#### **Initialization**

Run the following code to import the modules you'll need. After your finish the assignment, **remember to run all cells** and save the note book to your local machine as a PDF for gradescope submission.

```
In []: import os
   import numpy as np
   import matplotlib.pyplot as plt
   import matplotlib.patches as patches
```

#### Download data

In this section we will download the data and setup the paths.

```
In []: # Download the data (Commented out because downloaded onto local machine)
    # if not os.path.exists('/content/carseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/carseq.npy -0 /content/carseq.npy
    # if not os.path.exists('/content/girlseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/girlseq.npy -0 /content/girlseq.npy
```

#### Q2.1: Theory Questions (5 points)

Please refer to the handout for the detailed questions.

## Q2.1.1: What is $\frac{\partial \mathbf{W}(\mathbf{x}; \mathbf{p})}{\partial \mathbf{p}^T}$ ? (**Hint**: It should be a 2x2 matrix)

==== your answer here! =====

$$W(x;p) = x + p = \left[egin{array}{c} x + p_x \ y + p_y \end{array}
ight]$$

$$rac{\partial \mathbf{W}(\mathbf{x};\mathbf{p})}{\partial \mathbf{p}^T} = egin{bmatrix} 1 & 0 \ 0 & 1 \end{bmatrix}$$

==== end of your answer =====

#### Q2.1.2: What is $\mathbf{A}$ and $\mathbf{b}$ ?

```
===== your answer here! =====
A = \nabla I \, \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \mathbf{b} = T(X) - I(W(x;p)) \mathbf{x} \text{ is } \Delta p. \mathbf{A}\mathbf{x} = \mathbf{b} ===== end of your answer =====
```

### Q2.1.3 What conditions must $\mathbf{A}^T \mathbf{A}$ meet so that a unique solution to $\Delta \mathbf{p}$ can be found?

```
==== your answer here! =====
A^TA must be positive semi-definite.
===== end of your answer =====
```

#### Q2.2: Lucas-Kanade (20 points)

Make sure to comment your code and use proper names for your variables.

```
In [ ]: from scipy.interpolate import RectBivariateSpline
        from numpy.linalg import lstsq
        def LucasKanade(It, It1, rect, threshold, num_iters, p0):
            :param[np.array(H, W)] It : Grayscale image at time t [float]
            :param[np.array(H, W)] It1 : Grayscale image at time t+1 [float]
            :param[np.array(4, 1)] rect : [x1 y1 x2 y2] coordinates of the rectangular temp
                                          where [x1, y1] is the top-left, and [x2, y2] is t
                                          [floats] that maybe fractional.
            :param[float] threshold
                                      : If change in parameters is less than thresh, term
                                       : Maximum number of optimization iterations
            :param[int] num_iters
            :param[np.array(2, 1)] p0 : Initial translation parameters [p_x0, p_y0] to ad
            :return[np.array(2, 1)] p : Final translation parameters [p_x, p_y]
            # ===== your code here! =====
            # Hint: Iterate over num_iters and for each iteration, construct a linear syste
            # Construct [A] by computing image gradients at (possibly fractional) pixel loc
            # We suggest using RectBivariateSpline from scipy.interpolate to interpolate pi
            # We suggest using lstsq from numpy.linalg to solve the linear system
            # Once you solve for [delta_p], add it to [p] (and move on to next iteration)
            # HINT/WARNING:
```

```
# RectBivariateSpline and Meshgrid use inconsistent defaults with respect to 'x
# https://docs.scipy.org/doc/scipy/reference/generated/scipy.interpolate.RectBi
# https://numpy.org/doc/stable/reference/generated/numpy.meshgrid.html
p = p0
px = p[0]
py = p[1]
i = 0
delta_p_norm_square = threshold
x1 = rect[0]
y1 = rect[1]
x2 = rect[2]
y2 = rect[3]
\# T_t = It[y1:y2+1,x1:x2+1]
# T_t_flat = np.reshape(T_t, (T_t.size,1))
dWdp = np.eye(2)
height = It.shape[0]
width = It.shape[1]
height_arr = np.arange(height)
width_arr = np.arange(width)
rbs_T_t = RectBivariateSpline(height_arr,width_arr,It)
iX = np.arange(x1+px,x2+px+0.5,1)
iY = np.arange(y1+py,y2+py+0.5,1)
xgrid, ygrid = np.meshgrid(iX,iY,indexing="ij")
T_t = rbs_T_t.ev(ygrid,xgrid).T
T_t_flat = np.reshape(T_t, (T_t.size,1))
rbs_IW = RectBivariateSpline(height_arr, width_arr, It1)
gradientAllX = np.gradient(It1,axis=1)
gradientAllY = np.gradient(It1,axis=0)
rbs gx = RectBivariateSpline(height arr,width arr,gradientAllX)
rbs_gy = RectBivariateSpline(height_arr, width_arr, gradientAllY)
while (i < num_iters) and (delta_p_norm_square >= threshold):
    px = p[0]
    py = p[1]
    iX = np.arange(x1+px,x2+px+0.5,1)
    iY = np.arange(y1+py,y2+py+0.5,1)
    xgrid, ygrid = np.meshgrid(iX,iY,indexing="ij")
    IW = rbs_IW.ev(ygrid,xgrid).T
    IW_flat = np.reshape(IW, (IW.size,1))
    gradientVecX = np.ravel(rbs_gx.ev(ygrid,xgrid).T)
    gradientVecY = np.ravel(rbs_gy.ev(ygrid,xgrid).T)
    gradientMatrix = np.vstack((gradientVecX,gradientVecY)).T # (pixPatch,2) gr
    A = gradientMatrix@dWdp
    b = T t flat-IW flat
```

```
#delta_p = np.linalg.lstsq(A.T@A,A.T@b,rcond=None)[0]
delta_p = np.linalg.lstsq(A,b,rcond=None)[0]

p = p + delta_p

delta_p_norm_square = np.square(np.linalg.norm(delta_p,ord=2,keepdims=True)
i = i + 1

# plt.figure(2)
# plt.imshow(T_t)
# plt.figure(3)
# plt.imshow(IW)
# ===== End of code =====
return p
```

#### Debug Q2.2

A few tips to debug your implementation:

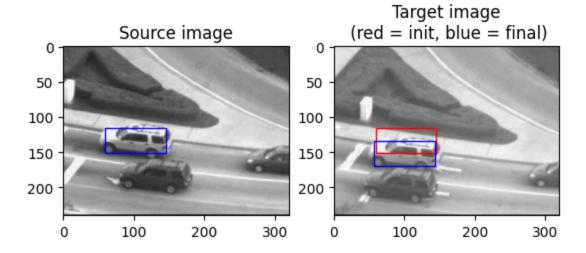
- Feel free to use and modify the following snippet to debug your implementation. The snippet simply visualizes the translation resulting from running LK on a single frame. You should be able to see a slight shift in the template.
- You may also want to visualize the image gradients you compute within your LK implementation
- Plot iterations vs the norm of delta p

```
In [ ]: def draw_rect(rect,color):
            w = rect[2] - rect[0]
            h = rect[3] - rect[1]
            plt.gca().add_patch(patches.Rectangle((rect[0],rect[1]), w, h, linewidth=1, edg
In [ ]: num_iters = 100
        threshold = 0.01
        seq = np.load("data\\carseq.npy")
        rect = np.array([59, 116, 145, 151])
        rect = np.reshape(rect, (rect.size,1))
        It = seq[:,:,0]
        # Source frame
        plt.figure()
        plt.subplot(1,2,1)
        plt.imshow(It, cmap='gray')
        plt.title('Source image')
        draw_rect(rect, 'b')
        # Target frame + LK
        It1 = seq[:,:, 20]
        plt.subplot(1,2,2)
```

```
plt.imshow(It1, cmap='gray')
plt.title('Target image\n (red = init, blue = final)')
p = LucasKanade(It, It1, rect, threshold, num_iters, np.zeros((2,1)))

rect_t1 = (rect + np.concatenate((p,p)))

draw_rect(rect,'r')
draw_rect(rect_t1,'b')
```



#### Q2.3: Tracking with template update (15 points)

```
In [ ]: def TrackSequence(seq, rect, num_iters, threshold):
                              : (H, W, T), sequence of frames
            :param seq
                             : (4, 1), coordinates of template in the initial frame. top-le
            :param num_iters : int, number of iterations for running the optimization
            :param threshold : float, threshold for terminating the LK optimization
            :return: rects : (T, 4) tracked rectangles for each frame
            0.00
            H, W, N = seq.shape
            rects = np.zeros((N,4))
            It = seq[:,:,0]
            pNow = np.zeros((2,1))
            \#rect = np.reshape(rect, (4,1))
            # Iterate over the car sequence and track the car
            for i in range(seq.shape[2]):
                # ===== your code here! =====
                # TODO: add your code track the object of interest in the sequence
                if (i == seq.shape[2]-1):
                    It = seq[:,:,i]
                    It1 = seq[:,:,i]
                else:
                    It = seq[:,:,i]
                    It1 = seq[:,:,i+1]
                pNow = LucasKanade(It,It1,rect,threshold,num_iters,pNow)
                rects[i,:] = (np.copy(rect) + np.concatenate((pNow,pNow))).T
```

```
# ===== End of code =====

#rects = np.array(rects)
assert rects.shape == (N, 4), f"Your output sequence {rects.shape} is not ({N}x
return rects
```

#### Q2.3 (a) - Track Car Sequence

Run the following snippets. If you have implemented LucasKanade and TrackSequence function correctly, you should see the box tracking the car accurately. Please note that the tracking might drift slightly towards the end, and that is entirely normal.

Feel free to play with these snippets of code by playing with the parameters.

```
In [ ]:
    def visualize_track(seq,rects,frames,rect):
        # Visualize tracks on an image sequence for a select number of frames
        plt.figure(figsize=(15,15))
        for i in range(len(frames)):
            idx = frames[i]
            frame = seq[:, :, idx]
            plt.subplot(1,len(frames),i+1)
            plt.imshow(frame, cmap='gray')
            plt.axis('off')
            draw_rect(rects[idx],'b')
```

```
In []: seq = np.load("data\\carseq.npy")
    rect = np.array([59, 116, 145, 151])
    rect = np.reshape(rect, (rect.size,1))

# NOTE: feel free to play with these parameters
    num_iters = 10000
    threshold = 0.01

rects = TrackSequence(seq, rect, num_iters, threshold)

visualize_track(seq,rects,[0, 79, 159, 279, 409],rect)
#scale = 20
#visualize_track(seq,rects,[0*scale, 1*scale, 2*scale, 3*scale, 4*scale],rect) # Ch
```











#### Q2.3 (b) - Track Girl Sequence

Same as the car sequence.

```
In [ ]: # Loads the squence
    seq = np.load("data\\girlseq.npy")
    rect = np.array([280, 152, 330, 318])
```

```
rect = np.reshape(rect, (rect.size,1))

# NOTE: feel free to play with these parameters
num_iters = 10000
threshold = 0.01

rects = TrackSequence(seq, rect, num_iters, threshold)

visualize_track(seq,rects,[0, 14, 34, 64, 84],rect)
```











#### **Initialization**

Run the following code to import the modules you'll need. After your finish the assignment, **remember to run all cells** and save the note book to your local machine as a PDF for gradescope submission.

```
In []: import time
   import os
   import numpy as np
   import matplotlib.pyplot as plt
   import matplotlib.patches as patches
```

#### **Download data**

In this section we will download the data and setup the paths.

```
In []: # Download the data
    # if not os.path.exists('/content/aerialseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/aerialseq.npy -0 /content/aerialseq.n
    # if not os.path.exists('/content/antseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/antseq.npy -0 /content/antseq.npy
```

#### **Q4: Efficient Tracking**

#### Q4.1: Inverse Composition (15 points)

```
H = It.shape[0]
W = It.shape[1]
xVals = np.arange(0, W, 1)
yVals = np.arange(0,H,1)
p1 = p[0,0]
p2 = p[1,0]
p3 = p[2,0]
p4 = p[3,0]
p5 = p[4,0]
p6 = p[5,0]
M = np.array([[1 + p1, p2, p3], [p4, 1 + p5, p6], [0, 0, 1]]) # (3,3) and there
Minv = np.linalg.inv(M)
yGrid, xGrid = np.meshgrid(yVals,xVals,indexing="ij")
xGrid_flat = xGrid.ravel()
yGrid_flat = yGrid.ravel()
oneGrid_flat = np.zeros_like(xGrid_flat) + 1
points_flat = np.vstack((xGrid_flat,yGrid_flat,oneGrid_flat)) # [x_list;y_list;
points_flat_tf = M@points_flat
xGrid_tf_flat = points_flat_tf[0,:]
yGrid_tf_flat = points_flat_tf[1,:]
xGrid_tf = np.reshape(xGrid_tf_flat,(H,W))
yGrid_tf = np.reshape(yGrid_tf_flat,(H,W))
rbs_TW = RectBivariateSpline(yVals,xVals,It)
TW = rbs_TW.ev(xGrid_tf,yGrid_tf)
T t = np.copy(It)
T_t_flat = T_t.ravel()
gradientT_X = np.gradient(T_t,axis=1)
gradientT_Y = np.gradient(T_t,axis=0)
gradientT_X_flat = gradientT_X.ravel()
gradientT_Y_flat = gradientT_Y.ravel()
gradientT_all = np.vstack((gradientT_X_flat,gradientT_Y_flat))
xVals = np.arange(0,W,1)
yVals = np.arange(0,H,1)
yGrid, xGrid = np.meshgrid(yVals,xVals,indexing="ij")
xGrid_flat = xGrid.ravel()
yGrid_flat = yGrid.ravel()
maskX = np.logical_and(xGrid_tf_flat<W,xGrid_tf_flat>=0)
maskY = np.logical_and(yGrid_tf_flat<H,yGrid_tf_flat>=0)
maskAll = maskX*maskY
N = xGrid_flat.size
gradientX_zeros = np.copy(gradientT_X_flat)
gradientX_zeros[~maskAll] = 0
gradientY_zeros = np.copy(gradientT_Y_flat)
gradientY zeros[~maskAll] = 0
```

```
A = np.zeros((N,6))
A[:,0] = gradientX_zeros*xGrid flat
A[:,1] = gradientY_zeros*xGrid_flat
A[:,2] = gradientX_zeros*yGrid_flat
A[:,3] = gradientY_zeros*yGrid_flat
A[:,4] = gradientX_zeros*1
A[:,5] = gradientY_zeros*1
while (i < num_iters) and (delta_p_length >= threshold):
    points_flat_tf = M@points_flat
    xGrid_tf_flat = points_flat_tf[0,:]
    yGrid tf flat = points flat tf[1,:]
    xGrid_tf = np.reshape(xGrid_tf_flat,(H,W))
    yGrid_tf = np.reshape(yGrid_tf_flat,(H,W))
    TW = rbs_TW.ev(xGrid_tf,yGrid_tf)
    TW_flat = TW.ravel()
    b = (T_t_flat - TW_flat)
    # print(A.shape)
    # print(b.shape)
    delta_p = np.linalg.lstsq(A,b,rcond=None)[0]
    p = p + delta_p
    delta_p_length = np.square(np.linalg.norm(delta_p,ord=2))
    p1 = p[0,0]
    p2 = p[1,0]
   p3 = p[2,0]
   p4 = p[3,0]
    p5 = p[4,0]
    p6 = p[5,0]
   M = np.array([[1 + p1, p2, p3], [p4, 1 + p5, p6], [0, 0, 1]]) # (3,3) and t
   i = i + 1
# Adjust M to be (2,3) again
newM = M[0:2,0:3]
# ==== End of code =====
return newM
```

#### Debug Q4.1

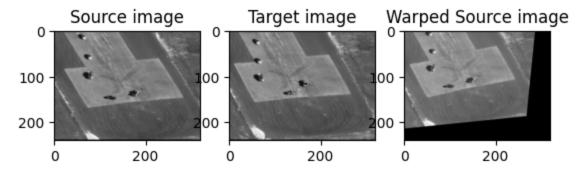
Feel free to use and modify the following snippet to debug your implementation. The snippet simply visualizes the translation resulting from running LK on a single frame. When you warp the source frame using the obtained transformation matrix, it should resemble the target frame.

```
In [ ]: import cv2

num_iters = 100
threshold = 0.01
```

```
seq = np.load("data\\aerialseq.npy")
It = seq[:,:,0]
It1 = seq[:,:,10]
# Source frame
plt.figure()
plt.subplot(1,3,1)
plt.imshow(It, cmap='gray')
plt.title('Source image')
# Target frame
plt.subplot(1,3,2)
plt.imshow(It1, cmap='gray')
plt.title('Target image')
# Warped source frame
M = InverseCompositionAffine(It, It1, threshold, num_iters)
warped_It = cv2.warpAffine(It, M,(It.shape[1],It.shape[0]))
plt.subplot(1,3,3)
plt.imshow(warped_It, cmap='gray')
plt.title('Warped Source image')
```

Out[]: Text(0.5, 1.0, 'Warped Source image')



#### Q4.2 Tracking with Inverse Composition (10 points)

Re-use your impplementation in Q3.2 for subtract dominant motion. Just make sure to use InverseCompositionAffine within.

Re-use your implementation in Q3.3 for sequence tracking.

```
In [ ]: from tqdm import tqdm
        def TrackSequenceAffineMotion(seq, num_iters, threshold, tolerance):
                              : (H, W, T), sequence of frames
            :param seq
            :param num_iters : int, number of iterations for running the optimization
            :param threshold : float, if the length of dp < threshold, terminate the optimi
            :param tolerance : (float), binary threshold of intensity difference when compu
            :return: masks : (T, 4) moved objects for each frame
            .....
            H, W, N = seq.shape
            masks = []
            It = seq[:,:,0]
            # ===== your code here! =====
            for i in tqdm(range(1, seq.shape[2])):
                if (i == seq.shape[2]-1):
                    It = seq[:,:,i]
                    It1 = seq[:,:,i]
                else:
                    It = seq[:,:,i]
                    It1 = seq[:,:,i+1]
                mask = SubtractDominantMotion(It, It1, num_iters, threshold, tolerance)
                masks.append(mask)
                # print(mask)
            # ===== End of code =====
            masks = np.stack(masks, axis=2)
            return masks
```

Track the ant sequence with inverse composition method.

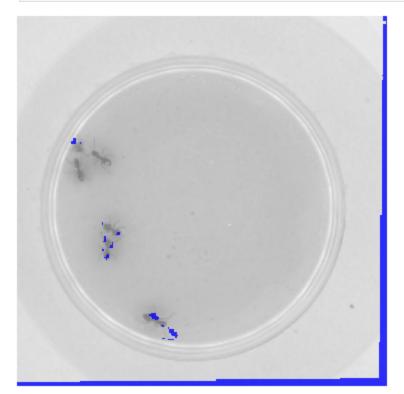
```
In [ ]: seq = np.load("data\\antseq.npy")

# NOTE: feel free to play with these parameters
num_iters = 20
```

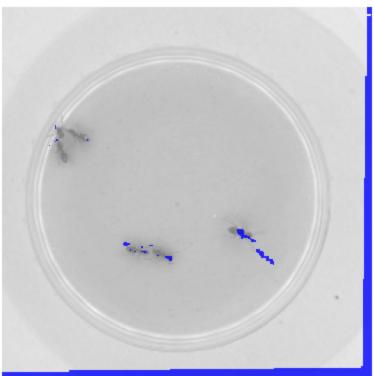
```
In []: frames_to_save = [29, 59, 89, 119]

# TODO: visualize
for idx in frames_to_save:
    frame = seq[:, :, idx]
    mask = masks[:, :, idx]

plt.figure()
    plt.imshow(frame, cmap="gray", alpha=0.5)
    plt.imshow(np.ma.masked_where(np.invert(mask), mask), cmap='winter', alpha=0.8)
    plt.axis('off')
```







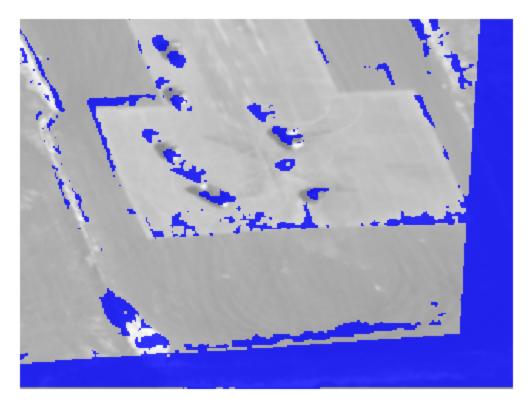


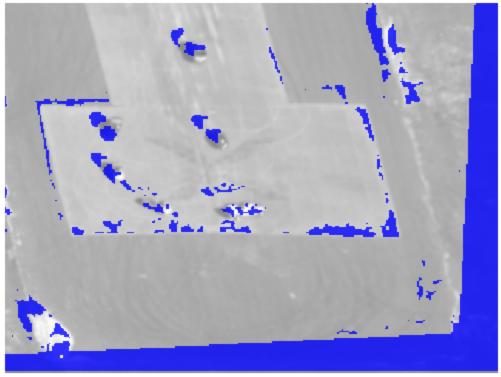
Track the aerial sequence with inverse composition method.

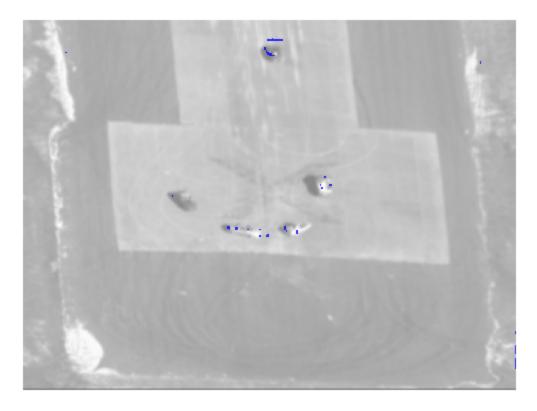
```
In []: frames_to_save = [29, 59, 89, 119]

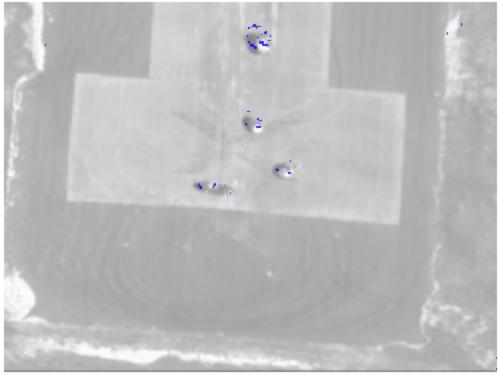
# TODO: visualize
for idx in frames_to_save:
    frame = seq[:, :, idx]
    mask = masks[:, :, idx]

plt.figure()
    plt.imshow(frame, cmap="gray", alpha=0.5)
    plt.imshow(np.ma.masked_where(np.invert(mask), mask), cmap='winter', alpha=0.8)
    plt.axis('off')
```









Q4.2.1 Compare the runtime of the algorithm using inverse composition (as described in this section) with its runtime without inverse composition (as detailed in the previous section) in the context of the ant and aerial sequences:

==== your answer here! =====

The ant sequence normally took 56 seconds but was decreased to around 53 seconds using the inverse composition method.

The aerial sequence normally took 79 seconds but was decreased to around 66 seconds using the inverse composition method.

==== end of your answer ====

# Q4.2.2 In your own words, please describe briefly why the inverse compositional approach is more computationally efficient than the classical approach:

==== your answer here! =====

You don't have to recompute the Hessian over and over again. For my computation strategy that's equivalent to not having to compute the A matrix over and over again.

==== end of your answer ====

#### **Initialization**

Run the following code to import the modules you'll need. After your finish the assignment, **remember to run all cells** and save the note book to your local machine as a PDF for gradescope submission.

```
In []: import time
   import os
   import numpy as np
   import matplotlib.pyplot as plt
   import matplotlib.patches as patches
```

#### **Download data**

In this section we will download the data and setup the paths.

```
In []: # Download the data
    # if not os.path.exists('/content/aerialseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/aerialseq.npy -0 /content/aerialseq.n
    # if not os.path.exists('/content/antseq.npy'):
    # !wget https://www.cs.cmu.edu/~deva/data/antseq.npy -0 /content/antseq.npy
```

#### **Q3: Affine Motion Subtraction**

#### Q3.1: Dominant Motion Estimation (15 points)

```
W = It.shape[1]
xVals = np.arange(0, W, 1)
yVals = np.arange(0,H,1)
yGrid, xGrid = np.meshgrid(yVals,xVals,indexing="ij")
xGrid_flat = xGrid.ravel()
yGrid_flat = yGrid.ravel()
oneGrid flat = np.zeros like(xGrid flat) + 1
points_flat = np.vstack((xGrid_flat,yGrid_flat,oneGrid_flat)) # [x_list;y_list;
T t = np.copy(It)
T_t_flat = T_t.ravel()
rbs IW = RectBivariateSpline(yVals,xVals,It1)
gradientX = np.ravel(np.gradient(It1,axis=1))
gradientY = np.ravel(np.gradient(It1,axis=0))
while (i < num_iters) and (delta_p_length >= threshold):
    p1 = p[0,0]
   p2 = p[1,0]
    p3 = p[2,0]
   p4 = p[3,0]
    p5 = p[4,0]
   p6 = p[5,0]
   M = np.array([[1 + p1, p2, p3], [p4, 1 + p5, p6]])
    points_flat_tf = M@points_flat
    xGrid_tf_flat = points_flat_tf[0,:]
   yGrid tf flat = points flat tf[1,:]
    xGrid_tf = np.reshape(xGrid_tf_flat,(H,W))
   yGrid_tf = np.reshape(yGrid_tf_flat,(H,W))
    IW = rbs IW.ev(xGrid tf,yGrid tf)
    IW_flat = IW.ravel()
   maskX = np.logical and(xGrid tf flat<W,xGrid tf flat>=0)
   maskY = np.logical_and(yGrid_tf_flat<H,yGrid_tf_flat>=0)
   maskAll = maskX*maskY
    x_flat_short = xGrid_tf_flat[maskAll]
    y_flat_short = yGrid_tf_flat[maskAll]
    IW_flat_short = IW_flat[maskAll]
   T_t_flat_short = T_t_flat[maskAll]
    b = (T_t_flat_short - IW_flat_short).T # (N,1)
    #b = (It1.ravel()[maskAll] - IW_flat_short).T # (N,1)
    gradientX_short = gradientX[maskAll]
    gradientY_short = gradientY[maskAll]
    gradientMatrix = np.vstack((gradientX short,gradientY short)).T # (N,6)
   N = gradientX_short.size
   A = np.zeros((N,6))
   A[:,0] = gradientX_short*x_flat_short
   A[:,1] = gradientY short*x flat short
```

```
A[:,2] = gradientX_short*y_flat_short
    A[:,3] = gradientY_short*y_flat_short
    A[:,4] = gradientX_short*1
    A[:,5] = gradientY_short*1
    delta_p = np.linalg.lstsq(A,b,rcond=None)[0]
    \# A = gradientMatrix*dWdp \# (1,2)(2,6) = (1,6) --> (N,6)
    # b = T t - IW # (N,1)
    \# Ax = b
    i = i + 1
    delta_p_length = np.square(np.linalg.norm(delta_p,ord=2))
    p = p + delta_p
p1 = p[0,0]
p2 = p[1,0]
p3 = p[2,0]
p4 = p[3,0]
p5 = p[4,0]
p6 = p[5,0]
M = np.array([[1 + p1, p2, p3], [p4, 1 + p5, p6]])
# print(M)
# plt.figure(4)
# plt.imshow(T_t)
# plt.figure(5)
# plt.imshow(IW)
# print(T_t.shape)
# print(IW.shape)
# print(points_flat.shape)
return M
```

#### Debug Q3.1

Feel free to use and modify the following snippet to debug your implementation. The snippet simply visualizes the translation resulting from running LK on a single frame. When you warp the source frame using the obtained transformation matrix, it should resemble the target frame.

```
In []: import cv2

num_iters = 100 # Defaults to 100
    threshold = 0.01
    seq = np.load("data\\aerialseq.npy")
    It = seq[:,:,0]
    It1 = seq[:,:,10]

# Source frame
plt.figure()
```

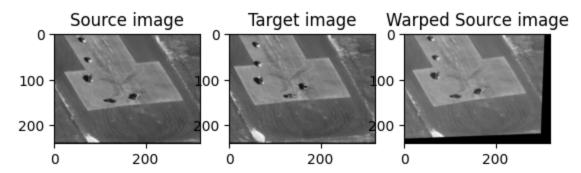
```
plt.subplot(1,3,1)
plt.imshow(It, cmap='gray')
plt.title('Source image')

# Target frame
plt.subplot(1,3,2)
plt.imshow(It1, cmap='gray')
plt.title('Target image')

# Warped source frame
M = LucasKanadeAffine(It, It1, threshold, num_iters)
warped_It = cv2.warpAffine(It, M,(It.shape[1],It.shape[0]))
plt.subplot(1,3,3)
plt.imshow(warped_It, cmap='gray')
plt.title('Warped Source image')

# plt.figure()
# plt.imshow(It1-warped_It)
```

Out[]: Text(0.5, 1.0, 'Warped Source image')



#### Q3.2: Moving Object Detection (10 points)

```
In [ ]: import numpy as np
        from scipy.ndimage import binary_erosion
        from scipy.ndimage import binary dilation
        from scipy.ndimage import affine_transform
        import scipy.ndimage
        import cv2
        def SubtractDominantMotion(It, It1, num_iters, threshold, tolerance):
            :param It
                             : (H, W), current image
                             : (H, W), next image
            :param It1
            :param num_iters : (int), number of iterations for running the optimization
            :param threshold : (float), if the length of dp < threshold, terminate the opti
            :param tolerance : (float), binary threshold of intensity difference when compu
            :return: mask : (H, W), the mask of the moved object
            mask = np.ones(It.shape, dtype=bool)
            # ===== your code here! =====
            M = LucasKanadeAffine(It, It1, threshold, num_iters)
```

```
warped_It = cv2.warpAffine(It, M,(It.shape[1],It.shape[0]))
absDiff = np.abs(It1 - warped_It)
mask1 = absDiff > tolerance
mask2 = absDiff < np.max(absDiff)*1.0
mask = mask1*mask2
# ==== End of code =====</pre>
return mask
```

#### Q3.3: Tracking with affine motion (10 points)

```
In [ ]: from tqdm import tqdm
        def TrackSequenceAffineMotion(seq, num_iters, threshold, tolerance):
                             : (H, W, T), sequence of frames
            :param num_iters : int, number of iterations for running the optimization
            :param threshold : float, if the length of dp < threshold, terminate the optimi
            :param tolerance : (float), binary threshold of intensity difference when compu
            :return: masks : (T, 4) moved objects for each frame
            H, W, N = seq.shape
            masks = []
            It = seq[:,:,0]
            # ===== your code here! =====
            for i in tqdm(range(1, seq.shape[2])):
                if (i == seq.shape[2]-1):
                    It = seq[:,:,i]
                    It1 = seq[:,:,i]
                else:
                    It = seq[:,:,i]
                    It1 = seq[:,:,i+1]
                mask = SubtractDominantMotion(It, It1, num_iters, threshold, tolerance)
                masks.append(mask)
                # print(mask)
            # ===== End of code =====
            masks = np.stack(masks, axis=2)
            return masks
```

#### Q3.3 (a) - Track Ant Sequence

```
In []: seq = np.load("data\\antseq.npy")

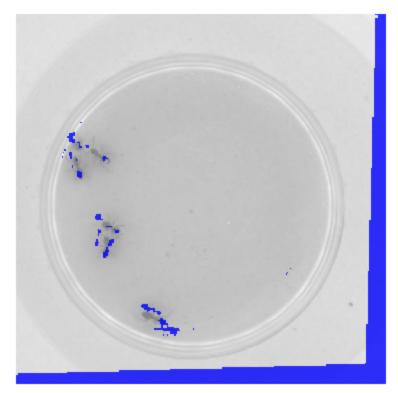
# NOTE: feel free to play with these parameters
num_iters = 20 #
threshold = 0.01
tolerance = 0.2

tic = time.time()
masks = TrackSequenceAffineMotion(seq, num_iters, threshold, tolerance)
```

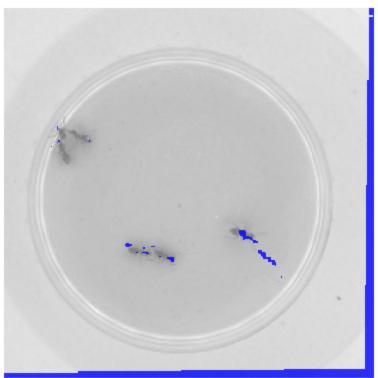
```
In []: frames_to_save = [29, 59, 89, 119]

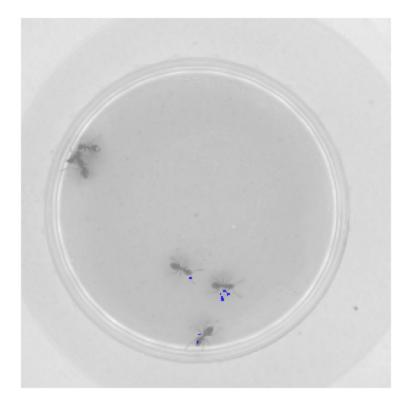
# TODO: visualize
for idx in frames_to_save:
    frame = seq[:, :, idx]
    mask = masks[:, :, idx]
    # print(masks[0,0,0])

plt.figure()
    plt.imshow(frame, cmap="gray", alpha=0.5)
    plt.imshow(np.ma.masked_where(np.invert(mask), mask), cmap='winter', alpha=0.8)
    plt.axis('off')
```









#### Q3.3 (b) - Track Aerial Sequence

```
In []: frames_to_save = [29, 59, 89, 119]

# TODO: visualize
for idx in frames_to_save:
    frame = seq[:, :, idx]
    mask = masks[:, :, idx]

plt.figure()
    plt.imshow(frame, cmap="gray", alpha=0.5)
    plt.imshow(np.ma.masked_where(np.invert(mask), mask), cmap='winter', alpha=0.8)
    plt.axis('off')
```

