

Algorithmic Market Making

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Symbology Glossary

1. Tight Skew: α_T
2. Loose Skew: α_L
3. Tight Width: ω_T
4. Loose Width: ω_L
5. Algorithmically generated Ideal Mid Cash Price: Π_{Ideal}
6. Position: P (expressed in cumulative net position per unit under consideration – firm/desk/trader)
7. Position Pivot: P_{Pivot} . Dimensionless ontological view of the scaling position metric – roughly equivalent to the Reynolds' number of market making position units. Expressed in currency units.
8. Risk: R (expressed in cumulative net risk per unit under consideration – firm/desk/trader)
9. Risk Pivot: R_{Pivot} . Dimensionless ontological view of the scaling risk metric – roughly equivalent to the Reynolds' number of market making risk units. Expressed in PV01 currency units.

Framework Glossary

1. Equilibrium quantity: Quantity that only changes with the macro drivers/factors, and not the technical factors. Typically stable, but jumpy and undergoes changes when drivers shift – and introduces perturbations on the disequilibrium quantities.
2. Disequilibrium quantity: Quantity that changes with the technical, transient factors.

Width/Skew/Size Estimation Models

1. Tight Models:

- Tight models estimate the market making quantities on a trader/firm/desk independent manner.
- They estimate the “secular” market making parameters – width, skew, and size for either the Market Making Outputs or the Axe Outputs – estimate them based on classes of input parameters.
- For each input parameter class, the following are needed:
 - a. A proxy that serves as a quantitative estimate of the desired parameter class.
 - b. Segmentation of the proxy over the sub-classified parameter set.

2. Input Class => Risk Profile:

- Captures all the cumulative risk components => the credit/solvency, market, and liquidity risk behind the issue.
- Proxy => CDS Spread, rating, bond basis
- Sub-classification => Issue, issuer, and sector.

3. Input Class => Liquidity:

- Captures the frequency and volume of the trade flow of a given issue, and the ease of getting in and getting out at the given side.
- Proxy:
 - i. Aggregated periodic (e.g., daily) volume for each side (buy/sell).
 - ii. Aggregated periodic (e.g., daily) notional for each side (buy/sell).
- Sub-classification => Issue, issuer, sector, and the instrument universe.

4. Firm/Desk/Trader level parameters: These provide aggregated controls for trading.
 - Net Position => vital metric for inventory control.
 - Risk limits => to control/manage exposure to specific granules – issue, issuer, tenor, sector, unit etc:
5. Monitor Mobility: Certain measures such as PV01 based risk, inventory, etc: are more easily human-monitored, so they are done daily. Others (such as tenor 01s) are less easily monitored, so they are done infrequently.

Market Making System SKU

1. Intra day Curve Generation Scheme
2. Mid Price Estimation Models
 - i. Accommodate different mid price estimation models, and their respective parameters
3. Algorithmic Quote Construction => used for generating venue/ECN independent width/skew/size [composed of tight/loose components]. Broadly speaking achieves the following:
 - i. Specific parameters to control skew for targeted alpha generation strategies
 - ii. Accommodate different width and size estimation models, and their respective parameters
 - iii. Venue-independent base quote synthesis/construction
 - iv. Circuit breaker heuristics
 - v. Policy driven/policy enforcement/policy control applied at this level
4. Quote Management: Publishing/tailoring the constructed quote towards specific venues (possibly with order routing applied at this stage).
 - i. Venue specific rules (and thereby external vendor incorporations, like Broadway etc© at this stage.

Market Making Parameter Types

1. Model Parameters: Parameters for generation of algorithmic generation of width, skew, and size.
2. Quote Generation Control Parameters
3. Quote Heuristics Control
4. Quote Management Control

Intra-day Pricing Curve Generation Schemes

1. Issue Benchmark Bonds: The following set of threshold criteria are used to determine the issuer specific benchmark bonds:

- ii. Threshold of daily TRACE volume/number of trades
- iii. Threshold of outstanding notional
- iv. Only senior obligations
- v. Some combination of the following threshold of the ratios:

- $$\frac{CUMULATEDAILYISSUETRACEVOLUME}{OUTSTANDINGNOTIONAL}$$
- $$\frac{CUMULATEDAILYISSUETRACEVOLUME}{CUMULATEDAILYISSUERTRACEVOLUME}$$

2. Benchmark bonds basis tracking: Track the bid side and ask side credit basis of the benchmark bonds from each TRACE print, using EMA VWAP/TWAP from the intra-day rates/credit curves. This will be the attempt to estimate the mid credit basis for the, and it is generally well behaved.
 - Need to find a way to accommodate the institutional closing CDS mid marks and the benchmark bonds into the credit curve construction – these are highly valid points.
3. Intra-day credit curve generation inputs: Need a way to generate the credit curve from
 - i. The CDS marks

- ii. The basis-adjusted benchmark bonds
 - iii. It always needs to be used in conjunction with tension splines.
 - iv. Also need intra-day TRACE series to update the basis (direct or EMA) – will use this to establish the intra-day relationship between the CDS nodes and the TRACE cut-off threshold).
4. Intra-day credit curve updating:
- a. Use the relationship grid between CDS 5Y, the off-tenors, and the benchmark bonds
 - b. Any change in any of them automatically re-adjusts using the set relationships.
 - c. CDS Curves are trader set; bond basis are EMA'd from the TRACE series using the prior credit curve
 - d. Relationships are either reviewed daily EOD
5. Live updating of bond prices: Use the live curve (either pure CDS, or a mixture of CDS/bond instruments) to extract the basis of each print, and then EMA that to generate the bond live prices.

Mid Price Models

- i. Definition: Computed theoretical mid-price, as to where the next print should be – assuming zero transaction costs, zero position/risk constraints, and infinite liquidity. Mid Price is an *Equilibrium Quantity*.
- ii. Estimation parameters: Typical mid price estimation parameters are: the IR curve, the survival curve, and the recovery curve. The other possible drivers are: funding curve – typically for long position, and repo curve – typically for shorts.

Width Models

1. Tight Width: Computed theoretical width, after accounting for the issue liquidity and the issue riskiness. Tight width is the first in the set of disequilibrium quantities. Tight width is:
 - a. Proportional to issue risk (combination of credit and market risk – not counter party risk).
 - b. Inversely proportional to liquidity

Skew Models

1. Tight Skew: This measure how far the last print has been OFF from the theoretical mid price. Thus Tight Skew is representative of the alpha potential – for a theoretical mid price that chases the print in a sequence, the tight skew is zero.
2. Tight Bid Skew and Tight Ask Skew: This is an alternative SKU – instead of tight width and tight skew cognitive view, tight bid/ask skew parameters are determined only from their corresponding liquidity and flow metrics (i.e., bid/ask liquidity metrics).
3. Loose Skew: Simply put, loose skew is:

$$\alpha_L = \max\left(\frac{P}{P_{Pivot}}, \frac{R}{R_{Pivot}}\right)$$

4. Heuristic Checks on Loose Skew: Following checks applied to round out quoting:
 1. Ceiling/floor applied
 2. Maximum cutoff for width
 3. Best right skew – bid becomes ask.
 4. Best left skew – ask becomes bid.

Size Models

1. Tight bid size/tight ask size: Basically, tight size is inversely proportional to tight width, to within normalized bounds.

Heuristics Control

1. Can Buy/Can Short: Can But/Can Short => whether the bid/ask stays within the LONGABLE/SHORTABLE cutoff.
2. ECN Threshold Cross: Check to see if there is a cross between the published bid/ask and a given ECN's bid/ask.

Published Market Quote Picture

1. Bid/Ask Sizes: Truncated to their appropriate rounding.
2. Bid Price: $\Pi_{Ideal} - \frac{1}{2}\omega_L\alpha_L$
3. Ask Price: $\Pi_{Ideal} + \frac{1}{2}\omega_L\alpha_L$
4. Bid/Ask Prices rounded downward/upward to their appropriate increments.