# Quantitative Analysis

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#### Abstract

The goal of this vignette is to demonstrate key concepts in Financial Risk Manager (FRM <sup>®</sup>) Part 1: Quantitative Analysis using R and the GARPFRM package. This vignette will cover exploratory data analysis, basic probability and statistics, and linear regression.

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# 1 Exploratory Data Analysis

Load the GARPFRM package and the returns dataset. Other packages are also loaded for plotting functions. The returns dataset and prices dataset includes weekly returns and weekly prices for SPY, AAPL, XOM, GOOG, MSFT, and GE from 2005-01-07 to 2013-11-22.

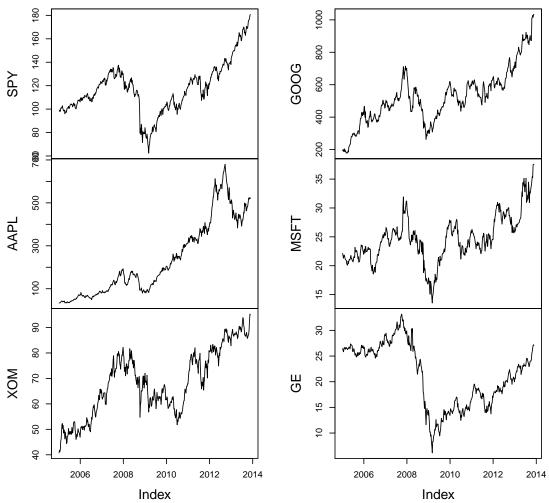
```
suppressMessages(library(GARPFRM))
suppressMessages(library(lattice))
suppressMessages(library(pcaPP))
suppressMessages(library(hexbin))
data(returns)
```

```
data(prices)
# Get the names of the stocks and view the first 5 rows of returns and
# prices
colnames(returns)
## [1] "SPY" "AAPL" "XOM" "GOOG" "MSFT" "GE"
head(returns, 5)
##
                           AAPL
                                     MOX
                                            GOOG
                   SPY
                                                     MSFT
## 2005-01-14 -0.001714 0.013740 0.02552 0.03157 -0.02033 -0.0136003
## 2005-01-21 -0.012322 0.004125 -0.01220 -0.05846 -0.01798 -0.0107239
## 2005-01-28 0.005522 0.049589 0.01647 0.01094 0.02066 0.0174216
## 2005-02-04 0.023899 0.065698 0.07839 0.07366 0.00506 0.0140791
## 2005-02-11 0.004470 0.029906 0.01966 -0.08299 -0.01327 -0.0007505
head(prices, 5)
                SPY AAPL XOM GOOG MSFT
##
## 2005-01-07 99.18 33.48 40.76 193.8 22.14 26.47
## 2005-01-14 99.01 33.94 41.80 200.0 21.69 26.11
## 2005-01-21 97.79 34.08 41.29 188.3 21.30 25.83
## 2005-01-28 98.33 35.77 41.97 190.3 21.74 26.28
## 2005-02-04 100.68 38.12 45.26 204.4 21.85 26.65
```

Plot the prices of each asset.

```
plot(zoo(prices), main = "Weekly Prices")
```

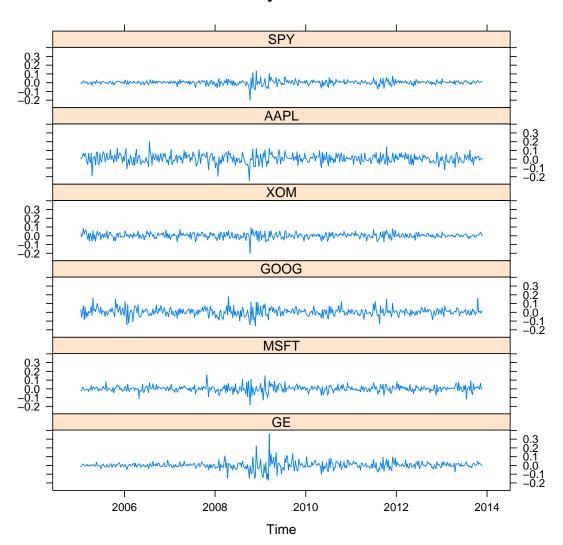
# Weekly Prices



Plot of the weekly returns of each asset.

```
xyplot(returns, scale = list(y = "same"), main = "Weekly Returns")
```

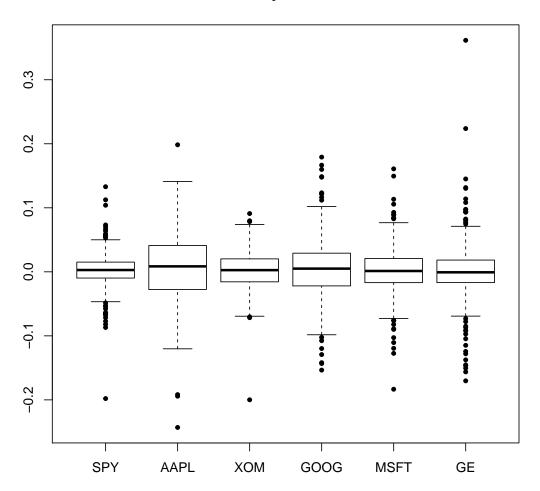
# **Weekly Returns**



Another way to compare returns of several assets is with a boxplot.

boxplot(coredata(returns), pch = 20, main = "Weekly Returns")

# **Weekly Returns**

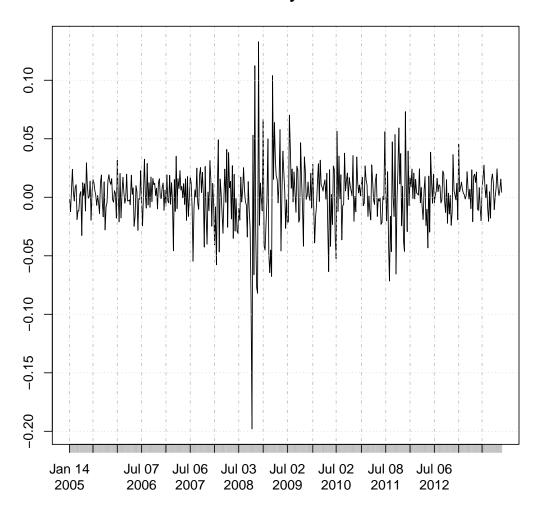


The exploratory data analysis, basic probability and statistics will use the SPY weekly returns.

```
# Extract the column labeled 'SPY' to get the SPY returns
SPY.ret <- returns[, "SPY"]</pre>
```

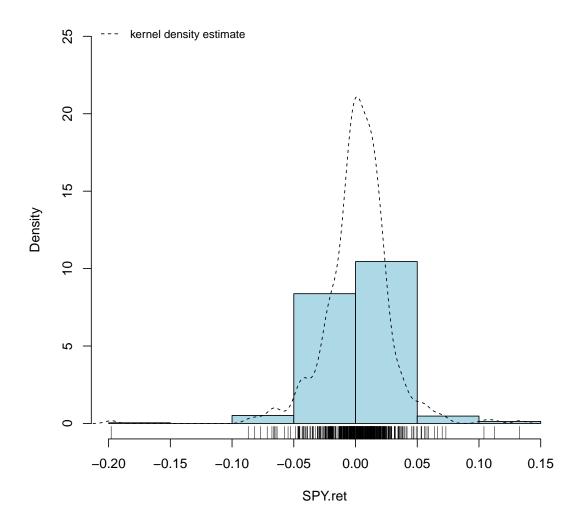
Plot of the SPY weekly returns.

## **SPY Weekly Returns**



A histogram and kernel density estimate of the SPY weekly returns is plotted to better understand its distribution.

## **Histogram of SPY Returns**

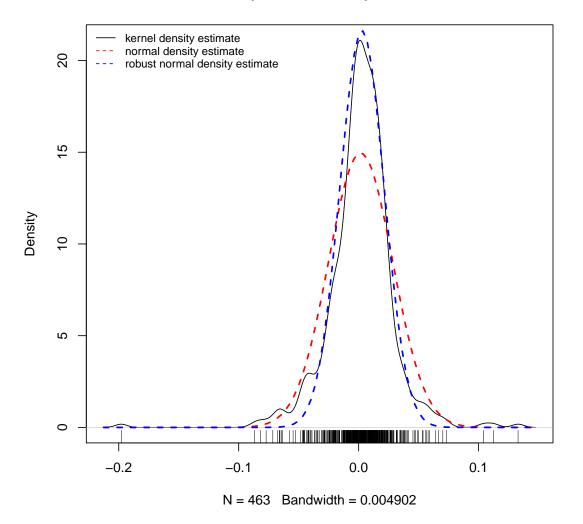


A normal density is overlayed on the plot of the kernel density estimate with standard estimates of the sample mean and standard deviation. Another normal density is overlayed using robust estimates. It is clear from the chart that the robust estimates provide a better fit than the standard estimates of the sample mean and sample standard deviation, but it is not clear if the SPY returns are normally distributed.

```
# Plot the kernel density estimate of SPY Weekly Returns
plot(density(SPY.ret), main = "Density of SPY Weekly Returns")
rug(SPY.ret)
# sample estimates
curve(dnorm(x, mean = mean(SPY.ret), sd = sd(SPY.ret)), add = TRUE, col = "red",
```

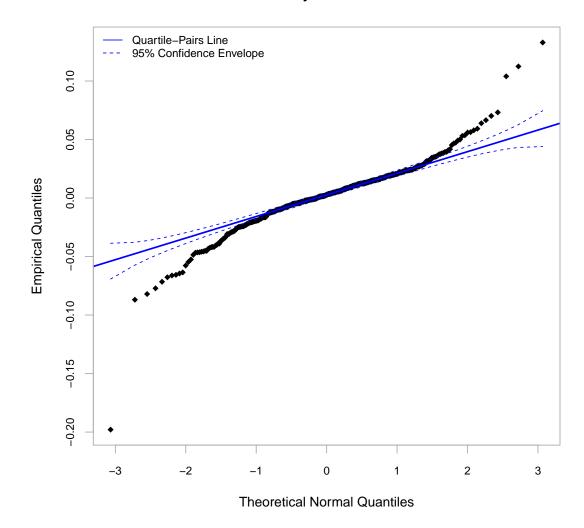
```
lty = 2, lwd = 2)
# robust estimates
curve(dnorm(x, mean = median(SPY.ret), sd = mad(SPY.ret)), add = TRUE, col = "blue",
    lty = 2, lwd = 2)
legend("topleft", legend = c("kernel density estimate", "normal density estimate",
    "robust normal density estimate"), col = c("black", "red", "blue"), lty = c(1, 2, 2), bty = "n", cex = 0.8)
```

## **Density of SPY Weekly Returns**



Quantile-Quantile plot of SPY weekly returns with a 95% confidence envelope. It can be seen from the Normal Q-Q plot that the tails of the SPY returns are well outside of the 95% confidence envelope.

#### SPY Weekly Returns QQ Plot



We can test if the SPY weekly returns came from a normal distribution using the Shapiro-Wilk test of normality. The null hypothesis is that the data came from a normal distribution. The p-value is very small and we can reject the null hypothesis.

```
shapiro.test(coredata(SPY.ret))
##
```

```
## Shapiro-Wilk normality test
##
## data: coredata(SPY.ret)
## W = 0.9096, p-value = 5.567e-16
```

### 1.1 Basic Statistics

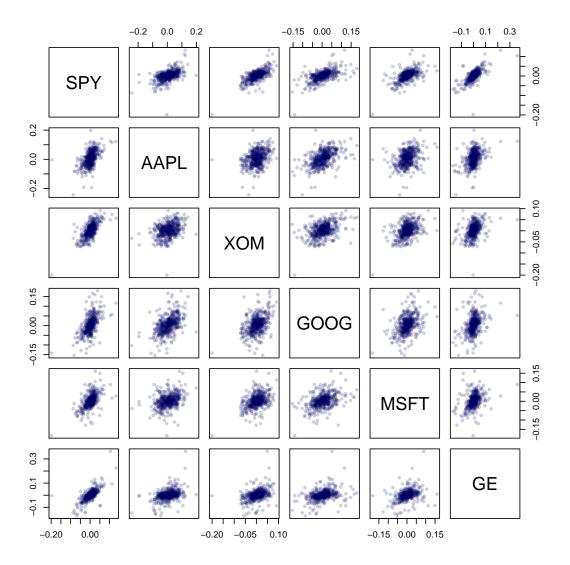
Here we calculate some basic statisities on the SPY weekly returns.

```
# Sample mean of SPY return
mean(SPY.ret)
## [1] 0.001658
# Sample Variance of SPY returns
var(SPY.ret)
##
             SPY
## SPY 0.0007114
# Sample standard deviation of SPY returns
sd(SPY.ret)
## [1] 0.02667
# Standard error of SPY returns
sd(SPY.ret)/sqrt(nrow(SPY.ret))
## [1] 0.00124
# Sample skewness of SPY returns. See ?skewness for additional methods
# for calculating skewness
skewness(SPY.ret, method = "sample")
## [1] -0.7003
```

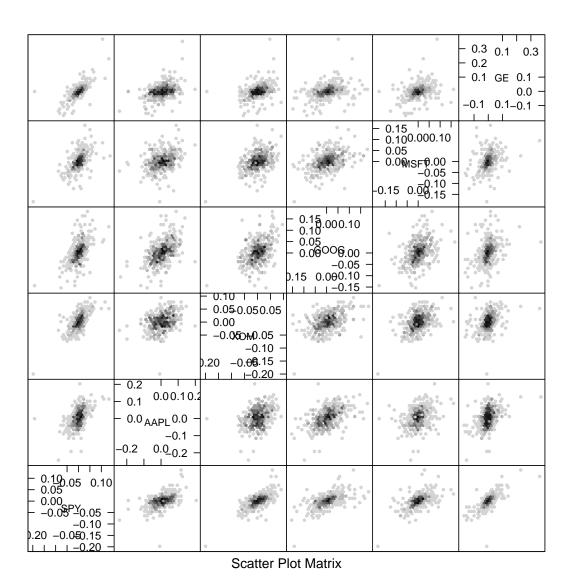
```
{\it\# Sample kurtosis of SPY returns.} \ {\it See ?kurtosis for additional methods}
# for calculating kurtosis
kurtosis(SPY.ret, method = "sample")
## [1] 11.96
# Summary statistics of SPY returns
summary(SPY.ret)
       Index
                             SPY
##
  Min.
          :2005-01-14 Min. :-0.19792
  1st Qu.:2007-04-02 1st Qu.:-0.00974
##
  Median :2009-06-19 Median : 0.00280
## Mean :2009-06-18 Mean : 0.00166
## 3rd Qu.:2011-09-05 3rd Qu.: 0.01516
## Max.
          :2013-11-22 Max. : 0.13291
# Sample quantiles of SPY returns
quantile(SPY.ret, probs = c(0, 0.25, 0.5, 0.75, 1))
##
         0%
                  25%
                            50%
                                      75%
                                               100%
## -0.197921 -0.009744 0.002803 0.015164 0.132913
```

Scatter plot of each pair of assets in the returns dataset.

```
pairs(coredata(returns), pch=20, col=rgb(0,0,100,50,maxColorValue=255))
```



hexplom(coredata(returns), varname.cex=0.75)



Correlation and covariance matrices of assets in the returns dataset.

```
# Sample correlation of returns

cor(returns)

## SPY AAPL XOM GOOG MSFT GE

## SPY 1.0000 0.5301 0.6987 0.5891 0.5837 0.7105

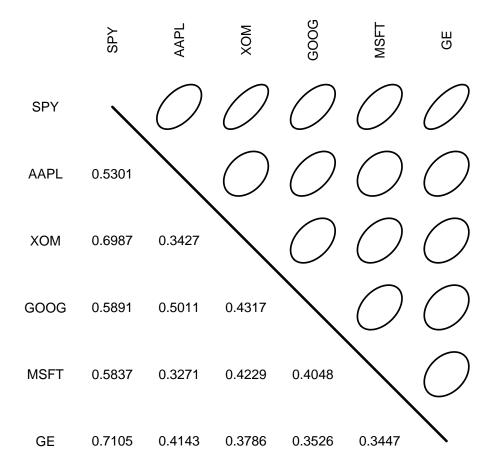
## AAPL 0.5301 1.0000 0.3427 0.5011 0.3271 0.4143

## XOM 0.6987 0.3427 1.0000 0.4317 0.4229 0.3786

## GOOG 0.5891 0.5011 0.4317 1.0000 0.4048 0.3526

## MSFT 0.5837 0.3271 0.4229 0.4048 1.0000 0.3447

## GE 0.7105 0.4143 0.3786 0.3526 0.3447 1.0000
```



Sample Correlation Estimate

```
# SPY AAPL XOM GOOG MSFT GE

## SPY 0.0007114 0.0007224 0.0005693 0.0007086 0.0005597 0.0008329

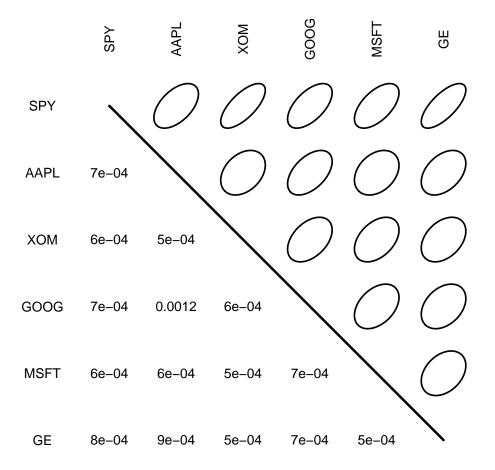
## AAPL 0.0007224 0.0026103 0.0005349 0.0011545 0.0006009 0.0009303

## XOM 0.0005693 0.0005349 0.0009331 0.0005947 0.0004645 0.0005083

## GOOG 0.0007086 0.0011545 0.0005947 0.0020335 0.0006562 0.0006989

## MSFT 0.0005597 0.0006009 0.0004645 0.0006562 0.0012926 0.0005447

## GE 0.0008329 0.0009303 0.0005083 0.0006989 0.0005447 0.0019318
```



Sample Covariance Estimate

#### 1.2 Distributions

R has functions to compute the density, distribution function, quantile, and random number generation for several distributions. The continuous distributions covered in chapter 1 are listed here.

- Normal Distribution: dnorm, pnorm, qnorm, rnorm
- Chi-Squared Distribution: dchisq, pchisq, qchisq, rchisq
- Student t Distribution: dt, pt, qt, rt
- F Distribution: df, pf, qf, rf

In general, the functions are as follows:

- $d^*$ : density
- $p^*$ : distribution function (probability)
- q\*: quantile function
- r\*: random generation

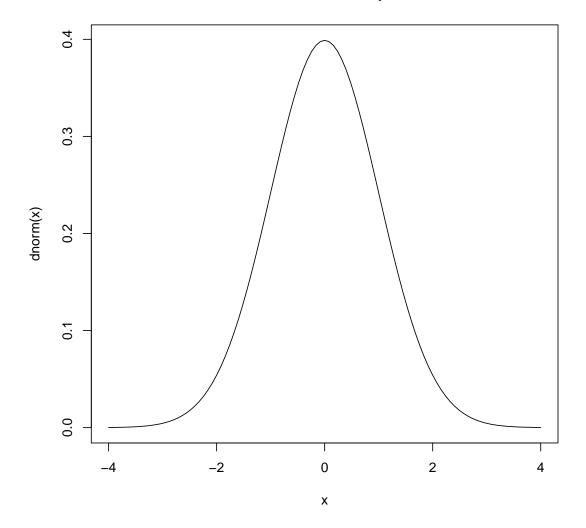
where  $\ast$  is the appropriate distribution.

Here we demonstrate these functions for the normal distribution.

Use dnorm to plot the pdf of a standard normal distribution

```
curve(dnorm(x), from = -4, to = 4, main = "Standard Normal pdf")
```

# **Standard Normal pdf**



Calculate the probability that  $Y \leq 2$  when Y is distributed N(1,4) with mean of 1 and variance of 4.

```
pnorm(q = 2, mean = 1, sd = 2)

## [1] 0.6915

# Normalize as is done in the book
pnorm(q = 0.5)

## [1] 0.6915
```

Quantile function of the standard normal distribution at probability 0.975.

```
qnorm(p = 0.975)
## [1] 1.96
```

Generate 10 random numbers from a normal distribution with mean 0.0015 and standard deviation 0.025.

```
# Set the seed for reproducible results
set.seed(123)
rnorm(n = 10, mean = 0.0015, sd = 0.025)

## [1] -0.012512 -0.004254  0.040468  0.003263  0.004732  0.044377  0.013023
## [8] -0.030127 -0.015671 -0.009642
```

#### 1.3 Hypothesis Test

The null hypothesis is that the true mean return of SPY is equal to 0

```
t.test(x = SPY.ret, alternative = "two.sided", mu = 0)

##

## One Sample t-test

##

## data: SPY.ret

## t = 1.338, df = 462, p-value = 0.1817

## alternative hypothesis: true mean is not equal to 0
```

```
## 95 percent confidence interval:
## -0.0007778 0.0040940
## sample estimates:
## mean of x
## 0.001658
\# Replicate the results of t.test using the method outlined in the book
t_stat <- (mean(SPY.ret) - 0)/(sd(SPY.ret)/sqrt(nrow(SPY.ret)))</pre>
p_value \leftarrow 2 * pt(q = -abs(t_stat), df = 462)
df <- nrow(SPY.ret) - 1</pre>
ci <- mean(SPY.ret) + c(-1, 1) * 1.96 * sd(SPY.ret)/sqrt(nrow(SPY.ret))</pre>
paste("t = ", round(t_stat, 4), ", df = ", df, ", p-value = ", round(p_value,
   4), sep = ""
## [1] "t = 1.3377, df = 462, p-value = 0.1817"
print("95% Confidence Interval")
## [1] "95% Confidence Interval"
print(ci)
## [1] -0.0007714 0.0040877
```

## 2 Regression

#### 2.1 Regression with a single regressor

Extract the weekly returns of AAPL and SPY from the returns object. The returns of AAPL and SPY will be used to demonstrate linear regression in R.

```
AAPL.ret <- returns[, "AAPL"]

SPY.ret <- returns[, "SPY"]

# Fitting linear models works with xts objects, but works better with

# data.frame objects. This is especially true with the predict method for

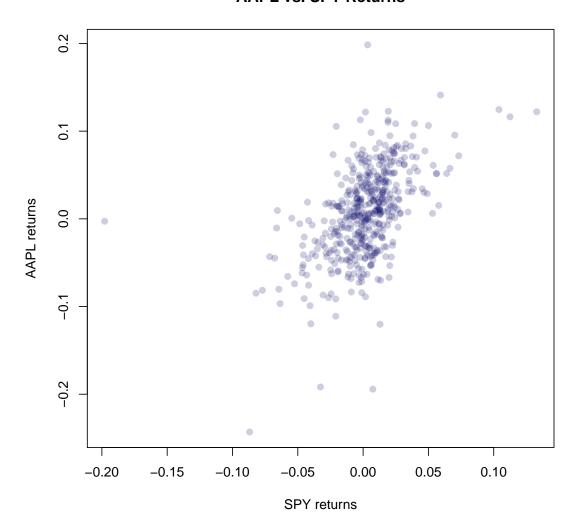
# linear models.
```

```
ret.data <- as.data.frame(cbind(AAPL.ret, SPY.ret))</pre>
```

Scatterplot of AAPL and SPY returns.

```
plot(coredata(SPY.ret), coredata(AAPL.ret), pch = 19, col = rgb(0, 0, 100, 50,
    maxColorValue = 255), xlab = "SPY returns", ylab = "AAPL returns", main = "AAPL vs. SPY Returns"
```

### **AAPL vs. SPY Returns**



Fit the linear regression model. AAPL.ret is the response variable and SPY.ret is the explanatory variable.

```
model.fit <- lm(AAPL ~ SPY, data = ret.data)</pre>
```

The print and summary methods for lm objects are very useful and provide several of the statistics covered in the book. Note that summary(model.fit) will print the summary statistics, but it is often useful to assign the summary object to a variable so that elements from the summary object can be extracted as shown below.

```
# The print method displays the call and the coefficients of the linear
# model
model.fit
##
## Call:
## lm(formula = AAPL ~ SPY, data = ret.data)
## Coefficients:
## (Intercept)
                        SPY
##
      0.00557
                   1.01539
# The summary method displays additional information for the linear model
model.summary <- summary(model.fit)</pre>
model.summary
##
## Call:
## lm(formula = AAPL ~ SPY, data = ret.data)
##
## Residuals:
        Min
                  1Q
                      Median
                                    3Q
                                            Max
## -0.20741 -0.02582 -0.00002 0.02736 0.19262
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.00557
                           0.00202
                                      2.76
                                              0.006 **
## SPY
               1.01539
                           0.07565
                                     13.42
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 0.0434 on 461 degrees of freedom
## Multiple R-squared: 0.281,Adjusted R-squared: 0.279
## F-statistic: 180 on 1 and 461 DF, p-value: <2e-16</pre>
```

#### Access elements of the 1m object

```
# Coefficients
coef(model.fit)

## (Intercept) SPY

## 0.005573 1.015387

# Extract the fitted values fitted(model.fit) Extract the residuals
# resid(model.fit) Exctract the standardized residuals
# rstandard(model.fit)
```

#### Access elements of the lm.summary object

```
# Coefficients
model.coef <- coef(model.summary)</pre>
model.coef
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.005573 0.002019 2.76 6.017e-03
## SPY
          1.015387 0.075648 13.42 6.607e-35
# Get the alpha and beta and the standard errors
alpha <- round(model.coef[1, 1], 6)</pre>
alpha.se <- round(model.coef[1, 2], 6)</pre>
beta <- round(model.coef[2, 1], 6)</pre>
beta.se <- round(model.coef[2, 2], 6)</pre>
# Sigma
model.summary$sigma
## [1] 0.04337
# R squared
model.summary$r.squared
```

```
## [1] 0.281

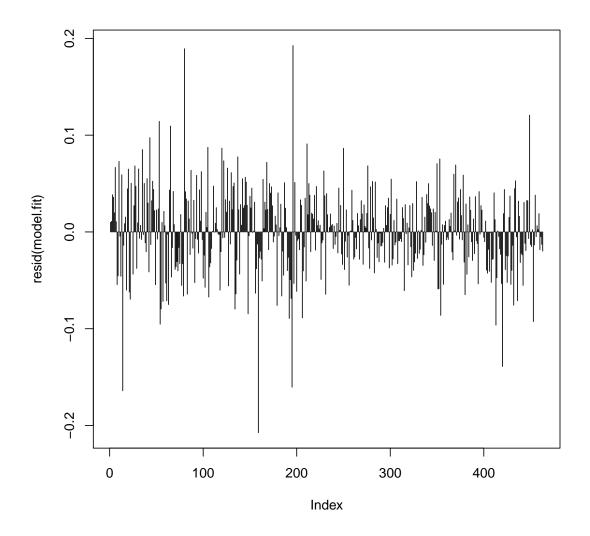
# Adjusted R squared

model.summary$adj.r.squared

## [1] 0.2794
```

Plot the residuals of the model.

```
plot(resid(model.fit), type = "h")
```

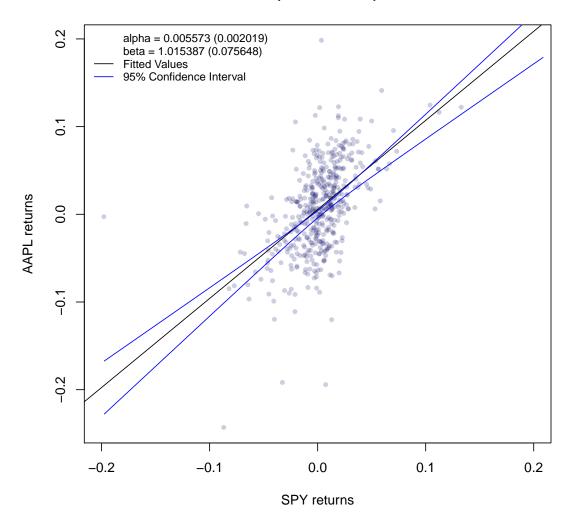


Use the  $\operatorname{\mathtt{predict}}$  method to calculate the confidence and prediction intervals of the fitted model.

```
new <- data.frame(SPY = seq(from = -0.2, to = 0.2, length.out = nrow(ret.data)))
model.ci <- predict(object = model.fit, newdata = new, interval = "confidence")
model.pi <- predict(object = model.fit, newdata = new, interval = "prediction")</pre>
```

Plot the fitted model with the confidence interval.

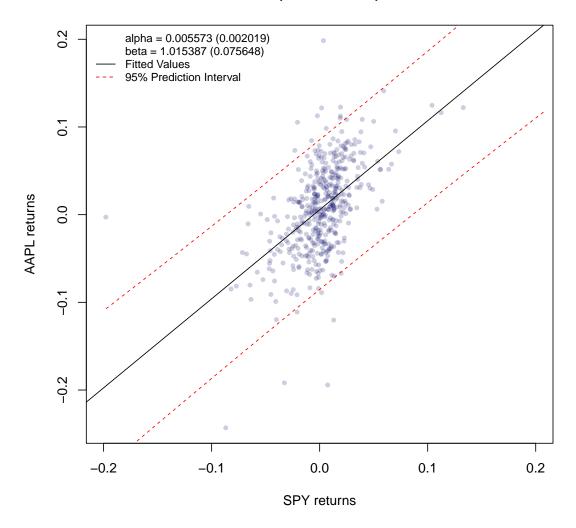
# Im(AAPL ~ SPY)



Plot the fitted model with the and prediction interval.

```
"Fitted Values", "95% Prediction Interval"), col=c("black", "red"), lty=c(0, 0, 1, 2), cex=0.8, bty="n")
```

# Im(AAPL ~ SPY)



## 2.2 Regression with multiple regressors

The Fama French 3 Factor model is used to demonstrate regression with multiple regressors. The first example will use AAPL weekly returns and the Fama French factors from 2005-01-14 to 2013-10-25. The premise of the model is that AAPL returns can be explained by the 3 factors of the Fama French model.

```
data(fama_french_factors)

# The first 3 columns are the factors, the 4th column is the risk free

# rate.

ff_factors <- fama_french_factors[, 1:3]
head(ff_factors, 5)

## Mkt-RF SMB HML

## 2005-01-14 0.00 0.44 1.10

## 2005-01-21 -1.33 0.17 0.58

## 2005-01-28 0.26 0.19 0.42

## 2005-02-04 2.90 0.94 0.39

## 2005-02-11 0.08 -0.68 0.50</pre>
```

Mkt-RF is the market excess return. SMB is  $\mathbf{S}$ mall  $\mathbf{M}$ inus  $\mathbf{B}$ ig in terms of market capitalization. HML is  $\mathbf{H}$ igh  $\mathbf{M}$ inus  $\mathbf{L}$ ow in terms of book-to-market.

```
# Align the dates of the Fama-French Factors and the returns
returns <- returns["/2013-10-25"]

AAPL.ret <- returns[, "AAPL"]

# AAPL excess returns
AAPL.e <- AAPL.ret - fama_french_factors[, "RF"]/100</pre>
```

```
# Fit the model
ff.fit <- lm(AAPL.e ~ ff_factors)</pre>
ff.fit
##
## lm(formula = AAPL.e ~ ff_factors)
##
## Coefficients:
        (Intercept) ff_factorsMkt-RF
##
                                           ff_factorsSMB
                                                              ff_factorsHML
                                                                    -0.00640
            0.00540
                               0.01145
                                                  0.00333
summary(ff.fit)
```

```
##
## Call:
## lm(formula = AAPL.e ~ ff_factors)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
                                          Max
## -0.19963 -0.02661 -0.00039 0.02387 0.20464
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   0.00540
                              0.00197 2.74 0.0065 **
## ff_factorsMkt-RF 0.01145 0.00087 13.16 <2e-16 ***
## ff_factorsSMB
                   0.00333 0.00186
                                       1.79 0.0735 .
## ff_factorsHML
                  -0.00640
                                      -3.75 0.0002 ***
                              0.00171
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0422 on 455 degrees of freedom
## Multiple R-squared: 0.327, Adjusted R-squared: 0.322
## F-statistic: 73.6 on 3 and 455 DF, p-value: <2e-16
```

If we wanted to fit the model to more assets, we could manually fit the model with different assets as the response variable. However, we can automatically fit several models very easily with R.

```
# Omit the first column of returns because it is the SPY weekly returns,
# which is a proxy for the market.
returns <- returns[, -1]

# Calculate the excess returns of all assets in the returns object
ret.e <- returns - (fama_french_factors[, "RF"]/100) %*% rep(1, ncol(returns))</pre>
```

The ret.e object contains the excess returns for AAPL, XOM, GOOG, MSFT, and GE.

```
# Show the first 5 rows of ret.e

head(ret.e, 5)

## AAPL XOM GOOG MSFT GE

## 2005-01-14 0.013340 0.02512 0.03117 -0.02073 -0.01400

## 2005-01-21 0.003725 -0.01260 -0.05886 -0.01838 -0.01112

## 2005-01-28 0.049189 0.01607 0.01054 0.02026 0.01702

## 2005-02-04 0.065298 0.07799 0.07326 0.00466 0.01368

## 2005-02-11 0.029506 0.01926 -0.08339 -0.01367 -0.00115
```

Here we fit the Fama French 3 Factor model to each asset in ret.e. This fits 5 models, 1 for each asset, and stores results of each model in the ff.fit object as a multiple linear model (mlm) object.

```
ff.fit <- lm(ret.e ~ ff_factors)</pre>
# Display the coefficients of each model
ff.fit
##
## Call:
## lm(formula = ret.e ~ ff_factors)
## Coefficients:
##
                     AAPL
                                 MOX
                                            GOOG
                                                        MSFT
                                                                   GE
## (Intercept)
                      0.005401
                                  0.000809
                                             0.002845
                                                         0.000300
                                                                   -0.001109
## ff_factorsMkt-RF
                      0.011450
                                  0.008784
                                             0.011521
                                                         0.009724
                                                                    0.009792
## ff_factorsSMB
                      0.003334
                                 -0.004706
                                            -0.000259
                                                        -0.003170
                                                                    0.001164
## ff_factorsHML
                     -0.006396
                                -0.002046
                                           -0.006467
                                                       -0.007470
                                                                    0.008276
```

Extract and plot the beta values and the R squared values for each asset from the Fama French 3 Factor model.

```
beta0 <- coef(ff.fit)[1, ]
beta1 <- coef(ff.fit)[2, ]
beta2 <- coef(ff.fit)[3, ]
beta3 <- coef(ff.fit)[4, ]
rsq <- sapply(X = summary(ff.fit), FUN = function(x) x$r.squared)</pre>
```

```
names(rsq) <- colnames(ret.e)

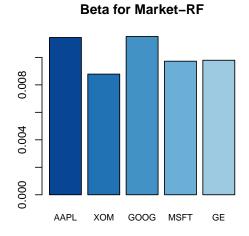
par(mfrow = c(2, 2))

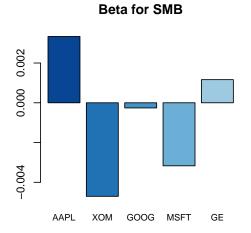
barplot(beta1, main = "Beta for Market-RF", col = bluemono, cex.names = 0.8)

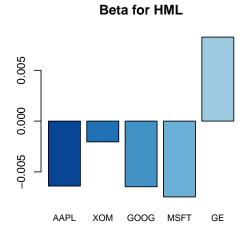
barplot(beta2, main = "Beta for SMB", col = bluemono, cex.names = 0.8)

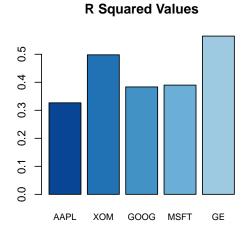
barplot(beta3, main = "Beta for HML", col = bluemono, cex.names = 0.8)

barplot(rsq, main = "R Squared Values", col = bluemono, cex.names = 0.8)</pre>
```









```
par(mfrow = c(1, 1))
```

Display the summary object for each model

```
summary(ff.fit)
## Response AAPL :
##
## Call:
## lm(formula = AAPL ~ ff_factors)
##
## Residuals:
##
            AAPL
## Min -0.199630
## 1Q
        -0.026608
## Median -0.000385
## 3Q
        0.023870
## Max
        0.204637
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                 0.00540 0.00197 2.74 0.0065 **
## (Intercept)
## ff_factorsMkt-RF 0.01145 0.00087 13.16 <2e-16 ***
## ff_factorsSMB
                  0.00333 0.00186 1.79 0.0735 .
## ff_factorsHML -0.00640
                             0.00171 -3.75 0.0002 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0422 on 455 degrees of freedom
## Multiple R-squared: 0.327, Adjusted R-squared: 0.322
## F-statistic: 73.6 on 3 and 455 DF, p-value: <2e-16
##
##
## Response XOM :
##
## Call:
## lm(formula = XOM ~ ff_factors)
##
## Residuals:
```

```
##
          MOX
## Min -0.071559
## 1Q
        -0.011856
## Median -0.000349
## 3Q
         0.012376
## Max
         0.092450
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
              0.000809 0.001016 0.80 0.43
## (Intercept)
## ff_factorsMkt-RF 0.008784 0.000448 19.61 < 2e-16 ***
## ff_factorsSMB -0.004706 0.000957 -4.92 1.2e-06 ***
## ff_factorsHML -0.002046 0.000878 -2.33 0.02 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0217 on 455 degrees of freedom
## Multiple R-squared: 0.498, Adjusted R-squared: 0.495
## F-statistic: 150 on 3 and 455 DF, p-value: <2e-16
##
## Response GOOG :
##
## Call:
## lm(formula = GOOG ~ ff_factors)
##
## Residuals:
##
            GOOG
## Min
        -0.13693
## 1Q
        -0.01741
## Median -0.00232
## 3Q
         0.01527
        0.15804
## Max
```

```
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.002845 0.001668 1.71 0.089.
## ff_factorsMkt-RF 0.011521 0.000735 15.68 < 2e-16 ***
## ff_factorsSMB -0.000259 0.001570 -0.17 0.869
## ff_factorsHML -0.006467 0.001441 -4.49 9.1e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0357 on 455 degrees of freedom
## Multiple R-squared: 0.383, Adjusted R-squared: 0.379
## F-statistic: 94.3 on 3 and 455 DF, p-value: <2e-16
##
##
## Response MSFT :
##
## Call:
## lm(formula = MSFT ~ ff_factors)
## Residuals:
            MSFT
## Min -0.125627
## 1Q
        -0.013886
## Median -0.000495
## 3Q
        0.012635
        0.137178
## Max
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.000300 0.001319 0.23 0.820
## ff_factorsMkt-RF 0.009724 0.000581 16.73 < 2e-16 ***
## ff_factorsSMB -0.003170 0.001241 -2.55 0.011 *
## ff_factorsHML -0.007470 0.001140 -6.56 1.5e-10 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0282 on 455 degrees of freedom
## Multiple R-squared: 0.39, Adjusted R-squared: 0.386
## F-statistic: 96.9 on 3 and 455 DF, p-value: <2e-16
##
##
## Response GE :
##
## Call:
## lm(formula = GE ~ ff_factors)
##
## Residuals:
##
            GE
## Min -0.13291
## 1Q
        -0.01460
## Median -0.00156
## 3Q
        0.01266
## Max
        0.21088
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
               -0.001109 0.001366 -0.81 0.42
## ff_factorsMkt-RF 0.009792 0.000602 16.27 < 2e-16 ***
## ff_factorsHML
                ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0292 on 455 degrees of freedom
## Multiple R-squared: 0.565, Adjusted R-squared: 0.562
## F-statistic: 197 on 3 and 455 DF, p-value: <2e-16
```