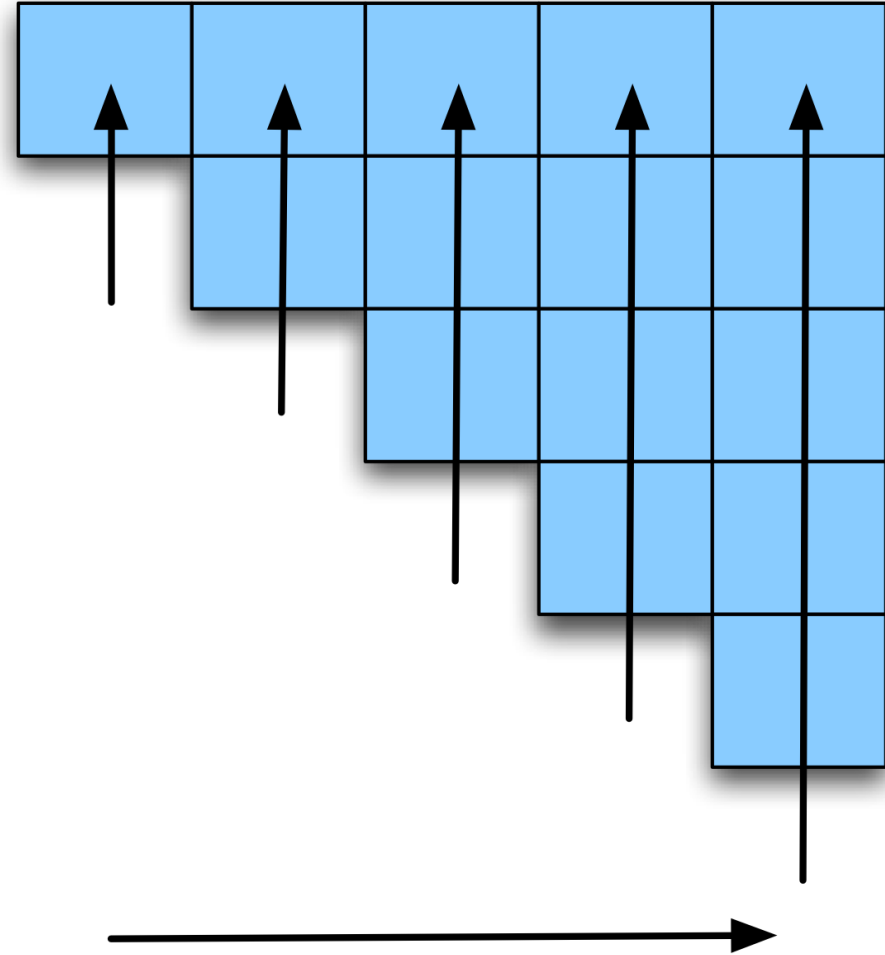
$NP \rightarrow Pronoun$
$NP \rightarrow Proper-Noun$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$
$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$

0	1	2	3	4	5
Book	the	flight	through	Houston	
S, VP, Verb Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	S, . . . ,X2 [0,5]	
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]	
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]	
			Prep [3,4]	PP [3,5]	
				NP, Proper- Noun [4,5]	

Parse table: Parsing sequence

Book the flight through Houston

S, VP, Verb Nominal, Noun [0,1]		S,VP,X2 [0,3]		S,VP,X2 [0,5]
	Det [1,2]	NP [1,3]		NP [1,5]
		Nominal, Noun [2,3]		Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]



Parse table: A fast method of filling in each cell

Assume an RHS has
exactly two items ($X \rightarrow Y Z$)

[book₁] [the₂ flight₃ through₄ Houston₅]
[0,1] [1,5]

[book₁ the₂] [flight₃ through₄ Houston₅]
[0,2] [2,5]

...

[book₁ the₂ flight₃ through₄] [Houston₅]
[0,4] [4,5]

[0,5] \rightarrow [0,k] [k,5] for $0 < k < 5$

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb Nominal, Noun [0,1]				S,VP,X2 [0,3]				S,VP,X2 [0,5]		
	Det [1,2]			NP [1,3]				NP [1,5]		
				Nominal, Noun [2,3]				Nominal [2,5]		
								Prep [3,4]	PP [3,5]	
									NP, Proper- Noun [4,5]	

Parse table:

Assume an RHS
has exactly two items

$[\text{word}_{i+1}] [\text{word}_{i+2} \text{ word}_{i+3} \dots \text{word}_j]$

$[i, i+1] [i+1, j]$

$[\text{word}_{i+1} \text{ word}_{i+2}] [\text{word}_{i+3} \dots \text{word}_j]$

$[i, i+2] [i+2, j]$

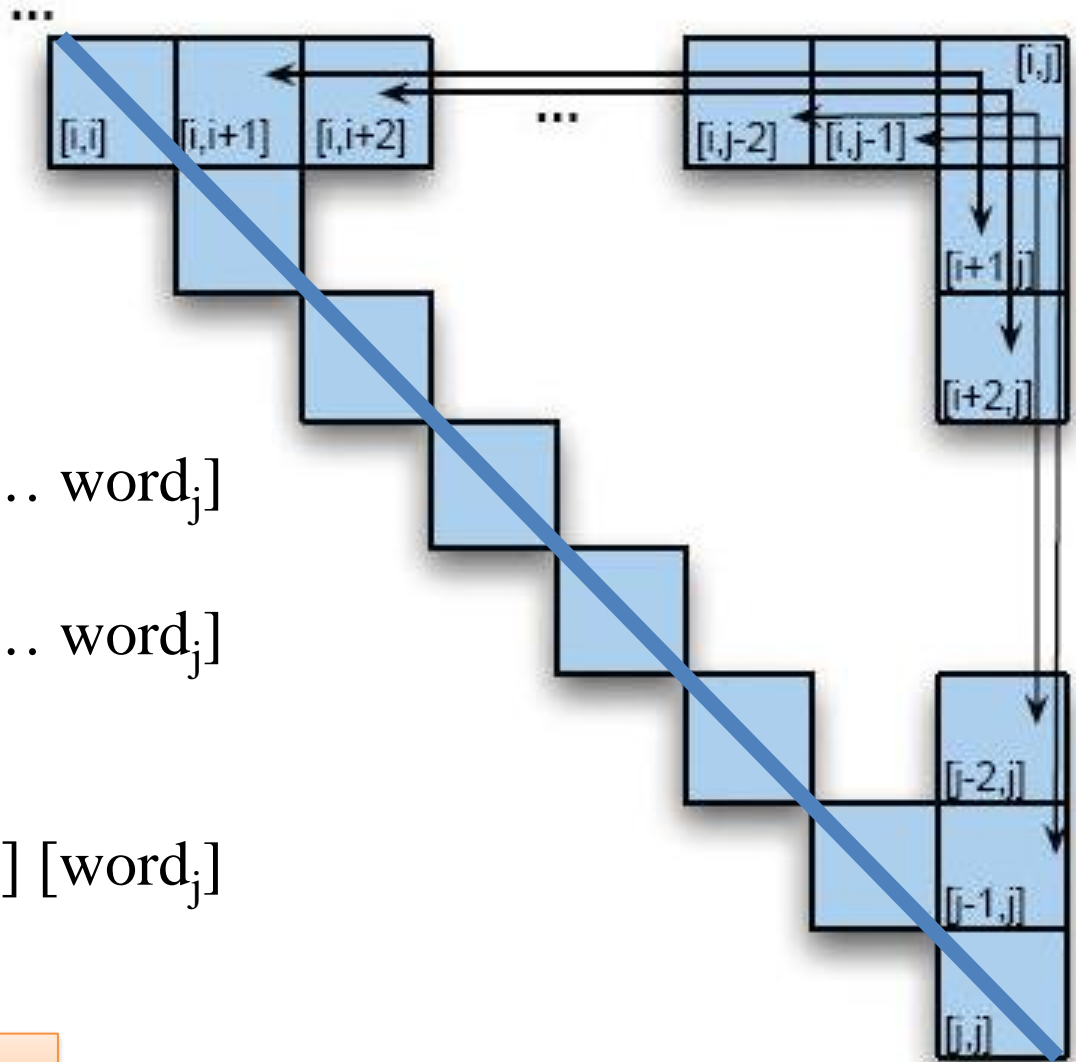
...

$[\text{word}_{i+1} \text{ word}_{i+2} \text{ word}_{i+3} \dots] [\text{word}_j]$

$[i, j-1] [j-1, j]$

$[i, j] \rightarrow [i, k] [k, j] \text{ for } i < k < j$

How can we create a CFG following the assumption?



CKY parsing

- Requirement
 - All rules should be in Chomsky normal form (CNF)
- CNF rules have the form of either
 - $A \rightarrow B C$ or $A \rightarrow w$ (w is a terminal)
 - RHS must have two non-terminals or one terminal
- Conversion to CNF
 - Example on next slide

POS Tagging



CNF grammar: example

\mathcal{L}_1 Grammar	\mathcal{L}_1 in CNF
$S \rightarrow NP VP$	$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$	$S \rightarrow X1 VP$
	$X1 \rightarrow Aux NP$
$S \rightarrow VP$	$S \rightarrow book \mid include \mid prefer$
	$S \rightarrow Verb NP$
	$S \rightarrow X2 PP$
	$S \rightarrow Verb PP$
	$S \rightarrow VP PP$
$NP \rightarrow Pronoun$	$NP \rightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$	$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$	$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$	$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$	$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$	$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$	$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$	$VP \rightarrow X2 PP$
	$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$	$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$	$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$	$PP \rightarrow Preposition NP$

Example : filling the 5th column

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb, Nominal, Noun [0,1]			S,VP,X2 [0,3]			[0,4]		[0,5]		
	Det [1,2]		NP [1,3]			[1,4]		[1,5]		
			Nominal, Noun [2,3]			[2,4]		[2,5]		
						Prep [3,4]		[3,5]		
								NP, Proper- Noun [4,5]		

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal \mid$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Example : filling the 5th column

	1	2	3	4	5
S, VP, Verb, Nominal, Noun		S,VP,X2			
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]	
	Det	NP			
	[1,2]	[1,3]	[1,4]	[1,5]	
		Nominal, Noun			
		[2,3]	[2,4]	[2,5]	
			Prep ←	PP	
			[3,4]	[3,5]	
				NP, Proper- Noun	
				[4,5]	

PP → *Preposition NP*

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal \mid$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Example : filling the 5th column

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb, Nominal, Noun [0,1]			S,VP,X2							
	Det [1,2]		NP					NP		
			Nominal, Noun [2,3]					Nominal [2,5]		
						Prep [3,4]		PP [3,5]		
								NP, Proper- Noun [4,5]		

Nominal → *Nominal PP*

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Example : filling the 5th column

Diagram illustrating the parsing of the sentence "Book the flight through Houston" using a shift-reduce parser. The diagram shows the sequence of shifts and reductions on a stack.

Initial Shift: The word "Book" is shifted onto the stack. The stack contains: S, VP, Verb, Nominal, Noun. The interval is [0,1].

Shifts and Reductions:

- Shift:** The word "the" is shifted onto the stack. The stack contains: S, VP, Verb, Nominal, Noun, Det. The interval is [0,2].
- Shift:** The word "flight" is shifted onto the stack. The stack contains: S, VP, Verb, Nominal, Noun, Det, NP. The interval is [0,3].
- Shift:** The word "through" is shifted onto the stack. The stack contains: S, VP, Verb, Nominal, Noun, Det, NP, Prep. The interval is [0,4].
- Shift:** The word "Houston" is shifted onto the stack. The stack contains: S, VP, Verb, Nominal, Noun, Det, NP, Prep, NP, Proper-Noun. The interval is [0,5].

Reduction: The NP (Nominal, Proper-Noun) is reduced to a Det (the). The stack now contains: S, VP, Verb, Nominal, Noun, Det, NP, Prep. The interval is [1,2].

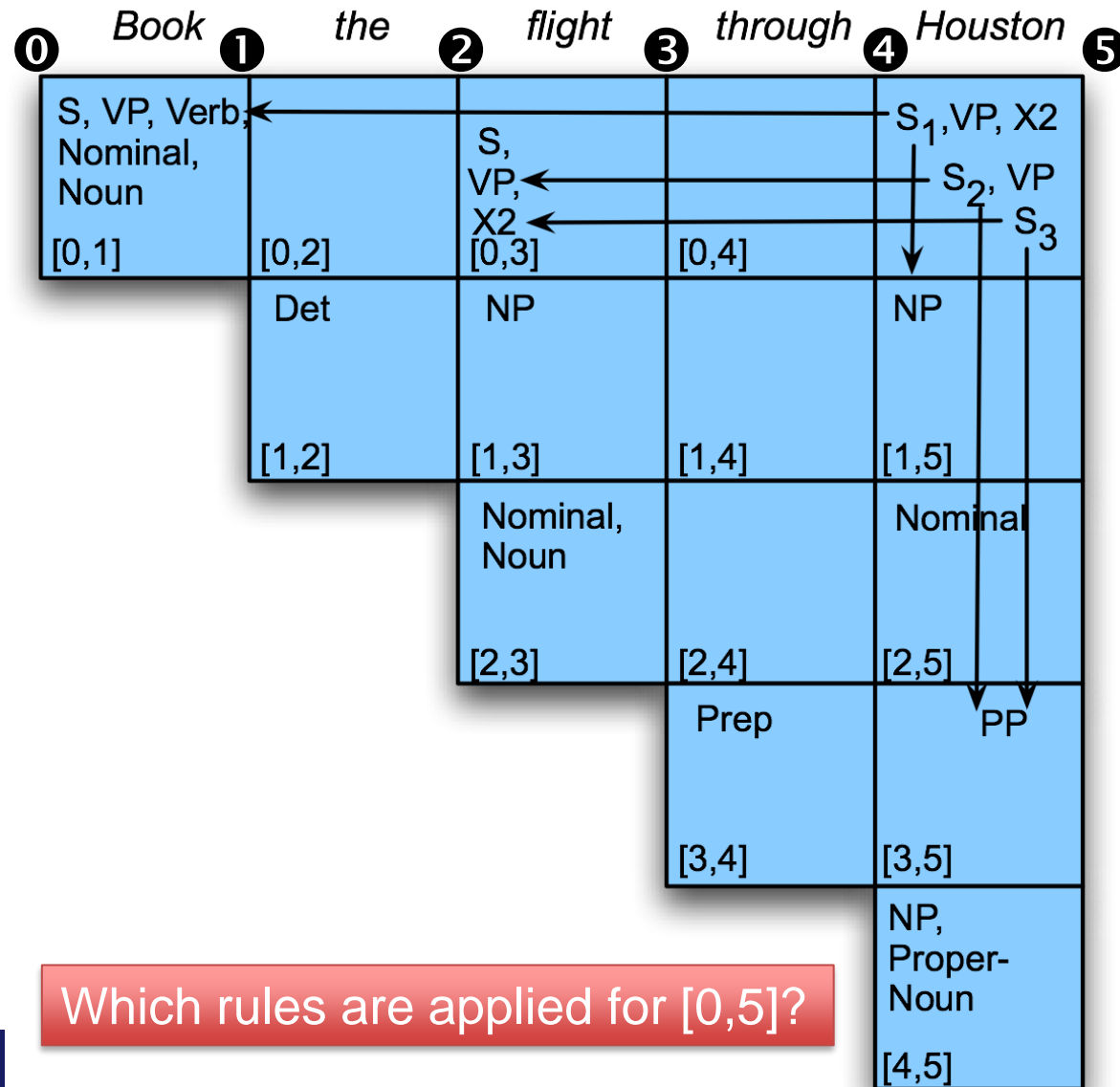
Final Reduction: The NP (Nominal, Proper-Noun) is reduced to a Det (the). The stack now contains: S, VP, Verb, Nominal, Noun, Det, NP, Prep. The interval is [1,2].

Final Stack: S, VP, Verb, Nominal, Noun, Det, NP, Prep. The interval is [1,2].

Final Rule: $NP \rightarrow Det\ Nominal$

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal \mid$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Exercise: CKY parsing



$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

CKY algorithm

0	1	2	3	4	5
Book	the	flight	through	Houston	
S, VP, Verb Nominal, Noun [0,1]		S,VP,X2 [0,3]		S,VP,X2 [0,5]	
	Det [1,2]	NP [1,3]		NP [1,5]	
		Nominal, Noun [2,3]		Nominal [2,5]	
			Prep [3,4]	PP [3,5]	
				NP, Proper- Noun [4,5]	

function CKY-PARSE(*words*, *grammar*) **returns** *table*

for $j \leftarrow$ **from** 1 **to** LENGTH(*words*) **do**

$table[j-1, j] \leftarrow \{A \mid A \rightarrow words[j] \in grammar\}$

for $i \leftarrow$ **from** $j-2$ **downto** 0 **do**

for $k \leftarrow i+1$ **to** $j-1$ **do**

$table[i, j] \leftarrow table[i, j] \cup$

$\{A \mid A \rightarrow BC \in grammar,$
 $B \in table[i, k],$
 $C \in table[k, j]\}$

CKY parsing: summary

- Requirement: CNF grammar
 - Binarization: $[i,j] \rightarrow [i,k] [k,j]$ for $i < k < j$
- Bottom-up approach
 - Process from $[j-1,j]$ to $[0,j]$
 - This assures us that whenever we're filling a cell, the parts needed to fill it are already in the table (to the left and below)
 - It's somewhat natural in that it processes the input, from left to right, a word at a time

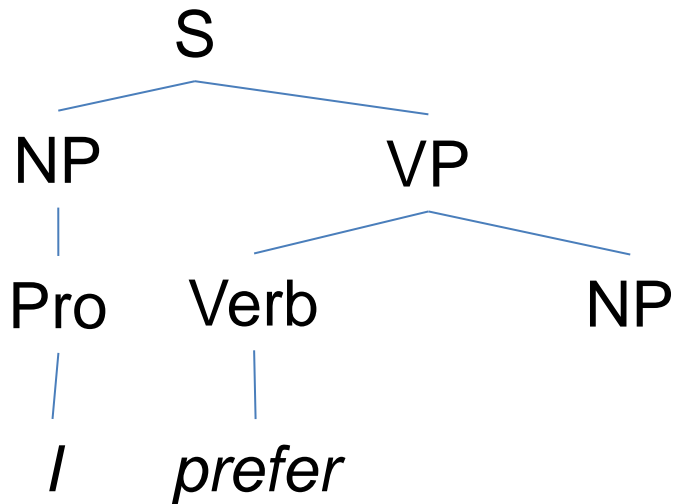


CKY parsing: Issue

- Trees that have no hope of leading to an S are generated
 - To avoid this we can switch to a top-down control strategy
 - Or we can add some kind of filtering that blocks constituents where they cannot happen in a final analysis.

<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
S, VP, Verb Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	S,VP,X2 [0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]

Top-down parsing: intermediate state example



1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

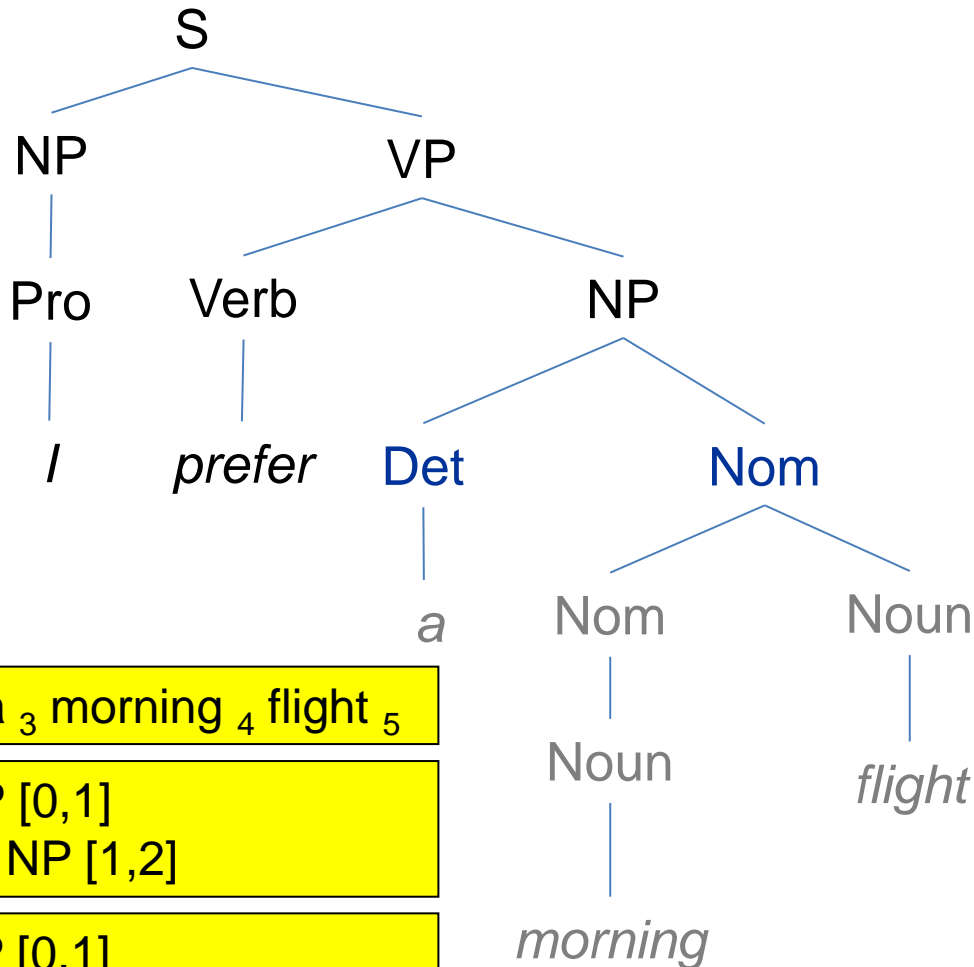
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

₀ I ₁ prefer ₂ a ₃ morning ₄ flight ₅

Dotted rules

$S \rightarrow NP \bullet VP [0,1]$
 $VP \rightarrow Verb \bullet NP [1,2]$

Top-down parsing: Next state



1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$

5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$

6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

$_0 I \ _1 prefer \ _2 a \ _3 morning \ _4 flight \ _5$

$S \rightarrow NP \bullet VP [0,1]$
 $VP \rightarrow Verb \bullet NP [1,2]$

$S \rightarrow NP \bullet VP [0,1]$
 $VP \rightarrow Verb \bullet NP [1,2]$
 $NP \rightarrow \bullet Det Nom [2,2]$

Earley algorithm: States

- $NP \rightarrow \bullet \text{ Det Nom } [2,2]$
 - A Det is predicted at position 2
- $VP \rightarrow \text{ Verb } \bullet \text{ NP } [1,2]$
 - A VP is in progress; the Verb goes from 1 to 2
- $VP \rightarrow \text{ Verb NP } \bullet [1,4]$
 - A VP has been found, starting at 1 and ending at 4
- $S \rightarrow \alpha \bullet [0,N]$
 - Parsing is finished

0 I 1 prefer 2 a 3 morning 4 flight 5

Earley algorithm: How it works

1. Predict all the states you can upfront [**Predictor**]
2. Read a word [**Scanner**]
 - Extend states based on matches [**Completer**]
 - Generate new predictions
 - Repeat step 2
3. When you're out of words, look at the chart to see if you have a winner



Earley algorithm: Example (1) ₀ Book ₁ that ₂ flight ₃

S0	$\gamma \rightarrow \bullet S$	[0,0]	Dummy start state
S1	$S \rightarrow \bullet NP VP$	[0,0]	Predictor
S2	$S \rightarrow \bullet Aux NP VP$	[0,0]	Predictor
S3	$S \rightarrow \bullet VP$	[0,0]	Predictor
S4	$NP \rightarrow \bullet Pronoun$	[0,0]	Predictor
S5	$NP \rightarrow \bullet Proper-Noun$	[0,0]	Predictor
S6	$NP \rightarrow \bullet Det Nominal$	[0,0]	Predictor
S7	$VP \rightarrow \bullet Verb$	[0,0]	Predictor
S8	$VP \rightarrow \bullet Verb NP$	[0,0]	Predictor
S9	$VP \rightarrow \bullet Verb NP PP$	[0,0]	Predictor
S10	$VP \rightarrow \bullet Verb PP$	[0,0]	Predictor
S11	$VP \rightarrow \bullet VP PP$	[0,0]	Predictor

\mathcal{L}_1 Grammar
$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$
$S \rightarrow VP$
$NP \rightarrow Pronoun$
$NP \rightarrow Proper-Noun$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$
$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

Note that given a grammar, these entries are the same for all inputs; they can be pre-loaded.

Earley algorithm: Example (2) ₀ Book ₁ that ₂ flight ₃

S12	<i>Verb</i> → <i>book</i> •	[0,1]	Scanner
S13	<i>VP</i> → <i>Verb</i> •	[0,1]	Completer
S14	<i>VP</i> → <i>Verb</i> • <i>NP</i>	[0,1]	Completer
S15	<i>VP</i> → <i>Verb</i> • <i>NP PP</i>	[0,1]	Completer
S16	<i>VP</i> → <i>Verb</i> • <i>PP</i>	[0,1]	Completer
S17	<i>S</i> → <i>VP</i> •	[0,1]	Completer
S18	<i>VP</i> → <i>VP</i> • <i>PP</i>	[0,1]	Completer
S19	<i>NP</i> → • <i>Pronoun</i>	[1,1]	Predictor
S20	<i>NP</i> → • <i>Proper-Noun</i>	[1,1]	Predictor
S21	<i>NP</i> → • <i>Det Nominal</i>	[1,1]	Predictor
S22	<i>PP</i> → • <i>Prep NP</i>	[1,1]	Predictor

\mathcal{L}_1 Grammar
<i>S</i> → <i>NP VP</i>
<i>S</i> → <i>Aux NP VP</i>
<i>S</i> → <i>VP</i>
<i>NP</i> → <i>Pronoun</i>
<i>NP</i> → <i>Proper-Noun</i>
<i>NP</i> → <i>Det Nominal</i>
<i>Nominal</i> → <i>Noun</i>
<i>Nominal</i> → <i>Nominal Noun</i>
<i>Nominal</i> → <i>Nominal PP</i>
<i>VP</i> → <i>Verb</i>
<i>VP</i> → <i>Verb NP</i>
<i>VP</i> → <i>Verb NP PP</i>
<i>VP</i> → <i>Verb PP</i>
<i>VP</i> → <i>VP PP</i>
<i>PP</i> → <i>Preposition NP</i>

Note that “Noun → book• [,] can be also scanned

Earley algorithm: Example (3) ₀ Book ₁ that ₂ flight ₃

S23	<i>Det</i> → <i>that</i> •	[1,2]	Scanner
S24	<i>NP</i> → <i>Det</i> • <i>Nominal</i>	[1,2]	Completer
S25	<i>Nominal</i> → • <i>Noun</i>	[2,2]	Predictor
S26	<i>Nominal</i> → • <i>Nominal Noun</i>	[2,2]	Predictor
S27	<i>Nominal</i> → • <i>Nominal PP</i>	[2,2]	Predictor
S28	<i>Noun</i> → <i>flight</i> •	[2,3]	Scanner
S29	<i>Nominal</i> → <i>Noun</i> •	[2,3]	Completer
S30	<i>NP</i> → <i>Det Nominal</i> •	[1,3]	Completer
S31	<i>Nominal</i> → <i>Nominal</i> • <i>Noun</i>	[2,3]	Completer
S32	<i>Nominal</i> → <i>Nominal</i> • <i>PP</i>	[2,3]	Completer
S33	<i>VP</i> → <i>Verb NP</i> •	[0,3]	Completer
S34	<i>VP</i> → <i>Verb NP</i> • <i>PP</i>	[0,3]	Completer
S35	<i>PP</i> → • <i>Prep NP</i>	[3,3]	Predictor
S36	<i>S</i> → <i>VP</i> •	[0,3]	Completer
S37	<i>VP</i> → <i>VP</i> • <i>PP</i>	[0,3]	Completer

\mathcal{L}_1 Grammar
<i>S</i> → <i>NP VP</i>
<i>S</i> → <i>Aux NP VP</i>
<i>S</i> → <i>VP</i>
<i>NP</i> → <i>Pronoun</i>
<i>NP</i> → <i>Proper-Noun</i>
<i>NP</i> → <i>Det Nominal</i>
<i>Nominal</i> → <i>Noun</i>
<i>Nominal</i> → <i>Nominal Noun</i>
<i>Nominal</i> → <i>Nominal PP</i>
<i>VP</i> → <i>Verb</i>
<i>VP</i> → <i>Verb NP</i>
<i>VP</i> → <i>Verb NP PP</i>
<i>VP</i> → <i>Verb PP</i>
<i>VP</i> → <i>VP PP</i>
<i>PP</i> → <i>Preposition NP</i>

Earley algorithm: Summary (Pseudo codes: Section 13.4.2)

- Top-down approach
 - Breadth-first search
 - State representation
 - (compare with the cells of parse tree in CKY algorithm: subtrees)
- Waste lots of time in trying inconsistent rule applications

S31	$Nominal \rightarrow Nominal \bullet Noun$	[2,3]	Completer
S32	$Nominal \rightarrow Nominal \bullet PP$	[2,3]	Completer
S33	$VP \rightarrow Verb NP \bullet$	[0,3]	Completer
S34	$VP \rightarrow Verb NP \bullet PP$	[0,3]	Completer
S35	$PP \rightarrow \bullet Prep NP$	[3,3]	Predictor
S36	$S \rightarrow VP \bullet$	[0,3]	Completer
S37	$VP \rightarrow VP \bullet PP$	[0,3]	Completer

Top-down vs. Bottom-up parsing

- Top-down
 - Waste lots of time in trying inconsistent rule applications. The application of the rules does not lead the generation of the given string
 - Never explore subtrees that cannot find a place in some S-rooted tree. All trees are generated starting with S.
- Bottom-up
 - Never suggest trees that are not grounded in the input string. All trees are generated based on input string
 - Trees that have no hope of leading to an S are generated. Some trees cannot proceed further to reach S

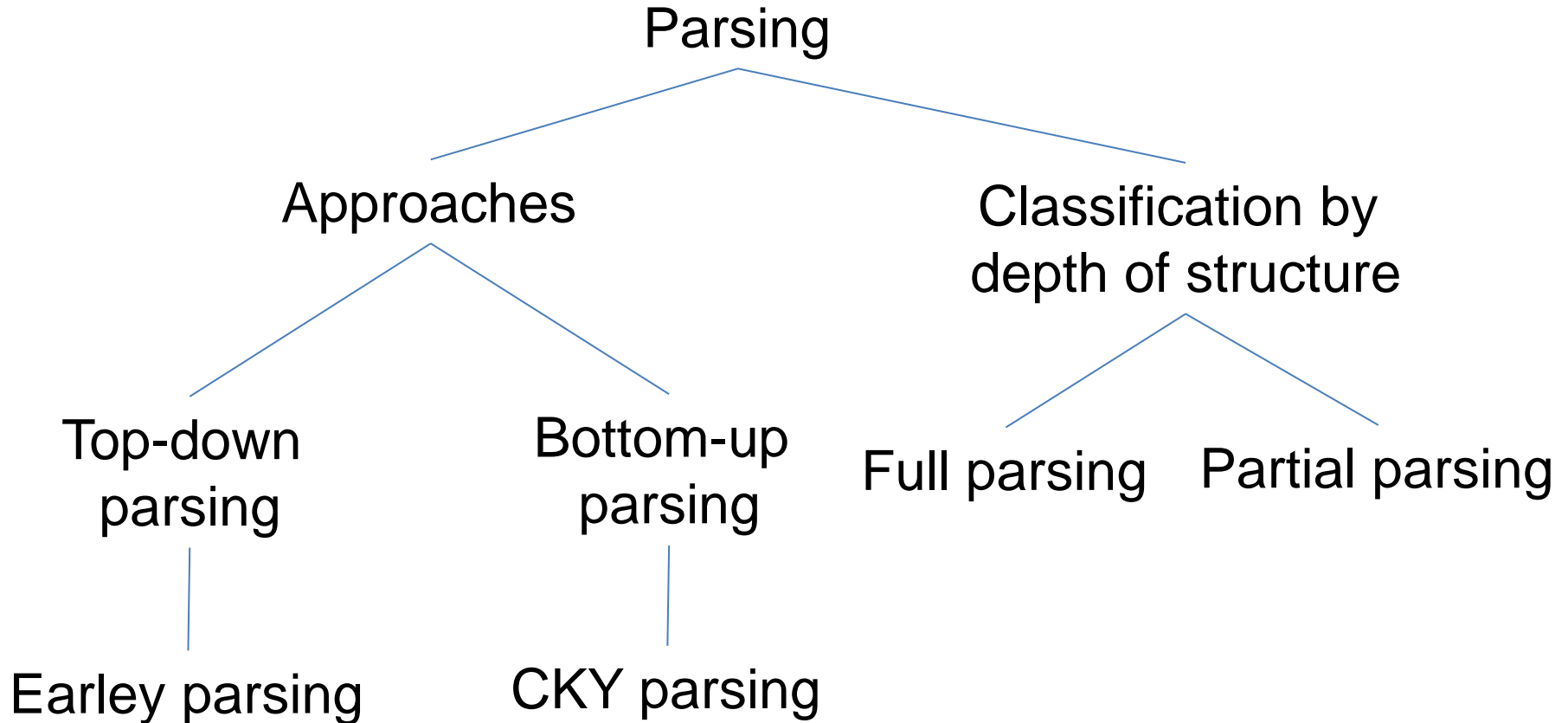


Full parsing vs. Partial parsing

- Full parsing
 - Identify the complete syntactic structure of a sentence
 - Oftentimes, parsing is the most time-consuming part
- Partial parsing
 - Identify parts of the syntactic structure of a sentence
 - Not all applications require full syntactic structures. Example: only Noun phrases need to be extracted in some applications but not the full syntactic structure of the sentence.



Summary

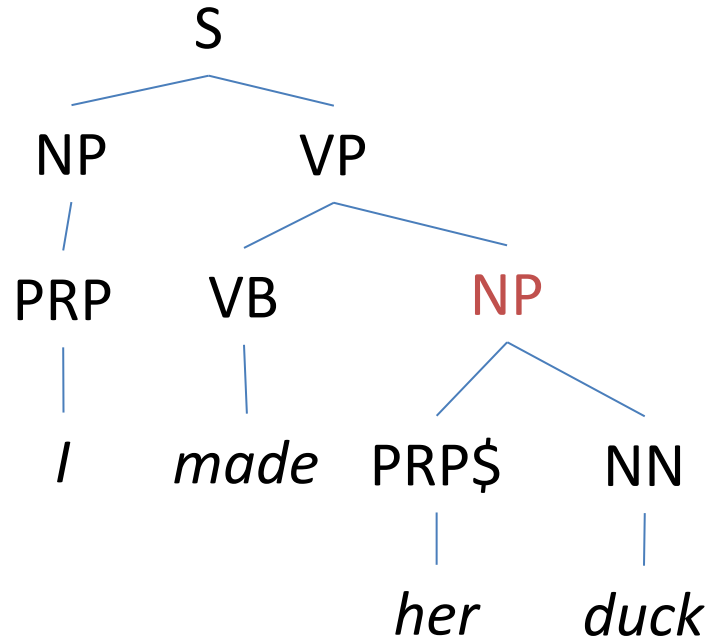


Ambiguity is Pervasive

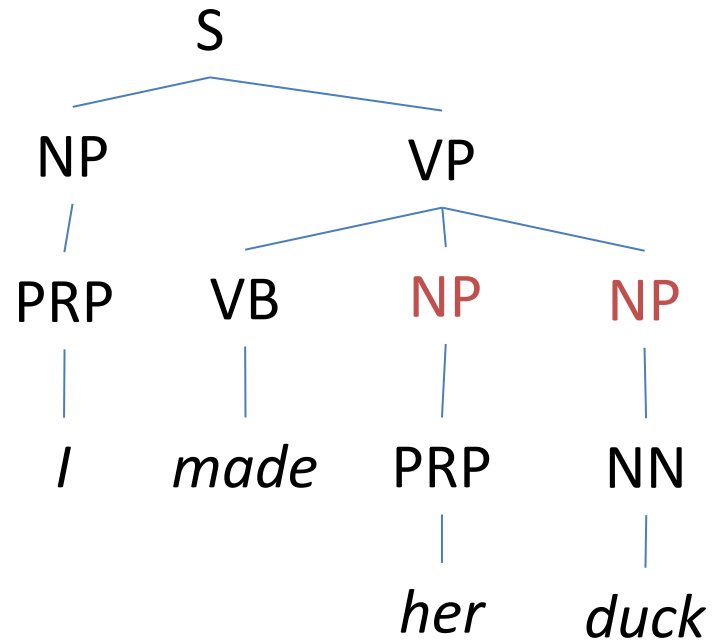
- Find at least 5 meanings of this sentence: **I made her duck**
- Possible meanings
 - I cooked waterfowl for her
 - I cooked waterfowl belonging to her
 - I created the (plaster?) duck she owns
 - I caused her to quickly lower her head and body
 - I waved my magic wand and turned her into undifferentiated waterfowl



Ambiguity Resolution by Syntactic Structures



I cooked waterfowl belonging to her
I created the duck she owns



I cooked waterfowl for her benefit
I waved my magic wand and turned
her into undifferentiated waterfowl

Exercise: Attachment Ambiguity

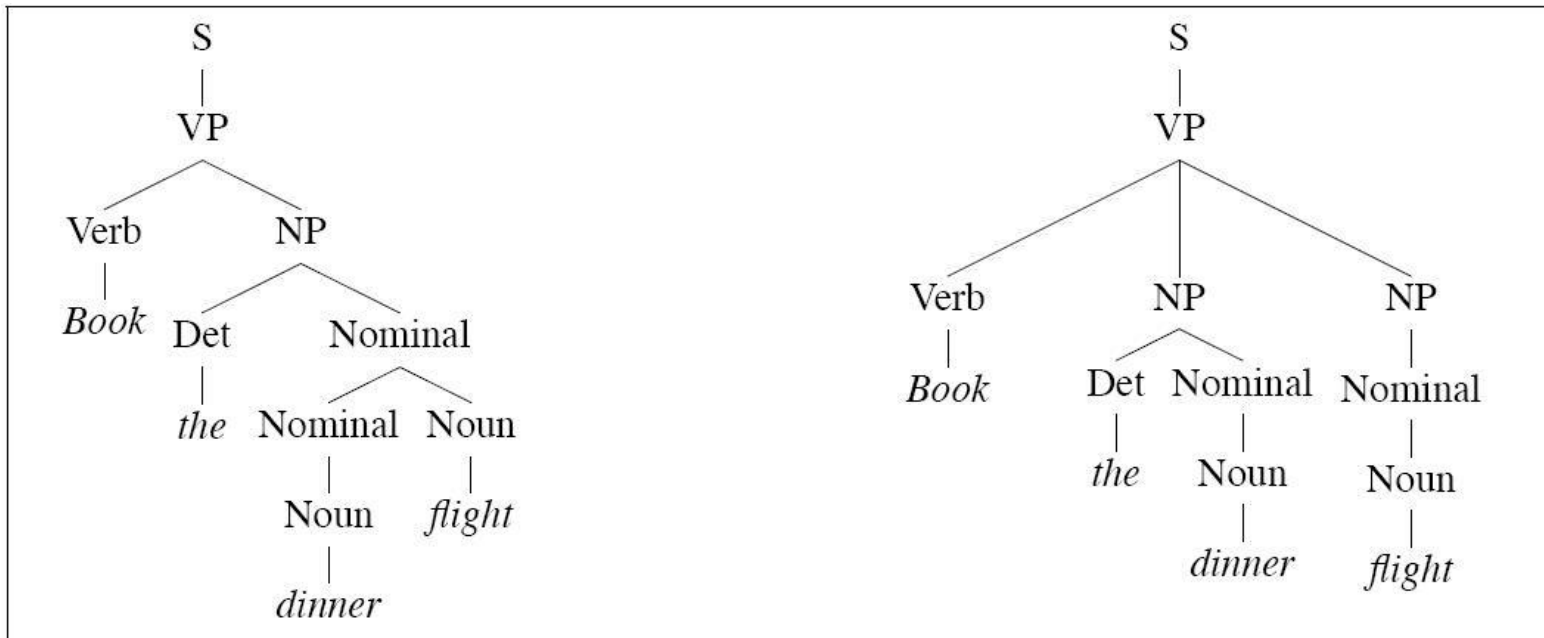
- How many distinct phrase structures may the following sentence have due to the prepositional phrase attachment ambiguities?

John wrote the book with a pen in the room



Need for Syntactic Disambiguation

- Consider the two parses of “Book the dinner flight”
- The left parse is sensible, while the right is not
 - How about “Can you book John a flight?”



Need for Common Sense

- People usually provide **only useful information** and take the rest for granted. The rest is common-sense: obvious things people know and usually leave unstated



Context-Free Grammar

- $G = (T, N, S, R)$
 - T: a set of terminals (e.g. 'flight')
 - N: a set of non-terminals (e.g. Noun)
 - S: the start symbol, a non-terminal
 - R: rules of the form $X \rightarrow \gamma$
 - X: a non-terminal
 - γ : a sequence of terminals and non-terminals

$\begin{aligned} NP &\rightarrow Det\ Nominal \\ NP &\rightarrow ProperNoun \\ Nominal &\rightarrow Noun \mid Nominal\ Noun \end{aligned}$
--

Probabilistic Context-Free Grammar (PCFG)

- $G = (T, N, S, R, P)$
 - T: a set of terminals (e.g. 'boy')
 - N: a set of non-terminals (e.g. Noun)
 - S: the start symbol, a non-terminal
 - R: rules of the form $X \rightarrow \gamma$
 - $P(R)$ gives the probability of each rule

Grammar	
$S \rightarrow NP VP$	[.80]
$S \rightarrow Aux NP VP$	[.15]
$S \rightarrow VP$	[.05]

$$\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$$

PCFG: Example

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.15] \mid money [.05]$
$NP \rightarrow Pronoun$	[.35]	$\mid flights [.40] \mid dinner [.10]$
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
$NP \rightarrow Det Nominal$	[.20]	$\mid prefer; [.40]$
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I [.40] \mid she [.05]$
$Nominal \rightarrow Noun$	[.75]	$\mid me [.15] \mid you [.40]$
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston [.60]$
$Nominal \rightarrow Nominal PP$	[.05]	$\mid NWA [.40]$
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does [.60] \mid can [.40]$
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

PCFG

- How to learn the probability of rules?

$$\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$$

- How to estimate the probability of parse trees with a PCFG?
- Once we have probabilities of possible parse trees, we can select the parse tree with the highest probability as the parse result for a given string

Probability of Rules

- Need for treebanks!

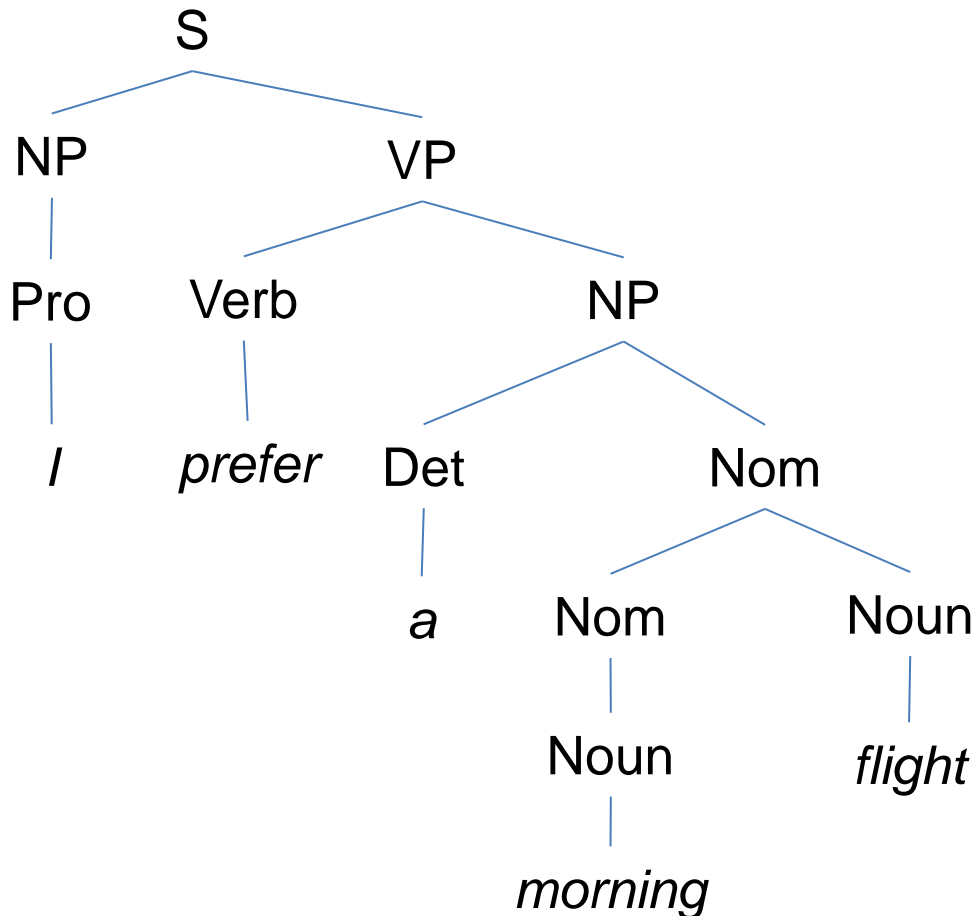
$$P(X \rightarrow \beta | X)$$

$$P(X \rightarrow \beta | X) = \frac{\text{count}(X \rightarrow \beta)}{\sum_{\gamma} \text{count}(X \rightarrow \gamma)} = \frac{\text{count}(X \rightarrow \beta)}{\text{count}(X)}$$

$$\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$$

Derivation

- A derivation (parse tree) consists of the bag of grammar rules that are in the tree



1. $S \rightarrow NP VP$
2. $NP \rightarrow Pro$
 $Pro \rightarrow I$
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$
4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$
5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow morning$
6. $Nom \rightarrow Noun$
 $Noun \rightarrow flight$

Probability of Parse Trees

- A derivation (parse tree) consists of the bag of grammar rules that are in the tree
 - The probability of a tree is the product of the probabilities of the rules in the derivation.

1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$

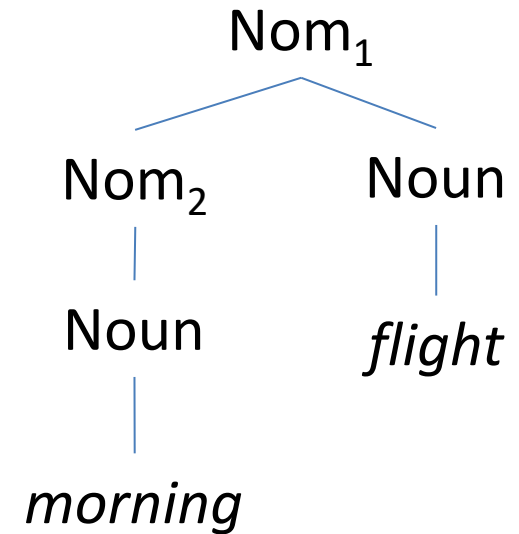
5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow morning$

6. $Nom \rightarrow Noun$
 $Noun \rightarrow flight$

$$P(T, S) = \prod_{node \in T} P(rule(n))$$

Probability of Parse Tree: Example

- Noun \rightarrow morning [0.10]
- Noun \rightarrow flight [0.40]
- Nom \rightarrow Noun [0.75]
- Nom \rightarrow Nom Noun [0.20]

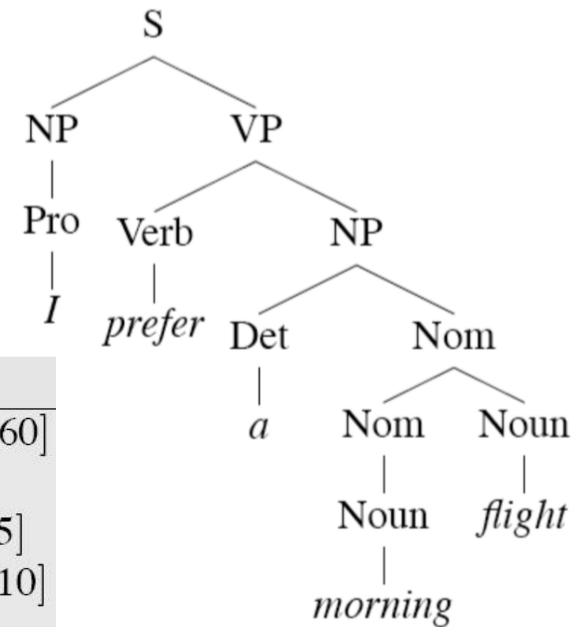


$$P(Nom_2) = 0.75 \times 0.1 = 0.75 \times 10^{-1}$$

$$P(Nom_1) = 0.2 \times 0.75 \times 10^{-1} \times 0.4 = 0.6 \times 10^{-2}$$

Exercise: Probability of Parse Tree

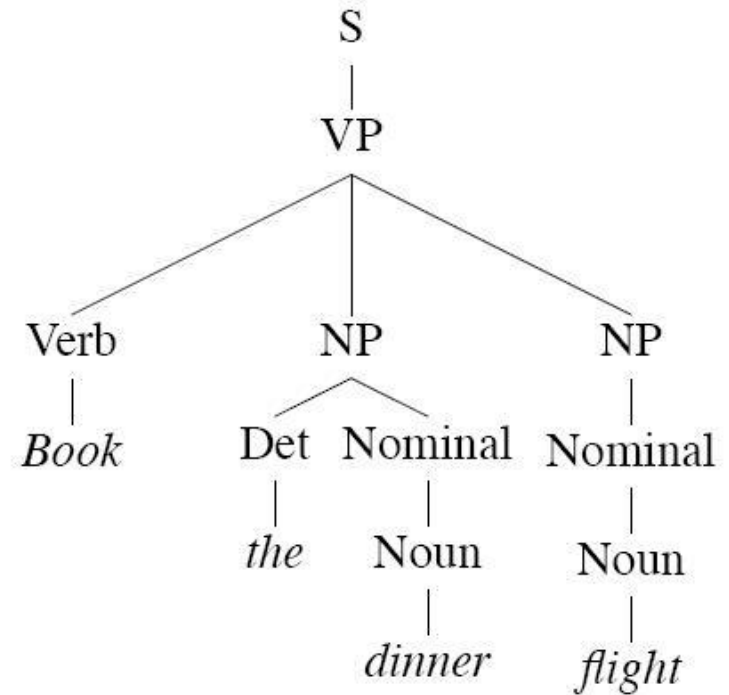
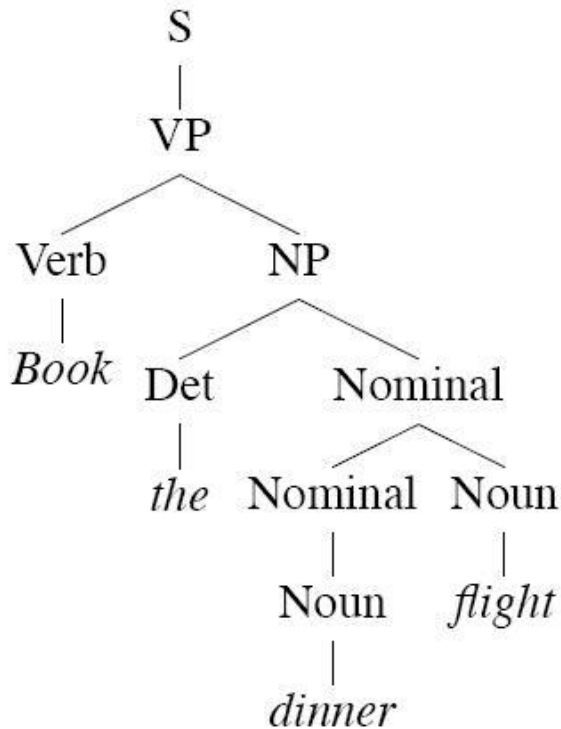
- Calculate the probability of the parse tree below



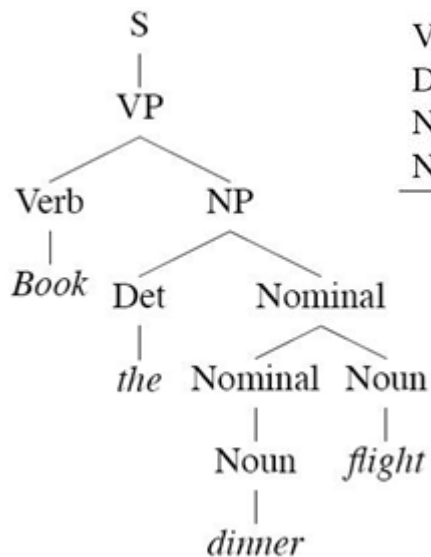
Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.15] \mid morning' [.05]$
$NP \rightarrow Pronoun$	[.35]	$\mid flights [.40] \mid dinner [.10]$
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
$NP \rightarrow Det Nominal$	[.20]	$\mid prefer; [.40]$
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I [.40] \mid she [.05]$
$Nominal \rightarrow Noun$	[.75]	$\mid me [.15] \mid you [.40]$
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$Nominal \rightarrow Nominal PP$	[.05]	$\mid NWA [.40]$
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does [.60] \mid can [.40]$
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

Why Do We Need Probability of Parse Trees?

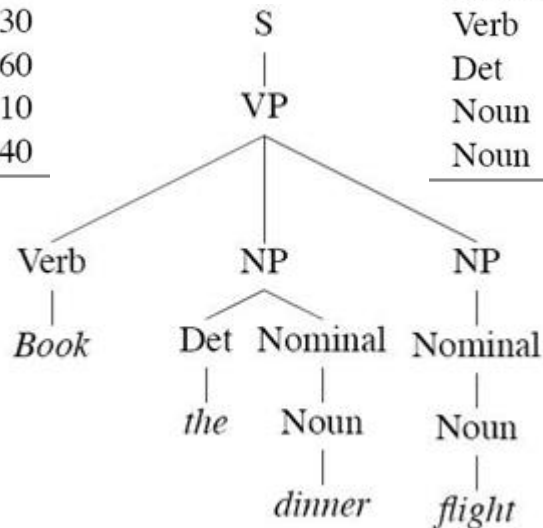
- Once we have probabilities of possible parse trees, we can select the parse tree with the highest probability as the parse result for a given string



Why Do We Need Probability of Parse Trees?



Rules		P
S	→ VP	.05
VP	→ Verb NP	.20
NP	→ Det Nominal	.20
Nominal	→ Nominal Noun	.20
Nominal	→ Noun	.75
Verb	→ book	.30
Det	→ the	.60
Noun	→ dinner	.10
Noun	→ flights	.40



Rules		P
S	→ VP	.05
VP	→ Verb NP NP	.10
NP	→ Det Nominal	.20
NP	→ Nominal	.15
Nominal	→ Noun	.75
Nominal	→ Noun	.75
Verb	→ book	.30
Det	→ the	.60
Noun	→ dinner	.10
Noun	→ flights	.40

$$P(T_{left}) = .05 * .20 * .20 * .20 * .75 * .30 * .60 * .10 * .40 = 2.2 \times 10^{-6}$$

$$P(T_{right}) = .05 * .10 * .20 * .15 * .75 * .75 * .30 * .60 * .10 * .40 = 6.1 \times 10^{-7}$$

But How Accurate/General Are These Probabilities?

- Probabilities are bound to specific datasets or corpora and, in general, are not domain-independent



Problems with PCFG

- Doesn't take the actual words (Grammar) into account
 - e.g., verb subcategorization
- Doesn't take into account where in the derivation a rule is used
 - e.g., NPs that are syntactic objects are more likely to be Pronouns.

Grammar		Lexicon	
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that$	[.10] a [.30] the [.60]
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book$	[.10] $flight$ [.30]
$S \rightarrow VP$	[.05]		$meal$ [.15] $money$ [.05]
$NP \rightarrow Pronoun$	[.35]		$flights$ [.40] $dinner$ [.10]
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book$	[.30] $include$ [.30]
$NP \rightarrow Det Nominal$	[.20]		$prefer$ [.40]
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I$	[.40] she [.05]
$Nominal \rightarrow Noun$	[.75]		me [.15] you [.40]
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston$	[.60]
$Nominal \rightarrow Nominal PP$	[.05]		NWA [.40]
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does$	[.60] can [.40]
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from$	[.30] to [.30]
$VP \rightarrow Verb NP PP$	[.10]		on [.20] $near$ [.15]
$VP \rightarrow Verb PP$	[.15]		$through$ [.05]
$VP \rightarrow Verb NP NP$	[.05]		
$VP \rightarrow VP PP$	[.15]		
$PP \rightarrow Preposition NP$	[1.0]		

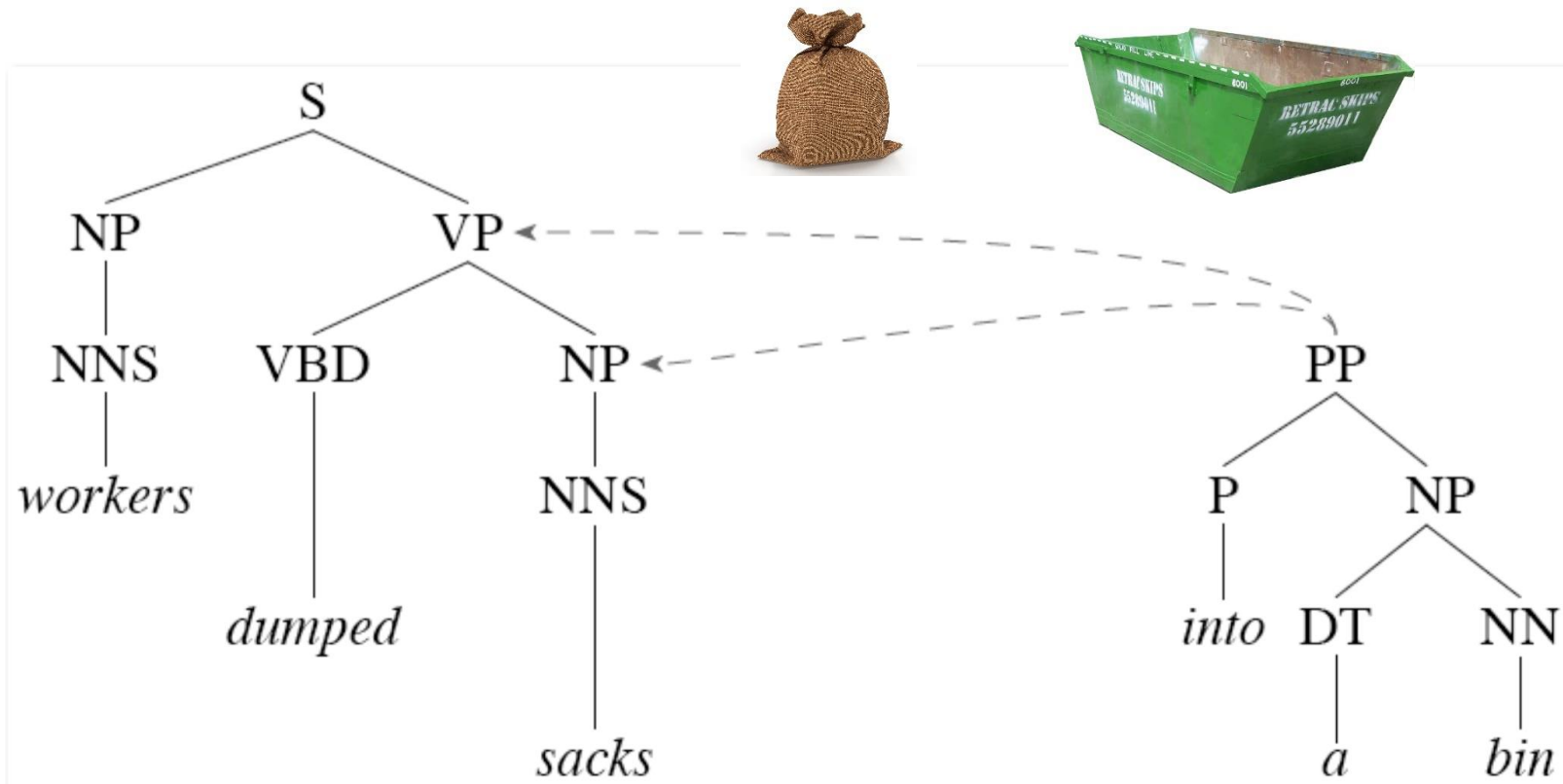
Specific Problems

- Attachment ambiguities
 - Prepositional phrase (PP) attachment
 - Coordination problem
- Structural dependencies between rules



PP Attachment

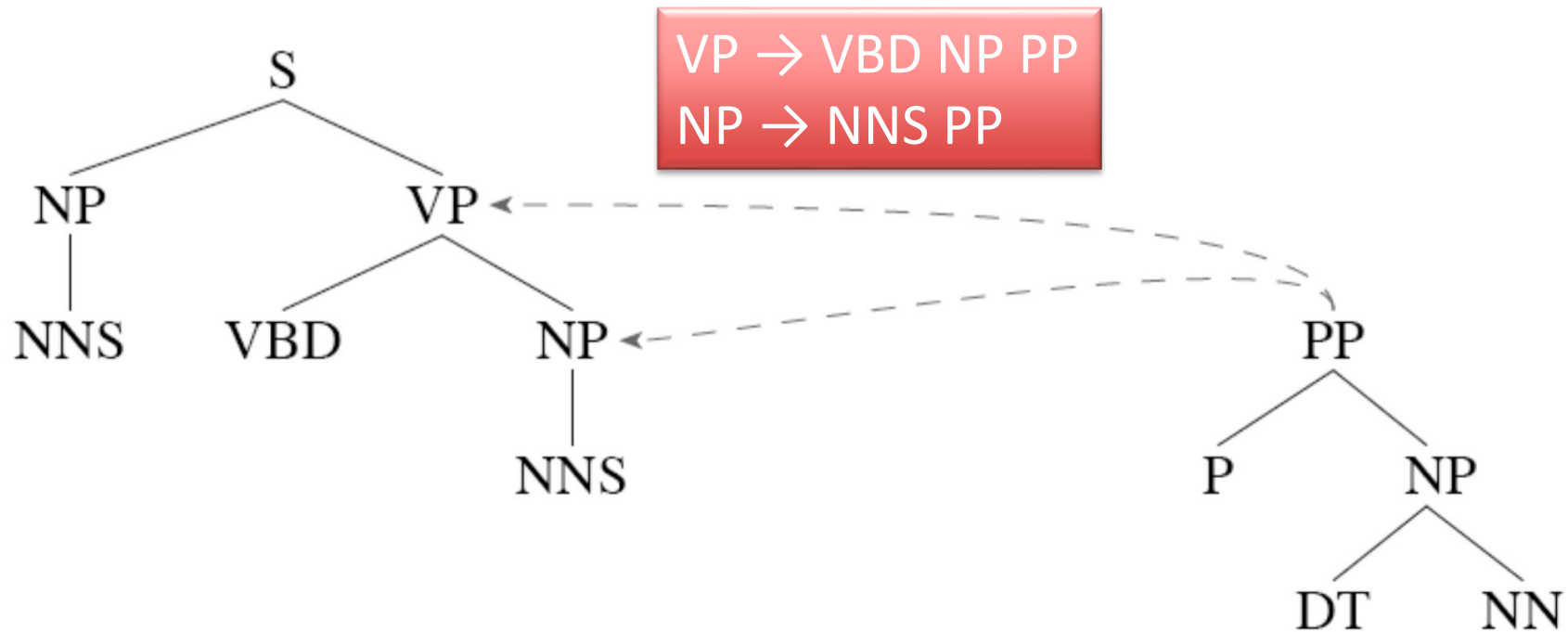
- Example sentence: Workers dumped sacks into a bin.



‘Dump’ has a stronger association with ‘into’

PP Attachment

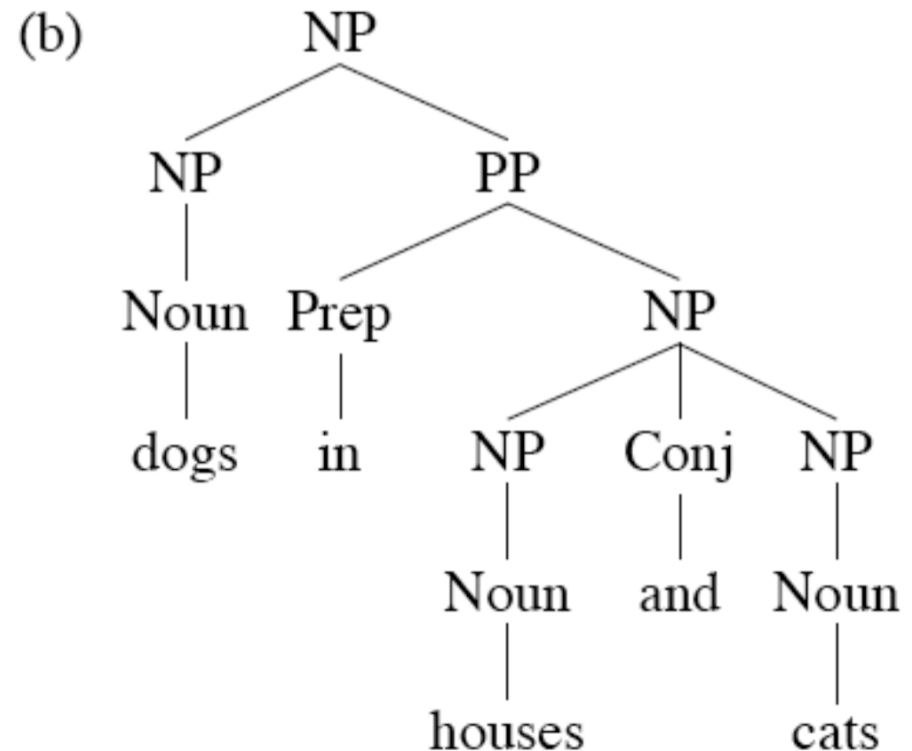
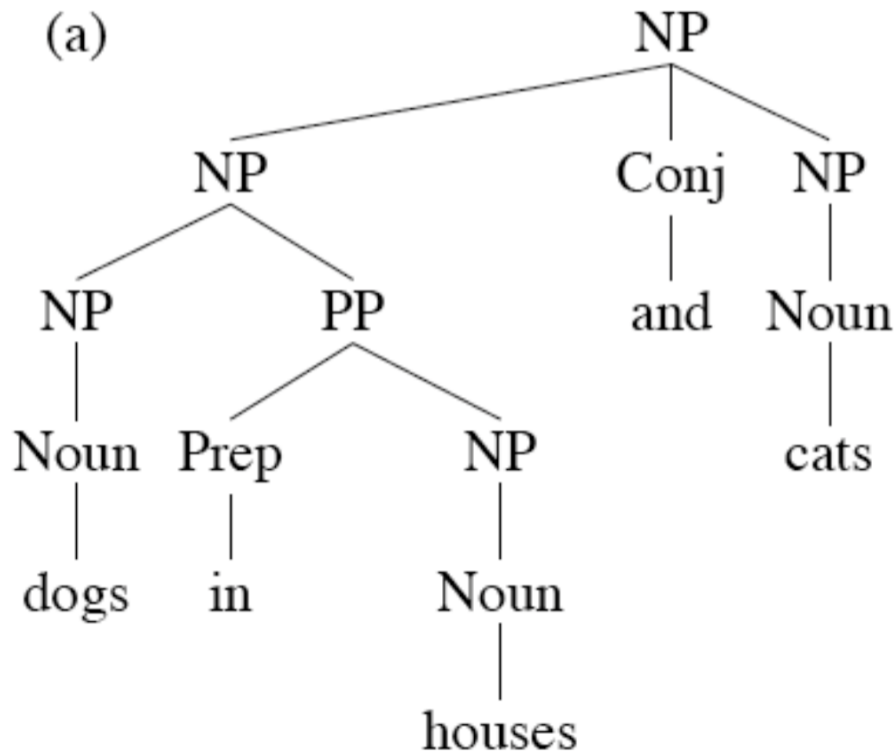
- NNS VBD NNS P DT NN
 - Rule does not consider the actual words in the sentence.
 - So we are not using the actual words here, but only the rules



Both rules are valid, and we cannot determine the attachment here.

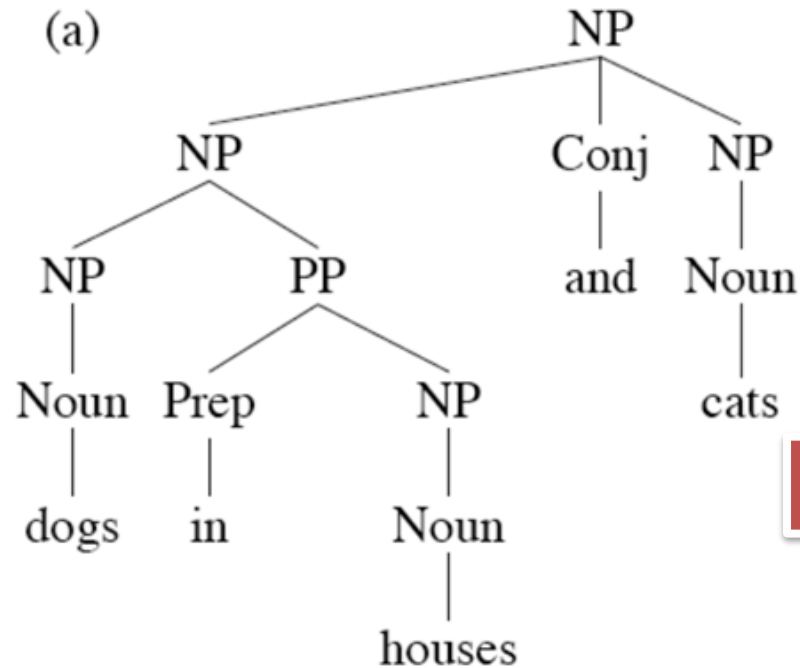
Coordination Problem

- Most grammars have such (implicit) rules as “ $X \rightarrow X \text{ and } X$ ”
 - This leads to massive ambiguity problems.

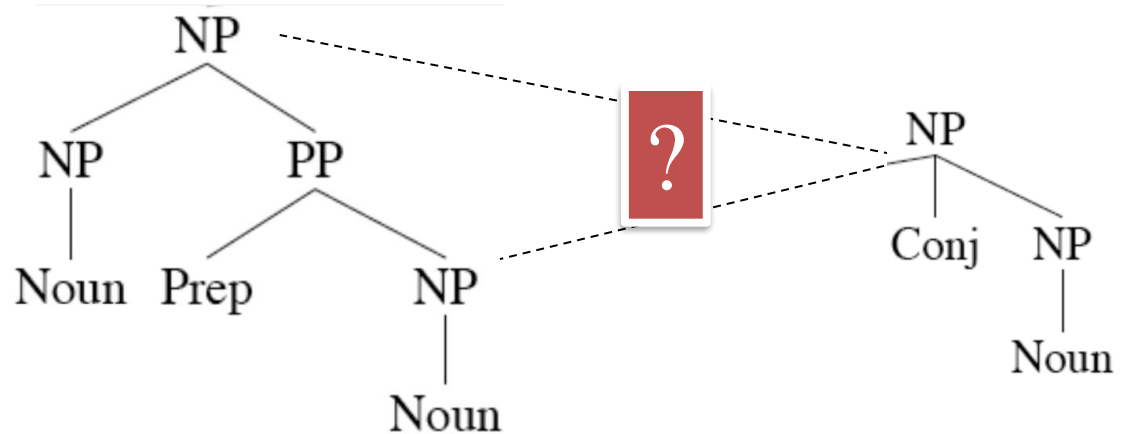


Coordination Problem

(a)



Again the rules do not consider the words



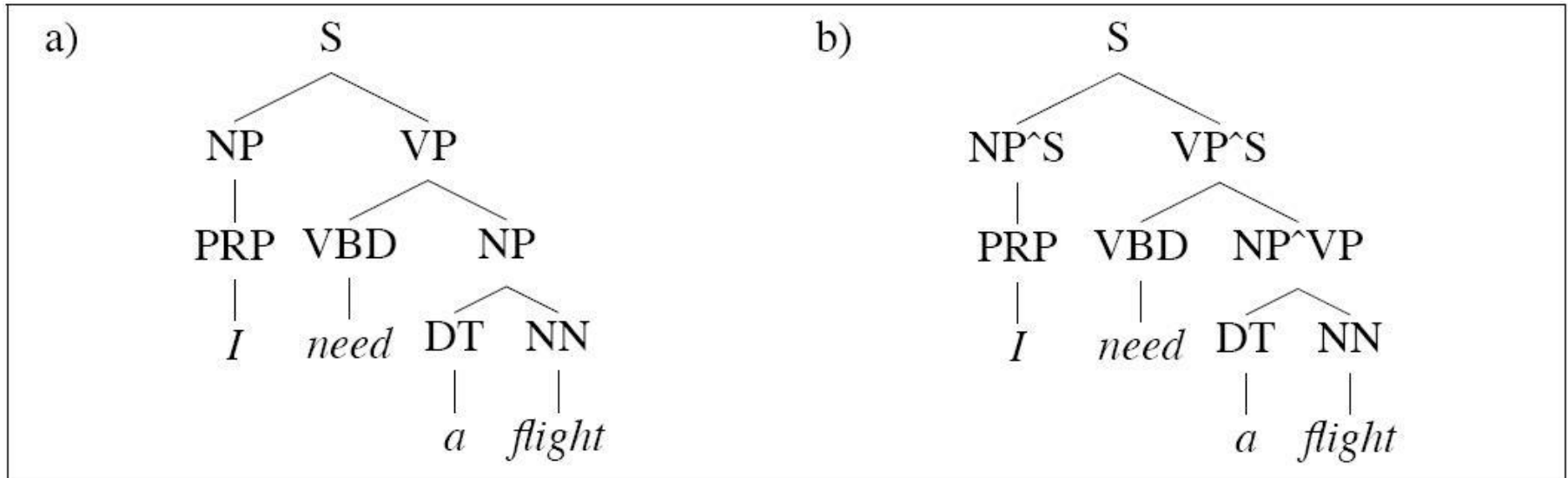
Structural Dependencies Between Rules

- Example probability for rules of NP
 - $\text{NP} \rightarrow \text{DT NN}$ (0.28)
 - $\text{NP} \rightarrow \text{Pronoun}$ (0.25)
- Rules that involve NP
 - $\text{S} \rightarrow \mathbf{NP} \text{ VP}$
 - $\text{VP} \rightarrow \text{Verb } \mathbf{NP}$

	Pronoun	Non-Pronoun
Subject	91%	9%
Object	34%	66%

Improving PCFG: Splitting Non-Terminals

- Encoding contextual dependencies into PCFG symbols
 - NP is a child of S \rightarrow NP^S
 - NP is a child of VP \rightarrow NP^{VP}



Improving PCFG: Splitting Non-Terminals

Grammar

$S \rightarrow NP VP$
 $S \rightarrow Aux NP VP$
 $S \rightarrow VP$
 $NP \rightarrow Pronoun$
 $NP \rightarrow Proper-Noun$
 $NP \rightarrow Det Nominal$
 $NP \rightarrow Nominal$
 $Nominal \rightarrow Noun$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow Verb$
 $VP \rightarrow Verb NP$
 $VP \rightarrow Verb NP PP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow Verb NP NP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

$NP^S \rightarrow Pronoun$
 $NP^{VP} \rightarrow Pronoun$
 $NP^{PP} \rightarrow Pronoun$

$NP^S \rightarrow Det Nominal^NP$
 $NP^{VP} \rightarrow Det Nominal^NP$
 $NP^{PP} \rightarrow Det Nominal^NP$

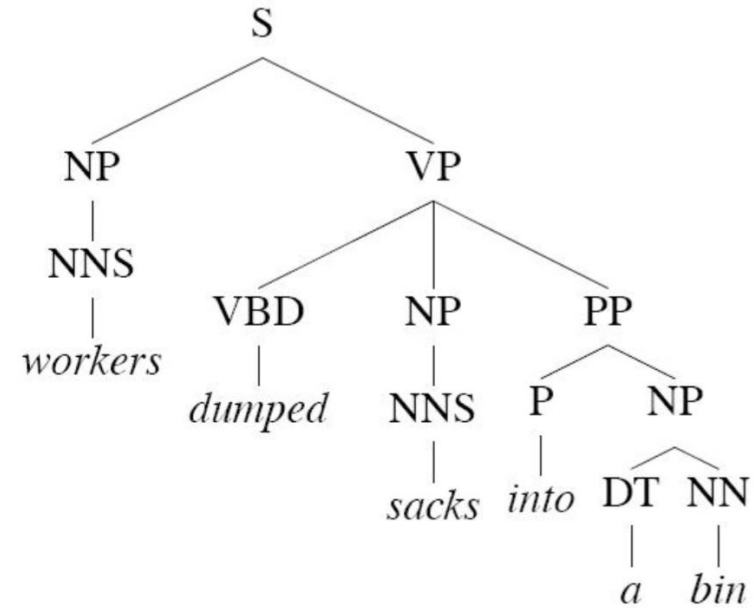
	Pronoun	Non-Pronoun
Subject	91%	9%
Object	34%	66%

Improving PCFG: Lexicalized PCFG

- How to add lexical information to rules?

- (Review) Lexical head

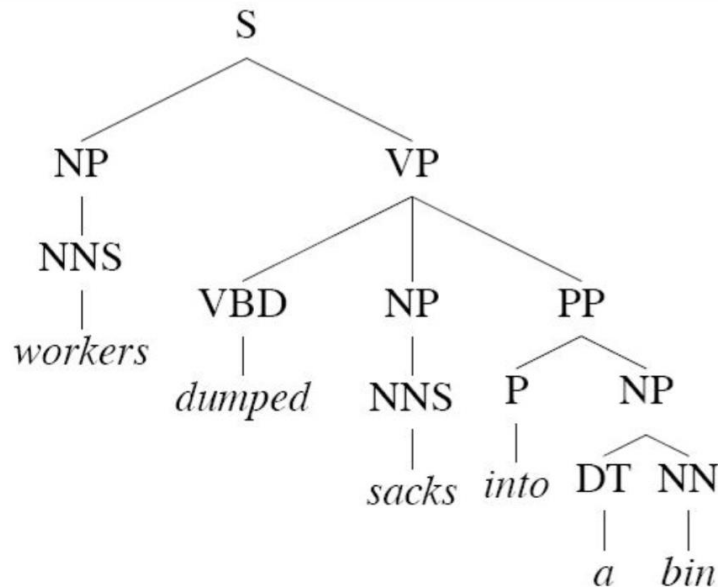
- The word in the phrase that is grammatically the most important
- E.g. N is the head of NP
- E.g. V is the head of VP



- Now, we put the **lexicon head** into the rules
- $VP \rightarrow VBD \ NP \ PP$
 - $VP(\text{dumped}) \rightarrow VBD(\text{dumped}) \ NP(\text{sacks}) \ PP(\text{into})$
 - $VP(\text{dumped}, \text{VBD}) \rightarrow VBD(\text{dumped}, \text{VBD}) \ NP(\text{sacks}, \text{NNS}) \ PP(\text{into}, \text{P})$

Evaluating Parsing Accuracy

- Sentence-level accuracy
 - But most sentences are not given a completely correct parse by any existing parser
- Constituent-level accuracy
 - Constituent as labeled span: [label, start, finish], e.g. [NP, 0, 1]



Evaluating Parsing Accuracy: Labeled Spans

- [S, 0, 5]
- [VP, 0, 5]
- [Verb, 0, 1]
- [NP, 1, 5]
- [Det, 1, 2]
- [Nominal, 2, 5]
- [Noun, 2, 3]
- [PP, 3, 5]
- [Prep, 3, 4]
- [NP, 4, 5]
- [Noun, 4, 5]

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb Nominal, Noun [0,1]			S,VP,X2 [0,3]				S,VP,X2 [0,5]			
	Det [1,2]		NP [1,3]				NP [1,5]			
			Nominal, Noun [2,3]				Nominal [2,5]			
						Prep [3,4]	PP [3,5]			
									NP, Proper- Noun [4,5]	

Example

Ground truth

(ROOT
(S
(INTJ (VB Please))
(VP (VB repeat)
(NP (DT that)))
(. .)))

(ROOT
(S
(ADVP (RB Please))
(VP (VB repeat)
(NP (DT that)))
(. .)))

TP = 5,

FP = 2,

FN = 2

(S, 0, 3)
(INTJ, 0, 1) (VB, 0, 1)
(VP, 1, 3) (VB, 1, 2)
(NP, 2, 3) (DT, 2, 3)

(S, 0, 3)
(ADVP, 0, 1) (RB, 0, 1)
(VP, 1, 3) (VB, 1, 2)
(NP, 2, 3) (DT, 2, 3)

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Example

(S (NP (PRP I))
 (VP (VBP need)
 (S (VP (TO to)
 (VP (VB fly)
 (PP (IN between)
 (NP (NNP Philadelphia)
 (CC and)
 (NNP Atlanta)))))) (. .)))

(S (NP (PRP I))
 (VP (VBP need)
 (S (VP (TO to)
 (VP (VB fly)
 (PP (IN between)
 (NP
 (NP (NNP Philadelphia))
 (CC and)
 (NP (NNP Atlanta)))))) (. .)))

Ground truth

(S,0,8) (NP,0,1) (PRP,0,1)
(VP,1,8) (VBP,1,2)
(S,2,8) (VP,2,8) (TO,2,3)
(VP,3,8) (VB,3,4)
(PP,4,8) (IN,4,5)
(NP,5,8) (NNP,5,6)
(CC,6,7) (NNP,7,8)

(S,0,8) (NP,0,1) (PRP,0,1)
(VP,1,8) (VBP,1,2)
(S,2,8) (VP,2,8) (TO,2,3)
(VP,3,8) (VB,3,4)
(PP,4,8) (IN,4,5)
(NP,5,8) (NP,5,6) (NNP,5,6)
(CC,6,7) (NP,7,8) (NNP,7,8)

TP = 16,
FP = 0,
FN = 2



Evaluating Parsing Accuracy: Measures

$$\text{Precision } (P) = \frac{TP}{TP + FP}$$

$$\text{Recall } (R) = \frac{TP}{TP + FN}$$

$$F_1 = \frac{2PR}{P + R}$$

