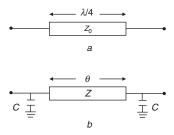
## **Highly miniaturised Wilkinson power** divider employing $\pi$ -type multiple coupled microstrip line structure

D.H. Lee, Y.B. Park and Y. Yun

Using a  $\pi$ -type multiple coupled microstrip line structure, a highly miniaturised Wilkinson power divider is fabricated. The line length of the power divider was reduced to about  $\lambda/44$ , and its size was 37% of a conventional Wilkinson power divider. The novel power divider showed good RF performances in S/C band.

Introduction: In RFIC devices such as PA and mixer [1], a combiner/divider is required for its operation. A Wilkinson power divider is one of the passive components widely used for power splitting/combining. However, a conventional Wilkinson power divider employs a quarter-wavelength line, which highly increases circuit size and manufacturing cost.

In this work, to realise a miniaturised Wilkinson power divider, we propose a  $\pi$ -type multiple coupled microstrip line structure (MCMLS). Concretely, the Wilkinson power divider was highly miniaturised by substituting a quarter-wavelength line for  $\pi$ -type MCMLS. In the  $\pi$ -type MCMLS, the characteristic impedance of the line does not increase rapidly, though the line is shortened by shunt capacitors, which facilitated the fabrication of the miniaturised RF passive components.



**Fig. 1** Quarter-wavelength line, and conventional  $\pi$ -type single microstrip line structure (SMLS) equivalent to quarter-wavelength line

- a Quarter-wavelength line
- b Conventional  $\pi$ -type SMLS equivalent to quarter-wavelength line

Novel microstrip line employing  $\pi$ -type MCMLS: Figs. 1a and b show a quarter-wavelength line and conventional  $\pi$ -type single microstrip line structure (SMLS) equivalent to the quarter-wavelength line, respectively. Equations (1)-(3) should be satisfied in order that the conventional  $\pi$ -type SMLS may be equivalent with the quarterwavelength line [2].

$$\omega C = \frac{\cos \theta}{Z} \tag{1}$$

$$Z = \frac{Z_0}{\sin \theta} \tag{2}$$

$$\omega C = \frac{\cos \theta}{Z}$$

$$Z = \frac{Z_0}{\sin \theta}$$

$$Z = \frac{Z_0}{\sqrt{1 - (\omega C Z_0)^2}}$$
(2)
(3)

From (1) and (2) we can see that as the line length of the  $\pi$ -type SMLS of Fig. 1b becomes shorter, the shunt capacitor C and characteristic impedance Z become larger in a range of  $0 \le \theta \le \pi/2$ , which makes it impossible to physically realise a microstrip line shorter than  $\lambda/10$  by using the  $\pi$ -type SMLS [2]; e.g. if the line length of the  $\pi$ -type SMLS becomes less than  $\lambda/10$ , the characteristic impedance Z becomes higher than 100  $\Omega$ . However, the microstrip line, the characteristic impedance of which is higher than 100  $\Omega$ , cannot be realised on semiconducting or dielectric substrate owing to its very thin line width [3]. Note that (3) indicates that a reduction of shunt capacitor C results in a decrease of the characteristic impedance Z. Therefore, to solve the above problem for the conventional  $\pi$ -type SMLS, a novel structure with a reduced shunt capacitor should be employed. For this reason, we propose a  $\pi$ type MCMLS in this work, which is shown in Fig. 2. The advantage of a  $\pi$ -type MCMLS is as follows. As shown in Fig. 2, for the  $\pi$ -type MCMLS, coupling capacitance  $C_p$  exists between lines, and a part of coupling capacitance  $C_p$  serves as the shunt capacitor like C of the  $\pi$ -type SMLS of Fig. 1b, because a part of  $C_p$  is connected to the grounded line. Therefore, a part of coupling capacitance  $\mathcal{C}_p$  contributes

to a reduction of line length like shunt capacitor C of the  $\pi$ -type SMLS shown in Fig. 1b, and the total shunt capacitor contributing to a reduction of line length for the  $\pi$ -type MCMLS is a summation of real shunt capacitor  $C_1$  and a part of coupling capacitance  $C_p$ ; i.e. the total shunt capacitor contributing to a reduction of line length for  $\pi$ -type MCMLS can be expressed as  $C_1 + \alpha C_p$ , where  $\alpha$  is a coefficient indicating a portion serving as the shunt capacitor. For this reason, real shunt capacitor  $C_1$  of the  $\pi$ -type MCMLS shows a lower value than C of the  $\pi$ -type SMLS, because  $\alpha C_p$  serves as the shunt capacitor. Therefore, from (3), we can see that the characteristic impedance  $Z_1$  of the  $\pi$ -type MCMLS becomes lower than Z of the  $\pi$ -type SMLS owing to its comparatively lower shunt capacitance  $C_1$ , which facilitates the fabrication of miniaturised passive components on semiconducting or dielectric substrate. For example, in case that the quarter-wave line of Fig. 1a is transformed to a  $\pi$ -type circuit with a length  $\lambda/44$ , the characteristic impedance Z of the  $\pi$ -type SMLS is increased to 200  $\Omega$ , while the characteristic impedance  $Z_1$  of the  $\pi$ -type MCMLS becomes 60  $\Omega$ , which can be realised on semiconducting or dielectric substrate. In this work, we developed a highly miniaturised Wilkinson power divider using the  $\pi$ -type MCMLS.

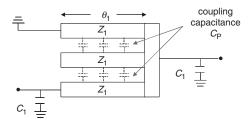


Fig. 2  $\pi$ -type multiple coupled microstrip line structure (MCMLS)

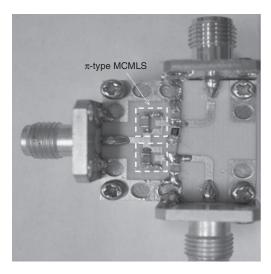


Fig. 3 Photograph of highly miniaturised Wilkinson power divider employing  $\pi$ -type MCMLS

Highly miniaturised Wilkinson power divider employing  $\pi$ -type MCMLS: Fig. 3 shows a photograph of the highly miniaturised Wilkinson power divider employing the  $\pi$ -type MCMLS, which was fabricated on teflon substrate. The line width and spacing between lines are 1 and 0.4 mm, respectively, and the resistance and shunt capacitor are 3.04  $\Omega$  and 1.83 pF, respectively. As shown in Fig. 3, the Wilkinson power divider was highly miniaturised by substituting a quarter-wavelength line for the  $\pi$ -type MCMLS. The size of the novel and conventional Wilkinson power divider on teflon substrate are summarised in Table 1. As shown in the Table, the shunt capacitance of the  $\pi$ -type MCMLS and  $\pi$ -type SMLS is 0.5 and 1 pF, respectively. The line length was highly reduced to  $\lambda/44$  using the  $\pi$ -type MCMLS, and the circuit size of the power divider employing the  $\pi$ -type MCMLS are 37 and 53% of the conventional one employing a quarter-wave line and a  $\pi$ -type SMLS, respectively. Figs. 4 and 5 exhibit power and phase division characteristics for the miniaturised Wilkinson power divider employing the  $\pi$ -type MCMLS. From 3 to 5.5 GHz, we can observe equal power and phase characteristics. Concretely, we can observe power division higher than  $-5.5 \, dB$ , and isolation better than -9 dB.

Table 1: Circuit size of novel and conventional Wilkinson power

	Power divider size	Line length	Shunt C
π-type MCMLS	17 mm <sup>2</sup>	1 mm	0.5 pF
π-type SMLS	32 mm <sup>2</sup>	8.2 mm	1 pF
Quarter-wave line	45 mm <sup>2</sup>	11.3 mm	

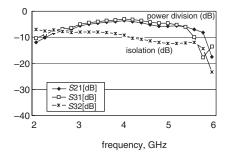


Fig. 4 Power division and isolation characteristics for miniaturised Wilkinson power divider employing  $\pi$ -type MCMLS

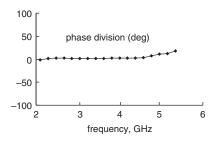


Fig. 5 Phase division characteristics for miniaturised Wilkinson power divider employing  $\pi$ -type MCMLS

Conclusion: We propose a  $\pi$ -type MCMLS, which facilitated development of miniaturised passive components on dielectric substrate. Using the  $\pi$ -type MCMLS, we fabricated a highly miniaturised Wilkinson power divider on teflon substrate. The line length of the Wilkinson power divider was reduced to  $\lambda/44$ , and its size was 37 and 53% of the conventional one employing a quarter-wave line and a  $\pi$ -type SMLS, respectively. The Wilkinson power divider exhibited good RF performances in the S/C band.

Acknowledgment: This work was supported by a Korea Research Foundation Grant funded by the Korea Government (MOEHRD) (KRF-2005 -003-D00263)

© The Institution of Engineering and Technology 2006 23 March 2006

Electronics Letters online no: 20060895

doi: 10.1049/el:20060895

D.H. Lee, Y.B. Park and Y. Yun (Department of Radio Sciences and Engineering, Korea Maritime University, 1, Dongsam-dong, Youngdo-ku, Busan 606-791, Korea)

E-mail: yunyoung@bada.hhu.ac.kr

## References

- Webster, D.R., Ataei, G., and Haigh, D.G.: 'Low-distortion MMIC power amplifier using a new form of derivative superposition', IEEE Trans. Microw. Theory Tech., 2001, 49, pp. 328-332
- Hirota, T., Minakawa, A., and Muraguchi, M.: 'Reduced-size branch-line and rat-race hybrids for uniplanar MMIC's', IEEE Trans. Microw. Theory Tech., 1991, 38, (3), pp. 270-275
- Pozar, D.M.: 'Microwave engineering' (Addison-Wesley, 1990, 2nd edn.), Chap. 8