

Practice Problem 9

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Problem 1 — Given the above data points, perform a k-means clustering on this dataset using Euclidean distance as the distance function. Here, k is chosen to be 3. The initial centroids are randomly selected as $(1,1)$, $(1,2)$, $(3,1)$. Show the steps of the algorithm until convergence. What are the final clusters and their final centroids?

Answer

| <i>Iteration</i> | <i>Centroids</i> | <i>Associated Points</i> | <i>New Centroids</i> |
|------------------|--|--|--|
| <i>0</i> | $(1, 1)$ $(1, 2)$ $(3, 1)$ | $(1, 1)$ $(1, 2), (2, 5)$ $(3, 1), (3, 2), (4, 1), (4, 4)$ | $(1, 1)$ $(1.5, 3.5)$ $(3.5, 2)$ |
| <i>1</i> | $(1, 1)$ $(1.5, 3.5)$ $(3.5, 2)$ | $(1, 1), (1, 2)$ $(2, 5)$ $(3, 1), (3, 2), (4, 1), (4, 4)$ | $(1, 1.5)$ $(2, 5)$ $(3, 2)$ |
| <i>2</i> | $(1, 1.5)$ $(2, 5)$ $(3, 2)$ | $(1, 1), (1, 2)$ $(2, 5)$ $(3, 1), (3, 2), (4, 1), (4, 4)$ | $(1, 1.5)$ $(2, 5)$ $(3, 2)$ |

Final centroids and associated points:

| <i>Centroid</i> | <i>Points</i> |
|-----------------|----------------------------------|
| $(1, 1.5)$ | $(1, 1), (1, 2)$ |
| $(2, 5)$ | $(2, 5)$ |
| $(3, 2)$ | $(3, 1), (3, 2), (4, 1), (4, 4)$ |