

# Course 2

## *Algorithm Scanning v2*

```
While (not.eof) do  
    detect(token);  
    if token is reserved word OR operator OR separator  
        then genPIF(token, 0)  
    else  
        if token is identifier OR constant  
            then index = pos(token, ST);  
                genPIF(token_type, index)  
            else message "Lexical error"  
        endif  
    endif  
endwhile
```

# Remarks:

- Also comments are eliminated
- Most important operations: SEARCH and INSERT

# Symbol Table

**Definition** = contains all information collected during compiling regarding the symbolic names from the source program

  
identifiers, constants, etc.

Variants:

- Unique symbol table – contains all symbolic names
- distinct symbol tables: IT (identifiers table) + CT (constants table)

# ST organization

*Remark:* search and insert

- |  |            |
|--|------------|
| 1. Unsorted table – in order of detection in source code | $O(n)$     |
| 2. Sorted table: alphabetic (numeric)                    | $O(\lg n)$ |
| 3. Binary search tree (balanced)                         | $O(\lg n)$ |
| 4. Hash table  | $O(1)$     |

# Hash table

- $K$  = set of keys (symbolic names)
- $A$  = set of positions ( $|A| = m$ ;  $m$  –prime number)

$$h : K \rightarrow A$$

$$h(k) = (\text{val}(k) \bmod m) + 1$$

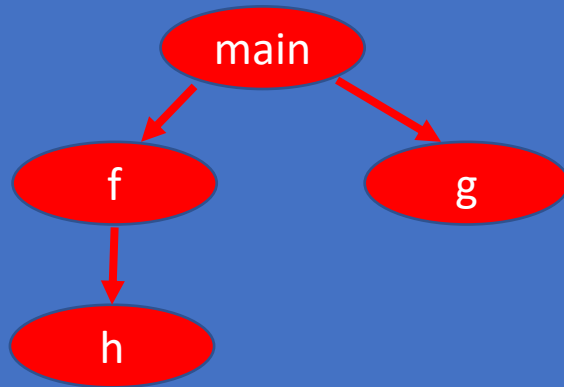
- Conflicts:  $k_1 \neq k_2$  ,  $h(k_1) = h(k_2)$

Toy hash function to use at  
lab:  
Sum of ASCII codes of chars

# Visibility domain (scope)

- Each scope – separate ST
- Structure -> inclusion tree

Hierarchical structure of STs:



**Example:**

```
Int main(){  
  ... int a;  
  
  void f()  
  {float a;  
    ... int h() {...}  
  }  
  ...  
  void g()  
  {char a;  
    ...  
  }  
}
```

# Formal Languages

- *basic notions* -



# Examples of languages

- natural (ex. English, Romanian)
- programming (ex. C, C++, Java, Python)
- formal

A formal language is a set

Ex.:

$L = \{a^n b^n \mid n > 0\}$   $L = \{ab, aabb, aaabbb, \dots\}$

$L' = \{01^n \mid n \geq 0\}$   $L' = \{0, 01, 011, \dots\}$

# Example

a boy has a dog

$S \rightarrow PV$   
 $P \rightarrow a N$   
 $N \rightarrow \text{boy} \text{ or } N \rightarrow \text{dog}$   
 $(N \rightarrow \text{boy} | \text{dog})$   
 $V \rightarrow QC$   
 $Q \rightarrow \text{has}$   
 $C \rightarrow BN$   
 $B \rightarrow a$

- $A \rightarrow \alpha$  = **rule**
- $S, P, V, N, Q, C, B$  = **nonterminal symbols**
- $a, \text{boy}, \text{dog}, \text{has}$  = **terminal symbols**

## Remarks

1. Sentence = word, sequence (contains only terminal symbols) ; denoted  $w$ .
2.  $S \Rightarrow PV \Rightarrow a NV \Rightarrow a NQC \Rightarrow a N \text{ has } C$  - sentential form

In general :  $w = a_1 a_2 \dots a_n$

3. The rule guarantees syntactical correctness, but not the semantical correctness (*A dog has a boy*)

# Grammar

- **Definition**: A (formal) **grammar** is a 4-tuple:  $G=(N,\Sigma,P,S)$  with the following meanings:
  - $N$  – set of nonterminal symbols and  $|N| < \infty$
  - $\Sigma$  - set of terminal symbols (alphabet) and  $|\Sigma| < \infty$
  - $P$  – finite set of productions (rules), with the propriety:  
$$P \subseteq (N \cup \Sigma)^* N (N \cup \Sigma)^* \times (N \cup \Sigma)^*$$
  - $S \in N$  – start symbol / axiom

## Remarks :

1.  $(\alpha, \beta) \in P$  is a production denoted  $\alpha \rightarrow \beta$
2.  $N \cap \Sigma = \emptyset$

$A^*$  = transitive and reflexive closure =  
 $\{a, aa, aaa, \dots\} \cup \{a^0\}$   
 $A = \{a\}$   
 $A^+ = \{a, aa, aaa, \dots\}$   
 $X^0 = \varepsilon$

# Binary relations defined on $(N \cup \Sigma)^*$

- **Direct derivation**

$\alpha \Rightarrow \beta$ ,  $\alpha, \beta \in (N \cup \Sigma)^*$  **if**  $\alpha = x1xy1$ ,  $\beta = x1yy1$  **and**  $x \rightarrow y \in P$   
(x is transformed in y)

- **k derivation**

$\alpha \xRightarrow{k} \beta$ ,  $\alpha, \beta \in (N \cup \Sigma)^*$

sequence of k direct derivations  $\alpha \Rightarrow \alpha_1 \Rightarrow \alpha_2 \Rightarrow \dots \Rightarrow \alpha_{k-1} \Rightarrow \beta$ ,  $\alpha, \alpha_1, \alpha_2, \dots, \alpha_{k-1}, \beta \in (N \cup \Sigma)^*$

- **+ derivation**

$\alpha \xRightarrow{+} \beta$  **if**  $\exists k > 0$  **such that**  $\alpha \xRightarrow{k} \beta$  (there exists at least one direct derivation)

- **\* derivation**

$\alpha \xRightarrow{*} \beta$  **if**  $\exists k \geq 0$  **such that**  $\alpha \xRightarrow{k} \beta$  namely,  $\alpha \xRightarrow{*} \beta \Leftrightarrow \alpha \xRightarrow{+} \beta$  **OR**  $\alpha \xRightarrow{0} \beta$  ( $\alpha = \beta$ )

**Definition:** *Language generated* by a grammar  $G=(N,\Sigma,P,S)$  is:

$$L(G)=\{w \in \Sigma^* \mid S \xRightarrow{*} w\}$$

**Remarks:**

1.  $S \xRightarrow{*} \alpha, \alpha \in (N \cup \Sigma)^* =$  sentential form  
 $S \xRightarrow{*} w, w \in \Sigma^* =$  word / sequence

2. Operations defined for languages (sets) :

$$L_1 \cup L_2, L_1 \cap L_2, L_1 - L_2, \bar{L} \text{ (complement)}, L^+ = \bigcup_{k>0} L^k, L^* = \bigcup_{k \geq 0} L^k$$

$$\text{Concatenation: } L = L_1 L_2 = \{w_1 w_2 \mid w_1 \in L_1, w_2 \in L_2\}$$

3.  $|w|=0$  (empty word - denoted  $\varepsilon$ )

$$L_1 = \{a, b, aa\}$$

$$L_2 = \{c, d, cd\}$$

$$L_1 L_2 = \{ac, ad, acd, bc, bd, bcd, aac, aad, aacd\}$$

**Definition:** Two grammar  $G_1$  and  $G_2$  are equivalent if they generate the same language

$$L(G_1) = L(G_2)$$

# Chomsky hierarchy(based on form $\alpha \rightarrow \beta \in P$ )

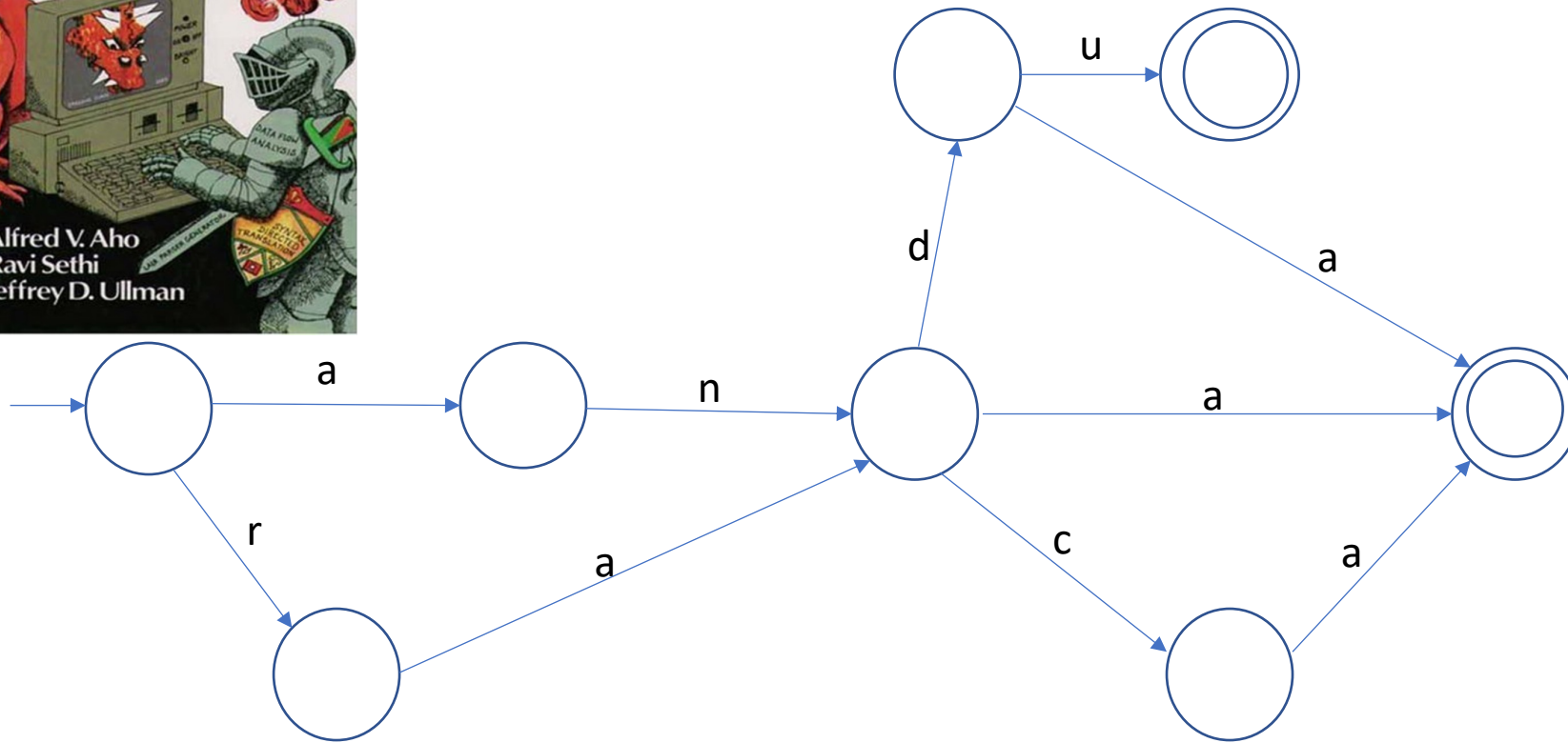
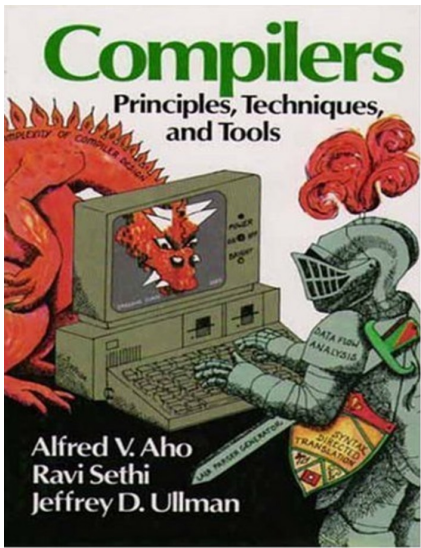
- type 0 : no restriction
- type 1 : context dependent grammar ( $x_1Ay_1 \rightarrow x_1\gamma y_1$ )
- type 2 : context free grammar ( $A \rightarrow \alpha \in P$ , where  $A \in N$  and  $\alpha \in (N \cup \Sigma)^*$ )
- type 3 : regular grammar ( $A \rightarrow aB \mid a \in P$ )

## **Remark :**

type 3  $\subseteq$  type 2  $\subseteq$  type 1  $\subseteq$  type 0

# Notations

- $A, B, C, \dots$  – nonterminal symbols
- $S \in N$  – start symbol
- $a, b, c, \dots \in \Sigma$  – terminal symbol
- $\alpha, \beta, \gamma \in (N \cup \Sigma)^*$  – sentential forms
- $\varepsilon$  – empty word
- $x, y, z, w \in \Sigma^*$  – words
- $X, Y, U, \dots \in (N \cup \Sigma)$  – grammar symbols (nonterminal or terminal)



**Problem:** The door to the tower is closed by the **Red Dragon**, using a complicated machinery. Prince Charming has managed to steal the plans and is asking for your help. Can you help him determining all the person names that can unlock the door