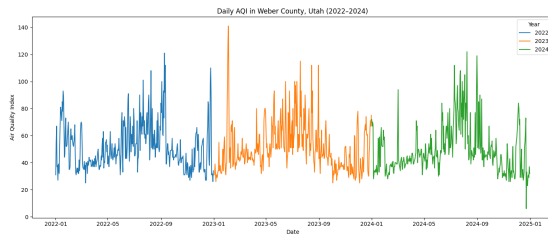


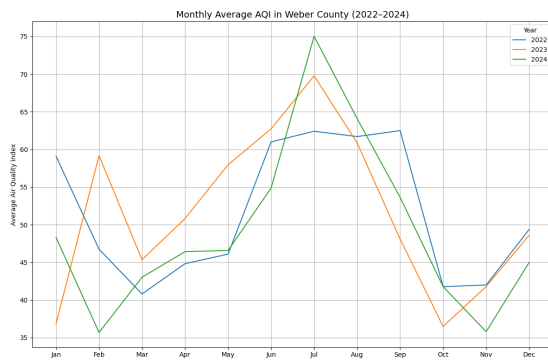
Math6450_Assignment3

October 16, 2025

Exploratory Data Analysis (EDA): The data was loaded in and filtered to remove all columns except for State Name, and county Name. Then additional steps were taken to only grab rows with Utah, and Weber in their state and county name. 2022 had 365 rows, 2023 had 365 rows, and 2024 had 366 rows. This meant that there was a valid data entry for every single day, and this was proven to be true since there were no missing or NA values in these datasets.

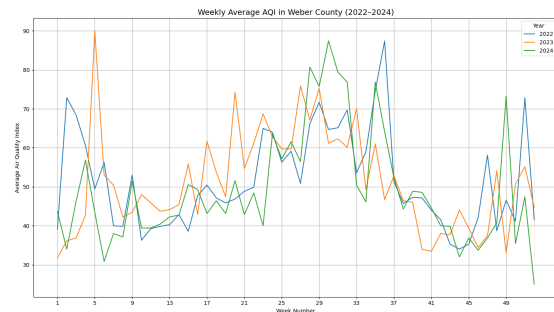


The daily AQI shows that there is quite a bit of fluctuations day to day, and that each year follows a similar pattern. This means there seasonality is present in this data.



Using the monthly average of the AQI shows a smoother line and a bigger picture view to how

the data has changed over the years. However, it can smooth the line too much and it may not be able to capture short-term AQI fluctuations and changes. Smoothing out the graph also shows the very obvious point where we have a seasonal trend. The month July consistently jumps up in AQI.



Looking at the weekly changes in AQI shows that there seems to be some seasonality and trends in the data, but we can see short term fluctuations as well. This may be an applicable middle ground since the lines aren't as smooth as they are in the monthly AQI plot.

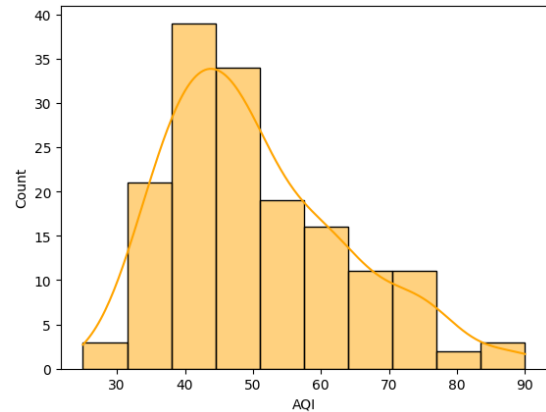
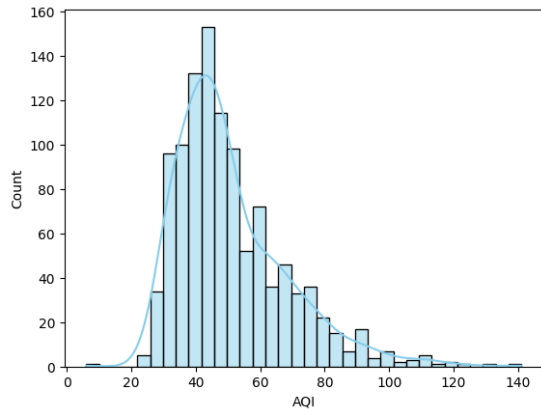
Reason for Aggregation (if applicable):

Upon initial data exploration, while there is enough data for daily time series modeling, the distribution was skewed right, and the daily trends were quite jagged. So, when graphing both monthly, and weekly averages the monthly data looked a little to smooth, and weekly data looked to be the most promising since there are still obvious seasonly patterns and the data didn't look so smoothed over it wouldn't capture other trends.

So, in an attempt to capture as much AQI patterns as possible this the weekly and monthly

data will be used to compare and contrast results.

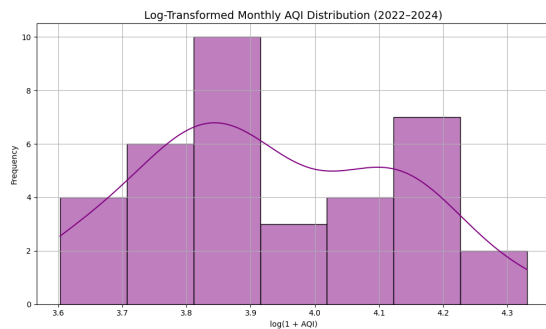
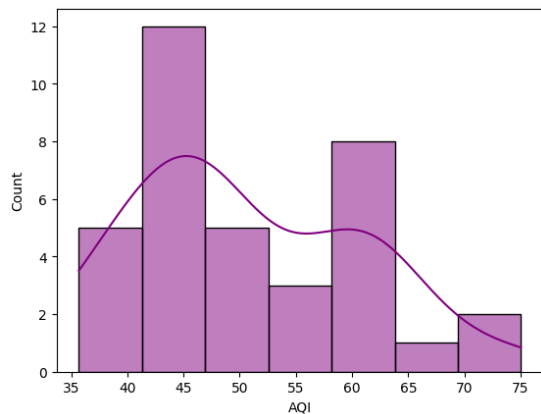
This means that from the daily AQI data we will aggregate the weekly and monthly means for analyzing, and AQI forecasting.



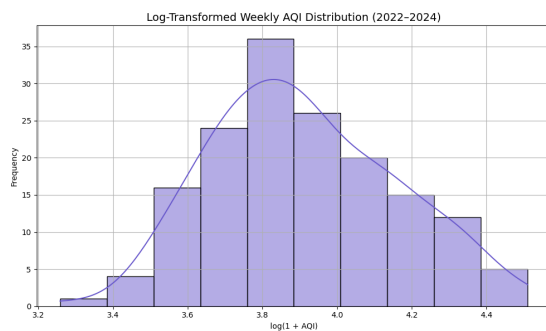
The variance is not as prevalent, but still there, so we will move to log transformations to ensure the data is stationary.

Transformations:

The daily AQI variance is a little skewed to the right, and so aggregation will be a good idea for making the variance more normal.



The distributuion looks quite normal now after log transformation.



The monthly AQI data shows a similar right-skewed pattern, but the tail is a little smaller now.

The log transformed weekly data also shows a more normal variance when plotted.

Seasonal Patterns: Well it passed after log transforming so we will still check for seasonality.

We first noticed of the seasonality of the data in the Daily AQI graph, and it was made clear there was seasonality when graphing the aggregated monthly avg AQI dataset. In order to get rid of this seasonality seasonal differencing will be needed to ensure this dataset is stationary and ready for modeling.

ADF Test - Monthly AQI AVG without Log
Transformation

ADF Statistic: -3.350751238120374

p-value: 0.012756803233213314

ADF Test - Monthly AQI AVG w/ Log

Transformation

ADF Statistic: -3.4826220890374864

p-value: 0.008444774199784521

ADF Test - Weekly AQI AVG without Log

Transformation

ADF Statistic: -3.2934795957089746

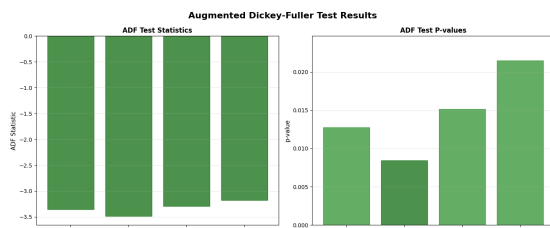
p-value: 0.015172464527294545

ADF Test - Weekly AQI AVG w/ Log

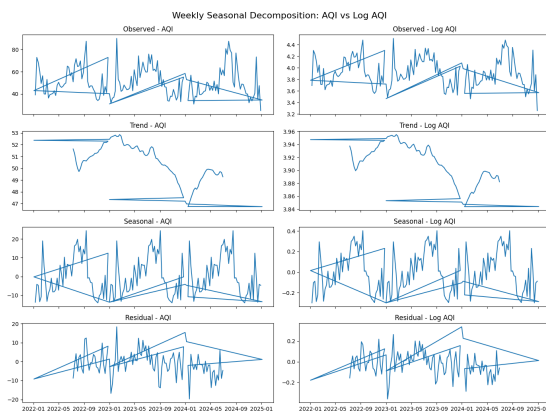
Transformation

ADF Statistic: -3.1750361754617558

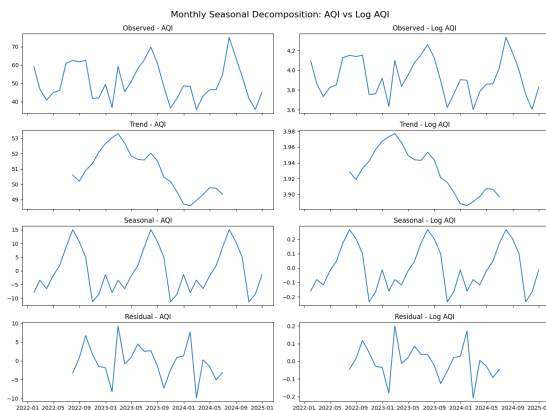
p-value: 0.021475924955530693



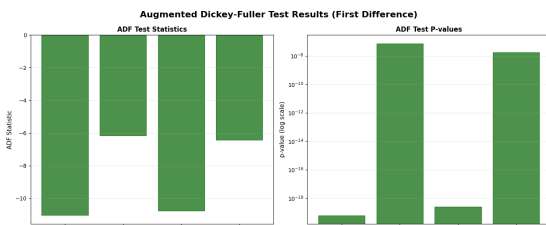
We can interpret the adf statistic as the more negative, the more evidence there is that the data is stationary. A smaller p-value means that there is high evidence we can reject the null resulting in a stationary time series. Both of these numbers are low so we can assume we have stationary time series data.



The seasonal decomposition shows there are several spikes in data here and there, but most importantly there is oscillating behavior in the visuals which means air quality does suffer from seasonality.



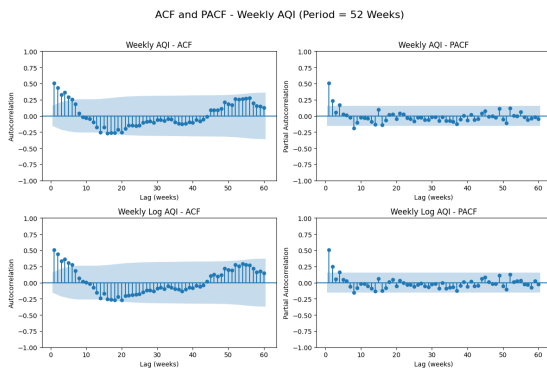
Since the trend and seasonality of this data was so obvious when looking at the values graphed, I wanted to also see what the monthly data looked like, and it is much more obvious that there is a major trend going on in this data.



We knew that there was seasonality in the data so by taking the season first difference we have adf stats that are more negative, and p-values that are even smaller, showing that the data has significant evidence that it is stationary.

Comparing the ADF p-value for the weekly aqi/logged-aqi values and the monthly aqi/logged-aqi values show that the p-value is very small meaning were making the data more stationarity.

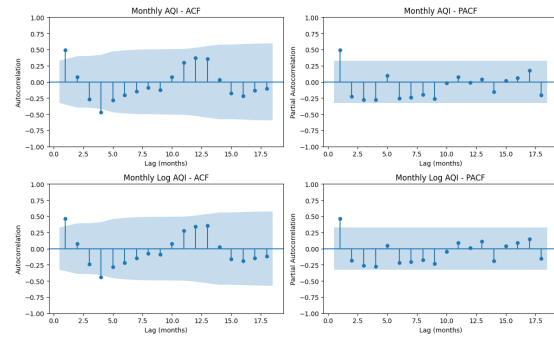
Autocorrelation:



The lags show that at about lag 8, we start to see a reverse of direction in correlation. This must mean that as it looks back further in the year, since the weather changes this also changes AQI.

The PACF graph starts high, and after 1 lag has a steep drop off and then tails off with no clear pattern. This can be interpreted as after 1 lag, there isn't a direct strong influence on the weekly AQI values.

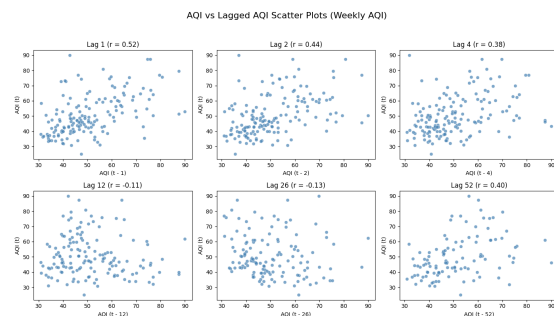
ACF and PACF - Monthly AQI (Period = 12 Months)

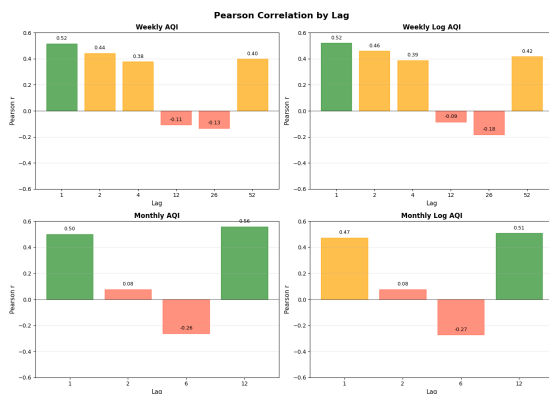
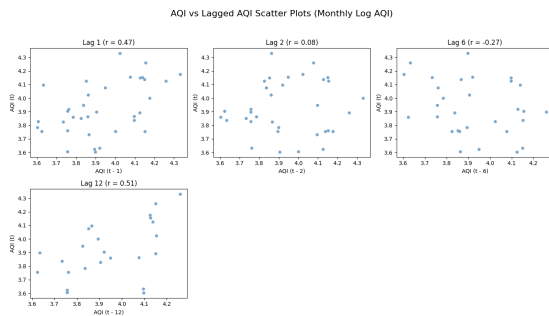
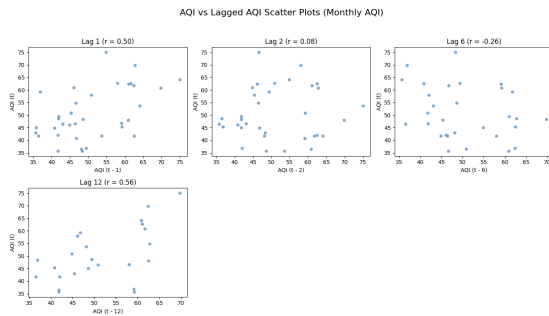
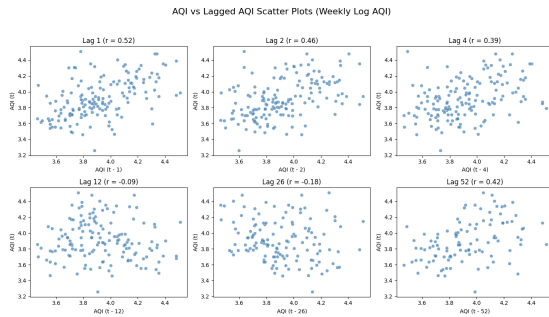


The monthly ACF graphs show a similar pattern to the weekly ACF graphs. There is usually a seasonal pattern that can be explained by the changing of the seasons showing that there is a correlation effect on AQI from the seasonal changes.

The monthly PACF graph also shows similar results to the weekly PACF plot results because of the immediate step drop off on lag 1, and then there is no clear pattern. This confirms the verdict above that there is no strong and direct influence from earlier months once the 1st month is accounted for.

Correlation Coefficients:





The weekly correlation shows seasonality due to what I'd assume literal seasons, like fall, winter, summer, and spring. It makes sense that on a lag of 1, there is a positive correlation because it is still within the season. However, looking at lags 12, and 26, that is comparing data to a different season which causes a negative correlation reversing the correlation. I can say since I start this lag in January, 26 weeks ago from January is in the summer, June or July, so it makes sense the lag would calculate a negative correlation.

Looking at the monthly data pretty much confirms this as well, since looking at lag 6 shows a negative correlation with the current value meaning winter is colder than summer. So, we can confirm that there is correlation and seasonality in this data, and we will now be able to better select a model to forecast the AQI.

Comparing the pearson_r scores with the plotted ACF graph shows they both agree with each other reinforcing that correlation and seasonality is present in this data due to changing seasons.

Data Splitting:

Model Selection:

Model Parameters and Diagnostics:

Final Model Equation:

Forecasting:

Model Performance:

Conclusion: