A Guide to the CDS Package

Heidi Chen, David Kane, Yang Lu, Kanishka Malik, and Skylar Smith June 24, 2014

1 Introduction

Over the past three decades, **credit derivatives** have become increasingly common tools for financial institutions that wish to pass on **credit risk** to investors who accept that risk for a premium, or fee. To put it simply, credit risk is the possibility that a borrower will default on his or her loan. In the modern financial world, there are many types of credit derivatives, including collaterized debt obligations (CDOs) and collaterized loan obligations (CLOs). In this vignette, we will focus on **credit default swaps** (CDSs), a type of credit derivative that has become quite popular among pensions funds, hedge funds, and investment banks, among other financial institutions (see Figure 1). We will explain the mechanics of this financial product and show how our **CDS** package can be used to manipulate and calcuate relevant information associated with CDSs.

Credit Default Swap Market Size

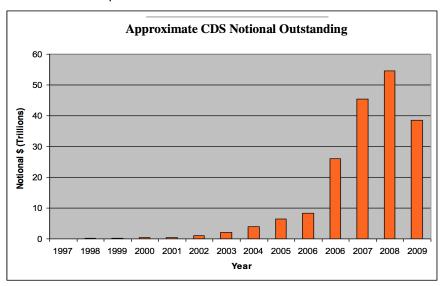


Figure 1: CDS notional outstanding from 1997-2009.

^{*}s.heidi.chen@gmail.com

[†]dave.kane@gmail.com

[‡]yang.lu2014@gmail.com

[§]kanishkamalik@gmail.com

[¶]sws2@williams.edu

CDSs originated in the late 1980s and were popularized by a team at J.P. Morgan that included Blythe Masters (Lenzner, 2009; Lanchester, 2009). The CDS market started to develop soon afterwards as banks used CDS contracts to hedge their credit exposures on balance sheets. Many different types of CDSs have since emerged including basket default swaps (BDSs), index CDSs, credit-linked notes, et cetera (Kallianiotis, 2013). In the CDS package, we focus on calculations related to single-name, or corporate, credit default swaps.

2 Credit Risk associated with Fixed Income

CDSs are used in order to hedge against the **credit risk** associated with **bonds or fixed income**. Before we understand CDSs work, we must understand the mechanics of a standard coupon bond, and the risk associated with them.

2.1 Bond Mechanics

Let's say that there is a manager of a pension fund who has to allocate her clients' money (a total sum of \$100 million). Pension funds are, for the most part, risk averse investors who want to minimize the possibility of making a loss, even if that results in a lower return on their investment. Pension funds also have to constantly return money to their clients so they want to purchase assets that pay a regular interest to the owner. They also want to invest in assets that are **liquid** i.e. whose sale does not affect their price. In such a scenario, coupon bonds seem like an attractive investment.

A **coupon bond** is an agreement in which one party lends money to another party in exchange for that same sum of money, plus interest, at a future date. Since the bonds pays a regular interest to the bondholder, it is also termed as **fixed income**. A major advantage of holding bonds over shares (equity) is that in the case of a liquidiation, a company's bondholders are compensated before the shareholders. Furthermore, bonds can be categorized as "senior" or "junior" (there exist many other classifications, but we'll stick to these two for now). As the terms suggest, senior bonds usually have the greatest seniority in the issuer's capital structure and in the case of default, are repaid before junior bonds.

2.2 Bond Pricing

To understand the different variables used in determining the cash flows and pricing of a bond, let's take data of an actual bond maturing five years from now, of a company called Alcoa Inc. This data is from a source called Bloomberg, one of the most widely used sources of financial data



Figure 2: Bloomberg Senior Bonds for Alcoa Inc., maturing on February 23, 2019

If we look at the top of Figure 2.2, we can see that these bonds have a **Coupon** of 5.72% and a **price** of \$112.063. The third number is the **spread**. When a company first issues bonds,

The key variables to note in order to understand the pricing of a bond are:

Principal: is the sum that will be returned to the investor when the bond reaches its maturity date. So if we own a bond of Alcoa Inc. for \$100 on the day it was issued, we will be paid a balloon payment of \$100 when it matures. This is, of course, in addition to the interest payments.

Coupon: payments made by the company to the bondholder. This is a fixed amount and is usually paid semi-annually.

Spread: the fair interest payment for owning the bond. Although the coupon is a fixed variable, this could vary based on different factors.

Maturity: length of the bond's life. This will tell us how many coupon payments must be made until the bonds maturity.

2.3 Credit Risk Associated with Bonds

When a company like Alcoa Inc. issues bonds, there is always the possibility that it may not be able to meet its debt obligations. The risk that a company will be unable to meet its debt obligations is known as **credit risk**. The creditworthiness of a company is often represented by the **credit rating**—a score determined by rating agencies such as Standard & Poor's (S&P), Moody's or Fitch. We will not go into the details of how these ratings are determined; we only note that an Investment Grade bond has a rating of BBB- or higher from S&P or Baa3 or higher from Moody's.

A risk-averse investor, like our portfolio manager, would naturally want to purchase senior bonds from a company that has a low credit risk, like Alcoa Inc., which has a rating of BBB- from S&P and Ba1 from Moody's. A company with a low credit risk, such as Alcoa Inc., is considered to be **credit** worthy and its bonds are classified as **Investment Grade** (IG).

3 CDS Basics

3.1 Why CDSs?

Let's assume that our portfolio manager buys \$10 millions dollars of senior Alcoa Inc. bonds maturing 5 years from now. Six months after the she makes this trade, her confidence in the creditworthiness of Alcoa Inc. begins to waiver. In other words, the manager is worried about some **credit event** related to the company. A credit event can signify the risk of a company's bankruptcy and resulting default, but the term can also expand to include failure to pay out debt within a certain amount of time, a credit downgrade or the confiscation of assets, among other events. Of course, she could simply sell the bonds; however, that may be premature or even unprofitable. Instead, she could textbfhedge her position by purchasing a financial product whose value rises with a drop in the bonds' value. In other words, she could take a position that allows her to *profit* from increased credit risk.

One convenitional technique of doing this is shorting bonds. Shorting is the process of borrowing and selling a security with the obligation to repurchase it in the future and return it to the lender. Clearly, this is profitable if the value of the security drops by the time it is repurchased in the future. However, there are several issues associated with this method. It is difficult to short bonds that are not **liquid**. The portfolio manager may not be able to find enough bonds that will mature at the same time. Moreover, she would have to spend \$100 million to hedge her entire portfolio of \$100 million, which is a substantial opportunity cost.

3.2 CDS Mechanics

CDSs were invented in order to resolve these issues associated with hedging against risk (as described in Section 3.1).

As shown in Figure 3.2, a CDS is an agreement between two **counterparties**, or opposing groups, in which the buyer (in this case, the portfolio manager) pays a **fixed periodic coupon** to the seller in exchange for protection against a credit event associated with the buyer's bond.



Figure 3: Cash flows in a single name CDS contract.

In our example, the portfolio manager is the **protection buyer**. Let's say that the **protection seller** is a hedge fund. The hedge fund sells protection to the portfolio manager for \$10 million of senior debt. This amount known as the **notional amount**. In return, she has to pay the hedge fund an annual coupon rate of over 1%, or 100 basis points, for a period of five years. These \$100,000 payments are made quarterly, so she would have to pay 0.25% every quarter until the maturity date.

In the case of default, the hedge fund would have to pay a compensation equal to the notional amount minus the company's recovery rate. The recovery rate is defined as the amount that the company is able to give back to its debt holders after default. When a company goes into bankruptcy and is forced to default on its debt, whatever remains in the company's assets is paid out according to the firm's capital structure. This transaction protects the portfolio from the bonds' associated credit risk without having to sell them. The hedge fund, on the other hand, receives a fee and walks away without any losses if there is no credit event.

Our example above can be described as a single-name CDS contract, in which the transfer of credit risk takes place between two parties. The protection buyer of a CDS contract transfers the credit risk to the CDS protection seller by paying a series of coupons until the contract terminates. In other words, the protection buyer is **short credit** by selling the credit risk of an underlying bond to the protection seller. Note that there is no involvement of the Alcoa Inc. in the transaction; this exchange only takes place between the two counterparties.

4 CDS Terminology and Cash Flows

Although the cash flows involved in a CDS seem pretty simple in figure 3.2, the underlying mechanics of a CDS are a bit more complex. To understand this, let's look at actual CDS data for Alcoa Inc., from Bloomberg. Bloomberg and Markit are the two most commonly used sources for CDS related data; we will discuss these extensively in a later section. Figure 4 below displays many different variables such as RED Pair Code, REF Entity, Trade Date, Debt Type etc. for the CDS of Alcoa Inc. for June 02, 2014. These are standard terms of CDS contracts that were set by the **International Swaps and Derivatives Association (ISDA)**, the organization that regulates over-the-counter derivatives such as CDSs. Let us understand what these variables are and how they are important for understanding the cash flow¹.

¹Some of the definitions come from *Credit Derivatives Glossary* (Markit, 2009), *Standard Corporate CDS Handbook* (Leeming et al., 2010), *Credit Derivatives* (Green and Witschen, 2012), and *The Pricing and Risk Management of Credit Default Swaps, with a Focus on the ISDA Model* (White, 2013).



Figure 4: CDS figures from Bloomberg for Alcoa Inc. Note that this **REF Obligation** (Reference Obligation) matches the ISIN in Figure 2.2

4.1 Entity-Specific Variables

Some of these variables seem self-explanatory. **REF Entity** (Reference Entity) refers to the name of the company (Alcoa Inc., in this case) that the buyer wants protection against. The **ticker** is an abbreviated reference symbol for the CDS. Moreover, the **Trade Date** is the date on which we are making the trade – June 02, 2014.

The **RED Pair Code** is a Markit product that stands for Reference Entity Database. Each entity/seniority pair has a unique six-digit RED code that matches the first six digits of the nine-digit RED pair code. Each entity also has a "preferred reference obligation," which is the default reference obligation for CDS trades. A user can input either the six-digit RED code or the nine-digit RED pair code. The input "014B98" is the six-digit RED code for "Alcoa Inc.".

We can also note the label **Debt type**, marked as 'Senior'. Clearly, this refers to the seniority of the debt. The **notional amount** is printed as '10' or \$10 million USD (US Dollars). The 'MM' between the amount and the currency refers to the type of restructuring of the contract—in this case, 'Modified Modified' Restructuring (explained further in Section 4.3). The **REF Obligation** (Reference Obligation) is the reference for the bond to which this CDS is tied. Since our portfolio manager is purchasing protection on the same bonds she purchased before, this **REF Obligation** (Reference Obligation) matches the ISIN in Figure 2.2.

Maturity refers to the **tenor**, or length, of the contract. The most commonly traded contracts have a maturity of five years. The Bloomberg screenshot displays the length of the contract, as well as the

implied maturity date. Interestingly, the maturity date for the CDS of Alcoa on June 02, 2014 is June 20, 2019. This seems odd since we would expect it to be on June 02, 2019, exactly five years from the Trade Date. However, the maturity date always falls on one of the four **roll dates**: March 20, June 20, September 20 and December 20. Therefore, the maturity date for this contract will be on the roll date after June 02, 2019, which is – June 20, 2019. Also note that this contract is of the type **SNAC** or Standard North American Contract, which is a convention that specifies how North American single-name CDSs are supposed to trade.

4.2 Cash flows in the Absence of a Credit Event

The two terms in Figure 4 that are essential for understanding the cash flow are **Trd Sprd** (Trade Spread) and **Coupon**, both given in basis points (bps). In section 3.2, we stated that the protection buyer pays the protection seller a fixed coupon for purchasing protection. Until 2009, the two counterparties in a CDS contract would agree on the coupon level before the trade. Then, as the market moved, this tradable coupon would vary. In this type of contract, the present value of the contract (the current worth of a future sum of money) would be zero. So if our portfolio manager was purchasing a CDS before 2009, she would have had to negotiate a fixed coupon with the hedge fund, which would then vary as the company's credit risk varied.

In April 2009 in North America, the ISDA introduced a series of mandatory modifications to the CDS contract known as the "Big Bang Protocol." Under the new rules, coupon rates were standardized in North America, and even in Europe from June 2009. Dealers would now have to quote **standard coupons** of 100bps or 500bps in North America, or 25bps, 100bps, 500bps or 1000bps in Europe. The coupon is also paid quarterly on one of the four roll dates. The **Coupon** printed in the figure above is the fixed coupon for Alcoa Inc., which is 100bp or 1% of the notional amount. However, the dealers may not feel that this is the fair premium for protection. For instance, the hedge fund selling protection to the portfolio manager may feel that the fair premium should be 160bps, and not 100bps. This fair premium rate is known as **Trade Spread** (or **Par Spread**, or just **Spread**), labeled as 160 in the figure above.

Naturally, if the hedge fund believes that the fair premium should be 160bps, it would like to be compensated for receiving just 100bps. As a result, the portfolio manager would have to make what is known as an **Upfront Payment** at the trade inception. Therefore, in the absence of a credit event, the cash flow between the two parties, over the life of the contract, would look like Figure 4.2.



Figure 5: CDS cash flows when there is no credit event.

The ISDA protocol, since April 2009, specifies that all premium payments, by default, start on the roll date before the Trade Date. So if the Trade Date is June 02, 2014, the **Accrual Begin Date** is, by default, March 20, 2014. Now if the Accrual Begin Date is 75 days before the Trade Date, the portfolio manager would not want to pay interest for the 75 days she has not received protection for.

We must note that we are dividing 75 by 360 instead of 365 in the above calculation. This is to do with the **Day Count Convention** (**Day Cnt** in Figure 4) of the contract, which specifies that the accrual factor between two dates is ACT/360 or Actual/360.

If we subtract the **Accrued Interest** over the past 75 days from the upfront payment, we get the **Dirty Upfront** or **Cash Settlement Amount**. With the information for Alcoa given in the Figure 4, the dirty upfront value for this contract is \$258478. **Clean Upfront**, on the other hand, is the dirty upfront less any accrued interest payment, and is also called the **Principal**. In this case, it is \$279311. Moreover, we can also note a variable called **Pts Upf** in Figure 4. This is the **Points Upfront**, or simply **points**, which is the Clean Upfront experessed as a percentage of the notional amount.

As we can see, the Upfront and Points Upfront values are positive in this case, since the Spread of the CDS is higher than the fixed Coupon rate. If instead, the portfolio manager and hedge fund agree that the fair premium should be 60 points, the Upfront value would be negative i.e. the hedge fund would pay the portfolio manager a compensation for receiving a Coupon higher than the fair premium or spread. The cash flows would then look like the values in Figure 4.2. The clean and dirty value are now both negative.

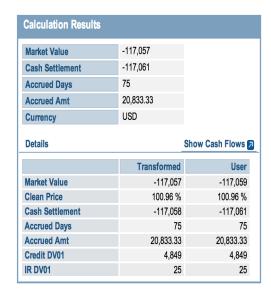


Figure 6: CDS cash flows for Alcoa Inc. when Spread is 60bp and and Coupon is 100bp. These have been calculated using the calculator provided by Markit at http://www.markit.com/markit.jsp?jsppage=pv.jsp

4.3 Cash Flows when a Credit Event does Occur

So far we have only discussed the stream of payments for a contract in which a credit event does not occur If, however, there is a credit event, the cash flow would look like Figure 4.3.

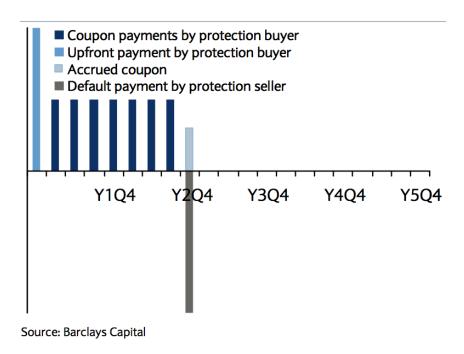


Figure 7: CDS cash flows when there is a credit event.

5 CDS Pricing

In this section we will discuss the methods and formulas used for calculating certain information related to CDSs, and the assumptions involved in doing so.

6 CDS Indices

Holding a portfolio of a disproportionate number of Alcoa Inc. bonds is naturally a risky idea. It is akin to putting all your eggs in one basket, as the saying goes. In the real world, most successful portfolio managers prefer to distribute their risk by holding a portfolio with hundreds, if not thousands, of different positions. Instead of holding a 100 million USD of Alcoa Inc. bonds, let's say our portfolio manager decides to take less risk by holding bonds of 100 different Investment Grade companies. This is known as **diversification**. Although this strategy reduces her exposure to the credit risk of any particular company, she hasn't reduced her exposure to factors that might affect a wide variety of assets simulatenously, such as interest rate risk or political risk. Fortunately, in the modern financial world, she has the option of purchasing multi-name CDSs, or CDS indices, which contain a basket of CDSs.

Moreover, if our portfolio manager has a high-risk appetite and wants to earn a higher return for her investors, she may invest a portion of her portfolio in bonds that have a lower credit rating but provide a higher yield. She may consider investing in a tranche of CDS indices known as CDX.NA.HY.

7 Pricing Sources

Bloomberg and Markit are the most widely used sources for data related to pricing of CDSs. We compared the results from our package with results from Bloomberg and Markit. Interestingly, the results from Markit and Bloomberg were not always identical.

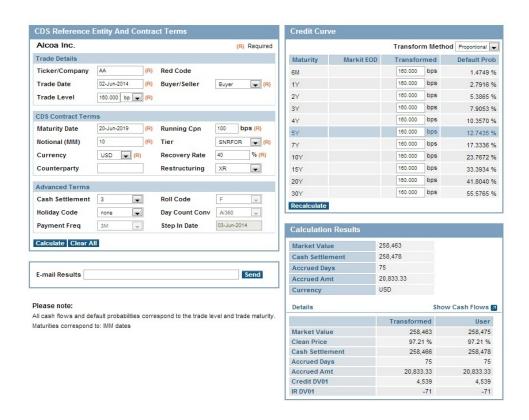


Figure 8: CDS figures from Markit.com



Figure 9: CDS figures from Bloomberg

The interest rate results were identical, at least until the fourth decimal place.

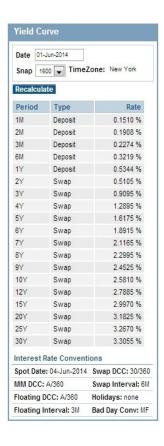


Figure 10: Interest Rate figures from Markit.com



Figure 11: Interest Rate figures from Bloomberg

8 Glossary of CDS terminology

Here is a glossary of CDS terminology necessary for determining the pricing and cash flows associated with CDSs²:

²Some of the definitions come from *Credit Derivatives Glossary* (Markit, 2009), *Standard Corporate CDS Handbook* (Leeming et al., 2010), *Credit Derivatives* (Green and Witschen, 2012), and *The Pricing and Risk Management of Credit Default Swaps, with a Focus on*

Reference Entity refers to the legal entity that is the subject of a CDS contract (Alcoa Inc., in our example).

RED is a Markit product that stands for Reference Entity Database. Each entity/seniority pair has a unique six-digit RED code that matches the first six digits of the nine-digit RED pair code. Each entity also has a "preferred reference obligation," which is the default reference obligation for CDS trades. A user can input either the six-digit RED code or the nine-digit RED pair code. The input "014B98" is the six-digit RED code for "Alcoa Inc.".

Trade Date indicates the trade date of the CDS contract, as shown in the argument of the CDS function. In our exmaple, the trade date is June 02, 2014 in cds1.

Maturity refers to the fixed date on which a CDS contract terminates. However, colloquially speaking, it can also represent the length of time remaining until that date. This length is also called the **tenor** of a CDS contract. The most commonly traded CDSs have maturities of five years. The protection buyer continues to make payments to the protection seller until the maturity of the contract or the occurrence of a credit event. The maturity is five years in cds1.

Notional is the amount of the underlying asset on which the payments are based. It is \$10 million in cds1.

Coupon is quoted in basis points (bps). It specifies the payment amount from the protection buyer to the seller on an annual basis. Coupons are paid quarterly. This contract has a coupon of 100 bps.

Spread is quoted in basis points per year. If, instead of using a fixed coupon and exchanging upfront fees, the buyer and seller of protection were to agree on a variable coupon, then the spread would be the coupon size that they agree on. It is quoted as 50 bps in cds1.

An ISDA standard CDS contract specifies the following:³

Trade Date refers to the date of the trade.

Maturity is the length of the contract. The most commonly traded contracts have a maturity of 5 years.

Maturity Date falls on one of the four dates (Mar/Jun/Sep/Dec 20th) in a year. One can add the maturity of the contract to the trade date; the next available date among those four dates is the maturity date.

Backstop Date is the date from which protection is provided,

Backstop Date = T - 60 Calender Days.

Notional Amount is in millions.

Standard Coupon is either 100 or 500 bps per year for CDS contracts in North America.

the ISDA Model (White, 2013).

³Refer to the ISDA Standard CDS Converter Specification for details.

Recovery Rate is the estimated percentage of par value that bondholders will receive after a credit event. It is commonly reported in percentage of notional value. CDS contracts for corporate bonds assume a 40% recovery rate for valuation purposes.

Par Spread is the spread value which makes the present value of a CDS contract zero. It is quoted in basis points.

Upfront Payment is quoted in the currency amount. Since a standard contract is traded with fixed coupons, upfront payment is introduced to reconcile the difference in contract value due to the difference between the fixed coupon and the par spread. There are two types of upfront, dirty and clean. Dirty upfront (**Cash Settlement Amount**) refers to the market value of a CDS contract. Clean upfront is dirty upfront less any accrued interest payment, and is also called the **Principal**.

Points Upfront, or simply **points**, are quoted as a percentage of the notional amount. They represent the upfront payment excluding the accrual payment. High yield CDS contracts are often quoted in points upfront. The protection buyer pays the upfront payment if points upfront are positive, and the buyer is paid by the seller if the points are negative.

The Standard Model allows market participants to convert between the par spread and the upfront payment, and compute the cash settlement amount for a standard contract. A few key assumptions and definitions used when valuing a Standard CDS contract are the following:⁴

Trade Date (T) means 11:59pm on the trade date.

Days of Protection is the number of days from Maturity Date to Trade Date.

Mark-to-market (MTM) represents the contract value to the protection buyer. It is computed by discounting the expected protection leg and premium leg cashflows to T.

Accrued Premium is the premium that has accrued from accrual begin date to T where both dates are inclusive.

The ISDA also standardizes the interest rates used by the Standard Model in valuing a CDS contract. There are two types of rates used in valuing a USD denominated CDS contract: cash rates and swap rates. Cash rates are of the following maturities: one, two, three, and six month(s), and one year. They are provided by the British Bankers' Association (BBA). Swap rates are of maturity 2, 3, 4, 5, 6, 7, 8, 9, 10, 12, 15, 20, 25, and 30 years, and are provided by ICAP (Markit, 2013). The Standard Model follows the conventions below for interpolation of the entire USD yield curve:

- The day count convention (DCC) for money market instruments and floating legs of the swaps is ACT/360.
- DCC for floating legs of the swaps is 30/360.
- Payment frequency for fixed legs of the swaps is 6 months.

⁴Please refer to http://bit.ly/1kg5qPw for more infrmation on the ISDA standard CDS model assumptions.

- Payment frequency for floating legs of the swaps is 3 months.⁵
- A business day calendar of weekdays (Monday to Friday) is assumed. Saturdays and Sundays will be the only non-business days.
- If a date falls on a non-business day, the convention used for adjusting coupon payment dates is
 M (Modified Following).

Besides parSpread, a market paricipant can choose to specify either ptsUpfront or upfront to construct a CDS class object.⁶ ptsUpfront or upfront refer to points upfront (in %), and upfront payment (in dollar amount) of a CDS contract, respectively. One of the three arguments has to be specified in order to construct the CDS class object.

9 Using the CDS package

The International Swaps and Derivatives Association (ISDA) has created a set of standard terms for CDS contracts, the so-called "Standard Model." This allows market participants to calculate cash settlement from conventional spread quotations, convert between conventional spread and upfront payments, and build the spread curve of a CDS. The CDS package implements the Standard Model, allowing users to value credit default swaps and calculate various risk measures associated with these instruments.

In the **CDS** package, we call the function CDS to construct an object of a class CDS. Below we show an example of how to construct a CDS contract in the package.

Here the user enters the CDS contract with "Alcoa Inc." as the underlying entity and sets the spread at 50 bps and the coupon at 100 bps. However, the valuation of a CDS contract requires neither the Reference Entity or the RED Code. She does not have to know that information to use the **CDS** package. As shown below, as long as she inputs the same Trade Date, parSpread, and maturity information, the valuation of the contract will be the same.

Currently, a market participant can conduct CDS-related calculations by using the **CDSW Calculator** on a Bloomberg Terminal or the Markit CDS Calculator.⁷ The **CDS** package provides tools for

⁵See http://www.fincad.com/derivatives-resources/wiki/swap-pricing.aspx for details on floating and fixed legs calculation.

⁶See Section ?? for definitions on both terms.

⁷The Markit CDS Calculator is available at http://www.markit.com/markit.jsp?jsppage=pv.jsp.

valuing a single-name CDS contract. The default setting allows a user to value a USD-denominated CDS contract following the Standard Model as mentioned in Section ??. She can also specify her own set of parameters to customize the calculation. We have illustrated the construction of a CDS contract using the CDS package in previous sections. In this section, we will demonstrate the use of the CDS package in more detail and provide a series of examples.

Recall that in Section 'Using the CDS package', a CDS class object called cds1 has been constructed. Its maturity is five years. Its spread is set at 50 bps and its coupon at 100 bps. The notional amount is \$10 million. A user can call summary on a cds1 to view essential information on the contract.

> summary(cds1)

Contract Type:	SNAC	TDate:	2014-04-15
Entity Name:	Alcoa Inc.	RED:	49EB20
Currency:	USD	End Date:	2019-06-20
Spread:	50	Coupon:	100
Upfront:	-256,577	Spread DV01:	5,086
IR DV01:	66.14	Rec Risk (1 pct):	90.03

In the summary output, it shows that the type of the CDS contract is "SNAC". Trade Date refers to the trade date and is April 15, 2014. Reference Entity (called entityName in the package) refers to the entity name of the CDS contract and is "Alcoa Inc.". The RED code is "48EB20" as specified by the user. spread shows that the quoted spread for the contract is 50 bps and the coupon is 100 bps as shown in the coupon field. upfront indicates the dirty upfront payment in dollars or the cash settlement amount. It is -256,577 dollars, which means that from a buyer's perspective, the net present value of the remaining expected cashflows is -\$256,577.

To understand the remaining three items from the summary output (Spread DV01, IR DV01, and Rec Risk (1 pct)), one needs to understand **PV01**, an essential component to the mark-to-market calculation of a CDS contract. PV01 is the present value of a stream of 1 basis point payments at each CDS coupon date. It is sometimes referred to as the **CDS duration** or **risky duration**.

Analytically, PV01 can be calculated by

$$PV01 = \sum_{t} Df(t_i)S(t_i)B(t_i),$$

where

- i = coupon index,
- $t_i = \text{coupon date}$,
- $Df(f_i)$ = discount factor until t_i ,
- $S(t_i) = \text{survival probability until } t_i$,
- $B(t_i) = \text{day count fraction at } t_i$.

We can thus calculate the principal amount (clean upfront payment) paid from the protection buyer to the seller using the following formula:

Principal Amount = (Par Spread - Coupon) \times PV01.

Using the concept of PV01, we show the calculation of the main risks (exposures) of a CDS position, **Spread DV01**. Spread DV01 reflects the risk duration of a CDS trade, also known as **Sprd DV01**, **Credit DV01**, **Spread Delta**, and just **DV01**.

It measures the sensitivity of a CDS contract mark-to-market to a parallel shift in the term structure of the par spread. DV01 should always be positive for a protection buyer since he or she is short credit, and a rising spread is a sign of credit deterioration. Starting with PV01 and taking the derivative with respect to the spread gives us:

$$PV\& = \&(S-C)*PV01$$

$$DV01\& = \&\frac{\partial PV}{\partial S}$$

$$\& = \&PV01 + (S-C)\frac{\partial PV01}{\partial S},$$

where *S* is the spread of the contract and *C* is the coupon.

Both DV01 and PV01 are measured in dollars and are equal if the spread equals the coupon. The Spread DV01 of cds1 is \$5,086.

IR DV01 is the change in value of a CDS contract for a 1 bp parallel increase in the interest rate curve. IR DV01 is, typically, a much smaller dollar value than Spread DV01 because moves in overall interest rates have a much smaller effect on the value of a CDS contract than does a move in the CDS spread itself. In cds1, the IR DV01 is \$66.14. Recovery Risk 01 or Rec Risk (1 pct) as shown in the summary output, is the dollar value change in market value if the recovery rate used in the CDS valuation were increased by 1%. It is \$90.03 in cds1.

The default settings of valuing a CDS contract in the **CDS** package follow the Standard North American Corporate (SNAC) CDS Contract specifications.⁸ Below we list the ISDA specifications implemented in the **CDS** package. Additional default settings in the package which are not specified by the Standard Model, such as the default notional amount, are also listed.

- Currency: USD.
- Trade Date (T): the current business day.
- CDS Date: Mar/Jun/Sep/Dec 20th of a year.
- Maturity: five years.
- Maturity Date (End Date): It falls on a CDS date without adjustment.
- Coupon Rate: 100 bps.
- Notional Amount (MM): 10MM.
- Recovery Rate (%): 40% for senior debts.

⁸See http://www.cdsmodel.com/assets/cds-model/docs/Standard%20CDS%20Contract%20Specification.pdf for details.

• Premium Leg:

- Payment Frequency: quarterly
- DCC: ACT/360
- Pay Accrued On Default: It determines whether accrued interest is paid on a default. If a company defaults between payment dates, there is a certain amount of accrued payment that is owed to the protection seller. "True" means that this accrued will need to be paid by the protection buyer, "False" otherwise. The defalt is "True,"
- Adjusted CDS Dates: "F." It means that it assumes the next available business day when a CDS date falls on a non-business day except the maturity date.
- First Coupon Payment: It is the earliest Adjusted CDS Date after T + 1.
- Accrual Begin Date (Start Date): It is the latest Adjusted CDS Date on or before T + 1.
- Accrual Period: It is from previous accrual date (inclusive) to the next accrual date (exclusive), except for the last accrual period where the accrual end date (Maturity Date) is included.

• Protection Leg:

- Protection Effective Date (Backdrop Date): T 60 calendar days for credit events.
- Protection Maturity Date: Maturity Date.
- Protection Payoff: Par minus Recovery.

9.1 More on CDS pricing

CS10 is a method which calculates the change in value of the CDS contract when the spread of the contract increases by 10%. CS10 takes in a CDS class object formed by calling the CDS function. The CS10 of cds1 is \$25385.2.

```
> cds1.CS10 <- CS10(cds1)
> cds1.CS10
[1] 25385.2
```

A market participant can also update the CDS class objects she has constructed by calling the update method. It updates a CDS class object with a new spread and points upfront by specifiying the relevant input.

```
> cds3 <- update(cds1, spread = 55)
```

cds3 is a new CDS class object with a spread of 55 bps; all other specifications of the contract are the same as those in cds1 since it is updated from cds1. One can also specify upfront (in dollar amount) or ptsUpfront (in bps) in the update method.

Besides calling the summary method, one can type in the name of the CDS class object in the current R Session and obtain a full description of the CDS contract.

> cds3

CDS Contract

Contract Type:	SNAC	Currency:	USD
Entity Name:	Alcoa Inc.	RED:	49EB20
TDate:	2014-04-15	End Date:	2019-06-20
Start Date:	2014-03-20	Backstop Date:	2014-02-14
1st Coupon:	2014-06-20	Pen Coupon:	2019-03-20
Day Cnt:	ACT/360	Freq:	Q
Calculation			
Value Date:	2014-04-18	Price:	102.24
Spread:	55	Pts Upfront:	-0.0224
Principal:	-223,692	Spread DV01:	5,064
Accrual:	-7,500	IR DV01:	59.35
Upfront:	-231,192	Rec Risk (1 pct):	88.87
Default Prob:	0.047	Default Expo:	6,223,692

Credit curve effective of 2014-04-15

Term	Rate	Term	Rate	
1M	0.001517	7Y	0.022630	
2M	0.001923	84	0.024580	
ЗМ	0.002287	9Y	0.026265	
6M	0.003227	10Y	0.027590	
1Y	0.005465	12Y	0.029715	
2Y	0.005105	15Y	0.031820	
ЗҮ	0.009265	20Y	0.033635	
4 Y	0.013470	25Y	0.034420	
5Y	0.017150	30Y	0.034780	
6Y	0.020160			

There are three parts of the output. The first part "CDS Contract" provides basic information on the contract including "Contract Type", "Currency", "Reference Name" (called Entity Name in the package), "RED", "Trade Date", various dates related to the contract, and the day count conventions for cds3.

The second part of the output contains relevant risks measures of cds3. Price refers to the clean dollar price of the contract and is calculated by

$$\label{eq:price} \begin{split} \text{Price\&} &= (1 - \text{Principal/Notional})*100 \\ &\&= 100 - \text{Points Upfront.} \end{split}$$

The price of cds3 is 102.24, greater than 100. A CDS will have a price greater than 100 if the points upfront are negative; that is, the CDS buyer needs to receive money to obtain protection because he promises to pay a coupon of, say, 100 even if the spread is 60. This is analogous to a bond investor paying more than the face value of a bond because current interest rates are lower than the coupon rate on the bond.

"Default Prob" refers to the default probability which is the estimated probability of default for each maturity by a given time. It can be approximated by

Default Prob
$$\approx \left[1 - exp\left(\frac{rt}{1 - R}\right)\right]$$
,

where r is the spread, t is the time to maturity, and R is the recovery rate. The default probability for cds3 is 4.7%.

"Default Expo" refers to the expoure to the default of a CDS contract based on the formula below.

```
Default Exposure = (1 - Recovery Rate) * Notional - Principal.
```

The last part of the output reports the interest rates used in the calculation.

Calling the function getRates also produces the rates used in building a curve for CDS valuation.

```
> cds3Rates <- getRates(date = "2014-04-15")</pre>
```

The output consists of two list objects. The first list contains rates of various maturities. They are directly obtained from the Markit website based on the specifications (Markit, 2013).

```
expiry matureDate
1
       1M 2014-05-19 0.001517
                                 М
2
       2M 2014-06-17 0.001923
                                 М
3
       3M 2014-07-17 0.002287
                                 М
       6M 2014-10-17 0.003227
                                 М
       1Y 2015-04-17 0.005465
6
       2Y 2016-04-17 0.005105
7
       3Y 2017-04-17 0.009265
                                 S
8
       4Y 2018-04-17 0.01347
                                 S
9
       5Y 2019-04-17 0.01715
                                 S
10
       6Y 2020-04-17 0.02016
                                 S
11
       7Y 2021-04-17 0.02263
                                 S
       8Y 2022-04-17 0.02458
                                 S
13
       9Y 2023-04-17 0.026265
                                 S
14
      10Y 2024-04-17 0.02759
                                 S
15
      12Y 2026-04-17 0.029715
                                 S
      15Y 2029-04-17 0.03182
16
                                 S
17
     20Y 2034-04-17 0.033635
                                 S
      25Y 2039-04-17 0.03442
18
                                 S
19
      30Y 2044-04-17 0.03478
```

The second list reports the specific day count conventions and payment frequencies regarding the interest rate curve used.

```
text
effectiveDate "2014-04-15"
badDayConvention "M"
```

mmDCC "ACT/360"

mmCalendars "none"

fixedDCC "30/360"

floatDCC "ACT/360"

fixedFreq "6M"

floatFreq "3M"

swapCalendars "none"

10 Conclusion

In this paper, we describe the basics of a CDS contract and the ISDA Standard Model. We also provide a simple collection of tools to implement the Standard Model in **R** with the CDS package. Moreover, the flexibility of **R** itself allows users to extend and modify this package to suit their own needs and/or create their preferred models for valuing CDS contracts. An **R** package, backtest Campbell et al. (2007), provides facilities to explore portfolio-based conjectures about credit default swaps. It is possible to use the backtest package based on the output from the CDS package. Before reaching that level of complexity, however, CDS provides a good starting point for valuing credit default swaps.

References

- K. Campbell, J. Enos, D. Gerlanc, and D. Kane. Backtests. *R News*, 7(1):36–41, April 2007. URL http://cran.r-project.org/doc/Rnews/Rnews_2007-1.pdf.
- S. Green and E. Witschen. Credit Derivatives. Bloomberg, January 2012.
- J. Kallianiotis. *Exchange Rates and International Financial Economics: History, Theories, and Practices*. Palgrave Macmillan, Oct. 2013.
- J. Lanchester. Outsmarted. The New Yorker, June 2009.
- M. Leeming, S. Willemann, A. Ghosh, and R. Hagemans. Standard Corporate CDS Handbook, Ongoing Evolution of the CDS Market. *Barclays Capital*, February 2010.
- R. Lenzner. Who's Afraid Of Credit Default Swaps? Forbes, March 2009.
- Markit. Credit Derivatives Glossary. Markit, March 2009.
- Markit. Markit Interest Rate Curve XML Specifications Version 1.15. Markit, May 2013.
- R. White. The Pricing and Risk Management of Credit Default Swaps, with a Focus on the ISDA Model. *OpenGamma*, October 2013.