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### Chapter 1

# The *oligopoly* project: the making of the simulation model

The model is published in Mazzoli et al. (2017). To obtain a perfectly replicate othe results reported there, please use the code version at

https://github.com/terna/oligopoly/releases/tag/V5 or at https://github.com/terna/oligopoly/releases/tag/V5bP2\_fd¹or download the zip file of

https://github.com/terna/oligopoly/tree/masterP2, running the project with SLAPP 2.0<sup>2</sup> and controlling that the parameters are those of Table 1 of Mazzoli *et al.* (2017).

Using SLAPP<sup>3</sup>, the oligopoly project is contained in a stand alone folder, having the same name of the model.

Let us introduce the starting phase in a detailed way.

- We can launch the SLAPP shell in several ways.
  - We can launch SLAPP via the runShell.py file that we find in the main folder of SLAPP, from a terminal, with:

<sup>&</sup>lt;sup>1</sup>The same of V5, underlining the use of Python 2 and adding the output of the data of each firm in each cycle; \_fd as firm data.

<sup>&</sup>lt;sup>2</sup>https://github.com/terna/SLAPP2.

<sup>&</sup>lt;sup>3</sup>https://github.com/terna/SLAPP; SLAPP has a Reference Handbook at the same address and it is deeply described in Chapters 2–7 in Boero *et al.* (2015).

Run oligopoly with the Python 3 version of SLAPP.

From its build 20170611 the oligopoly project, version 5bPy3, adopts the PEP8 style. PEP8 contains the Style Guide for Python Code and it is at https://www.python.org/dev/peps/pep-0008/.

Due to this adoption, the reader can notice some aesthetic differences between the code reported here and that listed into the files.

python runShell.py

- Alternatively, we launch SLAPP via the start.py file that we find in the folder of SLAPP as a simulation shell, i.e.
   6 objectSwarmObserverAgents\_AESOP\_turtleLib\_NetworkX, from a terminal, with:
   python start.py
- Using IPython (e.g., in a Jupyter notebook) we go to the main folder of SLAPP (or we start Jupyter notebook) form there, and we can launch SLAPP via the iRunShell.ipynb file that we find in that main folder, simply clicking on it.

In all cases, we immediately receive the request of choosing a project: Project name?

• We can predefining a default project: if we place in the main SLAPP folder or in the folder 6 objectSwarmObserverAgents\_AESOP\_turtleLib\_NetworkX a file named project.txt containing the path to the folder of the project we are working on (oligopoly in our case, with /Users/pt/GitHub/oligopoly, as an example of location), the initial message of SLAPP is:

```
path and project = /Users/pt/GitHub/oligopoly
do you confirm? ([y]/n):
```

• Resuming the explanation, we continue receiving the messages:

```
running in Python
debug = False
random number seed (1 to get it from the clock)
```

We have to enter an integer number (positive or negative) to trigger the sequence of the random numbers used internally by the simulation code. If we reply 1, the seed—used to start the generation of the random series—comes from the internal value of the clock at that instant of time. So it is different anytime we start a simulation run. This reply is useful to replicate the simulated experiments with different conditions. If we chose a number different from 1, the random sequence would be repeated anytime we will use that seed. This second solution is useful while debugging, when we need to repeat exactly the sequence generating errors, but also to give to the user the possibility of replicating exactly an experiment.

The running in Python sentence signals the we are running the program in plain Python. Alternatively, the message could be running in IPython. About running SLAPP in IPython have a look the Handbook, in the SLAPP web site.<sup>4</sup>

• The program sends several messages about the project parameters, as specified into the file commonVar.py and managed via the file parameters.py, both in the project folder.

One of these messages reports the version of the project.

- The program informs us about the «sigma of the normal distribution used in randomizing the position of the agents/nodes», e.g., 0.7; this value produces uniquely a graphic effect, as in Figure 1.3.
- We introduce now time management, split into several (consistent) levels of scheduling.

The general picture is that of Figure 1.1: in an abstract way we can imagine having a clock opening a series of containers or boxes. Behind the boxes, we have the *action groups*, where we store the information about the actions to be done.<sup>5</sup>

#### 1.1 The agents and their sets

We have files containing the agents of the different types. Those files are listed in a file with name agTypeFile.txt: in our case, it simply contains the record entrepreneurs workers.

• entrepreneurs.txt lists the agents of type entrepreneurs; it reports the identification numbers (currently from 1 to 10) and the x and y positions on the screen. See above the sigma value determining random shift from the stated positions; in this way, we can attribute close or equal positions to several entrepreneurs having them anyway visible in the map; if necessary, we can increase sigma:

```
1 -10 75
2 -10 65
```

<sup>&</sup>lt;sup>4</sup>https://github.com/terna/SLAPP.

<sup>&</sup>lt;sup>5</sup>The structure is highly dynamical because we can associate a probability to an event, or an agent of the simulation can be programmed to add or eliminate one or more events into the boxes.

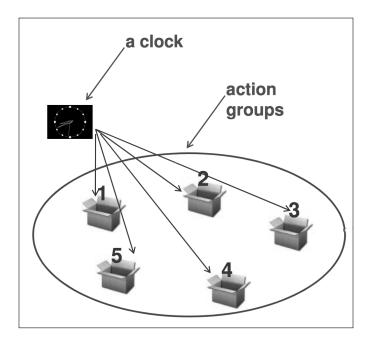


Figure 1.1: The representation of the schedule

- 3 -10 55
- 4 -10 45
- 5 -10 35
- 6 -10 70
- 7 -10 60
- 8 -10 50
- 9 -10 40
- 10 -10 30
- inVersions 0 to 2, "workers.txt" list the agents of type workers, not used here; it is reporting the identification numbers and the x and y positions on the screen; see above the sigma value determining random shift from the stated positions; in this way, we can attribute close or equal positions to several entrepreneurs having them anyway visible in the map; if necessary, we can increase sigma;
- the Version 3 of the oligopoly project uses the file workers.txtx where the extension .txtx or eXtended text, means that the file si built following the rule described into the Reference Handbook<sup>6</sup>, subsection "The use of files .txtx to define the agents".

<sup>&</sup>lt;sup>6</sup>https://github.com/terna/SLAPP.

In version 3 the content is:

```
1001@11000 10 &v=10*int((n-1001)/50)+5&
```

that we read in the following way:

- 1001@11000 as the order of creating 10 thousand workers, from number 1001 to number 11,000;
- 10 is the constant value of the x coordinate of the worker-agents;
- &v=10\*int((n-1001)/50)+5& is a formula calculating the y coordinate of each agent:
  - & opens and closes the formula;
  - $\mathbf{v}$  is the result of the calculation, in our case the y coordinate;
  - **n** is the number of the agent, in the sequence generated in the interval from 1001 to 11,000.
- numbering starts from 1001 for the reasons explained at page 39.

The agents are created by ModelSwarm.py (in folder \$\$slapp\$\$) via the specific rules contained into the file mActions.py, specific for this project (indeed, the file is into the folder oligopoly).

```
def createTheAgent(self,line,num,leftX,rightX,bottomY,topY,agType):
                \ensuremath{\text{\#}} explicitly pass self, here we use a function
                 # workers
                 if agType=="workers":
                 anAgent = Agent(num, self.worldStateList[0],
                                      float(line.split()[1])+random.gauss(0,common.sigma),
                                      float(line.split()[2])+random.gauss(0,common.sigma),
                                      agType=agType)
                 self.agentList.append(anAgent)
                 anAgent.setAgentList(self.agentList)
                 # entrepreneurs
                 elif agType=="entrepreneurs":
                 anAgent = Agent(num, self.worldStateList[0],
                                  float(line.split()[1])+random.gauss(0,common.sigma),
                                  float(line.split()[2])+random.gauss(0,common.sigma),
                                  agType=agType)
                 self.agentList.append(anAgent)
                else:
                 print "Error in file "+agType+".txt"
                 os.sys.exit(1)
```

The following bullets describe how this code works.

- The number identifying the agent is read outside this function, as a mandatory first element in each line into a file containing agent descriptions. The content of the agType variable is directly the name of the agent file currently open.
- We check the input file, which has to contain three data per row. We modify the second and the third values with the *sigma* correction.

Each agent is added to the agentList.

#### 1.1.1 Agents and reset action

The reset (see page 15) action, working into the scheduling of the model (Section 1.2.2), activates the method setNewCycleValues defined, as an empty step, in the class SuperAgent in agTools of SLAPP (folder \$\$slapp\$\$). In the oligopoly project, that method is redefined in Agent.py. The reset action acts once in each simulation cycle, because in our case is related only to common variables of the simulation. The agent executing the cleaning operation is that with the identifier (the variable number) equal to 1. If no agent has that identifier, all will be acting, with not useful repetitions of the same task.

As a consequence, in this project pay attention that at least one of the agents has 1 as identifier.

An important application of the **reset** function is in Section 1.3.3.1 and specifically at p. 23.

#### 1.1.2 Sets of agents

The files containing the agents are of two families, the second one with two types of files:

- files listing the agents with their characteristics (if any): in folder oligopoly we have the files entrepreneurs.txt and workers.txt;
- files defining groups of agents:
  - the list of the types of agents (mandatory); from this list SLAPP searches the file describing the agents; as seen, in folder oligopoly we have the file agTypeFile.txt (the name of this file is mandatory) containing:

entrepreneurs workers

 the list of the operating sets of agents (optional); in folder oligopoly this file is missing. Indeed we receive the message

Warning: operating sets not found.

In the file agOperatingSets.txt (the name of this file is mandatory), with could place names of groups of agents, corresponding to files listing the agents in the group. Project verb"school" can be used as a useful example.

All the names contained in the file are related to other .txt or .txtx files reporting the identifiers of agents specified in the lists of the previous bullet. The goal of this feature is that of managing clusters of agents, recalling them as names in Col. A in schedule.xls file.

#### 1.2 Macro scheduling

In SLAPP, we have the following three schedule mechanisms driving the events.

- Two of those mechanisms are operating in a *macro* way: one at the level of the Observer and the other of the Model, with recurrent sequences of actions to be done.<sup>7</sup>
- In our oligopoly code, these two sequences are reported in the files observerActions.txt and modelActions.txt in the folder of the project.

The explanations are in Section 1.2.1 and 1.2.2.

• The third sequence, operating in a *micro* way, is the more detailed one (see Section 1.2.3).

#### 1.2.1 The scheduling mechanism at the level of the Observer

- The first schedule mechanism is described in the first file (observerActions.txt), having content (unique row, remembering that anyway row changes are not relevant to this group of files):
  - version without pauses contained in observerActions no pause.txt, to be copied to observerActions.txt to run it:

<sup>&</sup>lt;sup>7</sup>The level of the Observer is our level, where the experimenter looks at the model (the level of the Model) while it runs.

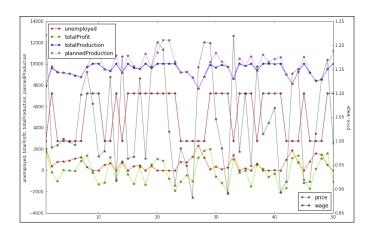


Figure 1.2: Time series generated by the model. version 4

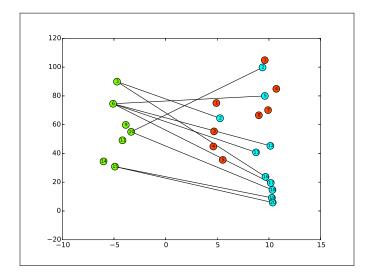


Figure 1.3: The agents (nodes), with random displacements, and links connecting entrepreneurs and workers  $\frac{1}{2}$ 

collectStructuralData modelStep collectTimeSeries
visualizePlot visualizeNet clock

- version with pauses contained in observerActions with pause.txt, to be copied to observerActions.txt to run it:

collectStructuralData modelStep collectTimeSeries
visualizePlot visualizeNet pause clock

#### The interpretation is the following.

- First of all, we have to take into consideration that the execution of the content of the file is "with repetition", until an end item will appear (see below).
- collectStructuralData collects the number of workers and of entrepreneurs at the beginning of each period, both as a basis for internal calculations and for the final output of the model, when two files of data are generated.
- modelStep orders to the model to make a step forward in time.
- collectTimeSeries collects the data of the outcomes of the simulation at the end of each period, both as a basis for the action of visualizePlot and for the final output of the model, when two files of data are generated (with extension .csv and date and time<sup>9</sup> in their names).<sup>8</sup>
- visualizePlot update the plot of the time series generated by the model (Figure 1.2).<sup>10</sup>
- visualizeNet update the windows reporting the links connecting entrepreneurs and workers, on a network basis (Figure 1.3).
- pause, if any, puts the program in wait until we reply to the message Hit enter key to continue, hitting the key . This action is useful to examine the graphical outputs (as in Figures 1.2 and 1.3), step by step.
- clock asks the clock to increase its counter of one unit. When the count will reach the value we have entered replying to the How many cycles? query, the internal scheduler of the Observer will add the end item into the sequence of the file observerActions.txt. The item is placed

<sup>&</sup>lt;sup>8</sup> collect Time Series, visualize Plot and save Time Series are contained in "oActions.py" and are all using pandas as dataframe manager (look at http://pandas.pydata.org).

<sup>&</sup>lt;sup>9</sup>Avoiding: into the name, for compatibility reasons with Windows

 $<sup>^{10}</sup>$ We can use both visualizePlot and visualizeNet—strictly in this order—or only one of them.

immediately after the clock call. The end item stops the sequence contained in the file.

- (We can also consider a potential prune item, eliminating the links on the basis of their weight (in case, asking for a threshold below which we cut); weights could be introduced to measure the seniority—skill, experience—of the workers).

# 1.2.1.1 The scheduling mechanism at the level of the Observer: using the *special action* feature to modify the parameters while the model is running

.

We use here the *special action* feature of SLAPP, described in the related Reference Manual (use the Index to find it). In this specific application that feature, we implement the following definition in commonVar.py:

```
specialAction = "makeSpecialAction()"
```

with, always in this specific case,

#### file\_modPars=False

As a consequence, the specialAction item in observerActions.txt activates the function makeSpecialAction() in oActions.py.

If a file modPars.txt exists, the program asks us in which cycles the modified parameters will be used.

Within the file modPars.txt we specify the internal names of the Python variables used as parameters in the model, look for them in parameters.py; an example of use is in specialAction where the name of the variable is followed by its new value.

observerActions with specialAction.txt contains the specialAction item; to use that file, you have to rename or copy it as observerActions.txt.

#### 1.2.2 The scheduling mechanism at the level of the Model

.

• The second file—modelActions.txt—quoted above at the beginning of Section 1.2, is related to the second of the schedule mechanisms, i.e., that of the Model. About the Observer/Model dualism, the reference is to note 7.

It contains (unique row, remembering that anyway row changes are not relevant to this group of files):

#### reset read\_script

The interpretation is the following.

- Also at the Model level, we have to take into consideration that the execution of the content of the file is "with repetition", never ending. It is the Observer that stops the experiment, but operating at its level.
- reset orders to the agents to make a reset, related to their variables. The order acts via the code in the file ModelSwarm.py.<sup>11</sup> reset contains the doO variable, linking a method that is specified as a function in the file mActions.py in the folder of the project. In this way, the application of the basic method reset can be flexibly tailored to the specific applications, defining which variables to reset.

In our specific case, the content of the doO function in mActions.py asks all the agents to execute the method setNewCycleValues. The method is defined in an instrumental file (agTools.py in \$\$slapp\$\$) and it is as default doing nothing. We can redefined it in Agent.py in the project folder.

Always in our case, as explained in Section 1.1.1, we suppose that the acting agent in resetting step would be that with 1 as identifier.

In our model, we clean the variables:

totalProductionInA\_TimeStep,

totalPlannedConsumptionInValueInA\_TimeStep,

totalProfit and

totalPlannedProduction

at the beginning of each step of the time. The code, in Agent.py is:

```
# reset values, redefining the method of agTools.py in $$slapp$$
def setNewCycleValues(self):
    # the if is to save time, given that the order is arriving to
    # all the agents (in principle, to reset local variables)
    if not common.agentlexisting:
        print "At least one of the agents has to have number==1"
        print "Missing that agent, all the agents are resetting common values"

if self.number==1 or not common.agentlexisting:
        common.totalProductionInA_TimeStep=0
        common.totalPrlannedConsumptionInValueInA_TimeStep=0
        common.totalProfit=0
        common.totalPlannedProduction=0
```

read\_script orders to the Model to open a new level of scheduling, described in Section 1.2.3. The order acts via the code of the file ModelSwarm.py. We have here one of the stable instances of the

<sup>&</sup>lt;sup>11</sup>That is in the "\$\$slapp\$\$" folder.

class ActionGroup within the Model. The ActionGroup related to read\_script item is the actionGroup100 that contains the do100 function, used internally within ModelSwarm.py to manage the script reported into the schedule.xls file (or directly into the schedule.txt one).

# 1.2.3 The detailed scheduling mechanism within the Model (AESOP level)

AESOP comes from Agents and Emergencies for Simulating Organizations in Python.

• The third scheduling mechanism, as anticipated in Section 1.2, operates at a *micro* scale and it is based on a detailed script system that the Model executes while the time is running. The time is managed by the clock item in the sequence of the Observer.

The script system is activated by the item read\_script in the sequence of the Model.

- This kind of script system does not exist in Swarm, so it is a specific feature of SLAPP, introduced as implementation of the AESOP (Agents and Emergencies for Simulating Organizations in Python) idea: a layer that describes in a fine-grained way the actions of the agents in our simulation models.
- Now we take in exam the timetable of our Oligopoly model.
- The file schedule.xls can be composed of several sheets, with: (a) the first one with name schedule; (b) the other ones with any name (those names are macro instruction names). We can recall the macro instructions in any sheet, but not within the sheet that creates the macro (that with the same name of the macro), to avoid infinite loops.

We differentiate the execution sequences in our model via the schedule.xls sheet contained in the folder oligoply.

Within the sheet, we have the action containers as introduce above (Figure 1.1), starting with the sign #.

#### 1.3 Micro scheduling: the AESOP level

From now on we explain the micro level of AESOP, i.e., the structure of the implementation of the Agents and Emergencies for Simulating Organizations in

Python for the Oligopoly model,

#### 1.3.1 Model versions via the AESOP level in scheduling

.

We have several versions of the model defined via the sequences of actions. To use one of them, we have to copy its schedule to the basic schedule.xls file.

#### 1.3.1.1 Version 0 (GitHub: V0 sub releases tab), preliminary step

In schedule0.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
# 1 100
entrepreneurs produce
entrepreneurs evaluateProfitV0
entrepreneurs 0.5 hireIfProfit
entrepreneurs 0.5 fireIfProfit
```

#### 1.3.1.2 Version 1, random production as engine (GitHub: release V1&2)

In schedule1.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
# 1 100

entrepreneurs makeProductionPlan
entrepreneurs hireFireWithProduction
entrepreneurs produce
WorldState specialUse setMarketPriceV1
entrepreneurs evaluateProfit
entrepreneurs 0.5 fireIfProfit
```

### 1.3.1.3 Version 2 (GitHub: , random production as engine (GitHub: release V1&2)

Here we have (i) random production as engine, (ii) individual demand curves with more realistic price determination, (iii) new entrant firms.

In schedule2.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
# 1 100
entrepreneurs makeProductionPlan
entrepreneurs hireFireWithProduction
entrepreneurs produce
entrepreneurs planConsumptionInValue
workers planConsumptionInValue
WorldState specialUse setMarketPriceV2
```

entrepreneurs	evaluateProfit	
entrepreneurs	0,5	fireIfProfit
workers	toEntrepreneur	
entrepreneurs	toWorker	

#### 1.3.1.4 Version 3 (GitHub: release V3)

Here we have (i) random production only at time 1, (ii) adaptation in production plans, (iii) individual demand curves with more realistic price determination, (iv) new entrant firms.

In schedule3.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
1
                  100
                     makeProductionPlan
entrepreneurs
                     adaptProductionPlan
entrepreneurs
entrepreneurs
                     hireFireWithProduction
entrepreneurs
                     produce
                     planConsumptionInValue
entrepreneurs
                     planConsumptionInValue
workers
WorldState
                     specialUse
                                              setMarketPriceV3
entrepreneurs
                     evaluateProfit
entrepreneurs
                     0.0001
                                              fireTfProfit
workers
                     toEntrepreneurV3
entrepreneurs
                     toWorkerV3
```

#### 1.3.1.5 Version 4 (GitHub: release V4)

Here we have (i) random production only at time 1, (ii) adaptation in production plans, (iii) individual demand curves with more realistic price determination, (iv) new entrant firms.

In schedule4.xls (to be copied to schedule.xls for the use) we have (comments start at column E) three columns:

```
entrepreneurs
                       makeProductionPlan
entrepreneurs
                        adaptProductionPlan
entrepreneurs
                       hireFireWithProduction
                       planConsumptionInValue
entrepreneurs
                       planConsumptionInValue
WorldState
                        specialUse
                                                   setMarketPriceV3
                        evaluateProfit
entrepreneurs
                                                   fireIfProfit
entrepreneurs
                       0.0001
                        toEntrepreneurV3
entrepreneurs
                                                                COMMENT: below an experimental step
                       toWorkerV3
                                                               WorldState spe
Temporary step
to check the model
                                                                                                       randomShockToWages
                                                                                 specialUse
                                                                sensitivity
                                                   fullEmploymentEffectOnWages incumbentActionOnWages
WorldState
                        specialUse
WorldState
                        specialUse
```

### 1.3.1.6 Version 5, 5b, 5bPy3, 5c, 5c\_fd (GitHub: versions V5bPy3, V5c, V5bP2\_fd, V5c\_fd)

Version 5c\_fd adds to 5c the saving with the related output file of data of each firm in each period (production and profit). The output file has name date+hour+\_firms.csv.

The individual data of each firm are elaborated via the iPython program readingCsvOutput.ipynb, to obtain mean and standard deviations about production and profits. The results are very close, but the dimensionality, to those obtained via the same program using the aggregated time series. The differences are due to the changes in number of entrepreneurs in each period, so the calculations based on the time series use data not always homogeneous.

Version 5c continues the set of small changes introduced to version 5, now adding the capability of changing the parameters of the simulation while the model is running; this capability is based upon the specialAction feature of SLAPP, at the level of the observer. See above, section 1.2.1.1.

Version 5b is related uniquely to a correction in method adaptProductionPlan, as in subsection 1.3.6.1, now modified as in subsection ??. The schedule is unchanged from Version 5 to 5b.

Version 5b3P is exactly the same as version 5b, but revised for Python 3 (SLAPP 3.0 or more).

NB NB NBTo replicate results calculated until May 2017, please use version 5b with SLAPP 2.0.

The differences are coming from a significant novelty in random number use.

With version 5b, we added the possibility of work troubles in firms, via the method entrepreneurs p work troubles, where p is a probability.

In schedule5.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
# 1 100
entrepreneurs makeProductionPlan
entrepreneurs adaptProductionPlan
entrepreneurs hireFireWithProduction
entrepreneurs 0.05 workTroubles
```

Unfortunately, random.shuffle() behaves in a different way in the two Python versions, as you can read at http://stackoverflow.com/questions/38943038/difference-between-python-2-and-3-for-shuffle-with-a-given-seed and also, after a call to shuffle the successive sequence of random realizations will be different in the two Python versions.

Due to this behavior we cannot reproduce in a full detailed way a run of a project in SLAPP working with Python 2 and with Python 3.

<sup>&</sup>lt;sup>12</sup>Working with the example basic (via SLAPP) we can verify that a sequence of "random.random()" numbers has the same content in Python 2 and in Python 3 if "n" in random.seed(n) is the same.

entrepreneurs	produceV5		
entrepreneurs	planConsumptionInValueV6		
workers	planConsumptionInValue	V6	
WorldState	computationalUse	setMarketPriceV3	
entrepreneurs	evaluateProfitV5		
entrepreneurs	0.0001	fireIfProfit	
workers	toEntrepreneurV3		
entrepreneurs	toWorkerV3		
WorldState	computationalUse	fullEmploymentEffectOnWages	
WorldState	computationalUse	incumbentActionOnWages	

# 1.3.1.7 Version 6, the hayekian market (Github: this version will become the release V6, currently is the branch develHayekian-Market @@)

We introduce now experiments with the introduction of a hayekian market inside the *Oligopoly* model, remembering Bowles *et al.* (2017), Boettke (1990) and Lewis (2014) as examples of relevant references to the hayekian market analysis.

The main reference above those above is Bowles *et al.* (2017), absolutely worth to be considered; from there, we report the Hayek quotation:

[The market is] a system of the utilization of knowledge which nobody can possess as a whole, which ... leads people to aim at the needs of people whom they do not know, make use of facilities about which they have no direct information; all this condensed in abstract signals ... [T]hat our whole modern wealth and production could arise only thanks to this mechanism is, I believe, the basis not only of my economics but also much of my political views (Hayek, 1994, p. 69).

In schedule6.xls (to be copied to schedule.xls for the use) we have (comments start at column E and are missing) three columns:

```
100
         1
                     makeProductionPlan
entrepreneurs
                      adaptProductionPlanV6
entrepreneurs
                     hireFireWithProduction
entrepreneurs
                      0.05
                                              workTroubles
entrepreneurs
entrepreneurs
                     produceV5
                     planConsumptionInValueV5
entrepreneurs
workers
                     planConsumptionInValueV5
macro
WorldState
                     computationalUse
                                               setMarketPriceV6
                     evaluateProfitV6
entrepreneurs
workers
                     toEntrepreneurV3
entrepreneurs
                     toWorkerV3
                                               fullEmploymentEffectOnWages
WorldState
                      computationalUse
WorldState
                      computationalUse
                                               incumbentActionOnWages
```

In schedule6.xls we have a second sheet named act containing:

```
# 1 100
all actOnMarketPlace
all actOnMarketPlace
all actOnMarketPlace
all actOnMarketPlace
all actOnMarketPlace
all actOnMarketPlace
```

The number of repetition of the method actOnMarketPlace in each cycle is determinate by the number of rows in the macro sheet act.

#### 1.3.2 The items of our AESOP level in scheduling

We have several items, not all used in each version of the model.

• # 1 100 fills 100 steps of the time schedule (or any other number of them) with the sequence below it, creating 100 (in this case) time containers.

The actual step repetition upon time can be  $\leq 100$ ; if > 100 the steps after the  $100^{\text{th}}$  will be lacking of activity of the detailed scheduling activity (AESOP layer).

#### 1.3.3 Methods used in Version 6 only

#### 1.3.3.1 adaptProductionPlanV6

• While we are in the pre hayekian period, i.e., in *the warming up* phase of the run of the model, the method adaptProductionPlanV6 works as the method described in Section 1.3.6.2.

Indeed, the easier way to start the *Olygopoly* model with a hayekian market inside is that of warming up the model with the price setting employed until version 5c\_fd, i.e., comparing the total offer in quantity and the total demand in value and calculating a clearing price.

After k-1 cycles of warming, the last price is used in cycle k, considering it to be the previous cycle price that both the entrepreneurs—as producers—and the entrepreneurs and the workers—as consumers—remember and use in their first step, starting to act in a decentralize market, in the hayekian perspective.

With  $t \geq k$ , the methods is operating in the direction of the hayekian market.

The entrepreneurs evaluate expected production in each period by dividing the total consumption of the previous period, measured in quantity (prices are too heterogeneous in a hayekian situation), by the number of entrepreneurs.

#### With:

- $-\varphi_{i,t}$  as individual firm production in t;
- $-C_{n_s,t-1}$  as one of the *n* buying actions, measured in quantity, of consumer s at time t-1;
- $-N_E$  as the entrepreneur number;
- $-u_t$  as a random addendum (drawn from a uniform distribution to have super-fat tails) representing the difficulty of having correct information about all the buy action made into the economic system;

we have:

$$\varphi_{i,t} = \frac{\sum_{s} \sum_{n_s} C_{n_s,t-1}}{N_E} + u_t \tag{1.1}$$

The code is:

```
# adaptProductionPlanV6
def adaptProductionPlanV6(self):
    # pre hayekian period
    if common.cycle > 1 and common.cycle < common.startHayekianMarket:
        # count of the entrepreneur number
        nEntrepreneurs = 0
        for ag in self.agentList:
            if ag.agType == "entrepreneurs":
                nEntrepreneurs += 1
        # with the scheme of prices until V.5c_fd
        if len(common.ts_df.price.values) == 1:
            previuosPrice = common.ts_df.price.values[-1] # t=2
        if len(common.ts_df.price.values) > 1:
            previuosPrice = common.ts_df.price.values[-2] # t>2
        # NB adapt acts from t>1
        self.plannedProduction = (common.totalDemandInPrevious_TimeStep /
                                  previuosPrice) \
            / nEntrepreneurs
        shock = uniform(
            -common.randomComponentOfPlannedProduction,
            common.randomComponentOfPlannedProduction)
        if shock >= 0:
            self.plannedProduction \star= (1. + shock)
        if shock < 0:
```

```
shock *=-1.
        self.plannedProduction /= (1. + shock)
    # print self.number, self.plannedProduction
   common.totalPlannedProduction += self.plannedProduction
    # print "entrepreneur", self.number, "plan", self.plannedProduction,\
        "total", common.totalPlannedProduction
# hayekian period
if common.cycle >= common.startHayekianMarket:
    if common.startHayekianMarket <=1:</pre>
      print("startHayekianMarket must be > 1")
       os.sys.exit(1) \# to stop the execution, in the calling module
                      # we have multiple except, with 'SystemExit' case
   nEntrepreneurs = 0
   for ag in self.agentList:
        if ag.agType == "entrepreneurs":
            nEntrepreneurs += 1
    self.plannedProduction = \
              common.totalConsumptionInQuantityInPrevious_TimeStep \
              / nEntrepreneurs
   shock = uniform(
        -common.randomComponentOfPlannedProduction,
        \verb|common.randomComponentOfPlannedProduction||\\
   if shock >= 0:
        self.plannedProduction \star= (1. + shock)
   if shock < 0:
        shock \star = -1.
        self.plannedProduction /= (1. + shock)
    # print self.number, self.plannedProduction
   common.totalPlannedProduction += self.plannedProduction
    # print "entrepreneur", self.number, "plan", self.plannedProduction,\
        "total", common.totalPlannedProduction
     # to record sold production
   self.soldProduction=0
```

The internal variable common.totalDemandInQuantityInPrevious\_TimeStep is updated in the following way:

- the internal variable common.totalConsumptioInQuantityInPrevious\_TimeStep is set within the reset function in Agent.py (about reset, see Section 1.1.1), saving in it the value of previous step common.totalConsumptionInQuantityInA\_TimeStep, before resetting it to 0; the code here is:

```
elif common.cycle > common.startHayekianMarket:
    common.totalConsumptionInQuantityInPrevious_TimeStep = \
        common.totalConsumptionInQuantityInA_TimeStep
```

common.totalConsumptionInQuantityInA\_TimeStep is determined in actOnMarketPlace in Section 1.3.3.3;

- we have a special case when
 common.cycle == common.startHayekianMarket
 and the previous value does not exist because actOnMarketPlace has
 still to start to operate;

in this case we use the previous planned amount of consumption in value,

common.totalPlannedConsumptionInValueInA\_TimeStep, transformed in quantity using prices at t-2 using the scheme of adaptProductionPlan (Section 1.3.6.2), i.e.:

```
if len(common.ts_df.price.values) == 1:
    previuosPrice = common.ts_df.price.values[-1] # t=2
if len(common.ts_df.price.values) > 1:
    previuosPrice = common.ts_df.price.values[-2] # t>2
# NB the code above can act only from t>1
```

we underline that previuosPrice (as a local variable) can be used in the unique case

common.cycle == common.startHayekianMarket.

- The whole specific code is:

```
# introduced with V6
# V6 reset block starts hene
# this part is specific of the first hayekian cycle
# where it replaces the lack of a previous values in
# quantity
if common.cycle == common.startHayekianMarket:
    if len(common.ts_df.price.values) == 1:
      previuosPrice = common.ts_df.price.values[-1] # t=2
    if len(common.ts_df.price.values) > 1:
      previuosPrice = common.ts_df.price.values[-2] # t>2
    # NB the code above can act only from t>1
    common.totalConsumptionInQuantityInPrevious_TimeStep = \
    common.totalPlannedConsumptionInValueInA_TimeStep
    / previuosPrice
elif common.cycle > common.startHayekianMarket:
    common.totalConsumptionInQuantityInPrevious_TimeStep = \
      common.totalConsumptionInQuantityInA_TimeStep
common.totalConsumptionInQuantityInA_TimeStep = 0
 \# list of all the transaction prices in a cycle of the
# hayekian market
common.hayekianMarketTransactionPriceList_inACycle=[]
# v6 reset block ends here
```

#### 1.3.3.2 planConsumptionInValueV6

• The method (or command) planConsumptionInValueV6, 13 sent to workers or entrepreneurs, produces the following evaluations, using the parameters detailed in commonVar.py file.

The method is equal to planConsumptionInValueV5 one, but the conclusion, where no update of *common* value totalPlannedConsumptionInValueInA\_TimeStep is made after the conclusion of the *pre-hayekian* periodo.

Consumption behavior with

$$C_i = a_k + b_k Y_i + u \tag{1.2}$$

with  $u \sim \mathcal{N}(0, common.consumptionRandomComponentSD)$ .

The individual i can be:

- 1. an entrepreneur, with  $Y_i = profit_{i,t-1} + wage$ ;
- 2. an employed worker, with  $Y_i = wage$  and the special <sup>14</sup> case  $Y_i = wc_t^i$ , with  $wc_t^i$  defined in eq.1.21;
- 3. an unemployed workers<sup>15</sup>, with  $Y_i = socialWelfareCompensation$ .

The  $a_k$  and  $b_k$  values are set via the file commonVar.py and reported in output, when the program starts, via the parameters.py.

The code in Agent.py is:

<sup>&</sup>lt;sup>13</sup>Related to Version 6

 $<sup>^{14}</sup>$ Activated if the common value wageCutForWorkTroubles is true

<sup>&</sup>lt;sup>15</sup>In this case, if the random component exceeds the consumption coming from social welfare compensation, we can have negative consumption; in case, in version 6, consumption are set to 0.

```
# the followin if/else structure is for control reasons because if
  # not common.wageCutForWorkTroubles we do not take in account
  # self.workTroubles also if != 0; if = 0 is non relevant in any case
 if common.wageCutForWorkTroubles:
   self.consumption = common.a2 + \
                       common.b2 * common.wage*(1.-self.workTroubles) + \
                       gauss(0,common.consumptionRandomComponentSD)
   #print "worker", self.number, "wage x",(1.-self.workTroubles)
 else:
   self.consumption = common.a2 + \
                       common.b2 * common.wage + \
                       gauss(0,common.consumptionRandomComponentSD)
#case (3)
#Y3=socialWelfareCompensation
if self.agType == "workers" and not self.employed:
   self.consumption = common.a3 + \
                       common.b3 * common.socialWelfareCompensation + \
                       gauss(0,common.consumptionRandomComponentSD)
# update totalPlannedConsumptionInValueInA_TimeStep
if common.cycle < common.startHayekianMarket:</pre>
common.totalPlannedConsumptionInValueInA_TimeStep += self.consumption
# print "C sum", common.totalPlannedConsumptionInValueInA_TimeStep
self.consumptionPlanningInCycleNumber=common.cycle
```

Referring to totalPlannedConsumptionInValueInA\_TimeStep, the method updates that *common* value only until the starting point of the hayekian market; on the contrary, the V5 version of the method updates it always.

When the hayekian market operates, the consumption total amount comes from summing up all the consumption actions in actOnMarketPlace method.

#### 1.3.3.3 actOnMarketPlace

• The method (or command) actOnMarketPlace, <sup>16</sup> operates only in the *hayekian* phase of each run.

In the first execution, only once, both a buy and a sell price are initialized for each agent in a way close to that of the Section 1.3.6.2. Here the previous price to be used is that at t-1 because we are on the side of the consumers. Instead, in the pre-hayekian setting, the producers look at the price used by the consumers to guess quantities in the previous period, so that in t-2.

Both the entrepreneurs and the workers are *buyers*, while the *sellers* are uniquely the entrepreneurs.

<sup>&</sup>lt;sup>16</sup>Related to Version 6

- Search for sellers. In the first step of each multiple call of actOnMarketPlace in each cycle, and for each buyer, a seller is choses from a temporary list locally generated.
- The method actOnMarketPlace is included in a macro, The number of repetitions for each buyer in each cycle (the number of buy attempts) is regulated by the number of repetition into the macro. In each repetition the program shuffles the agents. Each agent has in memory the effect of the action done in the previous repetition within a cycle.
- Sold products are recorded in quantity in self.soldProduction, always reset to 0 in any new cycle adaptProductionPlanV6 step.

thedeal between a buyer and a seller is based on the confrontation of the prices. If  $p_{B,i}$ , as buy price of agent i, is  $\geqslant$  of  $p_{S,j}$  as sell price of agent j, the agents exchange, at the seller price, the min quantity between the buying capacity of the buyer at that price and the actual production (accounting for workers availability) residual quantity.

The revenue of the seller (one of the entrepreneurs) is accounted for profit calculations.

- Prices: what price in each action for each agent?
  - The best is their, price, i.e., the price at which they have concluded a deal (the last one, if more than a deal was made in a same time interval)<sup>17</sup> or that of the last bid (if buyers) or ask (if sellers) they made without concluding a deal. This price is corrected with the rules below.
  - at time k, we use as starting point the price in k-1, being k the starting time of the hayekian market.

The code for the starting step (second bullet) is:

```
if not self.priceWarmingDone:
    # setting the price uniquely in the first hayekian step of the
    # first hayekian cycle

# this operation is close the usual scheme of adaptProductionPlan
    # with the correction introduced from the version 5b, but
    # here the previous price to be used is that at t-1 because
    # we are on the side of the consumers; instead, in the pre-hayekian
    # setting, the producers look at the price used by the consumers
    # to guess quantities in the previous period, so that in t-2.
    if len(common.ts_df.price.values) > 1:
        self.buyPrice = self.sellPrice = \
```

<sup>&</sup>lt;sup>17</sup>The event is possible if the agents buy or sell only fractions of their programmed buying or selling quantities, so repeating their actions

Both self.buyPrice and self.sellPrice are here in use, because each agent can take turns in doing both the actions.

\* We add a random correction to both the initial prices, to start with a mixed situation. Let initShock the internal variable containing the relative value  $\iota$  as the range of the correction of the individual starting prices in a random uniform way (but asymmetrically, with the internal variable initAsymmetry containing the value of  $\nu$  defined in the interval [0.5, 1] e.g., 0.60, as a quite large superimposition), with  $p_{B,i}$  as buy price of agent i and  $p_{S,i}$  as sell price of agent i, we have eqs,

$$p_{B,i} = p_{t-1}(1 + \varepsilon_{B,i})$$
 with  $\varepsilon_{B,i} \sim \mathcal{U}(-\nu \iota, (1 - \nu) \iota)$  and

$$p_{S,i} = p_{t-1}(1 + \varepsilon_{S,i}) \tag{1.4}$$

with  $\varepsilon_{S,i} \sim \mathcal{U}(-(1-\nu) \iota, \nu \iota)$ .

We adopt  $\nu = 0.60$  and  $\iota = 0.50$  as values for the experiment.

\* The continuous process of correction of the individual prices, applied to each transaction within each cycle, works in the following way: we modify the buy price (a random correction) if the last agent negotiation, also if unsuccessful, was on the buy side and the same on the sell price. Let runningShock be the internal variable containing the relative value  $\tilde{\iota}$  (e.g., 0.10) as the range of the correction or the individual running prices in a random uniform way (but asymmetrically, with the internal variable runningAsymmetry containing the value of  $\tilde{\nu}$  defined in the interval [0.5, 1] e.g., 0.90, as a very low superimposition), with  $p_{B,i}$  as buy price of agent i and  $p_{S,i}$  as sell price of agent i.

The equations are the same as 1.3 and 1.4, with  $\tilde{\nu}$  substituting  $\nu$  and  $\tilde{\iota}$  substituting  $\iota$ .

- After the starting cycle of the hayekian phase, each agent uses two status variable (technically: self.statusB and self.statusS), initialized to 0 and reporting its short term history both as a buyer (worker or entrepreneur) and as a seller (entrepreneur). Conventions:
  - \* self.statusB
    - · 0 means never used;
    - · 1 if previous action was a successful buy attempt;
    - $\cdot$  -1 if previous action was an unsuccessful buy attempt;
  - \* self.statusB
    - · 0 means never used;
    - · 1 if previous action was a successful sell attempt;
    - $\cdot$  -1 if previous action was an unsuccessful sell attempt.
  - \* Using the variables introduced above, we adopt  $\tilde{\nu} = 0.90$  and  $\tilde{\iota} = 0.05$  as values for the initial experiment.
  - \* Buyer case:
    - $\cdot$  if the last transaction succeeded (statusB is 1):

$$p_{B,i_t} = p_{B,i_{t-1}} (1 + \varepsilon_{B^{down},i}) \tag{1.5}$$

with  $\varepsilon_{B^{down},i} \sim \mathcal{U}(-\tilde{\nu} \ \tilde{\iota}, (1-\tilde{\nu}) \ \tilde{\iota})$ , so mostly negative (the agent tries to decrease its reservation price);

 $\cdot$  if the last transaction failed (status B is -1):

$$p_{B,i_t} = p_{B,i_{t-1}}(1 + \varepsilon_{B^{up},i})$$
 (1.6)

with  $\varepsilon_{B^{up},i} \sim \mathcal{U}(-(1-\tilde{\nu})\ \tilde{\iota},\tilde{\nu}\ \tilde{\iota})$ , so mostly positive (the agent tries to increase its reservation price).

- \* Seller case:
  - $\cdot$  if the last transaction succeeded (*statusS* is 1):

$$p_{S,i_t} = p_{S,i_{t-1}}(1 + \varepsilon_{S^{up},i}) \tag{1.7}$$

with  $\varepsilon_{S^{up},i} \sim \mathcal{U}(-(1-\tilde{\nu})\ \tilde{\iota},\tilde{\nu}\ \tilde{\iota})$ , so mostly positive (the agent tries to increase its reservation price);

· if the last transaction failed (statusS is -1):

$$p_{S,i_t} = p_{S,i_{t-1}} (1 + \varepsilon_{S^{down},i}) \tag{1.8}$$

with  $\varepsilon_{S^{down},i} \sim \mathcal{U}(-\tilde{\nu} \ \tilde{\iota}, (1-\tilde{\nu}) \ \tilde{\iota})$ , so mostly negative (the agent tries to decrease its reservation price).

#### • The resulting code of the whole method is:

```
# all acting as consumers on the market place
def actOnMarketPlace(self):
    if common.cycle < common.startHayekianMarket: return</pre>
    if not self.priceWarmingDone:
       # setting the price uniquely in the first hayekian step of the
       # first hayekian cycle
       # this operation is close the usual scheme of adaptProductionPlan
       # with the correction introduced from the version 5b, but
       \# here the previous price to be used is that at t-1 because
       # we are on the side of the consumers; instead, in the pre-hayekian
       # setting, the producers look at the price used by the consumers
       \# to guess quantities in the previous period, so that in t-2.
       if len(common.ts_df.price.values) > 1:
          self.buyPrice = self.sellPrice = \
                  common.ts_df.price.values[-1] # the last one
          self.buyPrice *= 1 + \
               uniform(-common.initAsymmetry*common.initShock, \
                       (1-common.initAsymmetry) *common.initAsymmetry)
          self.sellPrice *= 1+ \
               uniform(-(1-common.initAsymmetry)*common.initShock, \
                       common.initAsymmetry*common.initShock)
          #print("Ag.", self.number, "buying at", self.buyPrice,
                                    "selling at", self.sellPrice)
          #if self.buyPrice >= self.sellPrice:
                   print ("buyPrice >= sellPrice")
       # NB the code above can act only if t>1
       self.priceWarmingDone = True
    # first call in each cycle, prepearing action (only once per cycle)
    if self.currentCycle != common.cycle:
       self.currentCycle = common.cycle
       # we check that the planning of the consumtion has been
       # made for the current cycle
       if self.consumptionPlanningInCycleNumber != common.cycle:
           print('Attempt of using actOnMarketPlace method before'+\
                  consumption planning')
           os.sys.exit(1) \# to stop the execution, in the calling module
                       # we have multiple except, with 'SystemExit' case
       # create a tmp list of sellers
       self.sellerList=[]
       for anAg in self.agentList:
           if anAg.getType() == "entrepreneurs":
               self.sellerList.append(anAg)
    # acting (NB self.consumption comes from planConsumptionInValueV6)
    # if buying action is possible
    #print("cycle", common.cycle, "ag", self.number, "cons val", self.consumption)
    if self.consumption > 0 and self.sellerList != []:
        # chose a seller
        mySeller=self.sellerList[randint(0,len(self.sellerList)-1)]
        sellerQ=mySeller.production - mySeller.soldProduction>0
        if sellerQ>0:
```

```
# try a deal
      if self.buyPrice < mySeller.sellPrice:</pre>
         self.statusB=self.statusS=-1
      if self.buyPrice >= mySeller.sellPrice:
         self.statusB=self.statusS= 1
         # NB production can be < plannedProduction due to lack of workers
         buyerQ=min(self.consumption/mySeller.sellPrice, sellerQ)
         mySeller.soldProduction+=buyerQ
         mySeller.revenue+=buyerQ*mySeller.sellPrice
         self.consumption-=buyerQ*mySeller.sellPrice
         #print("cycle",common.cycle,"aq",self.number,"deal: cons val",\
                 buyerQ*mySeller.sellPrice, "price", mySeller.sellPrice)
         # saving the price of the transaction
         common.hayekianMarketTransactionPriceList_inACycle.\
                append(mySeller.sellPrice)
         common.totalConsumptionInQuantityInA_TimeStep += buyerQ
# correct running prices
# if the status is != 0 the agent has already been acting
if self.statusB == 1: # buyer case (statusB 1, successful buy attempt,
                       # acting mostly to decrease the reservation price)
   self.buyPrice *= 1 + uniform(-common.runningAsymmetry* \
                                common.runningShock, \
                                (1-common.runningAsymmetry) * \
                                common.runningShock)
if self.statusB == -1: # buyer case (statusB -1, unsuccessful buy attempt,
                       # acting mostly to increase the reservation price)
   self.buyPrice *= 1 + uniform(-(1-common.runningAsymmetry)* \
                                common.runningShock, \
                                common.runningAsymmetry* \
                                common.runningShock)
if self.statusS == 1: # seller case (statusS 2, successful sell attempt,
                       # acting mostly to increase the reservation price)
   self.sellPrice *= 1 + uniform(-(1-common.runningAsymmetry)* \
                                common.runningShock, \
                                common.runningAsymmetry* \
                                common.runningShock)
if self.statusS == -1: # seller case (statusS -2, unsuccess. s. attempt,
                       # acting mostly to decrease the reservation price)
   self.sellPrice *= 1 + uniform(-common.runningAsymmetry* \
                                common.runningShock, \
                                (1-common.runningAsymmetry) * \
                                common.runningShock)
#print("aq.", self.number, "new prices", self.buyPrice, self.sellPrice)
# cleaning the situation
self.statusB=self.statusA=0
```

#### 1.3.3.4 evaluateProfitV6

• The method (or command) evaluateProfitV6, <sup>18</sup> sent to the entrepreneurs, orders them to calculate their profit. Being  $P_t^i$  the production and the labor force  $L_t^i$  measured via the network connecting the entrepreneur to her workers plus 1 to take in account the entrepreneur herself.

The use of  $P_t^i$ , the actual production of the entrepreneurs, accounts both for the production plan decided with adaptProductionPlan, page 41, and for the limits in hiring, if any, as in hireFireWithProduction, page 36. The sum of all the actual productions of each entrepreneur is used, as at page 62, in setMarketPriceV3.

The method has been improved in version 2, to manage extra costs for the new entrant firms, but keeping safe the backward compatibility of the method.

 $p_t$  is the price, clearing the market at time t and it is calculated by the abstract item WorldState via the method setMarketPrice, as explained in Section 1.3.16.

w is the wage per employee and time unit, set to 1.0 in common variable space, not changing with t, but the case of the important events of:

- wage rise due both to full employment (Subsection 1.3.7.1) and
- to the creation of barriers against new entrants (Subsection 1.3.7.3).

C are extra costs for new entrant firms. They are calibrated to assure the effectivness of the action described in Subsection 1.3.7.3, but in a non deterministic way, thanks to the movements in prices.

If the *common* variable wageCutForWorkTroubles is set to *True* the costs determination takes in account the reduction in the wages (but the wage of the entrepreneur, not changing).

Considering the presence of work troubles (see subsection 1.3.8.1) the determination of the clearing price, as at page 62, can signal an increase in the equilibrium price, due to the lacking production.

The (relative) shock  $\psi_{i,t} > 0$  due to work troubles is defined in subsection 1.3.8.1.

In presence of work troubles the firm has to accept a reduction of its price, to compensate its customers for having undermined the confidence in the

<sup>&</sup>lt;sup>18</sup>Related to Version 6.

implicit commitment of producing a given quantity (the production plan, specified in subsection 1.3.4.1).

That penalty value, as a relative measure, is in *common* as **penaltyValue** and here shortly as pv. Locally,  $pv_t^i$ , for the firm i at time t, is set to pv if  $\psi_{i,t} > 0$ ; otherwise  $(\psi_{i,t} = 0)$  is set to 0.

Here we have the difference with V5. Eqs. 1.9 and 1.10 are used in the pre-hakyean phase, while eqs. 1.11 and 1.12 work in the hayekian one.

The profit evaluation, if wageCutForWorkTroubles is set to True, is:

$$\Pi_t^i = p_t (1 - p v_t^1) P_t^i - (w - \psi_{i,t}) (L_t^i - 1) - 1w - C$$
(1.9)

being 1w the wage of the entrepreneur.

If wageCutForWorkTroubles is set to False, the result is:

$$\Pi_t^i = p_t (1 - p v_t^i) P_t^i - w L_t^i - C \tag{1.10}$$

In the hayekian phase we have, with  $REV_t^i$  reporting the revenue of firm i ant time t:

The profit evaluation, if wageCutForWorkTroubles is set to True, is:

$$\Pi_t^i = REV_t^i - (w - \psi_{i,t})(L_t^i - 1) - 1w - C \tag{1.11}$$

being 1w the wage of the entrepreneur.

If wageCutForWorkTroubles is set to False, the result is:

$$\Pi_t^i = REV_t^i - wL_t^i - C \tag{1.12}$$

The experiments run in April 2017 (with V5 of this method) for the final version for the Italian economic journal have the penalty value  $pv_t^i$  set to 0.

The new entrant firms have extra costs C to be supported, retrieved in XC variables, but only for k periods, as stated in commonVar.py and activated by method toEntrepreneur.

The code is:

```
# calculateProfit
def evaluateProfitV6(self):

# this is an entrepreneur action
if self.agType == "workers":
    return

# backward compatibily to version 1
```

```
try:
   XC = common.newEntrantExtraCosts
except BaseException:
   XC = 0
   k = self.extraCostsResidualDuration
except BaseException:
   k = 0
if k == 0:
   XC = 0
if k > 0:
    self.extraCostsResidualDuration -= 1
\# the number of pruducing workers is obtained indirectly via
# production/laborProductivity
# print self.production/common.laborProductivity
# how many workers, not via productvity due to possible troubles
# in production
laborForce = gvf.nx.degree(common.g, nbunch=self) + \
    1 + 1 to account for the entrepreneur herself
# the followin if/else structure is for control reasons because if
# not common.wageCutForWorkTroubles we do not take in account
# self.workTroubles also if != 0; if = 0 is non relevant in any case
if common.wageCutForWorkTroubles:
    self.costs = (common.wage - self.hasTroubles) \
       * (laborForce - 1) \
       + common.wage * 1 +
       XC
    # above, common.wage * 1 is for the entrepreur herself
else:
    self.costs = common.wage * laborForce + \
# print "I'm entrepreur", self.number, "costs are", self.costs
# penalty Value
0 = vq
if self.hasTroubles > 0:
   pv = common.penaltyValue
# V6 - before hayekian phase
if common.cycle < common.startHayekianMarket:</pre>
   \# the entrepreur sells her production, which is contributing - via
   # totalActualProductionInA_TimeStep, to price formation
   {\tt self.profit = common.price * (1. - pv) * self.production - self.costs}
   print("I'm entrepreur", self.number, "my price is ",
     common.price \star (1. - pv))
# V6 - into the hayekian phase
else:
   self.profit = self.revenue - self.costs
   print("I'm entrepreur", self.number, "my individual price is ",
     self.sellPrice)
# individual data collection
# creating the dataframe
trv:
```

```
common.dataCounter
except BaseException:
   common.dataCounter=-1
   common.firm_df
except BaseException:
   common.firm_df = pd.DataFrame(
           columns=[
                'production',
                'profit'])
   print("\nCreation of fhe dataframe of the firms (individual data)\n")
common.dataCounter+=1
common.firm_df.set_value(common.dataCounter, \
                         'production', self.production)
common.firm_df.set_value(common.dataCounter, \
                         'profit', self.profit)
common.totalProfit += self.profit
```

#### 1.3.3.5 setMarketPriceV6

• The method (or command) setMarketPriceV6, 19 sent to the WorldState, orders it to evaluate the market clearing prices in the pre-hayekian phase and successively to record the mean and the standard deviation to the hayekian prices in each cycle. See below Section 1.3.16 and specifically Section 1.3.16.4.

# 1.3.4 Methods used in Versions 1, 2, 3, 4, 5, 5b, 5bPy3, 5c, 5c\_fd, 6

#### 1.3.4.1 makeProductionPlan

• The method (or command) makeProductionPlan, <sup>20</sup> sent to the entrepreneurs, orders them to guess their production for the current period. The production plan  $\widehat{P}_t^i$  is determined in a random way, using a Poisson distribution, with  $\nu = 10$  as mean (suggested value kept in the *common* space).

As a definition, the production plan is:

$$\hat{P}_t^i \sim Pois(\nu)$$
 (1.13)

We suggest temporary a value of 5 for  $\nu$ , with (in Versions 1 and 2) the quantities: entrepreneurs 5, workers 20 + the 5 entrepreneurs, labor productivity

 $<sup>^{19}\</sup>mathrm{Related}$  to Version 6, jumping from 3 to 6 in numbering the method.

<sup>&</sup>lt;sup>20</sup>Related to Versions 1, 2; in the 3, 4, 5, 5b, 5bPy3 and 5c, 5c\_fd and 6 cases, only at time=1

1. Always in Versions 1 and 2, the value of  $\nu$  can be modified in the prologue of the run).

With Version 3, the makeProductionPlan method works uniquely with t=1 being t internally common.cycle created and set to 1 by ObserverSwarm when starts.

Version 3 calculates the initial value  $\nu$  (used uniquely in the first step) as:

$$\nu = \rho \frac{(N_{workers} + N_{entrepreneurs})}{N_{entrepreneurs}}$$
 (1.14)

In this way about a  $\rho$  ratio of the agents is producing in the beginning. Internally, the total numbers of the agents  $N_{workers} + N_{entrepreneurs}$  can be obtained as the length of the agentList; the number of entrepreneurs is calculated from the same list considering only the entrepreneurs.

The code is:

```
# makeProductionPlan
def makeProductionPlan(self):
    # this is an entrepreneur action
    if self.agType == "workers": return
    if common.projectVersion >= 3 and common.cycle==1:
        nEntrepreneurs = 0
        for ag in self.agentList:
            if ag.agType=="entrepreneurs":
                nEntrepreneurs+=1
        #print nEntrepreneurs
        nWorkersPlus_nEntrepreneurs=len(self.agentList)
        #print nWorkersPlus_nEntrepreneurs
        common.nu=(common.rho*nWorkersPlus_nEntrepreneurs)/nEntrepreneurs
        #print common.rho, common.nu
    if (common.projectVersion >= 3 and common.cycle==1) or \
        common.projectVersion < 3:</pre>
        self.plannedProduction=npr.poisson(common.nu,1)[0] # 1 is the number
        # of element of the returned matrix (vector)
        #print self.plannedProduction
    common.totalPlannedProduction+=self.plannedProduction
```

#### 1.3.4.2 hireFireWithProduction

• The method (or command) hireFireWithProduction, <sup>21</sup> sent to the entrepreneurs, orders them to hire or fire comparing the labor forces required for the pro-

<sup>&</sup>lt;sup>21</sup>Related to Versions 1, 2, 3, 4, 5, 5b, 5bPy3, 5c, 5c fd, 6.

duction plan  $\widehat{P}_t^i$  and the labor productivity  $\pi$ ; we have the required labor force ( $L_t^i$  is the current one):

$$\widehat{L}_t^i = \widehat{P}_t^i / \pi \tag{1.15}$$

Now:

- 1. if  $\widehat{L}_t^i = L_t^i$  nothing has to be done;
- 2. if  $\hat{L}_t^i > L_t^i$ , the entrepreneur is hiring with the limit of the number of unemployed workers;
- 3. if  $\hat{L}_t^i < L_t^i$ , the entrepreneur is firing the workers in excess.

The code is:

```
def hireFireWithProduction(self):
    # workers do not hire/fire
    if self.agType == "workers": return
    # to decide to hire/fire we need to know the number of employees
    # the value is calcutated on the fly, to be sure of accounting for
    # modifications coming from outside
    # (nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.)
    laborForce0=gvf.nx.degree(common.g, nbunch=self) + \
                       1 # +1 to account for the entrepreneur itself
    # required labor force
    laborForceRequired=int(
                self.plannedProduction/common.laborProductivity)
    # no action
    if laborForce0 == laborForceRequired: return
    if laborForce0 < laborForceRequired:</pre>
        n = laborForceRequired - laborForce0
        tmpList=[]
        for ag in self.agentList:
          if ag != self:
             if ag.agType=="workers" and not ag.employed:
                tmpList.append(ag)
        if len(tmpList) > 0:
            k = min(n, len(tmpList))
            shuffle(tmpList)
            for i in range(k):
                hired=tmpList[i]
                hired.employed=True
                gvf.colors[hired]="Aqua"
                gvf.createEdge(self, hired)
                #self, here, is the hiring firm
        # count edges (workers) of the firm, after hiring (the values is
```

```
# recorded, but not used directly)
    self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
    # nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.
   print "entrepreneur", self.number, "has", \
         self.numOfWorkers, "edge/s after hiring"
if laborForce0 > laborForceRequired:
   n = laborForce0 - laborForceRequired
    # the list of the employees of the firm
   entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    #print "entrepreneur", self.number, "could fire", entrepreneurWorkers
    #the list returnes by nx is unstable as order
   entrepreneurWorkers = mySort(entrepreneurWorkers)
   if len(entrepreneurWorkers) > 0: # has to be, but ...
         shuffle(entrepreneurWorkers)
         for i in range(n):
            fired=entrepreneurWorkers[i]
            gvf.colors[fired]="OrangeRed"
            fired.employed=False
           common.g_edge_labels.pop((self,fired))
           common.g.remove_edge(self, fired)
    # count edges (workers) after firing (recorded, but not used
    # directly)
   self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
   # nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.
   print "entrepreneur", self.number, "has", \
          self.numOfWorkers, "edge/s after firing"
```

An important technical detail is the use of the function mySort to avoid inconsistencies in the order of the agents returned by the graph of the networks as workers of the entrepreneur. Different orders would produce different sets of fired workers, becoming different sets of potential entrepreneurs and producing different sequences of events in the simulation.

Why the differences in the order of the list of the agents? The graph is managed by networkX, which is using internally a dictionary structure, whose order is neither defined in any way in Python, nor constant from execution to execution<sup>22</sup>. The list, in our case, contains the addresses of the instances

<sup>&</sup>lt;sup>22</sup> With version 3.6, as we can see at https://docs.python.org/3.6/whatsnew/3.6.html# new-dict-implementation, within the "CPython implementation improvements", the *dict* type has been reimplemented. Specifically, at least in CPython (which is the more diffused Python implementation):

The order-preserving aspect of this new implementation is considered an implementation detail and should not be relied upon (this may change in the future, but it is desired to have this new dict implementation in the language for a few releases be-

of the agents. A simple sort of this list does not give us a stable order, due to the fact that the addresses and their order can change form a run to another.

For these reasons we use here a custom function to sort the list, using the internal number of the agents, to reorder them.<sup>23</sup>

As a related consequence, we have to keep in mind to avoid duplicated numbers: in the *Oligopoly* model the entrepreneurs can switch to workers and vice versa, so the numbers assigned to the entrepreneurs start from 1 and those assigned to the workers from 1001 (see the file workers.txtx).

The code of the function mySort is:

```
def mySort(ag):
    if ag==[]: return []
    numAg=[]
    for a in ag:
        numAg.append((a.number,a))
    numAg.sort()
    agSorted=[]
    for i in range(len(numAg)):
        agSorted.append(numAg[i][1])
    return agSorted
```

# 1.3.5 Methods used in Version 3, 4, 5, 5b, 5bPy3, 5c 5c fd, 6

#### 1.3.5.1 toEntrepreneurV3

• With the method (or command) to Entrepreneur V3,  $^{24}$  sent to workers, the agent, being a worker, decides to became an entrepreneur at time t, if its employer has a relative profit (reported to the total of the costs)  $\geq$  a given threshold at time t-1. The threshold is retrieved from the variable threshold To Entrepreneur.

The decision is a quite rare one, so we have to pass a higher level threshold, that we define as absoluteBarrierToBecomeEntrepreneur; the value is defined in commonVar.py and shown via parameters.py file.

fore changing the language spec to mandate order-preserving semantics for all current and future Python implementations; this also helps preserve backwards-compatibility with older versions of the language where random iteration order is still in effect, e.g. Python 3.5).

So dict structures, with Python 3.6 are order-preserving, but this new implementation is considered an implementation detail and should not be relied upon.

<sup>&</sup>lt;sup>23</sup>A related marginal problem, not eliminated, is the order in plotting the nodes in the graph plot: in the area where the nodes are superimposed, we can see the nodes exactly in the same position in every run, but differently placed as layer in the foreground/background sequence.

<sup>&</sup>lt;sup>24</sup>Related to Version 3, 4, 5, 6.

This parameter represents a potential max number of new entrepreneurs in each cycle.

Internally, it works in the following way: given an absolute value as number workers actually became entrepreneur, we transform that value in a probability, dividing it by the total number of the agents, used as an adaptive scale factor.

The agent changes its internal type, position (not completely at the left as the original entrepreneurs, but if it was an entrepreneur moved to worker and coming back, it goes completely at the left) and color and it deletes the previous edge to the entrepreneur/employer. Finally, it starts counting the k periods of extra costs (to k is assigned the value common.ExtraCostsDuration, in the measure stated in common.newEntrantExtraCosts.

The code in Agent.py is:

```
#to entrepreneurV3
def toEntrepreneurV3(self):
    if self.agType != "workers" or not self.employed: return
    if random() <= common.absoluteBarrierToBecomeEntrepreneur:</pre>
      myEntrepreneur=gvf.nx.neighbors(common.g, self)[0]
      myEntrepreneurProfit=myEntrepreneur.profit
      myEntrepreneurCosts=myEntrepreneur.costs
      if myEntrepreneurProfit/myEntrepreneurCosts >= \
        common.thresholdToEntrepreneur:
        print "Worker \&2.0f is now an entrepreneur (previous firm relative profit \&4.2f)" \&
              (self.number, myEntrepreneurProfit/myEntrepreneurCosts)
        common.g.remove_edge(myEntrepreneur, self)
        #originally, it was a worker
        if self.xPos>0:gvf.pos[self] = (self.xPos-15, self.yPos)
        #originally, it was an entrepreneur
        else:gvf.pos[self] = (self.xPos, self.yPos)
        # colors at http://www.w3schools.com/html/html_colornames.asp
        gvf.colors[self]="LawnGreen"
        self.agType="entrepreneurs"
        self.employed=True
        self.extraCostsResidualDuration=common.extraCostsDuration
```

#### 1.3.5.2 toWorkerV3

• With the method (or command) toWorkerV3,  $^{25}$  an entrepreneur moves to be an unemployed worker if its a relative profit (reported to the total of the costs) at time t is  $\leq$  a given threshold in t. The threshold is retrieved from the variable thresholdToWorker.

The agent changes its internal type, position (not completely at the right as the original workers, but if it was a worker moved to entrepreneur and

<sup>&</sup>lt;sup>25</sup>Related to Version 3, 4, 5, 6.

coming back, it goes completely at the right) and color and it deletes the previous edge to the workers/employee if any.

The code in Agent.py is:

```
#to workersV3
def toWorkerV3(self):
    if self.agType != "entrepreneurs": return
    #check for newborn firms
       self.costs
    except:
        return
    if self.profit/self.costs <= common.thresholdToWorker:</pre>
        print "I'm entrepreneur %2.0f and my relative profit is %4.2f" % \
              (self.number, self.profit/self.costs)
        # the list of the employees of the firm, IF ANY
        entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
        print "entrepreneur", self.number, "has", len(entrepreneurWorkers), \
         "workers to be fired"
        if len(entrepreneurWorkers) > 0:
            for aWorker in entrepreneurWorkers:
                gvf.colors[aWorker]="OrangeRed"
                aWorker.employed=False
                common.g.remove_edge(self, aWorker)
        self.numOfWorkers=0
        #originally, it was an entrepreneur
        if self.xPos<0:gvf.pos[self] = (self.xPos+15, self.yPos)</pre>
        #originally, it was a worker
        else:gvf.pos[self] = (self.xPos, self.yPos)
        # colors at http://www.w3schools.com/html/html_colornames.asp
        gvf.colors[self]="OrangeRed"
        self.agType="workers"
        self.employed=False
```

# 1.3.6 Methods used in Version 3, 4, 5, 5b, 5bPy3, 5c $5c\_fd$

#### 1.3.6.1 adaptProductionPlan until Version 5

• The method (or command) adaptProductionPlan,  $^{26}$  sent to entrepreneurs, orders to the  $i^{th}$  firm to set its production plan for the current period to their (equal, being i here not relevant) fraction of the total demand of the previous

<sup>&</sup>lt;sup>26</sup>Related to Version 3, 4, 5.

period, corrected with a random uniform relative correction in the interval -k to +k, reported in the prologue as:

Random component of planned production.

This method works for time > 1.

Being  $\hat{P}_t^i$  the planned production of firm i, we have:

- if 
$$u_t^i \ge 0$$

$$\widehat{P}_t^i = \frac{D_{t-1}}{N_{entrepreneurs}} (1 + u_t^i) \tag{1.16}$$

- if 
$$u_t^i < 0$$
 
$$\widehat{P}_t^i = \frac{D_{t-1}}{N_{entrements}} / (1 + |u_t^i|)$$
 (1.17)

with  $u_t^i \sim \mathcal{U}(-k, k)$ 

The code in Agent.py until Version 5 is:

```
# adaptProductionPlan
def adaptProductionPlan(self):
    if common.cycle > 1:
      nEntrepreneurs = 0
      for ag in self.agentList:
         if ag.agType=="entrepreneurs":
             nEntrepreneurs+=1
      self.plannedProduction = common.totalDemandInPrevious_TimeStep \
              / nEntrepreneurs
      #self.plannedProduction += gauss(0,self.plannedProduction/10)
       -common.randomComponentOfPlannedProduction, \
        common.randomComponentOfPlannedProduction)
      if shock >= 0:
       self.plannedProduction *= (1.+shock)
      if shock < 0:
       shock \star = -1.
       self.plannedProduction /= (1.+shock)
      #print self.number, self.plannedProduction
      common.totalPlannedProduction+=self.plannedProduction
```

## 1.3.6.2 adaptProductionPlan with Version 5b, 5bPy3, 5c, 5c\_fd correction

• The method (or command) adaptProductionPlan,  $^{27}$  sent to entrepreneurs, orders to the  $i^{th}$  firm to set its production plan for the current period to their

<sup>&</sup>lt;sup>27</sup>Related to Version 5b, 5bPy3 and 5c, 5c fd.

(equal, being *i* here not relevant) fraction of the total demand—transformed from its nominal value to the real one (i.e., in quantity)<sup>28</sup>—of the previous period, corrected with a random uniform relative correction in the interval -v to v, reported in the prologue as:

Random component of planned production.

This method works for time > 1.

Being  $\widehat{P}_t^i$  the planned production of firm i, we have:

- if 
$$u_t^i \ge 0$$
 
$$\widehat{P}_t^i = \frac{\frac{D_{t-1}}{p_{t-2}}}{N_{entrepreneurs}} (1 + u_t^i)$$
 (1.18)

- if 
$$u_t^i < 0$$
 
$$\widehat{P}_t^i = \frac{\frac{D_{t-1}}{p_{t-2}}}{N_{entrepreneurs}}/(1+|u_t^i|) \tag{1.19}$$

with  $u_t^i \sim \mathcal{U}(-v, v)$  and  $p_{t-2}$  the lagged price.<sup>29</sup>

The double lagged price correction is justified because we are considering the production decisions at time t, which are based on the decisions of consumption at t-1, related to the income at time t-1; these decisions are made before the determination of the prices at t-1 (emerging only when comparing the demand and the predetermined offer). If we want to evaluate the consumption in quantity, without the effect of a too limited or too abundant offer, we have to use t-2 prices. This construction will be eliminated with a future version of the model, with the atomic interaction of buyers and sellers in a dispersed way.

The code in Agent.py from Version 5b/5bPy3/5c/5c fd is:

 $<sup>^{28}\</sup>mathrm{The}$  missing part until Version  $5\mathrm{b}/5\mathrm{bPy3}/5\mathrm{c}/5\mathrm{c}_{-}\mathrm{fd}$  was this transformation; as a consequence, the result was partially biased, anyway with limited effects being our prices always around the unity; I have to thank Enrico Minardi, a student of mine, for discovering the missing operation.

<sup>&</sup>lt;sup>29</sup>The method is applied only with t > 1, so the use of the lagged price starts at time 2, when  $p_{t-2}$  would be the undefined  $p_0$  value; as a simplification we use  $p_{t-1}$  in this case, look at the code.

```
#previous period price
if len(common.ts_df.price.values) == 1:
   previuosPrice=common.ts_df.price.values[-1] # t=2
  len(common.ts_df.price.values)>1:
   previuosPrice=common.ts_df.price.values[-2] # t>2
#NB adapt acts from t>1
self.plannedProduction = (common.totalDemandInPrevious_TimeStep / \
                      previuosPrice) \
                       / nEntrepreneurs
#self.plannedProduction += gauss(0, self.plannedProduction/10)
shock= uniform( \
-common.randomComponentOfPlannedProduction, \
 common.randomComponentOfPlannedProduction)
if shock >= 0:
self.plannedProduction *= (1.+shock)
if shock < 0:
shock *=-1.
self.plannedProduction /= (1.+shock)
#print self.number, self.plannedProduction
common.totalPlannedProduction+=self.plannedProduction
#print "entrepreneur", self.number, "plan", self.plannedProduction, \
    "total", common.totalPlannedProduction
```

#### 1.3.6.3 setMarketPriceV3

• The method (or command) setMarketPriceV3,<sup>30</sup> sent to the WorldState, orders it to evaluate the market clearing price. See below Section 1.3.16 and specifically Section 1.3.16.3.

# 1.3.7 Methods used in Version 4, 5, 5b, 5bPy3, 5c, 5c fd

#### 1.3.7.1 fullEmploymentEffectOnWages

The method (or command) fullEmploymentEffectOnWages,<sup>31</sup> sent to the WorldState, orders it to modify wages accordingly to full employment situation, in a reversible way. See below Section 1.3.16 and specifically Section 1.3.16.5.

<sup>&</sup>lt;sup>30</sup>Related to Version 3, 4, 5.

<sup>&</sup>lt;sup>31</sup>Related to Version 4, 5, 6.

#### 1.3.7.2 randomShockToWages

The method (or command) randomShockToWages,<sup>32</sup> sent to the WorldState, orders it to randomly modify wages. See below Section 1.3.16 and specifically Section 1.3.16.6.

This method is only used in model building, to verify the sensitivity of the model to changes in wages.

#### 1.3.7.3 incumbentActionOnWages

The method (or command) incumbentActionOnWages, sent to the WorldState, orders it to modify wages for one period, accordingly to the attempt of creating an entry barrier when new firms are observed into the market.

As a consequence, wage measure contains a variable addendum, set to 0 as regular value and modified temporary by this method.

See below Section 1.3.16 and specifically Section 1.3.16.7.

# 1.3.8 Methods used in Version 5, 5b, 5bPy3, 5c, 5c\_fd, 6

#### 1.3.8.1 workTroubles

•

• The method (or command) workTroubles,<sup>34</sup> is sent to the entrepreneurs, For each entrepreneur at time t, so for each firm i, we generate a shock  $\psi_{i,t} > 0$  due to work troubles, with probability  $p_{\psi}$  (set for all the entrepreneurs via the schedule.txt file)<sup>35</sup> and value uniformly distributed between  $V_{\Psi}/2$  and  $V_{\Psi}$ . The shock reduces the production of firm i in a relative way, as in:

$$Pc_t^i = P_t^i (1 - \psi_{i,t}) \tag{1.20}$$

where Pc means corrected production.

<sup>&</sup>lt;sup>32</sup>Related to Version 4, 5, 6.

<sup>&</sup>lt;sup>33</sup>Related to Version 4, 5, 6.

<sup>&</sup>lt;sup>34</sup>Related to Version 5, 6.

 $<sup>^{35}</sup>$ SLAPP displays—in its text output—a dictionary with the method probabilities, if at least one method is linked to a probability.

If the global logical value wageCutForWorkTroubles is true, also wages are cut in the same proportion that the production is suffering. With w indicating the constant basic wage level,  $cw_t^i$  is the corrected value at time t and for firm i; the correction is superimposed to the other possible corrections (due to full employment or to artificial barrier creation).

$$cw_t^i = w(1 - \psi_{i,t}) \tag{1.21}$$

The firm variable hasTroubles takes note—via  $\psi_{i,t}$  assuming a value > 0, being 0 otherwise—if the firm has work problems in the current time step and the worker variable workTroubles takes note of the same amount for all the workers of that specific firm.

Both the variable are set again to 0 in the **reset** step at the beginning of each model cycle.

The code in Agent.py is:

```
#work troubles
def workTroubles(self):
     # NB this method acts with the probability set in the schedule.txt
     # file
    if self.agType != "entrepreneurs": return
     # production shock due to work troubles
    psiShock=uniform(common.productionCorrectionPsi/2,
                       common.productionCorrectionPsi)
    self.hasTroubles=psiShock
    print "Entrepreneur", self.number, "is suffering a reduction of " \backslash
          "production of", psiShock*100, "%, due to work troubles"
    if common.wageCutForWorkTroubles:
      # the list of the employees of the firm
      entrepreneurWorkers=gvf.nx.neighbors(common.g, self)
      for aWorker in entrepreneurWorkers:
        #avoiding the entrepreneur herself, as we are refering to her
        # network of workers
        aWorker.workTroubles=psiShock
```

#### 1.3.8.2 produceV5

• The method (or command) produce V5,  $^{36}$  sent to the entrepreneurs, orders them—in a deterministic way, in each unit of time—to produce proportionally to their labour force, obtaining profit  $\Pi_t^i$ , where i identifies the firm and t the time.

<sup>&</sup>lt;sup>36</sup>Related to Version 5, 6.

 $L_t^i$  is the number of workers of firm i at time t, and also the number of its links. We add 1 to  $L_t^i$ , to account for the entrepreneur as a worker.  $\pi$  is the laborProductivity, with its value set to 1 in common variable space, currently not changing with t.  $P_t^i$  is the production of firm i at time t.

The production is:

$$P_t^i = \pi(L_t^i + 1) (1.22)$$

The production is corrected for work troubles (as in section 1.3.8.1) calculating the corrected value  $Pc_t^i$  with:

The production is:

$$Pc_t^i = P_t^i (1 - \psi_{i,t}) \tag{1.23}$$

The production (corrected or not) of the  $i^{\text{th}}$  firm is added to the total production of the time step, in the variable totalProductionInA\_TimeStep of the *common* space.

The code is:

```
# produce
def produce(self):
    # this is an entrepreneur action
    if self.agType == "workers": return
    # to produce we need to know the number of employees
    # the value is calcutated on the fly, to be sure of accounting for
    # modifications coming from outside
    # (nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.)
    laborForce=gvf.nx.degree(common.g, nbunch=self) + \
               1 \ \# \ +1 to account for the entrepreneur itself
    # productivity is set to 1 in the benginning
    self.production = common.laborProductivity *
                      laborForce
    # totalProductionInA_TimeStep
    common.totalProductionInA_TimeStep += self.production
```

We calculate the laborForce, i.e.  $L_t^i$ , counting the number of links or edges from the firm to the workers. We prefer this 'on the fly" evaluation to the internal variable self.numOfWorkers, to be absolutely sure of accessing the last datum in case of modifications coming from other procedures. E.g., a random subtraction or addition of workers to firms coming simulating some kind of shock . . .

## 1.3.9 Methods used in Version 5, 5b, 5bPy3, 5c, 5c fd

#### 1.3.9.1 planConsumptionInValueV5

• The method (or command) planConsumptionInValueV5,<sup>37</sup> sent to entrepreneurs or workers, produces the following evaluations, detailed in commonVar.py file.

Consumption behavior with

$$C_i = a_k + b_k Y_i + u \tag{1.24}$$

with  $u \sim \mathcal{N}(0, common.consumptionRandomComponentSD)$ .

The individual i can be:

- 1. an entrepreneur, with  $Y_i = profit_{i,t-1} + wage$ ;
- 2. an employed worker, with  $Y_i = wage$  and the special <sup>38</sup> case  $Y_i = wc_t^i$ , with  $wc_t^i$  defined in eq.1.21;
- 3. an unemployed workers, with  $Y_i = socialWelfareCompensation$ .

The  $a_k$  and  $b_k$  values are set via the file commonVar.py and reported in output, when the program starts, via the parameters.py.

The code in Agent.py is:

```
# compensation
def planConsumptionInValueV5(self):
    self.consumption=0
    #case (1)
    \#Y1=profit(t-1)+wage NB no negative consumption if profit(t-1) < 0
    # this is an entrepreneur action
    if self.agType == "entrepreneurs":
        self.consumption = common.a1 + \
                           common.b1 * (self.profit + common.wage) + \
                           gauss(0,common.consumptionRandomComponentSD)
        if self.consumption < 0: self.consumption=0
        \#profit, in V2, is at time -1 due to the sequence in schedule2.xls
    \#case (2)
    #Y2=wage
    if self.agType == "workers" and self.employed:
      # the followin if/else structure is for control reasons because if
      # not common.wageCutForWorkTroubles we do not take in account
      # self.workTroubles also if != 0; if = 0 is non relevant in any case
      if common.wageCutForWorkTroubles:
        self.consumption = common.a2 + \
                           common.b2 * common.wage*(1.-self.workTroubles) + \
```

 $<sup>^{37}</sup>$ Related to Version 5

<sup>&</sup>lt;sup>38</sup>Activated if the common value wageCutForWorkTroubles is true

```
gauss (0, common.consumptionRandomComponentSD)
    #print "worker", self.number, "wage x",(1.-self.workTroubles)
 else:
   self.consumption = common.a2 + \
                       common.b2 * common.wage + \
                       gauss (0, common.consumptionRandomComponentSD)
#case (3)
#Y3=socialWelfareCompensation
if self.agType == "workers" and not self.employed:
    self.consumption = common.a3 + \
                       common.b3 * common.socialWelfareCompensation + \
                       gauss(0,common.consumptionRandomComponentSD)
#update totalPlannedConsumptionInValueInA_TimeStep
\verb|common.totalPlannedConsumptionInValueInA\_TimeStep+=self.consumption| \\
#print "C sum", common.totalPlannedConsumptionInValueInA_TimeStep
self.consumptionPlanningInCycleNumber=common.cycle
```

The conclusion updates the *common* value totalPlannedConsumptionInValueInA\_TimeStep, cleaned at each reset, i.e., at each time step in modelActions.txt.

The totalPlannedConsumptionInValueInA\_TimeStep measure will be then randomly corrected within the setMarketPriceV3 method of the *WorldState* meta-agent, see page 63.

#### 1.3.9.2 evaluateProfitV5

• The method (or command) evaluateProfitV5, <sup>39</sup> sent to the entrepreneurs, orders them to calculate their profit. Being  $P_t^i$  the production and the labor force  $L_t^i$  measured via the network connecting the entrepreneur to her workers plus 1 to take in account the entrepreneur herself.

The use of  $P_t^i$ , the actual production of the entrepreneurs, accounts both for the production plan decided with adaptProductionPlan, page 41, and for the limits in hiring, if any, as in hireFireWithProduction, page 36. The sum of all the actual productions of each entrepreneur is used, as at page 62, in setMarketPriceV3.

The method has been improved in version 2, to manage extra costs for the new entrant firms, but keeping safe the backward compatibility of the method.

 $p_t$  is the price, clearing the market at time t and it is calculated by the abstract item WorldState via the method setMarketPrice, as explained in Section 1.3.16.

<sup>&</sup>lt;sup>39</sup>Related to Version 5.

w is the wage per employee and time unit, set to 1.0 in common variable space, not changing with t, but the case of the important events of:

- wage rise due both to full employment (Subsection 1.3.7.1) and
- to the creation of barriers against new entrants (Subsection 1.3.7.3).

C are extra costs for new entrant firms. They are calibrated to assure the effectivness of the action described in Subsection 1.3.7.3, but in a non deterministic way, thanks to the movements in prices.

If the *common* variable wageCutForWorkTroubles is set to *True* the costs determination takes in account the reduction in the wages (but the wage of the entrepreneur, not changing).

Considering the presence of work troubles (see subsection 1.3.8.1) the determination of the clearing price, as at page 62, can signal an increase in the equilibrium price, due to the lacking production.

The (relative) shock  $\psi_{i,t} > 0$  due to work troubles is defined in subsection 1.3.8.1.

In presence of work troubles the firm has to accept a reduction of its price, to compensate its customers for having undermined the confidence in the implicit commitment of producing a given quantity (the production plan, specified in subsection 1.3.4.1).

That penalty value, as a relative measure, is in *common* as penaltyValue and here shortly as pv. Locally,  $pv_t^i$ , for the firm i at time t, is set to pv if  $\psi_{i,t} > 0$ ; otherwise  $(\psi_{i,t} = 0)$  is set to 0.

The profit evaluation, if wageCutForWorkTroubles is set to True, is:

$$\Pi_t^i = p_t(1 - pv_t^1)P_t^i - (w - \psi_{i,t})(L_t^i - 1) - 1w - C$$
(1.25)

being 1w the wage of the entrepreneur.

If wageCutForWorkTroubles is set to False, the result is:

$$\Pi_t^i = p_t (1 - p v_t^i) P_t^i - w L_t^i - C \tag{1.26}$$

The experiments run in April 2017 for the final version for the Italian economic journal have the penalty value  $pv_t^i$  set to 0.

The new entrant firms have extra costs C to be supported, retrieved in XC variables, but only for k periods, as stated in commonVar.py and activated by method toEntrepreneur.

The code is:

```
def evaluateProfitV5(self):
    # this is an entrepreneur action
    if self.agType == "workers":
       return
    # backward compatibily to version 1
        XC = common.newEntrantExtraCosts
    except BaseException:
       XC = 0
    try:
       k = self.extraCostsResidualDuration
    except BaseException:
       k = 0
    if k == 0:
       XC = 0
    if k > 0:
        self.extraCostsResidualDuration -= 1
    # the number of pruducing workers is obtained indirectly via
    # production/laborProductivity
    # print self.production/common.laborProductivity
    # how many workers, not via productvity due to possible troubles
    # in production
    laborForce = gvf.nx.degree(common.g, nbunch=self) + \
       1 # +1 to account for the entrepreneur herself
    # the followin if/else structure is for control reasons because if
    # not common.wageCutForWorkTroubles we do not take in account
    # self.workTroubles also if != 0; if = 0 is non relevant in any case
    if common.wageCutForWorkTroubles:
        self.costs = (common.wage - self.hasTroubles) \
            * (laborForce - 1) \
            + common.wage * 1 +
           ХC
        \# above, common.wage * 1 is for the entrepreur herself
    else:
        self.costs = common.wage * laborForce + \
    # print "I'm entrepreur", self.number, "costs are", self.costs
    # penalty Value
    if self.hasTroubles > 0:
        pv = common.penaltyValue
    \# the entrepreur sells her production, which is contributing - via
    # totalActualProductionInA_TimeStep, to price formation
    self.profit = common.price * (1. - pv) * self.production - self.costs
    print("I'm entrepreur", self.number, "my price is ",
          common.price \star (1. - pv))
    # individual data collection
    # creating the dataframe
    try:
        common.dataCounter
```

### 1.3.10 Methods used in Versions 0, 1, 2, 3, 4

#### 1.3.10.1 produce

• The method (or command) produce, <sup>40</sup> sent to the entrepreneurs, orders them—in a deterministic way, in each unit of time—to produce proportionally to their labour force, obtaining profit  $\Pi_t^i$ , where i identifies the firm and t the time.

 $L_t^i$  is the number of workers of firm i at time t, and also the number of its links. We add 1 to  $L_t^i$ , to account for the entrepreneur as a worker.  $\pi$  is the laborProductivity, with its value set to 1 in common variable space, currently not changing with t.  $P_t^i$  is the production of firm i at time t.

The production is:

$$P_t^i = \pi(L_t^i + 1) (1.27)$$

The production of the  $i^{\text{th}}$  firm is added to the total production of the time step, in the variable totalProductionInA\_TimeStep of the *common* space. The code is:

```
# produce
def produce(self):
    # this is an entrepreneur action
    if self.agType == "workers": return
# to produce we need to know the number of employees
```

<sup>&</sup>lt;sup>40</sup>Related to Versions 0, 1, 2. 3, 4, 5

We calculate the laborForce, i.e.  $L_t^i$ , counting the number of links or edges from the firm to the workers. We prefer this 'on the fly" evaluation to the internal variable self.numOfWorkers, to be absolutely sure of accessing the last datum in case of modifications coming from other procedures. E.g., a random subtraction or addition of workers to firms coming simulating some kind of shock . . .

# 1.3.11 Methods used in Versions 0, 1, 2, 3, 4, 5, 5b, 5bPy3, 5c, 5c fd

#### 1.3.11.1 fireIfProfit

• The method (or command) fireIfProfit,<sup>41</sup> sent to the entrepreneurs, orders them—in a probabilistic way (50% of probability in versions 0, 1, 2; in version 3 and 4, considering that the probability is set directly in the schedule.xls file, we eliminate the effect of this command setting the probability to 0.01<sup>42</sup>), in each unit of time—to fire a worker (choosing her/him randomly in the list of the employees of the firm) if the profit (last calculation, i.e., current period as shown in the sequence contained in schedule.xls) is less than the value firingThreshold (temporary: 0):

$$\Pi_t^i < firingThreshold \rightarrow fire$$
 (1.28)

```
# fireIfProfit
def fireIfProfit(self):
    # workers do not fire
    if self.agType == "workers": return
```

 $<sup>^{41} \</sup>text{Used}$  in Versions 0, 1, 2, (temporary) 3, 4 and 5, 5b, 5bPy3, 5c, 5c\_fd.

<sup>&</sup>lt;sup>42</sup>Being 0 not allowed, see the Reference Handbook, subsection *The detailed scheduling mechanism within the Model (AESOP level)* 

```
if self.profit>=common.firingThreshold: return
# the list of the employees of the firm
entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
#print "entrepreneur", self.number, "could fire", entrepreneurWorkers
#the list returnes by nx is unstable as order
entrepreneurWorkers = mySort(entrepreneurWorkers)
if len(entrepreneurWorkers) > 0:
    fired=entrepreneurWorkers[randint(0,len(entrepreneurWorkers)-1)]
    gvf.colors[fired]="OrangeRed"
    fired.employed=False
    common.g_edge_labels.pop((self, fired))
    common.g.remove_edge(self, fired)
    # count edges (workers) after firing (recorded, but not used
    # directly)
    self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
    # nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.
    print "entrepreneur", self.number, "has", \setminus
          self.numOfWorkers, "edge/s after firing"
```

See page 38 for the technical detail of the function mySort.

### 1.3.12 Methods used in Versions 1, 2, 3, 4

#### 1.3.12.1 evaluateProfit

• The method (or command) evaluateProfit,<sup>43</sup> sent to the entrepreneurs, orders them to calculate their profit. Being  $P_t^i$  the production and  $\pi$  the labor productivity, we have the labor force  $L_t^i = P_t^i/\pi$ 

The use of  $P_t^i$ , the actual production of the entrepreneurs, accounts both for the production plan decided with adaptProductionPlan, page 41, and for the limits in hiring, if any, as in hireFireWithProduction, page 36. The sum of all the actual productions of each entrepreneur is used, as at page 62, in setMarketPriceV3.

The method has been improved in version 2, to manage extra costs for the new entrant firms, but keeping safe the backward compatibility of the method.

 $p_t$  is the price, clearing the market at time t and it calculated by the abstract item WorldState via the method setMarketPrice, as explained in Section 1.3.16.

<sup>&</sup>lt;sup>43</sup>Related to Versions 1, 2, 3, 4.

w is the wage per employee and time unit, set to 1.0 in common variable space, not changing with t. C are extra costs for new entrant firms.

The profit evaluation is:

$$\Pi_t^i = p_t P_t^i - w L_t^i - C \tag{1.29}$$

The new entrant firms have extra costs to be supported, retrieved in XC variables, but only for k periods, as stated in commonVar.py and activated by method to toEntrepreneur.

The code is:

```
# calculateProfit
def evaluateProfit(self):
    # this is an entrepreneur action
    if self.agType == "workers": return
    # backward compatibily to version 1
    try: XC=common.newEntrantExtraCosts
    except: XC=0
    try: k=self.extraCostsResidualDuration
    except: k=0
    if k==0: XC=0
    if k>0: self.extraCostsResidualDuration-=1
    # the number of pruducing workers is obtained indirectly via
    # production/laborProductivity
    #print self.production/common.laborProductivity
    self.costs=common.wage * (self.production/common.laborProductivity) + \
    # the entrepreur sells her production, which is contributing - via
    # totalActualProductionInA_TimeStep, to price formation
    self.profit=common.price * self.production - self.costs
    common.totalProfit+=self.profit
```

#### 1.3.12.2 planConsumptionInValue

• The method (or command) planConsumptionInValue, 44 sent to entrepreneurs or workers, produces the following evaluations, detailed in commonVar.py file.

The method (or command) planConsumptionInValue operates both with the entrepreneurs and the workers, producing the following evaluations, using the parameters reported, as an example, into Table 1 of Mazzoli *et al.* (2017). The description below is unique for both the cases.

<sup>&</sup>lt;sup>44</sup>Related to Version 2, 3, 4

The resulting consumption behavior if the agent i at time t is:

$$C_t^i = a_i + b_i Y_t^i + u (1.30)$$

with  $u \sim \mathcal{N}(0, common.consumptionRandomComponentSD)$ .

Considering w as wage, as above, and P for profit, the individual i can be:

- case j = 1: an entrepreneur, with  $Y_t^i = P_{t-1}^i + w_t$ ;
- case j = 2: an employed worker at time t, with  $Y_i = w$  and the special <sup>45</sup> case  $Y_t^i = wc_t^i$ , with  $wc_t^i$  defined in eq. 1.21;
- case j = 3: an unemployed worker at time t, with  $Y_t^i = sw$  (sw = social wage, as a welfare intervention).

The  $a_j$  and  $b_j$  values are reported in the initial output of each run; we set them via the parameters.py.

The code in Agent.py is:

```
# compensation
def planConsumptionInValue(self):
    self.consumption=0
    #case (1)
    \#Y1=profit(t-1)+wage NB no negative consumption if profit(t-1) < 0
    # this is an entrepreneur action
    if self.agType == "entrepreneurs":
        self.consumption = common.a1 + \
                           common.b1 * (self.profit + common.wage) + \
                           gauss(0,common.consumptionRandomComponentSD)
        if self.consumption < 0: self.consumption=0
        \mbox{\#profit,} in V2, is at time -1 due to the sequence in schedule2.xls
    #case (2)
    #Y2=wage
    if self.agType == "workers" and self.employed:
        self.consumption = common.a2 + \
                           common.b2 * common.wage + \
                           gauss(0,common.consumptionRandomComponentSD)
    #case (3)
    #Y3=socialWelfareCompensation
    if self.agType == "workers" and not self.employed:
        self.consumption = common.a3 + \
                           common.b3 * common.socialWelfareCompensation + \
                           gauss(0,common.consumptionRandomComponentSD)
    #update totalPlannedConsumptionInValueInA_TimeStep
    \verb|common.totalPlannedConsumptionInValueInA_TimeStep+=self.consumption| \\
    #print "C sum", common.totalPlannedConsumptionInValueInA_TimeStep
```

<sup>&</sup>lt;sup>45</sup>Activated if the parameter *cut also the wages* is set to *yes* 

The individual  $C_t^i$  updates totalPlannedConsumptionInValueInA\_TimeStep (a common value), cleaned at each reset, i.e., at each new time step.

The totalPlannedConsumptionInValueInA\_TimeStep measure will be then randomly corrected within the setMarketPriceV3 method of the *WorldState* meta-agent, see page 63.

### 1.3.13 Methods used in Version 2 only

#### 1.3.13.1 toEntrepreneur

• With the method (or command) to Entrepreneur,  $^{46}$  sent to workers, the agent, being a worker, decides if to became an entrepreneur at time t, if its employer has a profit  $\geq$  a given threshold in t. The threshold is retrieved from the variable threshold To Entrepreneur.

The agent changes its internal type, position (not completely at the left as the original entrepreneurs, but if it was an entrepreneur moved to worker and coming back, it goes completely at the left) and color and it deletes the previous edge to the entrepreneur/employer. Finally, it starts counting the k periods of extra costs (to k is assigned the value common.ExtraCostsDuration, in the measure stated in common.newEntrantExtraCosts.

The code in Agent.py is:

#### 1.3.13.2 toWorker

• With the method (or command) toWorker, <sup>47</sup> an entrepreneur moves to be an unemployed worker if its profit at time t is  $\leq$  a given threshold in t. The threshold is retrieved from the variable thresholdToWorker.

<sup>&</sup>lt;sup>46</sup>Related to Version 2.

<sup>&</sup>lt;sup>47</sup>Related to Version 2.

The agent changes its internal type, position (not completely at the right as the original workers, but if it was a worker moved to entrepreneur and coming back, it goes completely at the right) and color and it deletes the previous edge to the workers/employee if any.

The code in Agent.py is:

```
if self.profit <= common.thresholdToWorker:</pre>
   print "I'm entrepreneur %2.0f and my profit is %4.2f" %\
          (self.number, self.profit)
    # the list of the employees of the firm, IF ANY
   entrepreneurWorkers=gvf.nx.neighbors(common.g, self)
   print "entrepreneur", self.number, "has", len(entrepreneurWorkers),\
     "workers to be fired"
   if len(entrepreneurWorkers) > 0:
        for aWorker in entrepreneurWorkers:
            gvf.colors[aWorker]="OrangeRed"
            aWorker.employed=False
            common.g.remove_edge(self, aWorker)
   self.numOfWorkers=0
    #originally, it was an entrepreneur
   if self.xPos<0:gvf.pos[self] = (self.xPos+15, self.yPos)</pre>
    #originally, it was a worker
   else:gvf.pos[self] = (self.xPos, self.vPos)
    # colors at http://www.w3schools.com/html/html_colornames.asp
   gvf.colors[self]="OrangeRed"
   self.agType="workers"
   self.employed=False
```

#### 1.3.13.3 setMarketPriceV2

- The method (or command) setMarketPriceV2, 48 sent to the WorldState, orders it to evaluate the market clearing price. This method uses two common variables:
  - totalProductionInA\\_TimeStep, generated by the agents (entrepreneurs),via produce;
  - totalPlannedConsumptionInValueInA\_TimeStep, generated by the agents (entrepreneurs and workers) via planConsumptionInValue.

See below the Section 1.3.16 and specifically Section 1.3.16.2.

 $<sup>^{48}</sup>$ Related to Version 2.

### 1.3.14 Methods used in Version 1 only

#### 1.3.14.1 setMaketPriceV1

• The method (or command) setMarketPriceV1, 49 sent to the WorldState, orders it to evaluate the market clearing price. See below Section 1.3.16 and specifically Section 1.3.16.1.

### 1.3.15 Methods used in Version 0 only

#### 1.3.15.1 evaluateProfitV0

• The method (or command) evaluateProfitV0,  $^{50}$  sent to the entrepreneurs, orders them to calculate their profit. Being  $P_t^i$  the production and  $\pi$  the labor productivity, we have the labor force  $L_t^i = P_t^i/\pi$ 

R is revenuesOfSalesForEachWorker, set to 1.005 in common variable space, not changing with t; w is the wage per employee and time unit, set to 1.0 in common variable space, not changing with t.  $u_t^i \sim \mathcal{N}(0, 0.05)$  is a random normal addendum.

The profit evaluation is:

$$\Pi_t^i = L_t^i(R - w) + u_t^i \tag{1.31}$$

The code is:

#### 1.3.15.2 hireIfProfit

• The method (or command) hireIfProfit,<sup>51</sup> sent to the entrepreneurs, orders them—in a probabilistic way (50% of probability in Version 0 case), in

<sup>&</sup>lt;sup>49</sup>Related to Version 1.

<sup>&</sup>lt;sup>50</sup>Related to Version 0.

 $<sup>^{51}</sup>$ Used in Version 0.

each unit of time—to hire a worker (random choosing her/him in a temporary list of unemployed people) if the profit (last calculation, i.e., current period as shown in the sequence contained in schedule.xls) is a than the value hiringThreshold (temporary: 0):

$$\Pi_t^i > hiringThreshold \to hire$$
 (1.32)

As first attempt the hiringThreshold is 0 (in commonVar.py). We can modify this internal value, as others, while the simulation is running, via the *WorldState* feature, introduced below.

The code of the hireIfProfit method is:

```
# hireIfProfit
   def hireIfProfit(self):
        # workers do not hire
       if self.agType == "workers": return
        if self.profit<=common.hiringThreshold: return</pre>
       tmpList=[]
        for ag in self.agentList:
           if ag != self:
              if ag.agType=="workers" and not ag.employed:
                 tmpList.append(ag)
        if len(tmpList) > 0:
           hired=tmpList[randint(0,len(tmpList)-1)]
           hired.employed=True
           gvf.colors[hired]="Aqua"
            gvf.createEdge(self, hired) #self, here, is the hiring firm
        # count edges (workers) of the firm, after hiring (the values is
        # recorded, but not used directly)
       self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
        # nbunch : iterable container, optional (default=all nodes)
        # A container of nodes. The container will be iterated through once.
       print "entrepreneur", self.number, "has", \
              self.numOfWorkers, "edge/s after hiring"
```

## 1.3.16 Other features in scheduling

We also have two more sophisticates structures: the WorldState feature and the macros.

• Running a project—if we define the WorldState.py file—at the beginning of the output, we read:

World state has been created.

What does it mean?

The WorldState class interacts with the agents; we use a unique instance of the class.

The variables managed via WordState have to be added, with their methods, within the instance of class, with set/get methods for each variable.

In Agent.py we can ask to the WorldState, via get, for the values of the variables.

With the oligopoly project we made a step ahead, asking to the Worl-State to make a specific calculations about the whole state of the world. This capability has been incorporated in SLAPP since version 1.11 and has been definitively set with the reengineering of WorldState in version 1.33 of SLAPP.

The normal use has in Col. B a value and in Col. C the method used to set that value into the WorldState; it will be retrieved by the agents using a symmetric get method.<sup>52</sup>

If in Col. B we have the expression computationalUse<sup>53</sup>, the content of Col. C is a special method making world calculations.

A few examples, with their code, are below.

#### 1.3.16.1 setMarketPriceV1 as in WorldState, with details

• The method (or command) setMarketPriceV1,<sup>54</sup> sent to the WorldState, orders it to evaluate the market clearing price.

Setting the aggregate-demand  $D_t$  as equal to the production:

$$D_t = \sum_i P_t^i \tag{1.33}$$

We have the demand function, with  $p_t$  as price:

$$p_t = a + bD_t (1.34)$$

With the planned production coming from a Poisson distribution as in Eq. 1.13, considering  $\nu$  set to 4, we can set two consistent points (p, D) as (1, 20) and (0.8, 30) obtaining:

$$p_t = 1.4 - 0.02D_t \tag{1.35}$$

<sup>&</sup>lt;sup>52</sup>These methods have to be implemented by the user, see the example in the *basic* project.

<sup>&</sup>lt;sup>53</sup>the expression *specialUse* is still working, but it is deprecated.

<sup>&</sup>lt;sup>54</sup>Introduced above as related to Version 1 only.

The resulting code in WorldState.py is:

```
# set market price
def setMarketPriceV1(self):
    # to have a price around 1
    common.price= 1.4 - 0.02 * common.totalProductionInA_TimeStep
    print "Set market price to ", common.price
    common.price10=common.price*10 #to plot
```

#### 1.3.16.2 setMarketPriceV2, as in WorldState, with details

• The method (or command) setMarketPriceV2, 55 sent to the WorldState, orders it to evaluate the market clearing price considering each agent behavior.

Having:

$$p_t = D_t/O_t \tag{1.36}$$

with  $p_t$  clearing market price at time t;  $D_t$  demand in value at time t;  $O_t$  offer in quantity (the production) at time t.

As defined above (p. 58), the method uses two common variables:

- totalProductionInA\_TimeStep, generated by the agents (entrepreneurs), via produce;
- totalPlannedConsumptionInValueInA\\_TimeStep, generated by the agents (entrepreneurs and workers) via planConsumptionInValue.

The resulting code in WorldState.py is:

#### 1.3.16.3 setMarketPriceV3, as in WorldState, with details

• The method (or command) setMarketPriceV3, 56 sent to the WorldState, orders it to evaluate the market clearing price considering each agent behavior and an external shock, potentially large.

<sup>&</sup>lt;sup>55</sup>Introduced above as related to Version 2 only.

<sup>&</sup>lt;sup>56</sup>Introduced above as related to Version 3, 4 and 5.

We introduce a shock  $\Xi$  uniformly distributed between -L and +L where L is a rate on base 1, e.g., 0.10. To keep the effect as symmetric, we have the following equations determining the clearing price:

If the shock  $\Xi$  is  $(\geq 0)$ :

$$p_t = \frac{D_t(1+\Xi)}{O_t} \tag{1.37}$$

if the shock  $\Xi$  is (< 0):

$$p_t = \frac{D_t/(1+\Xi)}{O_t}$$
 (1.38)

with  $p_t$  clearing market price at time t;  $D_t$  demand in value at time t;  $O_t$  offer in quantity (the production) at time t.

The  $\Xi$  parameter is reported in the prologue of the execution as Total demand relative random shock, uniformly distributed between  $-\Xi\%$  and  $+\Xi\%$ .

As defined above (p. 58), the method uses two common variables:

- totalProductionInA\_TimeStep, generated by the agents (entrepreneurs), via produce;
- totalPlannedConsumptionInValueInA\_TimeStep, generated by the agents (entrepreneurs and workers) via planConsumptionInValue.

The resulting code in WorldState.py is:

```
# set market price V3
def setMarketPriceV3(self):
   shock0=random.uniform(-common.maxDemandRelativeRandomShock, \
                         common.maxDemandRelativeRandomShock)
   print "\n-----"
   if shock >= 0:
     common.totalDemandInPrevious_TimeStep = \
        common.totalPlannedConsumptionInValueInA_TimeStep * \
        (1 + shock)
     common.price= (common.totalPlannedConsumptionInValueInA_TimeStep * \
                    (1 + shock)) \
                    / common.totalProductionInA_TimeStep
     print "Relative shock (symmetric) ", shock0
     print "Set market price to ", common.price
   if shock < 0:
     shock \star=-1. #always positive, boing added to the denominator
     common.totalDemandInPrevious_TimeStep = \
         common.totalPlannedConsumptionInValueInA_TimeStep / \
         (1 + shock)
     common.price= (common.totalPlannedConsumptionInValueInA_TimeStep / \
```

#### 1.3.16.4 setMarketPriceV6, as in WorldState, with details

• The method (or command) setMarketPriceV6,<sup>57</sup> sent to the WorldState, orders it to evaluate the market clearing price considering each agent behavior and an external shock, potentially large in the pre-hayekian phase and successively to record the mean and the standard deviation to the hayekian prices in each cycle.

About the pre-hayekian phase look at Section 1.3.16.3. In the code reported here, the new part uses the function coded as:

```
def checkHayekianPrices(a):
    # list a not empty
    if a!=[]: m = statistics.mean(a)
    else: m = -100 # -100 will not appear in graphs
    # and with at least one element
    if len(a)>1: sd = statistics.stdev(a)
    else: sd=-100 # -100 will not appear in graphs
    return (m,sd)
```

strictly related to the code of the method actOnMarketPlace of agent.py. The resulting code in WorldState.py is:

 $<sup>^{57}</sup>$ Introduced above as related to Version 6, jumping in numbering from 3 to 6.

```
if shock < 0:
      shock \star = -1. # always positive, boing added to the denominator
      common.totalDemandInPrevious_TimeStep = \
          \verb|common.totalPlannedConsumptionInValueInA_TimeStep|/| \\ | \\ |
          (1 + shock)
      common.price=(common.totalPlannedConsumptionInValueInA_TimeStep \
                      /(1 + shock))
                      / common.totalProductionInA_TimeStep
       print("Relative shock (symmetric) ", shock0)
       print("Set market price to ", common.price)
else:
    (common.price, common.hPriceSd) = checkHayekianPrices(\
          common.hayekianMarketTransactionPriceList_inACycle)
   print("Hayekian phase (NA as not available values)")
   if common.price != -100: print("Mean price ",common.price)
                               print("Mean price NA")
   if common.hPriceSd != -100: print("Mean price s.d.",common.hPriceSd)
                               print("Mean price s.d. NA")
   else:
print("----\n")
```

## ${\bf 1.3.16.5} \quad {\bf full Employment Effect On Wages}, \ {\bf as} \ {\bf in} \ {\bf World State}, \ {\bf with} \ {\bf details}$

Being  $U_t$  the unemployment rate at time t,  $\zeta$  the unemployment threshold to recognize the *full employment* situation, s the proportional increase step (reversible) of the wage level and  $w_t$  the wage level at time t (being  $w_0$  the initial level), we have:

$$\begin{cases} w_t = w_0(1+s) \text{ if } U_t \le \zeta \\ w_t = w_0 \text{ if } U_t > \zeta \end{cases}$$
 (1.39)

The code in WorldState.py is:

```
# shock to wages (full employment case)
def fullEmploymentEffectOnWages(self):
      # wages: reset incumbent action if any
      if common.wageAddendum > 0:
          common.wage -= common.wageAddendum
          common.wageAddendum = 0
      # employed people
      peopleList=common.g.nodes()
      totalPeople=len(peopleList)
      totalEmployed=0
      for p in peopleList:
          if p.employed: totalEmployed+=1
      #print totalPeople, totalEmployed
      unemploymentRate=1. - float(totalEmployed)/ \
                            float(totalPeople)
      if not common.fullEmploymentStatus and \
```

```
unemploymentRate <= common.fullEmploymentThreshold:
    common.wage*=(1 + common.wageStepInFullEmployment)
    common.fullEmploymentStatus=True

if common.fullEmploymentStatus and \
    unemploymentRate > common.fullEmploymentThreshold:
        common.wage/=(1 + common.wageStepInFullEmployment)
        common.fullEmploymentStatus=False
```

#### 1.3.16.6 randomShocksToWages, as in WorldState, with details

• The method is used only in the model building phase, to verify the sensitivity of the model to changes in wages.

Being w the wage per employee defined in the setup, so  $w_1$ , from t=2 we have:

$$- \text{ if } u_t \ge 0$$

$$w_t = w_{t-1}(1+ut)$$
(1.40)

$$- \text{ if } u_t < 0$$

$$w_t = w_{t-1}/(1 + |u_t|) \tag{1.41}$$

with  $u_t \sim \mathcal{U}(-k, k)$  and k tentatively set to 0.10 or 10%.

The code in WorldState.py is:

```
# random shock to wages (temporary method to experiment with wages)
def randomShockToWages(self):
    k=0.10
    shock= uniform(-k,k)

if shock >= 0:
    common.wage *= (1.+shock)

if shock < 0:
    shock *= -1.
    common.wage /= (1.+shock)</pre>
```

## 1.3.16.7 incumbentActionOnWages, as in WorldState, with details

The current number of entrepreneurs  $H_t$  is calculated from the network and the previous one  $H_{t-1}$  is extracted from the structural dataframe (see collectStructuralData at page 13).

The wage level has two components, mutually exclusive:

1. the effects of full employment on wages, as in Section 1.3.16.5;

2. the effect described in this Section about incumbent oligopolists strategically increasing wages to create an artificial barrier against new entrants; the new entrepreneurs suffer temporary extra costs, so for them the wage increment can generate so relevant losses to produce their bankruptcy.

We have here two levels: K as the (relative) threshold of entrepreneur presence to determine the reaction on wages and k as the relative increment of wages.

Formally, in case 2 above:

$$\begin{cases} w_t = w_0(1+k) \text{ if } \frac{H_t}{H_{t-1}} - 1 > K \\ w_t = w_0 \text{ if } \frac{H_t}{H_{t-1}} - 1 \le K \end{cases}$$
(1.42)

The code in WorldState.py is:

```
# incumbents rising wages as na entry barrier
def incumbentActionOnWages(self):
    # current number of entrepreneurs
    peopleList=common.g.nodes()
    nEntrepreneurs=0
    for p in peopleList:
      if p.agType=="entrepreneurs": nEntrepreneurs+=1
    nEntrepreneurs=float (nEntrepreneurs)
    # previous number of entrepreneurs
    nEntrepreneurs0=common.str_df.iloc[-1,0] # indexes Python style
    #print nEntrepreneurs, nEntrepreneurs0
    # wages: reset incumbent action if any
    if common.wageAddendum > 0:
        common.wage -= common.wageAddendum
        common.wageAddendum = 0
    # wages: set
    if nEntrepreneurs > 1:
      if nEntrepreneurs / nEntrepreneurs0 - 1 > \
            common.maxAcceptableOligopolistRelativeIncrement:
        common.wageAddendum = common.wage *\
           common.temporaryRelativeWageIncrementAsBarrier
        common.wage += common.wageAddendum
```

#### 1.3.16.8 Macros

• Just a memo: we also have the possibility of using macros contained in separated sheets of the schedule.xls file (not used presently here).

To know more, use the SLAPP (Swarm-Like Protocol in Python) Reference Handbook on line at https://github.com/terna/SLAPP, looking for the item macros within the Index.

## **Bibliography**

Boero, R., Morini, M., Sonnessa, M. and Terna, P. (2015). Agent-based Models of the Economy Agent-based Models of the Economy – From Theories to Applications. Palgrave Macmillan, Houndmills.

URL http://www.palgrave.com/page/detail/agentbased-models-of-theeconomy-/?K=9781137339805

Boettke, P. J. (1990). The theory of spontaneous order and cultural evolution in the social theory of FA Hayek. In «Cultural Dynamics», vol. 3(1), pp. 61–83.

Bowles, S., Kirman, A. and Sethi, R. (2017). Retrospectives: Friedrich Hayek and the Market Algorithm. In «Journal of Economic Perspectives», vol. 31(3), pp. 215-30.

URL http://www.aeaweb.org/articles?id=10.1257/jep.31.3.215

Hayek, F. A. (1994). *Hayek on Hayek: an autobiographical dialogue*, vol. edited by Stephen Kresge and Leif Wenar. University of Chicago Press:.

Lewis, P. (2014). Hayek: from Economics as Equilibrium Analysis to Economics as Social Theory. In R. Garrison and N. Barry, eds., Elgar Companion to Hayekian Economics. Edward Elgar Publishing, pp. 195–223.

URL https://ssrn.com/abstract=2546259

Mazzoli, M., Morini, M. and Terna, P. (2017). Business Cycle in a Macromodel with Oligopoly and Agents' Heterogeneity: An Agent-Based Approach. In «Italian Economic Journal», pp. 1–29.

URL http://rdcu.be/tlE6

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