

## MATH1058: Problem Sheet 4

**Problem 1** (Sorting with mathematical programming\*). *Propose a mathematical programming formulation for solving the sorting problem.*

Hint: you can use a binary assignment variable  $x_{ij}$  defined for each pair of positions  $i, j \in \{1, \dots, n\}$ , with  $x_{ij} = 1$  if and only if item  $i$  is put in position  $j$ . You should also introduce an appropriate set of constraints to guarantee that 1) each item  $i$  ends up in exactly one position  $j$  and 2) that each item in position  $j$  is not smaller than the item in position  $j - 1$ .

**Problem 2** (Computational complexity). *Establish whether, for each of the following pairs of functions  $f$  and  $g$ ,  $f = O(g)$ ,  $g = O(f)$ , or both.*

$f(n)$	$g(n)$
$n - 100$	$n - 200$
$n^{1/2}$	$n^{2/3}$
$100n + \log n$	$n + (\log n)^2$
$n \log n$	$10n \log 10n$
$\log 2n$	$\log 3n$
$10 \log n$	$\log(n^2)$
$n^{1.01}$	$n \log^2 n$
$n^{0.1}$	$(\log n)^{10}$