

Oligopoly: the Making of the Simulation Model

Marco Mazzoli, Matteo Morini, and Pietro Terna

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Chapter 1

The *oligopoly* project: the making of the simulation model

Using SLAPP¹, the *oligopoly* project is contained in a stand alone folder, having the same name of the model.

Let us introduce the starting phase in a detailed way.

- We can launch the SLAPP shell in several ways.
 - We can launch SLAPP via the `runShell.py` file that we find in the main folder of SLAPP, from a terminal, with:
`python runShell.py`
 - Alternatively, we launch SLAPP via the `start.py` file that we find in the folder of SLAPP as a simulation shell, i.e.
`6 objectSwarmObserverAgents_AESOP_turtleLib_NetworkX`, from a terminal, with:
`python start.py`
 - Using IPython (e.g., in a Jupyter notebook) we go to the main folder of SLAPP (or we start Jupyter notebook) from there, and we can launch SLAPP via the `iRunShell.ipynb` file that we find in that main folder, simply clicking on it.

In all cases, we immediately receive the request of choosing a project:

Project name?

¹<https://github.com/terna/SLAPP>; SLAPP has a Reference Handbook at the same address and it is deeply described in Chapters 2–7 in Boero *et al.* (2015).

- We can predefining a default project: if we place *in the main SLAPP folder or in the folder* `objectSwarmObserverAgents_AESOP_turtleLib_NetworkX` a file named `project.txt` containing the path to the folder of the project we are working on (`oligopoly` in our case, with `/Users/pt/GitHub/oligopoly`, as an example of location), the initial message of SLAPP is:

```
path and project = /Users/pt/GitHub/oligopoly
do you confirm? ([y]/n):
```

- Resuming the explanation, we continue receiving the messages:

```
running in Python
debug = False
random number seed (1 to get it from the clock)
```

We have to enter an integer number (positive or negative) to trigger the sequence of the random numbers used internally by the simulation code. If we reply 1, the seed—used to start the generation of the random series—comes from the internal value of the clock at that instant of time. So it is different anytime we start a simulation run. This reply is useful to replicate the simulated experiments with different conditions. If we chose a number different from 1, the random sequence would be repeated anytime we will use that seed. This second solution is useful while debugging, when we need to repeat exactly the sequence generating errors, but also to give to the user the possibility of replicating exactly an experiment.

The `running in Python` sentence signals the we are running the program in plain Python. Alternatively, the message could be `running in IPython`. About running SLAPP in IPython have a look the the Handbook, in the SLAPP web site.²

- The program sends several messages about the project parameters, as specified into the file `commonVar.py` and managed via the file `parameters.py`, both in the project folder.

One of these messages reports the version of the project.

- The program informs us about the «sigma of the normal distribution used in randomizing the position of the agents/nodes», e.g., 0.7; this value produces uniquely a graphic effect, as in Figure 1.3.

²<https://github.com/terna/SLAPP>.

- We introduce now time management, split into several (consistent) levels of scheduling.

The general picture is that of Figure 1.1: in an abstract way we can imagine having a clock opening a series of containers or boxes. Behind the boxes, we have the *action groups*, where we store the information about the actions to be done.³



Figure 1.1: The representation of the schedule

1.1 The agents and their sets

We have files containing the agents of the different types. Those files are listed in a file with name `agTypeFile.txt`: in our case, it simply contains the record `entrepreneurs workers`.

- `entrepreneurs.txt` lists the agents of type `entrepreneurs`; it reports the identification numbers (currently from 1 to 10) and the x and y positions on the screen. See above the *sigma* value determining random shift from

³The structure is highly dynamical because we can associate a probability to an event, or an agent of the simulation can be programmed to add or eliminate one or more events into the boxes.

the stated positions; in this way, we can attribute close or equal positions to several entrepreneurs having them anyway visible in the map; if necessary, we can increase *sigma*:

```
1 -10 75
2 -10 65
3 -10 55
4 -10 45
5 -10 35
6 -10 70
7 -10 60
8 -10 50
9 -10 40
10 -10 30
```

- in Versions 0 to 2, "workers.txt" list the agents of type **workers**, *not used here*; it is reporting the identification numbers and the *x* and *y* positions on the screen; see above the *sigma* value determining random shift from the stated positions; in this way, we can attribute close or equal positions to several entrepreneurs having them anyway visible in the map; if necessary, we can increase *sigma*;
- the Version 3 of the **oligopoly** project uses the file **workers.txtx** where the extension **.txtx** or eXtended text, means that the file is built following the rule described into the Reference Handbook⁴, subsection "The use of files .txtx to define the agents".

In version 3 the content is:

```
1001@11000    10 &v=10*int((n-1001)/50)+5&
```

that we read in the following way:

- 1001@11000 as the order of creating 10 thousand workers, from number 1001 to number 11,000;
 - 10 is the constant value of the *x* coordinate of the worker-agents;
 - &v=10*int((n-1001)/50)+5& is a formula calculating the *y* coordinate of each agent:
- & opens and closes the formula;

⁴<https://github.com/terna/SLAPP>.

v is the result of the calculation, in our case the *y* coordinate;
n is the number of the agent, in the sequence generated in the interval from 1001 to 11,000.

- numbering starts from 1001 for the reasons explained at page 22.

The agents are created by `ModelSwarm.py` (in folder `$$$lapp$$$`) via the specific rules contained into the file `mActions.py`, specific for this project (indeed, the file is into the folder `oligopoly`).

```
def createTheAgent(self, line, num, leftX, rightX, bottomY, topY, agType):
    # explicitly pass self, here we use a function

    # workers
    if agType=="workers":
        anAgent = Agent(num, self.worldStateList[0],
                        float(line.split()[1])+random.gauss(0,common.sigma),
                        float(line.split()[2])+random.gauss(0,common.sigma),
                        agType=agType)
        self.agentList.append(anAgent)
        anAgent.setAgentList(self.agentList)

    # entrepreneurs
    elif agType=="entrepreneurs":
        anAgent = Agent(num, self.worldStateList[0],
                        float(line.split()[1])+random.gauss(0,common.sigma),
                        float(line.split()[2])+random.gauss(0,common.sigma),
                        agType=agType)
        self.agentList.append(anAgent)

    else:
        print "Error in file "+agType+".txt"
        os.sys.exit(1)
```

The following bullets describe how this code works.

- The number identifying the agent is read outside this function, as a mandatory first element in each line into a file containing agent descriptions. The content of the `agType` variable is directly the name of the agent file currently open.
- We check the input file, which has to contain three data per row. We modify the second and the third values with the *sigma* correction.

Each agent is added to the `agentList`.

1.1.1 Agents and reset action

The `reset` (see page 13) action, working into the scheduling of the model (Section 1.2.2), activates the method `setNewCycleValues` defined, as an empty step, in the

class `SuperAgent` in `agTools` of *SLAPP* (folder `$$$slapp$$`). In the `oligopoly` project, that method is redefined in `Agent.py`. The `reset` action acts once in each simulation cycle, because in our case is related only to common variables of the simulation. The agent executing the cleaning operation is that with the identifier (the variable *number*) equal to 1. If no agent has that identifier, all will be acting, with not useful repetitions of the same task.

As a consequence, in this project pay attention that at least one of the agents has 1 as identifier.

1.1.2 Sets of agents

The files containing the agents are of two families, the second one with two types of files:

- files listing the agents with their characteristics (if any): in folder `oligopoly` we have the files `entrepreneurs.txt` and `workers.txt`;
- files defining groups of agents:
 - the list of the types of agents (mandatory); from this list *SLAPP* searches the file describing the agents; as seen, in folder `oligopoly` we have the file `agTypeFile.txt` (the name of this file is mandatory) containing:

```
entrepreneurs workers
```

- the list of the operating sets of agents (optional); in folder `oligopoly` this file is missing. Indeed we receive the message
Warning: operating sets not found.

In the file `agOperatingSets.txt` (the name of this file is mandatory), with could place names of groups of agents, corresponding to files listing the agents in the group. Project verb "school" can be used as a useful example.

All the names contained in the file are related to other `.txt` or `.txtx` files reporting the identifiers of agents specified in the lists of the previous bullet. The goal of this feature is that of managing clusters of agents, recalling them as names in Col. A in `schedule.xls` file.

1.2 Macro scheduling

In *SLAPP*, we have the following three schedule mechanisms driving the events.

- Two of those mechanisms are operating in a *macro* way: one at the level of the Observer and the other of the Model, with recurrent sequences of actions to be done.⁵
- In our oligopoly code, these two sequences are reported in the files `observerActions.txt` and `modelActions.txt` in the folder of the project.

The explanations are in Section 1.2.1 and 1.2.2.

- The third sequence, operating in a *micro* way, is the more detailed one (see Section 1.2.3).

1.2.1 The scheduling mechanism at the level of the Observer



Figure 1.2: Time series generated by the model. version 4

- The first schedule mechanism is described in the first file (`observerActions.txt`), having content (unique row, remembering that anyway row changes are not relevant to this group of files):
 - version *without pauses* contained in `observerActions no pause.txt`, to be copied to `observerActions.txt` to run it:

⁵The level of the Observer is our level, where the experimenter looks at the model (the level of the Model) while it runs.

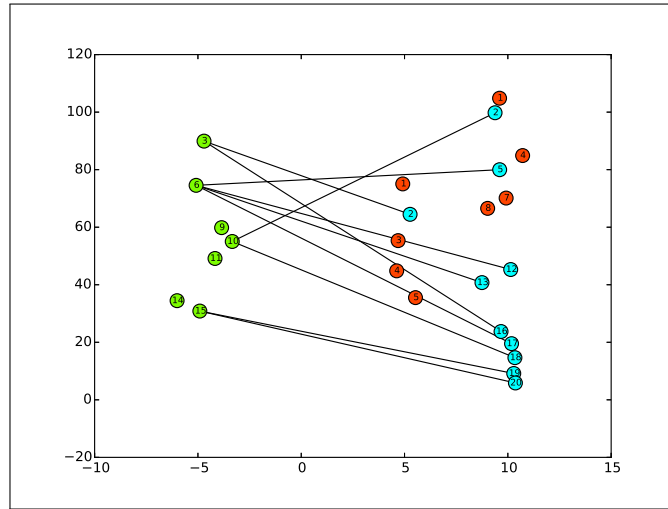


Figure 1.3: The agents (nodes), with random displacements, and links connecting entrepreneurs and workers

```
collectStructuralData modelStep collectTimeSeries
visualizePlot visualizeNet clock
```

- version *with pauses* contained in `observerActions` with `pause.txt`, to be copied to `observerActions.txt` to run it:


```
collectStructuralData modelStep collectTimeSeries
visualizePlot visualizeNet pause clock
```

The interpretation is the following.

- First of all, we have to take into consideration that the execution of the content of the file is “with repetition”, until an `end` item will appear (see below).
- `collectStructuralData` collects the number of workers and of entrepreneurs *at the beginning* of each period, both as a basis for internal calculations and for the final output of the model, when two files of data are generated.⁶
- `modelStep` orders to the model to make a step forward in time.
- `collectTimeSeries` collects the data of the outcomes of the simulation *at the end* of each period, both as a basis for the action of

⁶`collectTimeSeries`, `visualizePlot` and `saveTimeSeries` are contained in `"oActions.py"` and are all using `pandas` as dataframe manager (look at <http://pandas.pydata.org>).

`visualizePlot` and for the final output of the model, when two files of data are generated (with extension `.csv` and date and time⁷ in their names).⁶

- `visualizePlot` update the plot of the time series generated by the model (Figure 1.2).⁸
- `visualizeNet` update the windows reporting the links connecting entrepreneurs and workers, on a network basis (Figure 1.3).⁸
- `pause`, if any, puts the program in wait until we reply to the message Hit **enter** key to **continue**, hitting the key . This action is useful to examine the graphical outputs (as in Figures 1.2 and 1.3), step by step.
- `clock` asks the clock to increase its counter of one unit. When the count will reach the value we have entered replying to the **How many cycles?** query, the internal scheduler of the Observer will add the **end** item into the sequence of the file `observerActions.txt`. The item is placed immediately after the `clock` call. The **end** item stops the sequence contained in the file.
- (We can also consider a potential **prune** item, eliminating the links on the basis of their weight (in case, asking for a threshold below which we cut); weights could be introduced to measure the seniority—skill, experience—of the workers).

1.2.2 The scheduling mechanism at the level of the Model

- The second file—`modelActions.txt`—quoted above at the beginning of Section 1.2, is related to the second of the schedule mechanisms, i.e., that of the Model. About the Observer/Model dualism, the reference is to note 5.

It contains (unique row, remembering that anyway row changes are not relevant to this group of files):

```
reset read_script
```

The interpretation is the following.

⁷Avoiding `:` into the name, for compatibility reasons with Windows

⁸We can use both *visualizePlot* and *visualizeNet*—strictly in this order—or only one of them.

- Also at the Model level, we have to take into consideration that the execution of the content of the file is “with repetition”, never ending. It is the Observer that stops the experiment, but operating at its level.
- `reset` orders to the agents to make a reset, related to their variables. The order acts via the code in the file `ModelSwarm.py`.⁹ `reset` contains the `do0` variable, linking a method that is specified as a function in the file `mActions.py` in the folder of the project. In this way, the application of the basic method `reset` can be flexibly tailored to the specific applications, defining which variables to reset.

In our specific case, the content of the `do0` function in `mActions.py` asks all the agents to execute the method `setNewCycleValues`. The method is defined in an instrumental file (`agTools.py` in `$$$slapp$$`) and it is as default doing nothing. We can redefine it in `Agent.py` in the project folder.

Always in our case, as explained in Section 1.1.1, we suppose that the acting agent in resetting step would be that with 1 as identifier.

In our model, we clean the variables:

```
totalProductionInA_TimeStep,
totalPlannedConsumptionInValueInA_TimeStep,
totalProfit and
totalPlannedProduction
```

at the beginning of each step of the time. The code, in `Agent.py` is:

```
# reset values, redefining the method of agTools.py in $$$slapp$$
def setNewCycleValues(self):
    # the if is to save time, given that the order is arriving to
    # all the agents (in principle, to reset local variables)
    if not common.agentlexisting:
        print "At least one of the agents has to have number==1"
        print "Missing that agent, all the agents are resetting common values"

    if self.number==1 or not common.agentlexisting:
        common.totalProductionInA_TimeStep=0
        common.totalPlannedConsumptionInValueInA_TimeStep=0
        common.totalProfit=0
        common.totalPlannedProduction=0
```

- `read_script` orders to the Model to open a new level of scheduling, described in Section 1.2.3. The order acts via the code of the file `ModelSwarm.py`. We have here one of the stable instances of the class `ActionGroup` within the Model. The `ActionGroup` related to `read_script` item is the `actionGroup100` that contains the `do100` function, used internally within `ModelSwarm.py` to manage the script reported into the `schedule.xls` file (or directly into the `schedule.txt` one).

⁹That is in the `$$$slapp$$` folder.

1.2.3 The detailed scheduling mechanism within the Model (AESOP level)

AESOP comes from Agents and Emergencies for Simulating Organizations in Python.

- The third scheduling mechanism, as anticipated in Section 1.2, operates at a *micro* scale and it is based on a detailed script system that the Model executes while the time is running. The time is managed by the `clock` item in the sequence of the Observer.

The script system is activated by the item `read_script` in the sequence of the Model.

- This kind of script system does not exist in Swarm, so it is a specific feature of SLAPP, introduced as implementation of the AESOP (Agents and Emergencies for Simulating Organizations in Python) idea: a layer that describes in a fine-grained way the actions of the agents in our simulation models.
- Now we take in exam the timetable of our Oligopoly model.
- The file `schedule.xls` can be composed of several sheets, with: (a) the first one with name `schedule`; (b) the other ones with any name (those names are *macro instruction* names). We can recall the macro instructions in any sheet, but not within the sheet that creates the macro (that with the same name of the macro), to avoid infinite loops.

We differentiate the execution sequences in our model via the `schedule.xls` sheet contained in the folder `oligopoly`.

Within the sheet, we have the action containers as introduce above (Figure 1.1), starting with the sign `#`.

1.3 Micro scheduling: the AESOP level

From now on we explain the micro level of AESOP, i.e., the structure of the implementation of the Agents and Emergencies for Simulating Organizations in Python for the Oligopoly model,

1.3.1 Model versions via the AESOP level in scheduling

We have several versions of the model defined via the sequences of actions. To use one of them, we have to copy its schedule to the basic `schedule.xls` file.

1.3.1.1 Version 0 (GitHub: master), preliminary step

In `schedule0.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E and are missing) three columns:

```
#           1           100
entrepreneurs produce
entrepreneurs evaluateProfitV0
entrepreneurs 0.5       hireIfProfit
entrepreneurs 0.5       fireIfProfit
```

1.3.1.2 Version 1, random production as engine (GitHub: V1)

In `schedule1.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E and are missing) three columns:

```
#           1           100
entrepreneurs makeProductionPlan
entrepreneurs hireFireWithProduction
entrepreneurs produce
WorldState    specialUse           setMarketPriceV1
entrepreneurs evaluateProfit
entrepreneurs 0.5           fireIfProfit
```

1.3.1.3 Version 2 (GitHub: V2)

Here we have (i) random production as engine, (ii) individual demand curves with more realistic price determination, (iii) new entrant firms.

In `schedule2.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E and are missing) three columns:

```
#           1           100
entrepreneurs makeProductionPlan
entrepreneurs hireFireWithProduction
entrepreneurs produce
entrepreneurs planConsumptionInValue
workers       planConsumptionInValue
WorldState    specialUse           setMarketPriceV2
entrepreneurs evaluateProfit
entrepreneurs 0,5           fireIfProfit
workers       toEntrepreneur
entrepreneurs toWorker
```


1.3.1.4 Version 3 (GitHub: V3)

Here we have (i) random production only at time 1, (ii) adaptation in production plans , (iii) individual demand curves with more realistic price determination, (iv) new entrant firms.

In `schedule3.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E and are missing) three columns:

```
#          1          100
entrepreneurs      makeProductionPlan
entrepreneurs      adaptProductionPlan
entrepreneurs      hireFireWithProduction
entrepreneurs      produce
entrepreneurs      planConsumptionInValue
workers            planConsumptionInValue
WorldState         specialUse          setMarketPriceV3
entrepreneurs      evaluateProfit
entrepreneurs      0.0001              fireIfProfit
workers            toEntrepreneurV3
entrepreneurs      toWorkerV3
```

1.3.1.5 Version 4 (GitHub: V4)

Here we have (i) random production only at time 1, (ii) adaptation in production plans , (iii) individual demand curves with more realistic price determination, (iv) new entrant firms.

In `schedule4.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E) three columns:

```
#          1          100
entrepreneurs      makeProductionPlan
entrepreneurs      adaptProductionPlan
entrepreneurs      hireFireWithProduction
entrepreneurs      produce
entrepreneurs      planConsumptionInValue
workers            planConsumptionInValue
WorldState         specialUse          setMarketPriceV3
entrepreneurs      evaluateProfit
entrepreneurs      0.0001              fireIfProfit
workers            toEntrepreneurV3
entrepreneurs      toWorkerV3
WorldState         specialUse          sensitivity
WorldState         specialUse          fullEmploymentEffectOnWages
WorldState         specialUse          incumbentActionOnWages
WorldState         specialUse          randomShockToWages
Temporary step
to check the model
```

1.3.1.6 Version 5 (GitHub: V5)

We add now the possibility of work troubles in firms, via the method `entrepreneurs p work troubles`, where p is a probability.

In `schedule5.xls` (to be copied to `schedule.xls` for the use) we have (comments start at column E and are missing) three columns:

#	1	100	
entrepreneurs		makeProductionPlan	
entrepreneurs		adaptProductionPlan	
entrepreneurs		hireFireWithProduction	
entrepreneurs	0.05		workTroubles
entrepreneurs		produceV5	
entrepreneurs		planConsumptionInValueV5	
workers		planConsumptionInValueV5	
WorldState		specialUse	setMarketPriceV3
entrepreneurs		evaluateProfit	
entrepreneurs	0.0001		fireIfProfit
workers		toEntrepreneurV3	
entrepreneurs		toWorkerV3	
WorldState		specialUse	fullEmploymentEffectOnWages
WorldState		specialUse	incumbentActionOnWages

1.3.2 The items of our AESOP level in scheduling

We have several items, not all used in each version of the model.

- # 1 100 fills 100 steps of the time schedule (or any other number of them) with the sequence below it, creating 100 (in this case) time containers. The actual step repetition upon time can be ≤ 100 ; if > 100 the steps after the 100th will be lacking of activity of the detailed scheduling activity (AESOP layer).

1.3.3 Methods used in Versions 0, 1, 2, 3, 4, 5

1.3.3.1 fireIfProfit

- The method (or command) **fireIfProfit**¹⁰ sent to the **entrepreneurs** order them—in a probabilistic way (50% of probability in versions 0, 1, 2; in version 3 and 4, considering that the probability is set directly in the **schedule.xls** file, we eliminate the effect of this command setting the probability to 0.01¹¹), in each unit of time—to fire a worker (choosing her/him randomly in the list of the employees of the firm) if the profit (last calculation, i.e., current period as shown in the sequence contained in **schedule.xls**) is less than the value **firingThreshold** (temporary: 0):

$$\Pi_t^i < firingThreshold \rightarrow fire \quad (1.1)$$

¹⁰Used in Versions 0, 1, 2, (temporary) 3, 4 and 5.

¹¹Being 0 not allowed, see the Reference Handbook, subsection *The detailed scheduling mechanism within the Model (AESOP level)*

```
# fireIfProfit
def fireIfProfit(self):

    # workers do not fire
    if self.agType == "workers": return

    if self.profit>=common.firingThreshold: return

    # the list of the employees of the firm
    entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    #print "entrepreneur", self.number, "could fire", entrepreneurWorkers

    #the list returns by nx is unstable as order
    entrepreneurWorkers = mySort(entrepreneurWorkers)

    if len(entrepreneurWorkers) > 0:
        fired=entrepreneurWorkers[randint(0,len(entrepreneurWorkers)-1)]

        gvf.colors[fired]="OrangeRed"
        fired.employed=False

        common.g_edge_labels.pop((self,fired))
        common.g.remove_edge(self, fired)

    # count edges (workers) after firing (recorded, but not used
    # directly)
    self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
    # nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.
    print "entrepreneur", self.number, "has", \
        self.numOfWorkers, "edge/s after firing"
```

See page 21 for the technical detail of the function mySort.

1.3.4 Methods used in Versions 1, 2, 3, 4, 5

1.3.4.1 makeProductionPlan

- The method (or command) `makeProductionPlan`¹² sent to the **entrepreneurs** order them to guess their production for the current period. The production plan \hat{P}_t^i is determined in a random way, using a Poisson distribution, with $\lambda = 10$ as mean (suggested value kept in the *common* space).

As a definition, the production plan is:

$$\hat{P}_t^i \sim \text{Pois}(\lambda) \quad (1.2)$$

We suggest temporary a value of 5 for λ , with (in Versions 1 and 2) the quantities: entrepreneurs 5, workers 20 + the 5 entrepreneurs, labor productivity

¹²Related to Versions 1, 2; in the 3, 4 and 5 cases, only at time=1

1. Always in Versions 1 and 2, the value of λ can be modified in the prologue of the run).

With Version 3, the `makeProductionPlan` method works uniquely with $t = 1$ being t internally `common.cycle` created and set to 1 by `ObserverSwarm` when starts.

Version 3 calculates the initial value λ (used uniquely in the first step) as:

$$\lambda = \rho \frac{(N_{workers} + N_{entrepreneurs})}{N_{entrepreneurs}} \quad (1.3)$$

In this way about a ρ ratio of the agents is producing in the beginning. Internally, the total numbers of the agents $N_{workers} + N_{entrepreneurs}$ can be obtained as the length of the `agentList`; the number of entrepreneurs is calculated from the same list considering only the `entrepreneurs`.

The code is:

```
# makeProductionPlan
def makeProductionPlan(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    if common.projectVersion >= 3 and common.cycle==1:
        nEntrepreneurs = 0
        for ag in self.agentList:
            if ag.agType=="entrepreneurs":
                nEntrepreneurs+=1
        #print nEntrepreneurs
        nWorkersPlus_nEntrepreneurs=len(self.agentList)
        #print nWorkersPlus_nEntrepreneurs
        common.Lambda=(common.rho*nWorkersPlus_nEntrepreneurs)/nEntrepreneurs
        #print common.rho, common.Lambda

    if (common.projectVersion >= 3 and common.cycle==1) or \
        common.projectVersion < 3:
        self.plannedProduction=npr.poisson(common.Lambda,1)[0] # 1 is the number
        # of element of the returned matrix (vector)
        #print self.plannedProduction

    common.totalPlannedProduction+=self.plannedProduction
```

1.3.4.2 hireFireWithProduction

- The method (or command) `hireFireWithProduction`¹³ sent to the `entrepreneurs` order them to hire or fire comparing the labor forces required for the pro-

¹³Related to Versions 1, 2, 3, 4, 5.

duction plan \hat{P}_t^i and the labor productivity π ; we have the required labor force (L_t^i is the current one):

$$\hat{L}_t^i = \hat{P}_t^i / \pi \quad (1.4)$$

Now:

1. if $\hat{L}_t^i = L_t^i$ nothing has to be done;
2. if $\hat{L}_t^i > L_t^i$, the entrepreneur is hiring with the limit of the number of unemployed workers;
3. if $\hat{L}_t^i < L_t^i$, the entrepreneur is firing the workers in excess.

The code is:

```
def hireFireWithProduction(self):

    # workers do not hire/fire
    if self.agType == "workers": return

    # to decide to hire/fire we need to know the number of employees
    # the value is calculated on the fly, to be sure of accounting for
    # modifications coming from outside
    # (nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.)

    laborForce0=gvf.nx.degree(common.g, nbunch=self) + \
        1 # +1 to account for the entrepreneur itself

    # required labor force
    laborForceRequired=int(
        self.plannedProduction/common.laborProductivity)

    # no action
    if laborForce0 == laborForceRequired: return

    # hire
    if laborForce0 < laborForceRequired:
        n = laborForceRequired - laborForce0
        tmpList=[]
        for ag in self.agentList:
            if ag != self:
                if ag.agType=="workers" and not ag.employed:
                    tmpList.append(ag)

        if len(tmpList) > 0:
            k = min(n, len(tmpList))
            shuffle(tmpList)
            for i in range(k):
                hired=tmpList[i]
                hired.employed=True
                gvf.colors[hired]="Aqua"
                gvf.createEdge(self, hired)
                #self, here, is the hiring firm

    # count edges (workers) of the firm, after hiring (the values is
```

```

# recorded, but not used directly)
self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
# nbunch : iterable container, optional (default=all nodes)
# A container of nodes. The container will be iterated through once.
print "entrepreneur", self.number, "has", \
      self.numOfWorkers, "edge/s after hiring"

# fire
if laborForce0 > laborForceRequired:
    n = laborForce0 - laborForceRequired

    # the list of the employees of the firm
    entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    #print "entrepreneur", self.number, "could fire", entrepreneurWorkers

    #the list returns by nx is unstable as order
    entrepreneurWorkers = mySort(entrepreneurWorkers)

    if len(entrepreneurWorkers) > 0: # has to be, but ...
        shuffle(entrepreneurWorkers)
        for i in range(n):
            fired=entrepreneurWorkers[i]

            gvf.colors[fired]="OrangeRed"
            fired.employed=False

            common.g_edge_labels.pop((self,fired))
            common.g.remove_edge(self, fired)

# count edges (workers) after firing (recorded, but not used
# directly)
self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
# nbunch : iterable container, optional (default=all nodes)
# A container of nodes. The container will be iterated through once.
print "entrepreneur", self.number, "has", \
      self.numOfWorkers, "edge/s after firing"

```

An important technical detail is the use of the function `mySort` to avoid inconsistencies in the order of the agents returned by the graph of the networks as workers of the entrepreneur. Different orders would produce different sets of fired workers, becoming different sets of potential entrepreneurs and producing different sequences of events in the simulation.

Why the differences in the order of the list of the agents? The graph is managed by `networkX`, which is using internally a dictionary structure, whose order is neither defined in any way in Python, nor constant from execution to execution. The list, in our case, contains the addresses of the instances of the agents. A simple sort of this list does not give us a stable order, due to the fact that the addresses and their order can change from a run to another.

For these reasons we use here a custom function to sort the list, using the internal `number` of the agents, to reorder them.¹⁴

¹⁴A related marginal problem, not eliminated, is the order in plotting the nodes in the graph plot: in the area where the nodes are superimposed, we can see the nodes exactly in the same

As a related consequence, we have to keep in mind to avoid duplicated numbers: in the *Oligopoly* model the entrepreneurs can switch to workers and vice versa, so the numbers assigned to the entrepreneurs start from 1 and those assigned to the workers from 1001 (see the file `workers.txtx`).

The code of the function `mySort` is:

```
def mySort(ag):
    if ag==[]: return []
    numAg=[]
    for a in ag:
        numAg.append((a.number,a))
    numAg.sort()
    agSorted=[]
    for i in range(len(numAg)):
        agSorted.append(numAg[i][1])
    return agSorted
```

1.3.4.3 planConsumptionInValue

- The method (or command) `planConsumptionInValue`,¹⁵ sent to entrepreneurs or workers, produces the following evaluations, detailed in `commonVar.py` file.

Consumption behavior with

$$C_i = a_k + b_k Y_i + u \quad (1.5)$$

with $u \sim \mathcal{N}(0, common.consumptionRandomComponentSD)$.

The individual i can be:

1. an entrepreneur, with $Y_i = profit_{i,t-1} + wage$;
2. an employed worker, with $Y_i = wage$;
3. an unemployed workers, with $Y_i = socialWelfareCompensation$.

The a_k and b_k values are set via the file `commonVar.py` and reported in output, when the program starts, via the `parameters.py`.

The code in `Agent.py` is:

```
# compensation
def planConsumptionInValue(self):
    self.consumption=0
    #case (1)
    #Y1=profit(t-1)+wage NB no negative consumption if profit(t-1) < 0
    # this is an entrepreneur action
```

position in every run, but differently placed as layer in the foreground/background sequence.

¹⁵Related to Version 2, 3, 4

```

if self.agType == "entrepreneurs":
    self.consumption = common.a1 + \
        common.b1 * (self.profit + common.wage) + \
        gauss(0, common.consumptionRandomComponentSD)
    if self.consumption < 0: self.consumption=0
    #profit, in V2, is at time -1 due to the sequence in schedule2.xls

#case (2)
#Y2=wage
if self.agType == "workers" and self.employed:
    self.consumption = common.a2 + \
        common.b2 * common.wage + \
        gauss(0, common.consumptionRandomComponentSD)

#case (3)
#Y3=socialWelfareCompensation
if self.agType == "workers" and not self.employed:
    self.consumption = common.a3 + \
        common.b3 * common.socialWelfareCompensation + \
        gauss(0, common.consumptionRandomComponentSD)

#update totalPlannedConsumptionInValueInA_TimeStep
common.totalPlannedConsumptionInValueInA_TimeStep+=self.consumption
#print "C sum", common.totalPlannedConsumptionInValueInA_TimeStep

```

The conclusion updates the *common* value `totalPlannedConsumptionInValueInA_TimeStep`, cleaned at each reset, i.e., at each time step in `modelActions.txt`.

The `totalPlannedConsumptionInValueInA_TimeStep` measure will be then randomly corrected within the `setMarketPriceV3` method of the *WorldState* meta-agent, see page 40.

1.3.5 Methods used in Version 3, 4, 5

1.3.5.1 toEntrepreneurV3

- With the method (or command) `toEntrepreneurV3`,¹⁶ sent to `workers`, the agent, being a worker, decides to become an entrepreneur at time t , if its employer has a relative profit (reported to the total of the costs) \geq a given *threshold* at time $t - 1$. The threshold is retrieved from the variable `thresholdToEntrepreneur`.

The decision is a quite rare one, so we have to pass a higher level threshold, that we define as `absoluteBarrierToBecomeEntrepreneur`; the value is defined in `commonVar.py` file and shown via `paparameters.py` file.

This parameter represents a *potential max number of new entrepreneurs* in each cycle.

¹⁶Related to Version 3, 4, 5.

It works in the following way: given an absolute value as number workers being candidates to become entrepreneur, let say one each two time steps (0.5—as a mean—in each time step), we transform that value in a probability, dividing by the total number of the agents, used as an adaptive scale factor.

The agent changes its internal type, position (not completely at the left as the original entrepreneurs, but if it was an entrepreneur moved to worker and coming back, it goes completely at the left) and color and it deletes the previous edge to the entrepreneur/employer. Finally, it starts counting the k periods of extra costs (to k is assigned the value `common.ExtraCostsDuration`, in the measure stated in `common.newEntrantExtraCosts`).

The code in `Agent.py` is:

```
#to entrepreneurV3
def toEntrepreneurV3(self):
    if self.agType != "workers" or not self.employed: return

    if random() <= common.absoluteBarrierToBecomeEntrepreneur:
        myEntrepreneur=gvf.nx.neighbors(common.g, self)[0]
        myEntrepreneurProfit=myEntrepreneur.profit
        myEntrepreneurCosts=myEntrepreneur.costs
        if myEntrepreneurProfit/myEntrepreneurCosts >= \
            common.thresholdToEntrepreneur:
            print "Worker %2.0f is now an entrepreneur (previous firm relative profit %4.2f)" %\
                (self.number, myEntrepreneurProfit/myEntrepreneurCosts)
            common.g.remove_edge(myEntrepreneur, self)

            #originally, it was a worker
            if self.xPos>0:gvf.pos[self]=(self.xPos-15,self.yPos)
            #originally, it was an entrepreneur
            else:gvf.pos[self]=(self.xPos,self.yPos)
            # colors at http://www.w3schools.com/html/html_colornames.asp
            gvf.colors[self]="LawnGreen"
            self.agType="entrepreneurs"
            self.employed=True
            self.extraCostsResidualDuration=common.extraCostsDuration
```

1.3.5.2 toWorkerV3

- With the method (or command) `toWorkerV3`,¹⁷ an entrepreneur moves to be an unemployed worker if its a relative profit (reported to the total of the costs) at time t is \leq a given *threshold* in t . The threshold is retrieved from the variable `thresholdToWorker`.

The agent changes its internal type, position (not completely at the right as the original workers, but if it was a worker moved to entrepreneur and coming back, it goes completely at the right) and color and it deletes the previous edge to the workers/employee if any.

¹⁷Related to Version 3, 4, 5.

The code in `Agent.py` is:

```
#to workersV3
def toWorkerV3(self):
    if self.agType != "entrepreneurs": return

    #check for newborn firms
    try:
        self.costs
    except:
        return

    if self.profit/self.costs <= common.thresholdToWorker:
        print "I'm entrepreneur %.0f and my relative profit is %.2f" %\
            (self.number, self.profit/self.costs)

    # the list of the employees of the firm, IF ANY
    entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    print "entrepreneur", self.number, "has", len(entrepreneurWorkers),\
        "workers to be fired"

    if len(entrepreneurWorkers) > 0:
        for aWorker in entrepreneurWorkers:
            gvf.colors[aWorker]="OrangeRed"
            aWorker.employed=False

            common.g.remove_edge(self, aWorker)

    self.numOfWorkers=0

    #originally, it was an entrepreneur
    if self.xPos<0:gvf.pos[self]=(self.xPos+15,self.yPos)
    #originally, it was a worker
    else:gvf.pos[self]=(self.xPos,self.yPos)
    # colors at http://www.w3schools.com/html/html_colornames.asp
    gvf.colors[self]="OrangeRed"
    self.agType="workers"
    self.employed=False
```

1.3.5.3 adaptProductionPlan

- The method (or command) `adaptProductionPlan`,¹⁸ sent to **entrepreneurs** orders to the i^{th} firm to set its production plan for the current period to their (equal, being i independent) fraction of the total demand of the previous period, corrected with a random uniform relative correction in the interval $-k$ to $+k$, reported in the prologue as:

Random component of planned production.

This method works only for time > 1 .

Being \hat{P}_t^i the planned production of firm i , we have:

¹⁸Related to Version 3, 4, 5.

– if $u_t^i \geq 0$

$$\hat{P}_t^i = \frac{D_{t-1}}{N_{entrepreneurs}}(1 + u_t^i) \quad (1.6)$$

– if $u_t^i < 0$

$$\hat{P}_t^i = \frac{D_{t-1}}{N_{entrepreneurs}}/(1 + |u_t^i|) \quad (1.7)$$

with $u_t^i \sim \mathcal{U}(-k, k)$

The code in `Agent.py` is:

```
# adaptProductionPlan
def adaptProductionPlan(self):
    if common.cycle > 1:
        nEntrepreneurs = 0
        for ag in self.agentList:
            if ag.agType=="entrepreneurs":
                nEntrepreneurs+=1

    self.plannedProduction = common.totalDemandInPrevious_TimeStep \
        / nEntrepreneurs

    #self.plannedProduction += gauss(0,self.plannedProduction/10)

    shock= uniform( \
        -common.randomComponentOfPlannedProduction,\
        common.randomComponentOfPlannedProduction)

    if shock >= 0:
        self.plannedProduction *= (1.+shock)

    if shock < 0:
        shock *= -1.
        self.plannedProduction /= (1.+shock)
    #print self.number, self.plannedProduction

    common.totalPlannedProduction+=self.plannedProduction
```

1.3.5.4 setMarketPriceV3

- The method (or command) `setMarketPriceV3`,¹⁹ sent to the `WorldState`, orders it to evaluate the market clearing price. See below Section 1.3.13 and specifically Section 1.3.13.3.

¹⁹Related to Version 3, 4, 5.

1.3.6 Methods used in Version 4, 5 only

1.3.6.1 `fullEmploymentEffectOnWages`

The method (or command) `fullEmploymentEffectOnWages`,²⁰ sent to the `WorldState`, orders it to modify wages accordingly to full employment situation, in a reversible way. See below Section 1.3.13 and specifically Section 1.3.13.4.

1.3.6.2 `randomShockToWages`

The method (or command) `randomShockToWages`,²¹ sent to the `WorldState`, orders it to randomly modify wages. See below Section 1.3.13 and specifically Section 1.3.13.5.

This method is only used in model building, to verify the sensitivity of the model to changes in wages.

1.3.6.3 `incumbentActionOnWages`

The method (or command) `incumbentActionOnWages`,²² sent to the `WorldState`, orders it to modify wages for one period, accordingly to the attempt of creating an entry barrier when new firms are observed into the market.

As a consequence, wage measure as a variable addendum, set to 0 as basic value, modified temporary by this method.

See below Section 1.3.13 and specifically Section 1.3.13.6.

1.3.7 Methods used in Version 5 only

1.3.7.1 `planConsumptionInValueV5`

- The method (or command) `planConsumptionInValueV5`,²³ sent to `entrepreneurs` or `workers`, produces the following evaluations, detailed in `commonVar.py` file.

²⁰Related to Version 4, 5.

²¹Related to Version 4, 5.

²²Related to Version 4, 5.

²³Related to Version 5

Consumption behavior with

$$C_i = a_k + b_k Y_i + u \quad (1.8)$$

with $u \sim \mathcal{N}(0, \text{common.consumptionRandomComponentSD})$.

The individual i can be:

1. an entrepreneur, with $Y_i = \text{profit}_{i,t-1} + \text{wage}$;
2. an employed worker, with $Y_i = \text{wage}$ and the special ²⁴ case $Y_i = wc_t^i$, with wc_t^i defined in eq.1.10;
3. an unemployed workers, with $Y_i = \text{socialWelfareCompensation}$.

The a_k and b_k values are set via the file `commonVar.py` and reported in output, when the program starts, via the `parameters.py`.

The code in `Agent.py` is:

```
# compensation
def planConsumptionInValueV5(self):
    self.consumption=0
    #case (1)
    #Y1=profit(t-1)+wage NB no negative consumption if profit(t-1) < 0
    # this is an entrepreneur action
    if self.agType == "entrepreneurs":
        self.consumption = common.a1 + \
            common.b1 * (self.profit + common.wage) + \
            gauss(0, common.consumptionRandomComponentSD)
        if self.consumption < 0: self.consumption=0
        #profit, in V2, is at time -1 due to the sequence in schedule2.xls

    #case (2)
    #Y2=wage
    if self.agType == "workers" and self.employed:
        if common.wageCutForWorkTroubles and self.workTroubles != 0:
            self.consumption = common.a2 + \
                common.b2 * common.wage*(1.-self.workTroubles) + \
                gauss(0, common.consumptionRandomComponentSD)
            #print "worker", self.number, "wage x", (1.-self.workTroubles)
        else:
            self.consumption = common.a2 + \
                common.b2 * common.wage + \
                gauss(0, common.consumptionRandomComponentSD)

    #case (3)
    #Y3=socialWelfareCompensation
    if self.agType == "workers" and not self.employed:
        self.consumption = common.a3 + \
            common.b3 * common.socialWelfareCompensation + \
            gauss(0, common.consumptionRandomComponentSD)

    #update totalPlannedConsumptionInValueInA_TimeStep
    common.totalPlannedConsumptionInValueInA_TimeStep+=self.consumption
    #print "C sum", common.totalPlannedConsumptionInValueInA_TimeStep
```

²⁴Activated if the *common* value *wageCutForWorkTroubles* is *true*

The conclusion updates the *common* value `totalPlannedConsumptionInValueInA_TimeStep`, cleaned at each reset, i.e., at each time step in `modelActions.txt`.

The `totalPlannedConsumptionInValueInA_TimeStep` measure will be then randomly corrected within the `setMarketPriceV3` method of the *WorldState* meta-agent, see page 40.

1.3.7.2 workTroubles

At time t for firm i , we generate a shock $\lambda_{i,t} > 0$ due to work troubles, with probability p_λ (set for all the entrepreneurs via the `schedule.txt` file²⁵) and value uniformly distributed between $V_\Lambda/2$ and V_Λ . The shock reduces the production of firm i in a relative way, as (Pc means *corrected production*):

$$Pc_t^i = P_t^i(1 - \lambda_{i,t}) \quad (1.9)$$

If the global logical value `wageCutForWorkTroubles` is *true*, also wages are cut in the same proportion that the production is suffering. With w indicating the constant basic wage level, wc_t is the corrected value at time t and for firm i ; the correction is superimposed to the other possible corrections (due to full employment or to artificial barrier creation).

$$wc_t^i = w(1 - \lambda_{i,t}) \quad (1.10)$$

The firm variable `hasTroubles` takes note—via $\lambda_{i,t}$ assuming a value > 0 , being 0 otherwise—if the firm has work problems in the current time step and the worker variable `workTroubles` takes note of the same amount for all the workers of that specific firm.

Both the variable are set again to 0 in the `reset` step at the beginning of each model cycle.

The code in `Agent.py` is:

```
#work troubles
def workTroubles(self):

    # NB this metod acts with the probability set in the schedule.txt
    # file
    if self.agType != "entrepreneurs": return

    # production shock due to work trobles
```

²⁵SLAPP displays—in its text output—a dictionary with the method probabilities, if at least one method is linked to a probability.

```

lambdaShock=uniform(common.productionCorrectionLambda/2,
                    common.productionCorrectionLambda)
self.hasTroubles=lambdaShock
print "Entrepreneur", self.number, "is suffering a reduction of "\
      "production of", lambdaShock*100, "%, due to work troubles"

if common.wageCutForWorkTroubles:
    # the list of the employees of the firm
    entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    for aWorker in entrepreneurWorkers:
        #avoiding the entrepreneur herself using the network
        print "Worker ", aWorker.number, "is suffering a reduction of "\
              "wage of", lambdaShock*100, "%, due to work troubles"

```

1.3.7.3 produceV5

- The method (or command) `produceV5`²⁶ sent to the `entrepreneurs` order them—in a deterministic way, in each unit of time—to produce proportionally to their labour force, obtaining profit Π_t^i , where i identifies the firm and t the time.

L_t^i is the number of workers of firm i at time t , and also the number of its links. We add 1 to L_t^i , to account for the entrepreneur as a worker. π is the `laborProductivity`, with its value set to 1 in `common` variable space, currently not changing with t . P_t^i is the production of firm i at time t .

The production is:

$$P_t^i = \pi(L_t^i + 1) \quad (1.11)$$

The production is corrected for work troubles (as in section 1.3.7.2) calculating value the corrected Pc_t^i with:

The production is:

$$Pc_t^i = P_t^i(1 - \lambda_{i,t}) \quad (1.12)$$

The production (corrected or not) of the i^{th} firm is added to the total production of the time step, in the variable `totalProductionInA_TimeStep` of the *common* space.

The code is:

```

# produce
def produce(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    # to produce we need to know the number of employees

```

²⁶Related to Version 5

```
# the value is calculated on the fly, to be sure of accounting for
# modifications coming from outside
# (nbunch : iterable container, optional (default=all nodes)
# A container of nodes. The container will be iterated through once.)

laborForce=gvf.nx.degree(common.g, nbunch=self) + \
    1 # +1 to account for the entrepreneur itself

# productivity is set to 1 in the beginning
self.production = common.laborProductivity * \
    laborForce

# totalProductionInA_TimeStep
common.totalProductionInA_TimeStep += self.production
```

We calculate the `laborForce`, i.e. L_t^i , counting the number of links or edges from the firm to the workers. We prefer this ‘on the fly’ evaluation to the internal variable `self.numOfWorkers`, to be absolutely sure of accessing the last datum in case of modifications coming from other procedures. E.g., a random subtraction or addition of workers to firms coming simulating some kind of shock ...

1.3.7.4 evaluateProfitV5

- The method (or command) `evaluateProfit`²⁷ sent to the **entrepreneurs** order them to calculate their profit. Being P_t^i the production and π the labor productivity, we have the labor force $L_t^i = P_t^i / \pi$

The use of P_t^i , the actual production of the entrepreneurs, accounts both for the production plan decided with `adaptProductionPlan`, page 25, and for the limits in hiring, if any, as in `hireFireWithProduction`, page 19. The sum of all the actual productions of each entrepreneur is used, as at page 40, in `setMarketPriceV3`.

The method has been improved in version 2, to manage extra costs for the new entrant firms, but keeping safe the backward compatibility of the method.

p_t is the **price**, clearing the market at time t and it calculated by the abstract item `WorldState` via the method `setMarketPrice`, as explained in Section 1.3.13.

w is the **wage** per employee and time unit, set to 1.0 in `common` variable space, not changing with t . C are extra costs for new entrant firms.

The profit evaluation is:

$$\Pi_t^i = p_t P_t^i - w L_t^i - C \quad (1.13)$$

²⁷Related to Version 5.

The new entrant firms have extra costs to be supported, retrieved in `XC` variables, but only for k periods, as stated in `commonVar.py` and activated by method to `toEntrepreneur`.

The code is:

```
# calculateProfit
def evaluateProfit(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    # backward compatibily to version 1
    try: XC=common.newEntrantExtraCosts
    except: XC=0
    try: k=self.extraCostsResidualDuration
    except: k=0

    if k==0: XC=0
    if k>0: self.extraCostsResidualDuration-=1

    # the number of prducing workers is obtained indirectly via
    # production/laborProductivity
    #print self.production/common.laborProductivity
    self.costs=common.wage * (self.production/common.laborProductivity) + \
        XC

    # the entrepreur sells her production, which is cotributing - via
    # totalActualProductionInA_TimeStep, to price formation
    self.profit=common.price * self.production - self.costs

    common.totalProfit+=self.profit
```

1.3.8 Methods used in Versions 0, 1, 2, 3, 4

1.3.8.1 produce

- The method (or command) `produce`²⁸ sent to the `entrepreneurs` order them—in a deterministic way, in each unit of time—to produce proportionally to their labour force, obtaining profit Π_t^i , where i identifies the firm and t the time.

L_t^i is the number of workers of firm i at time t , and also the number of its links. We add 1 to L_t^i , to account for the entrepreneur as a worker. π is the `laborProductivity`, with its value set to 1 in `common` variable space, currently not changing with t . P_t^i is the production of firm i at time t .

The production is:

$$P_t^i = \pi(L_t^i + 1) \tag{1.14}$$

²⁸Related to Versions 0, 1, 2, 3, 4, 5

The production of the i^{th} firm is added to the total production of the time step, in the variable `totalProductionInA_TimeStep` of the *common* space.

The code is:

```
# produce
def produce(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    # to produce we need to know the number of employees
    # the value is calculated on the fly, to be sure of accounting for
    # modifications coming from outside
    # (nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.)

    laborForce=gvf.nx.degree(common.g, nbunch=self) + \
        1 # +1 to account for the entrepreneur itself

    # productivity is set to 1 in the beginning
    self.production = common.laborProductivity * \
        laborForce

    # totalProductionInA_TimeStep
    common.totalProductionInA_TimeStep += self.production
```

We calculate the `laborForce`, i.e. L_t^i , counting the number of links or edges from the firm to the workers. We prefer this ‘on the fly’ evaluation to the internal variable `self.numOfWorkers`, to be absolutely sure of accessing the last datum in case of modifications coming from other procedures. E.g., a random subtraction or addition of workers to firms coming simulating some kind of shock ...

1.3.9 Methods used in Versions 1, 2, 3, 4

1.3.9.1 evaluateProfit

- The method (or command) `evaluateProfit`²⁹ sent to the entrepreneurs order them to calculate their profit. Being P_t^i the production and π the labor productivity, we have the labor force $L_t^i = P_t^i / \pi$

The use of P_t^i , the actual production of the entrepreneurs, accounts both for the production plan decided with `adaptProductionPlan`, page 25, and for the limits in hiring, if any, as in `hireFireWithProduction`, page 19. The sum of all the actual productions of each entrepreneur is used, as at page 40, in `setMarketPriceV3`.

²⁹Related to Versions 1, 2, 3, 4.

The method has been improved in version 2, to manage extra costs for the new entrant firms, but keeping safe the backward compatibility of the method.

p_t is the **price**, clearing the market at time t and it calculated by the abstract item `WorldState` via the method `setMarketPrice`, as explained in Section 1.3.13.

w is the **wage** per employee and time unit, set to 1.0 in `common` variable space, not changing with t . C are extra costs for new entrant firms.

The profit evaluation is:

$$\Pi_t^i = p_t P_t^i - w L_t^i - C \quad (1.15)$$

The new entrant firms have extra costs to be supported, retrieved in `XC` variables, but only for k periods, as stated in `commonVar.py` and activated by method to `toEntrepreneur`.

The code is:

```
# calculateProfit
def evaluateProfit(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    # backward compatibily to version 1
    try: XC=common.newEntrantExtraCosts
    except: XC=0
    try: k=self.extraCostsResidualDuration
    except: k=0

    if k==0: XC=0
    if k>0: self.extraCostsResidualDuration-=1

    # the number of pruding workers is obtained indirectly via
    # production/laborProductivity
    #print self.production/common.laborProductivity
    self.costs=common.wage * (self.production/common.laborProductivity) + \
        XC

    # the entrepreneur sells her production, which is cotributing - via
    # totalActualProductionInA_TimeStep, to price formation
    self.profit=common.price * self.production - self.costs

    common.totalProfit+=self.profit
```

1.3.10 Methods used in Version 0 only

1.3.10.1 evaluateProfitV0

- The method (or command) `evaluateProfitV0`³⁰ sent to the **entrepreneurs** order them to calculate their profit. Being P_t^i the production and π the labor productivity, we have the labor force $L_t^i = P_t^i / \pi$

R is `revenuesOfSalesForEachWorker`, set to 1.005 in `common` variable space, not changing with t ; w is the `wage` per employee and time unit, set to 1.0 in `common` variable space, not changing with t . $u_t^i \sim \mathcal{N}(0, 0.05)$ is a random normal addendum.

The profit evaluation is:

$$\Pi_t^i = L_t^i(R - w) + u_t^i \quad (1.16)$$

The code is:

```
# calculateProfit
def evaluateProfitV0(self):

    # this is an entrepreneur action
    if self.agType == "workers": return

    # the number of producing workers is obtained indirectly via
    # production/laborProductivity
    #print self.production/common.laborProductivity
    self.profit=(self.production/common.laborProductivity) * \
        (common.revenuesOfSalesForEachWorker - \
         common.wage) + gauss(0,0.05)
```

1.3.10.2 hireIfProfit

- The method (or command) `hireIfProfit`³¹ sent to the **entrepreneurs** order them—in a probabilistic way (50% of probability in Version 0 case), in each unit of time—to hire a worker (random choosing her/him in a temporary list of unemployed people) if the profit (last calculation, i.e., current period as shown in the sequence contained in `schedule.xls`) is a than the value `hiringThreshold` (temporary: 0):

$$\Pi_t^i > hiringThreshold \rightarrow hire \quad (1.17)$$

As first attempt the `hiringThreshold` is 0 (in `commonVar.py`). We can modify this internal value, as others, while the simulation is running, via the *WorldState* feature, introduced below.

³⁰Related to Version 0.

³¹Used in Version 0.

The code of the `hireIfProfit` method is:

```
# hireIfProfit
def hireIfProfit(self):

    # workers do not hire
    if self.agType == "workers": return

    if self.profit <= common.hiringThreshold: return

    tmpList=[]
    for ag in self.agentList:
        if ag != self:
            if ag.agType=="workers" and not ag.employed:
                tmpList.append(ag)

    if len(tmpList) > 0:
        hired=tmpList[randint(0,len(tmpList)-1)]

        hired.employed=True
        gvf.colors[hired]="Aqua"
        gvf.createEdge(self, hired) #self, here, is the hiring firm

    # count edges (workers) of the firm, after hiring (the values is
    # recorded, but not used directly)
    self.numOfWorkers=gvf.nx.degree(common.g, nbunch=self)
    # nbunch : iterable container, optional (default=all nodes)
    # A container of nodes. The container will be iterated through once.
    print "entrepreneur", self.number, "has", \
        self.numOfWorkers, "edge/s after hiring"
```

1.3.11 Methods used in Version 1 only

1.3.11.1 setMaketPriceV1

- The method (or command) `setMarketPriceV1`,³² sent to the `WorldState`, orders it to evaluate the market clearing price. See below Section 1.3.13 and specifically Section 1.3.13.1.

1.3.12 Methods used in Version 2 only

1.3.12.1 toEntrepreneur

- With the method (or command) `toEntrepreneur`,³³ sent to `workers`, the agent, being a worker, decides if to became an entrepreneur at time t , if its employer has a profit \geq a given *threshold* in t . The threshold is retrieved from the variable `thresholdToEntrepreneur`.

³²Related to Version 1.

³³Related to Version 2.

The agent changes its internal type, position (not completely at the left as the original entrepreneurs, but if it was an entrepreneur moved to worker and coming back, it goes completely at the left) and color and it deletes the previous edge to the entrepreneur/employer. Finally, it starts counting the k periods of extra costs (to k is assigned the value `common.ExtraCostsDuration`, in the measure stated in `common.newEntrantExtraCosts`).

The code in `Agent.py` is:

```
myEntrepreneur=gvf.nx.neighbors(common.g, self)[0]
myEntrepreneurProfit=myEntrepreneur.profit
if myEntrepreneurProfit >= common.thresholdToEntrepreneur:
    print "I'm %2.0f and myEntrepreneurProfit is %4.2f" %\
        (self.number, myEntrepreneurProfit)
    common.g.remove_edge(myEntrepreneur, self)
    self.xPos-=15
    gvf.pos[self]=(self.xPos,self.yPos)
    # colors at http://www.w3schools.com/html/html_colornames.asp
    gvf.colors[self]="LawnGreen"
    self.agType="entrepreneurs"
    self.employed=True
    self.extraCostsResidualDuration=common.extraCostsDuration
```

1.3.12.2 toWorker

- With the method (or command) `toWorker`,³⁴ an entrepreneur moves to be an unemployed worker if its profit at time t is \leq a given *threshold* in t . The threshold is retrieved from the variable `thresholdToWorker`.

The agent changes its internal type, position (not completely at the right as the original workers, but if it was a worker moved to entrepreneur and coming back, it goes completely at the right) and color and it deletes the previous edge to the workers/employee if any.

The code in `Agent.py` is:

```
if self.profit <= common.thresholdToWorker:
    print "I'm entrepreneur %2.0f and my profit is %4.2f" %\
        (self.number, self.profit)

    # the list of the employees of the firm, IF ANY
    entrepreneurWorkers=gvf.nx.neighbors(common.g,self)
    print "entrepreneur", self.number, "has", len(entrepreneurWorkers),\
        "workers to be fired"

    if len(entrepreneurWorkers) > 0:
        for aWorker in entrepreneurWorkers:
            gvf.colors[aWorker]="OrangeRed"
            aWorker.employed=False
```

³⁴Related to Version 2.

```
common.g.remove_edge(self, aWorker)

self.numOfWorkers=0

#originally, it was an entrepreneur
if self.xPos<0:gvf.pos[self]=(self.xPos+15,self.yPos)
#originally, it was a worker
else:gvf.pos[self]=(self.xPos,self.yPos)
# colors at http://www.w3schools.com/html/html_colornames.asp
gvf.colors[self]="OrangeRed"
self.agType="workers"
self.employed=False
```

1.3.12.3 setMarketPriceV2

- The method (or command) `setMarketPriceV2`,³⁵ sent to the `WorldState`, orders it to evaluate the market clearing price. This method uses two common variables:
 - `totalProductionInA_TimeStep`, generated by the agents (*entrepreneurs*), via `produce`;
 - `totalPlannedConsumptionInValueInA_TimeStep`, generated by the agents (*entrepreneurs* and *workers*) via `planConsumptionInValue`.

See below the Section 1.3.13 and specifically Section 1.3.13.2.

1.3.13 Other features in scheduling [NB the notes with the \$\$ mark have to be reported in the Handbook and require code modification]

We also have two more sophisticated structures: the `WorldState` feature and the macros.

- Running a project, at the beginning of the output, we read:

```
World state number 0 has been created.
```

What does it mean?

The `WorldState` class interacts with the agents; at present we use a unique instance of the class, but the code is built upon a list of any number of

³⁵Related to Version 2.

instances of the class. The variables managed via `WorldState` have to be added, with their methods, within the class, with `set/get` methods for each variable.

In `Agent.py` we can ask to the `WorldState`, via `get`, for the values of the variables.

In the `oligopoly` project we make a step ahead, asking to the `WorldState` to make a specific evaluation.

\$\$ The normal use has in Col. B a value and in Col. C the method used to set that value in `WorldState`; the will be retrieved by the agents. Here, in Col. B we have a name, any name, in our case `specialUse` (an empty cell does not work) to signal the content of Col. C as a special method making *world calculations*. The final structure has to follow the usual one, having in Col. B a value or a method and, in the second case, with Col. C empty.

1.3.13.1 `setMarketPriceV1` as in `WorldState`, with details

- The method (or command) `setMarketPriceV1`,³⁶ sent to the `WorldState`, orders it to evaluate the market clearing price.

Setting the aggregate-demand D_t as equal to the production:

$$D_t = \sum_i P_t^i \quad (1.18)$$

We have the *demand function*, with p_t as price:

$$p_t = a + bD_t \quad (1.19)$$

With the planned production coming from a Poisson distribution as in Eq. 1.2, considering λ set to 4, we can set two consistent points (p, D) as $(1, 20)$ and $(0.8, 30)$ obtaining:

$$p_t = 1.4 - 0.02D_t \quad (1.20)$$

The resulting code in `WorldState.py` is:

```
# set market price
def setMarketPriceV1(self):
    # to have a price around 1
    common.price= 1.4 - 0.02 * common.totalProductionInA_TimeStep
    print "Set market price to ", common.price
    common.price10=common.price*10 #to plot
```

³⁶Introduced above as related to Version 1 only.

1.3.13.2 setMarketPriceV2, as in WorldState, with details

- The method (or command) `setMarketPriceV2`,³⁷ sent to the `WorldState`, orders it to evaluate the market clearing price considering each agent behavior.

Having:

$$p_t = D_t / O_t \quad (1.21)$$

with p_t clearing market price at time t ; D_t demand in value at time t ; O_t offer in quantity (the production) at time t .

As defined above (p. 38), the method uses two common variables:

- `totalProductionInA_TimeStep`, generated by the agents (*entrepreneurs*), via `produce`;
- `totalPlannedConsumptionInValueInA_TimeStep`, generated by the agents (*entrepreneurs* and *workers*) via `planConsumptionInValue`.

The resulting code in `WorldState.py` is:

```
# set market price V2
def setMarketPriceV2(self):
    common.price= common.totalPlannedConsumptionInValueInA_TimeStep / \
                  common.totalProductionInA_TimeStep
    print "Set market price to ", common.price
    common.price10=common.price*10 #to plot
```

1.3.13.3 setMarketPriceV3, as in WorldState, with details

- The method (or command) `setMarketPriceV3`,³⁸ sent to the `WorldState`, orders it to evaluate the market clearing price considering each agent behavior and *an external shock, potentially large*.

We introduce a shock Ξ uniformly distributed between $-L$ and $+L$ where L is a rate on base 1, e.g., 0.10. To keep the effect as symmetric, we have the following equations determining the clearing price:

If the shock Ξ is (≥ 0):

$$p_t = \frac{D_t(1 + \Xi)}{O_t} \quad (1.22)$$

³⁷Introduced above as related to Version 2 only.

³⁸Introduced above as related to Version 3, 4 and 5.

if the shock Ξ is (< 0):

$$p_t = \frac{D_t/(1 + \Xi)}{O_t} \quad (1.23)$$

with p_t clearing market price at time t ; D_t demand in value at time t ; O_t offer in quantity (the production) at time t .

The Ξ parameter is reported in the prologue of the execution as *Total demand relative random shock, uniformly distributed between $-\Xi\%$ and $+\Xi\%$.*

As defined above (p. 38), the method uses two common variables:

- `totalProductionInA_TimeStep`, generated by the agents (*entrepreneurs*), via `produce`;
- `totalPlannedConsumptionInValueInA_TimeStep`, generated by the agents (*entrepreneurs* and *workers*) via `planConsumptionInValue`.

The resulting code in `WorldState.py` is:

```
# set market price V3
def setMarketPriceV3(self):
    shock0=random.uniform(-common.maxDemandRelativeRandomShock, \
                           common.maxDemandRelativeRandomShock)

    shock=shock0

    print "\n-----"

    if shock >= 0:
        common.totalDemandInPrevious_TimeStep = \
            common.totalPlannedConsumptionInValueInA_TimeStep * \
            (1 + shock)
        common.price= (common.totalPlannedConsumptionInValueInA_TimeStep * \
                       (1 + shock)) \
                       / common.totalProductionInA_TimeStep
        print "Relative shock (symmetric) ", shock0
        print "Set market price to ", common.price

    if shock < 0:
        shock *=-1. #always positive, being added to the denominator
        common.totalDemandInPrevious_TimeStep = \
            common.totalPlannedConsumptionInValueInA_TimeStep / \
            (1 + shock)
        common.price= (common.totalPlannedConsumptionInValueInA_TimeStep / \
                       (1 + shock)) \
                       / common.totalProductionInA_TimeStep
        print "Relative shock (symmetric) ", shock0
        print "Set market price to ", common.price

    print "-----\n"
```

1.3.13.4 fullEmploymentEffectOnWages, as in WorldState, with details

Being U_t the unemployment rate at time t , λ the unemployment threshold to recognize the *full employment* situation, s the proportional increase step (reversible) of the wage level and w_t the wage level at time t (being w_0 the initial level), we have:

$$\begin{cases} w_t = w_0(1 + s) & \text{if } U_t \leq \lambda \\ w_t = w_0 & \text{if } U_t > \lambda \end{cases} \quad (1.24)$$

The code in `WorldState.py` is:

```
# shock to wages (full employment case)
def fullEmploymentEffectOnWages(self):

    # wages: reset incumbent action if any
    if common.wageAddendum > 0:
        common.wage -= common.wageAddendum
        common.wageAddendum = 0

    # employed people
    peopleList=common.g.nodes()
    totalPeople=len(peopleList)
    totalEmployed=0
    for p in peopleList:
        if p.employed: totalEmployed+=1
    #print totalPeople, totalEmployed
    unemploymentRate=1. - float(totalEmployed)/ \
        float(totalPeople)
    if not common.fullEmploymentStatus and \
        unemploymentRate <= common.fullEmploymentThreshold:
        common.wage*=(1 + common.wageStepInFullEmployment)
        common.fullEmploymentStatus=True

    if common.fullEmploymentStatus and \
        unemploymentRate > common.fullEmploymentThreshold:
        common.wage/= (1 + common.wageStepInFullEmployment)
        common.fullEmploymentStatus=False
```

1.3.13.5 randomShocksToWages, as in WorldState, with details

- The method is used only in the model building phase, to verify the sensitivity of the model to changes in wages.

Being w the wage per employee defined in the setup, so w_1 , from $t = 2$ we have:

$$\begin{aligned} & - \text{if } u_t \geq 0 \\ & w_t = w_{t-1}(1 + ut) \end{aligned} \quad (1.25)$$

– if $u_t < 0$

$$w_t = w_{t-1}/(1 + |u_t|) \quad (1.26)$$

with $u_t \sim \mathcal{U}(-k, k)$ and k tentatively set to 0.10 or 10%.

The code in `WorldState.py` is:

```
# random shock to wages (temporary method to experiment with wages)
def randomShockToWages(self):
    k=0.10
    shock= uniform(-k,k)

    if shock >= 0:
        common.wage *= (1.+shock)

    if shock < 0:
        shock *= -1.
        common.wage /= (1.+shock)
```

1.3.13.6 incumbentActionOnWages, as in WorldState, with details

The current number of entrepreneurs E_t is calculated from the network and the previous one E_{t-1} is extracted from the structural dataframe (see `collectStructuralData` at page 11).

The wage level has two components, mutually exclusive:

1. the effects of full employment on wages, as in Section 1.3.13.4;
2. the effect described in this Section about incumbent oligopolists strategically increasing wages to create an artificial barrier against new entrants; the new entrepreneurs suffer temporary extra costs, so for them the wage increment can determinant so relevant losses to produce their bankruptcy.

We have here two levels: K as the (relative) threshold of entrepreneur presence to determine the reaction on wages and k as the relative increment of wages.

N_t^E is the number of entrepreneurs a time t .

Formally, in case 2:

$$\begin{cases} w_t = w_0(1 + k) & \text{if } \frac{N_t^E}{N_{t-1}^E} - 1 > K \\ w_t = w_0 & \text{if } \frac{N_t^E}{N_{t-1}^E} - 1 \leq K \end{cases} \quad (1.27)$$

The code in `WorldState.py` is:

```
# incumbents rising wages as na entry barrier
def incumbentActionOnWages(self):

    # current number of entrepreneurs
    peopleList=common.g.nodes()
    nEntrepreneurs=0
    for p in peopleList:
        if p.agType=="entrepreneurs": nEntrepreneurs+=1
    nEntrepreneurs=float(nEntrepreneurs)

    # previous number of entrepreneurs
    nEntrepreneurs0=common.str_df.iloc[-1,0] # indexes Python style

    #print nEntrepreneurs, nEntrepreneurs0

    # wages: reset incumbent action if any
    if common.wageAddendum > 0:
        common.wage -= common.wageAddendum
        common.wageAddendum = 0

    # wages: set
    if nEntrepreneurs/nEntrepreneurs0 - 1 > \
        common.maxAcceptableOligopolistRelativeIncrement:
        common.wageAddendum = common.wage*\
            common.temporaryRelativeWageIncrementAsBarrier
        common.wage+=common.wageAddendum
```

1.3.13.7 Macros

- *Just a memo:* we also have the possibility of using *macros* contained in separated sheets of the `schedule.xls` file (not used presently here).

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