

Practice Problem 5

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Problem 1 — Create the confusion matrix for both models.

Answer

<i>Model 1</i>	<i>Predicted(+)</i>	<i>Predicted(-)</i>	<i>Model 2</i>	<i>Predicted(+)</i>	<i>Predicted(-)</i>
<i>Actual(+)</i>	3	2	<i>Actual(+)</i>	5	0
<i>Actual(-)</i>	1	4	<i>Actual(-)</i>	4	1

Problem 2 — Calculate the accuracy of each model. Which model is better on the basis of accuracy?

Answer

$$\text{Accuracy} = (TP + TN) / n$$

$$\text{Model 1: } (3 + 4) / 10 = 0.7$$

$$\text{Model 2: } (5 + 1) / 10 = 0.6$$

Model 1 has a higher accuracy.

Problem 3 — Calculate the true positive rate (TPR) of each model. Which model is better on the basis of TPR?

Answer

$$TPR = TP / (TP + FN)$$

$$\text{Model 1: } 3 / (3 + 2) = 0.6$$

$$\text{Model 2: } 5 / (5 + 0) = 1$$

Model 2 has a higher TPR.

Problem 4 — Calculate the F-measure (of the positive class only) for each model. Which model is better on the basis of F-measure?

Answer

$$\text{precision} = TP / (TP + FP)$$

$$\text{recall} = TP / (TP + FN)$$

$$F = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$

$$\text{precision}_1 = \frac{3}{3+1} = 0.75$$

$$\text{recall}_1 = \frac{3}{3+2} = 0.6$$

$$F_1 = \frac{2 \times 0.75 \times 0.6}{0.75 + 0.6} = 0.6667$$

$$\text{precision}_2 = \frac{5}{5+4} = 0.5556$$

$$\text{recall}_2 = \frac{5}{5+0} = 1$$

$$F_2 = \frac{2 \times 0.5556 \times 1}{0.5556 + 1} = 0.7143$$

Model 2 has a higher F-measure.