



# A new Arabic handwritten character recognition deep learning system (AHCR-DLS)

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## Abstract

Optical character recognition for the English text may be considered one of the most important research topics, whether, printed or handwritten. Although excellent results have been reached in the English text, there is a lack of this type of research in the Arabic text. This is because of the nature of the Arabic alphabet, and the multiplicity of forms of the same letter. Arabic handwritten character recognition (AHCR) systems involve several issues, and challenges from finding a suitable, and public Arabic handwritten text dataset phase to recognition, and classification phase passing through segmentation, and feature extraction phases. The paper objectives are: Firstly, a large, and complex Arabic handwritten characters' dataset (HMBD) is presented for training, testing, and validation phases, as well as, discussing its collection, preparation, cleaning, and preprocessing. Secondly, we introduce a deep learning (DL) system with two convolutional neural network (CNN) architectures (named HMB1 and HMB2); with the appliance of optimization, regularization, and dropout techniques. This system can serve as a baseline for future research on handwritten Arabic text. Different performance metrics were calculated such as accuracy, recall, precision, and F1. 16 experiments were applied to the described system using HMBD, and another two datasets: CMATER, and AIA9k. Experiments' results were captured and compared to study the effects of weight initializers, optimizers, data augmentation, and regularization on overfitting, and accuracy. He Uniform weight initializer and AdaDelta optimizer reported the highest accuracies. Data augmentation showed an improvement in the accuracies. HMB1 reported testing accuracy of 98.4% with 865,840 records using augmentation on HMBD. CMATER and AIA9k datasets were used for validating the generalization. Data augmentation was applied, and the best results were 100%, and 99.0% for testing accuracies, respectively. A cross-over validation between the described architectures, and a previous state-of-the-art architecture, and dataset was performed in two phases. First, the previous control architecture cannot generalize for the presented dataset in the current study. Second, the study described architectures generalize for the control dataset, with higher accuracies (97.3%, and 96.8% for HMB1, and HMB2, respectively), than the reported accuracy in the selected control study.

**Keywords** Arabic handwritten character recognition · Classification · Convolutional neural network · Data augmentation · Deep learning · Optical character recognition · Optimizers

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## Abbreviations

|          |   |
|----------|---|
| AdaDelta | An adaptive learning rate method                              |
| Adam     | A method for stochastic optimization                          |
| AHCR     | Arabic handwritten character recognition                      |
| AHCR-DLS | Arabic handwritten character recognition deep learning system |
| CNN      | Convolutional neural network                                  |
| DL       | Deep learning   |
| ReLU     | Rectified linear unit   |
| SGD      | Stochastic gradient descent                                   |
| UN       | United Nations  |

# 1 Introduction

Arabic “العربية” language is the official language of 26 countries, and as many as 420 million people around the world speak Arabic, making it the sixth most commonly spoken language [1]. It is also one of the six official languages of the United Nations (UN) joining Chinese, English, French, Russian, and Spanish. In addition, some languages such as Farsi, Kurdish, Urdu, and Pashto, use some of the Arabic words, features, and structures. The Arabic language has 28 characters; which, are written from right to left. The character size is not fixed; rather, it varies according to the shape, font, and position in the word; beginning, middle, end, or isolated. A single character may contain dots (from one to three) or special symbols such as “Hamza”, and “Tanween.” A single word in English may have different synonyms in Arabic such as the words; “Good”, and “Love.” That said, represents a major challenge for the researchers in the field of Arabic language understanding [2–6].

Pattern recognition is a major research field that comprises the process of identifying and recognizing different means of input; such as images or streams for various fields. The character, face, and speech recognition are common variants of pattern recognition [7, 8]. One of the pattern recognition steps involves the study of the object; in order to, identify attributes (features), and extract the difference; in other words, to determine matching or mismatching [9]. A significant advancement in the recognition process was achieved with the integration of deep learning (DL) approaches. DL is one of the classes of machine learning, which is based on the artificial neural network. DL is used in detection [10], classification [11, 12], and learning [10, 13, 14]. DL architectures are based on the automatic learning from the features without prior determination (extraction). DL uses many layers to get the final information from the raw data. Many applications in the health risk assessment, drug discovery, computer sciences, face, and sound recognition, medical image analysis, bioinformatics, and robotics adopt the image, and pattern recognition technologies, with the different DL architectures [15, 16]. Some of the frequently used DL classes are deep belief networks, convolutional neural networks (CNNs), recurrent neural networks, and stacked auto-encoders.

CNN is widely used in analyzing, segmenting, and classifying visual imagery. It uses the mathematical operation, convolutions, executed in parallel. CNN consists of one or more convolutional layers with one or more fully connected layers. Compared to the fully connected artificial neural network, CNN is easier, and faster to train and has fewer parameters. After training, CNNs converge and

generate acceptable results, and accurate decisions [17]. Arabic handwritten character recognition (AHCR) is considered one of the difficult tasks because of the different writers’ styles, ages, and knowledge which affect the shape of the characters, and words [18]. AHCR faces great challenges from different character positions to ligatures [19] passing through special, and punctuations characters [20]. Notwithstanding, a number of studies on AHCR were successful [21–23].

This paper introduces a new method for AHCR using deep learning. It has become recommended [24–26] to train deep neural networks because of the availability of huge amounts of data, and various algorithmic innovations that are taking place. However, for some datasets, the deep learning classification methods need adjustments in their structure and parameters. Arabic characters have certain requirements for processing, and network weights of the neural network to overcome the challenges such as the cursive nature of Arabic language. In this paper, we first introduce a system based on the characteristics of a DL, CNN. Then, we describe how to process the data and construct the dataset.

The paper is organized as follows: in the next section, we describe the previous related AHCR work. In Sect. 3, we discuss the research problem and aims of the work. In Sect. 4, we discuss the methodology from the described system, and data collection to the experimental environment and different validations passing through the data production, processing, and representation. In Sect. 5, we report the experimental results and discussion of these results. Finally, in Sect. 6, we provide a conclusion on this study.

## 2 Related work

AHCR has many challenges related to the pattern recognition approach in computer science. There are few large Arabic handwritten datasets compared to those in English. Table 1 lists the available Arabic databases that can be used in character recognition.

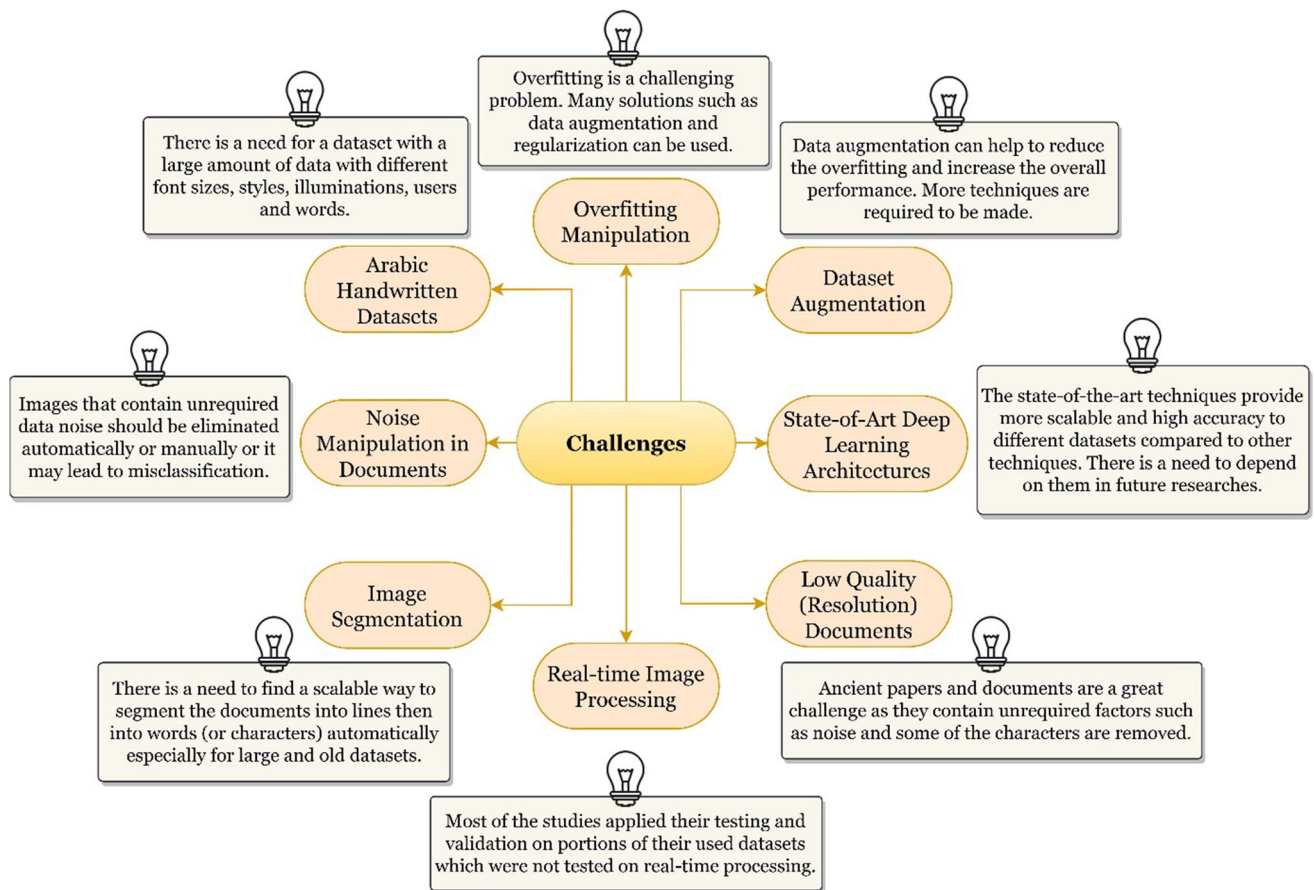
There are many challenges for researchers to work on in this field, and there is a demand for new methods to emerge as the computational technology is increasing and resource limitations are decreasing [30]. Figure 1 summarizes some of these trending challenges. **Arabic Handwritten Datasets:** Some of the available datasets have not many records as shown in Table 1. There is a need for a dataset with a large amount of data with different font sizes, styles, illuminations, users, and words. **Noise Manipulation:** Images that contain unrequired data noise should be eliminated automatically or manually or it may lead to misclassification. Some of the works depended on removing them

**Table 1** Arabic handwritten character databases

| Database         | Website (if available)  | Data type | Dataset size |
|------------------|---|-----------|--------------|
| IFN/ENIT         | <a href="http://www.ifnenit.com/">http://www.ifnenit.com/</a>   | Words     | 26,459       |
| ADBase MADBase   | <a href="http://datacenter.aucegypt.edu/shazeem/">http://datacenter.aucegypt.edu/shazeem/</a>   | Numbers   | 70,000       |
| KHATT            | <a href="http://khatt.ideas2serve.net/index.php">http://khatt.ideas2serve.net/index.php</a>   | Text      | 4000         |
| APTI             | <a href="https://diuf.unifr.ch/main/diva/APTI/index.html/">https://diuf.unifr.ch/main/diva/APTI/index.html/</a>                           | Words     | 45,313,600   |
| AIA9K [27]       | <a href="http://www.eng.alexu.edu.e.g/~mehussein/AIA9k/index.html">http://www.eng.alexu.edu.e.g/~mehussein/AIA9k/index.html</a>           | Letters   | 8737         |
| AlexU-Word       | <a href="http://www.eng.alexu.edu.e.g/~mehussein/alexu-word/index.html">http://www.eng.alexu.edu.e.g/~mehussein/alexu-word/index.html</a> | Words     | 25,114       |
| AHCD [24, 28]    | <a href="https://www.kaggle.com/mloey1/ahcd1">https://www.kaggle.com/mloey1/ahcd1</a>   | Letters   | 16,800       |
| CENPARMI [29]    | –   | –         | 21,426       |
| CMATERDB v.3.3.1 | <a href="https://code.google.com/archive/p/cmaterdb/downloads">https://code.google.com/archive/p/cmaterdb/downloads</a>                   | Numbers   | 3000         |

manually. There is a need to find an easy and fast way to remove them automatically especially for large datasets. **State-of-the-Art Architectures:** Some of the works depended on unsupervised learning and some of them depended on non-state-of-the-art techniques. It is worth to mention that although they achieved low accuracy values compared to the state-of-the-art approaches and architectures. The state-of-the-art supervised techniques provide

more scalable and high accuracy to different datasets compared to other techniques. There is a need to depend on these techniques in future researches. **Low-Quality Documents:** Ancient papers and documents are a great challenge as they contain unrequired factors such as noise and some of the characters are removed. It is an open area problem for researchers to work on. **Segmentation:** Some studies depended on the manual segmentation and feature

**Fig. 1** Trending AHCR Challenges

**Table 2** Recent research summarization

| Study                   | Year | Recognition accuracy  | Dataset type                           | Dataset name      |
|-------------------------|------|-----------------------|--|-------------------|
| El-Sawy et al. [24]     | 2017 | 94.9%                 | Arabic characters                      | Their own dataset |
| Younis et al. [25, 39]  | 2017 | 94.8%                 | Arabic characters                      | AIA9k             |
|                         |      | 97.6%                 |  | AHCD              |
| El-Melegy et al. [26]   | 2019 | 97.80%                | Arabic literal amounts                 | Their Own Dataset |
| Hamida et al. [36]      | 2019 | 99.22% for characters | English characters and Arabic numerals | MNIST [40]        |
|                         |      | 99.74% for digits     |  |                   |
| Ashiquzzaman et al. [9] | 2019 | 99.40%                | Eastern Arabic numerals                | CMATER            |
| Neri et al. [37]        | 2020 | Above 98%             | Arabic numerals                        | Their Own Dataset |

extraction of the datasets. There is a need to find a scalable way to segment the documents (pages) into lines then into words (or characters) automatically especially for large and old datasets. **Real-time Image Processing:** Most of the studies applied their testing and validation on portions of their used datasets which were not tested on real-time processing [31–33].

From Fig. 1, the current study works on: (i) Arabic handwritten datasets, (ii) Overfitting manipulation, (iii) Dataset augmentation, (iv) State-of-the-art deep learning architectures, and (v) Noise manipulation in documents. The rest of them can be handled in further studies.

## 2.1 Recent research in AHCR

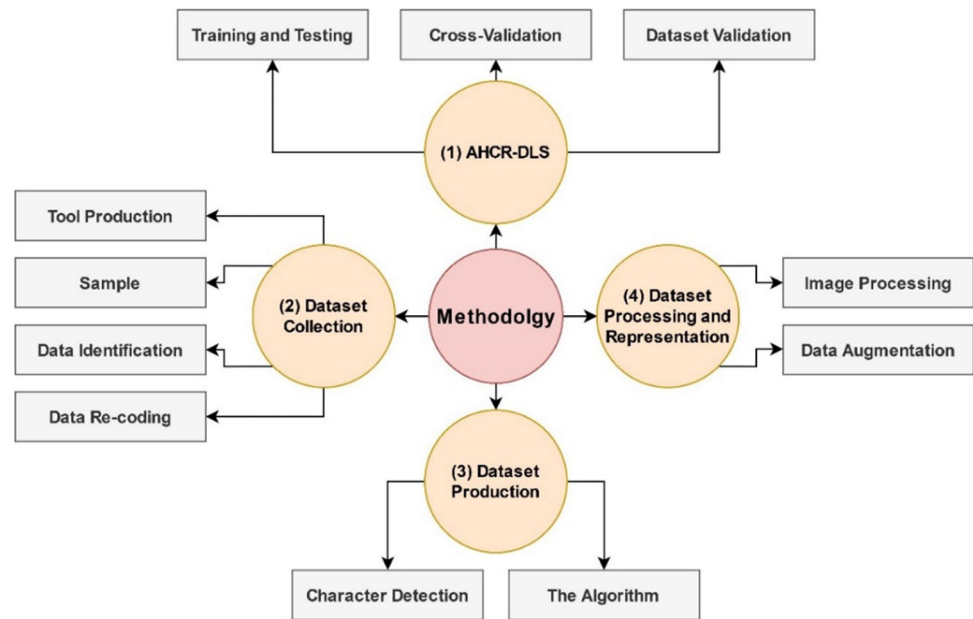
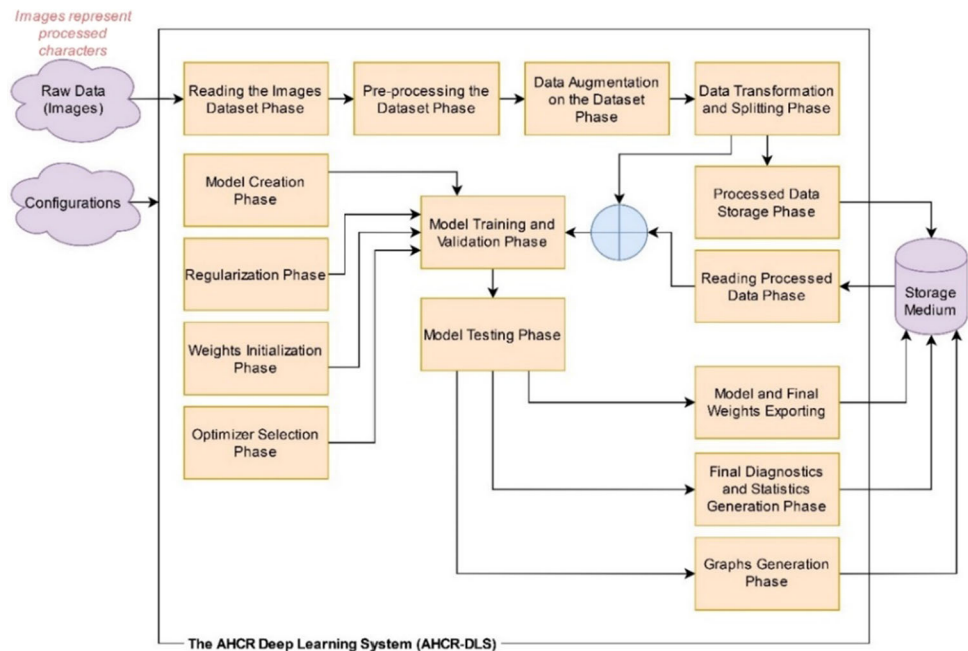
Recently, there have been many researches in the field of handwritten recognition in general and Arabic handwritten recognition in particular. A number of studies, based on different datasets, used different tools and methods to facilitate the recognition of the handwritten texts.

El-Sawy et al. [24] described a DL architecture for AHCR that consisted of an input layer, two convolutional layers, two max-pooling layers, a fully connected layer, and an output layer. Their CNN architecture was trained and tested on their dataset that contained 16,800 handwritten Arabic characters. They used only the 28 basic Arabic characters and did not include the different shapes of the Arabic characters nor the digits. They applied different optimization techniques such as regularization and dropout. Their described CNN architecture had an average 5.1% misclassification error on their testing data. El-Melegy et al. [26] investigated a DL architecture for Arabic handwritten literal amounts recognition that consisted of seventeen layers as follows: input layers, three convolutional layers, three batch normalization layers, three rectified linear unit (ReLU) activation layers, three max-pooling layers, three fully connected layers, and an output layer. They focused on the recognition of handwritten Arabic literal amounts with a limited lexicon. They compared their architecture with traditional methods. They applied data

augmentation [34, 35] and reached a 97.80% recognition rate.

Two architectures for offline handwritten character recognition were described by Hamida et al. [36]. One of them was a DL architecture that consisted of: an input layer, two convolutional layers (20 filters of  $5 \times 5$  size), two pooling layers ( $4 \times 4$  size), two fully connected layers, and an output layer. They reached an accuracy of 99.22% for characters and 99.74% for digits. They used the ReLU activation function for the hidden layers and SoftMax for the output layer. Neri et al. [37] described a CNN architecture for handwritten digit recognition. Their experiments showed that their described preprocessing technique led to an accuracy above 98%, which was better than the accuracy obtained with the dataset without the additional preprocessing. They created their datasets with a size of  $28 \times 28$ . Their described architecture consisted of: an input layer, three convolutional layers, two max-pooling layers, one fully connected layer and an output layer. They used ReLU and SoftMax activation functions for the hidden and output layers, respectively.

Another study described a recognition architecture for handwritten Arabic numerals using CNN with the help of data augmentation and dropout techniques [9]. Their architecture reached an accuracy of 99.40%. They trained their architecture on the CMATERDB v.3.3.1 Arabic handwritten digit dataset. The described architecture consisted of an input layer, four convolutional layers, one max-pooling layer, size dropout layers, three connected layers, and an output layer. They used the exponential linear unit (ELU) activation function [38] in the hidden layers. Younis et al. [25, 39] described a DL network for the AHCR problem that uses CNN architectures with regularization parameters such as batch normalization to prevent overfitting. They applied their CNN on the AIA9k [27] and the AHCD [24, 28] datasets, and the classification accuracies for the two datasets were 94.8% and 97.6%, respectively. Table 2 summarizes the recent researches in the field of handwritten recognition. They are sorted from the oldest to the newest.

**Fig. 2** Current study four phases**Fig. 3** The AHCR deep learning system (AHCR-DLS)

### 3 Problem formulation and plan of solution

As seen in Sect. 2, numerous AHCR systems have been described; but, most of them faced great challenges from finding a suitable and public dataset for segmentation and feature extraction, to the recognition and classification. The problem of different character positions, ligatures, diacritics, and punctuations characters mandates the presence of an inclusive and comprehensive dataset to cover all the potential combinations.

Previous studies showed promising results, but the datasets were small and not comprehensive. The quality

was high; however, it was not tested in such circumstances, of large combinations. They also did not present a complete AHCR system from collecting the data to classifying it. Actually, these two issues have not been adequately addressed in the literature.

The objectives of this study are to (i) present an AHCR deep learning system (AHCR-DLS) with the ability to select between two CNN architectures, (ii) prepare and design a large and complex dataset (HMBD) for AHCR problems (challenges) as previous datasets are not complex enough, (iii) evaluate the architectures' results by applying different experiments using the described two architectures



**Fig. 4** The AHCR deep learning system (AHCR-DLS) steps**Algorithm 1:** The AHCR Deep Learning System (AHCR-DLS) Steps

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```

1 Data: Images Dataset, Configurations
2 Result: Model, Results, Graphs
3 images = readAllImages(ImagesDataset);
4 images = preprocessImages(images, Configurations);
5 images = augmentImages(images, Configurations);
6 train, test, validation = splitImages(images, Configurations);
7 storeSplitImages(train, test, validation);
8 regularizer = selectRegularizer(Configurations);
9 initializer = selectWeightInitializer(Configurations);
10 optimizer = selectOptimizer(Configurations);
11 model = selectConfigModel(Configurations, regularizer, initializer, optimizer);
12 trainedModel = trainModel(model, train, validation);
13 Results = testModel(trainedModel, test);
14 Model = exportModel(trainedModel);
15 Graphs = generateGraphs(trainedModel, Results);

```

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**Table 3** The first CNN architecture (HMB1)

| layer type             | Output shape  | Layer type           | Output shape |
|------------------------|---------------|----------------------|--------------|
| 2D Convolutional Layer | (32, 32, 16)  | Batch Normalization  | (8, 8, 256)  |
| 2D Convolutional Layer | (32, 32, 16)  | 2D Max-Pooling Layer | (4, 4, 256)  |
| Batch Normalization    | (32, 32, 16)  | Flatten Layer        | (4096)       |
| 2D Convolutional Layer | (32, 32, 32)  | Dense Layer          | (1024)       |
| 2D Convolutional Layer | (32, 32, 32)  | Batch Normalization  | (1024)       |
| Batch Normalization    | (32, 32, 32)  | Dropout Layer        | (1024)       |
| 2D Max-Pooling Layer   | (16, 16, 32)  | Dense Layer          | (512)        |
| 2D Convolutional Layer | (16, 16, 64)  | Batch Normalization  | (512)        |
| 2D Convolutional Layer | (16, 16, 64)  | Dropout Layer        | (512)        |
| Batch Normalization    | (16, 16, 64)  | Dense Layer          | (256)        |
| 2D Convolutional Layer | (16, 16, 128) | Batch Normalization  | (256)        |
| 2D Convolutional Layer | (16, 16, 128) | Dropout Layer        | (256)        |
| Batch Normalization    | (16, 16, 128) | Dense Layer          | (128)        |
| 2D Max-Pooling Layer   | (8, 8, 128)   | Batch Normalization  | (128)        |
| 2D Convolutional Layer | (8, 8, 256)   | Dropout Layer        | (128)        |
| 2D Convolutional Layer | (8, 8, 256)   | Dense Layer          | (115)        |

and different datasets including the presented dataset, HMBD, (iv) study the effects of weight initializers, optimizers, data augmentation, and regularization on overfitting and accuracy and finally (v) cross-over validate the overall described work with one of the previous well-known architectures and datasets.

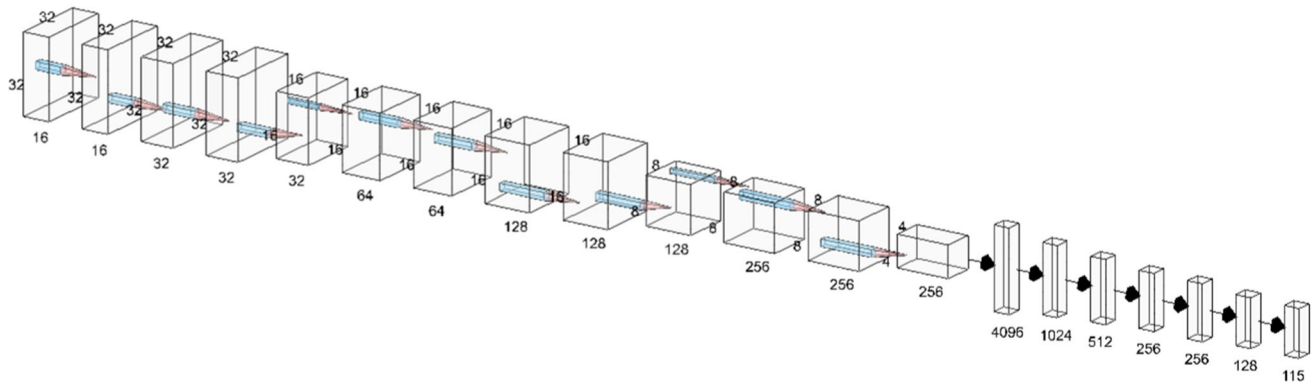
## 4 Methodology

As shown in Fig. 2, the study includes four phases; First: the AHCR-DLS, second: Data Collection, third: Dataset Production and fourth: Dataset Processing and Representation. The first phase can be used for training, testing, and cross-validation appliance on both the dataset and the architecture. In the next subsections, there will be a

detailed description of the four phases of the described methodology.

### 4.1 AHCR-DLS structure

The system provides an overview of the most trending techniques such as data augmentation and regularization, that can be applied in AHCR with the ability to apply or bypass (if not required). It can be used with different datasets: processed and non-processed datasets and can be used also in transfer learning [41, 42]. As shown in Fig. 3 and Algorithm 1 (Fig. 4), the inputs to the system are the dataset and configurations. The input dataset for the presented system is well-prepared (and will be discussed in a following section), so that, there is no need to further processing; hence, the preprocessing phase can be



**Fig. 5** The first CNN architecture (HMB1)—visual presentation

bypassed. However, it is included in the system design, if a further preprocessing is required. Data augmentation can also be applied as well if required. The dataset is split into training, testing, and validation subsets. Training and validation sets will be used to update the weights, and the test set will be used to measure the architecture performance.

#### 4.1.1 The presented two architectures

The creation phase generates the CNN architectures [43] (discussed separately in the following two paragraphs). They are not used at the same time, but only one is selected. The features are automatically extracted by the used architecture; hence, there is no need to extract the features manually as done in traditional machine learning algorithms. The input layer of all of the architectures is fed to a set of hidden layers and finally to an output layer. The CNN is utilized in the two described architectures of the dataset. The differences between the two described architectures are in the design of the hidden layers; such as the number and type of layers, the number and the size of kernels, and the size of strides. The stride is the number of move pixels that will be applied to the kernel. This will

lead to differences in the number of trainable parameters. Weight finalizer, regularization method, and optimizer are selected according to the predefined configurations and will be discussed in a following section. Final output weights, statistics, and graphs are exported and stored.

#### 4.1.2 First CNN architecture (HMB1)

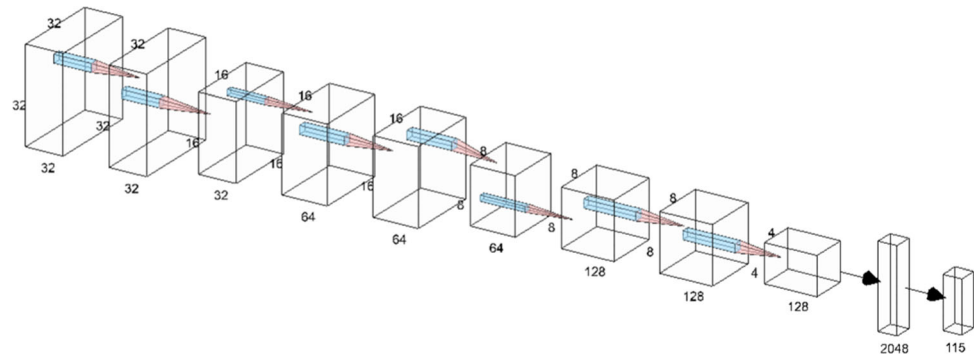
Table 3 and Fig. 5 show a summary of the design of the first described CNN architecture. The 2D convolutional layers have a kernel size of (3,3) and padding of a type “same.” The 2D max-pooling layers have a pooling size of (2,2). The dropout layers have a dropout ratio of 0.25 and are applied to avoid overfitting and reach better generalization [44]. Batch normalization is applied to stabilize the learning process and to reduce the internal covariate shift [45].

CNNs apply different filters in the whole original image called a convolutional layer. Each filter will represent a single specific image feature. Pooling layers can be used after the convolution layers to reduce the dimensionality and keep the most important features from the previous layer according to the type of the pooling layers such as:

**Table 4** The second CNN architecture (HMB2)

| Layer type             | Output shape | Layer type             | Output shape |
|------------------------|--------------|------------------------|--------------|
| 2D convolutional layer | (32, 32, 32) | 2D max-pooling layer   | (8, 8, 64)   |
| Batch normalization    | (32, 32, 32) | Dropout layer          | (8, 8, 64)   |
| 2D convolutional layer | (32, 32, 32) | 2D convolutional layer | (8, 8, 128)  |
| Batch normalization    | (32, 32, 32) | Batch normalization    | (8, 8, 128)  |
| 2D Max-Pooling Layer   | (16, 16, 32) | 2D convolutional layer | (8, 8, 128)  |
| Dropout layer          | (16, 16, 32) | Batch normalization    | (8, 8, 128)  |
| 2D convolutional layer | (16, 16, 64) | 2D max-pooling layer   | (4, 4, 128)  |
| Batch normalization    | (16, 16, 64) | Dropout layer          | (4, 4, 128)  |
| 2D convolutional layer | (16, 16, 64) | Flatten layer          | (2048)       |
| Batch normalization    | (16, 16, 64) | Dense layer            | (115)        |

**Fig. 6** The Second CNN architecture (HMB2): visual presentation



maximum, average and sum pooling. The last layer is a fully connected layer that uses a one-dimensional vector instead of the two-dimensional arrays used in the preceding layers. The last layer output is the selected class with the highest probability [46]. The 2D convolutional and max-pooling layer output shapes are calculated by Eqs. 1 and 2 [47, 48]:

$$O_{\text{conv}} = \frac{I - k + 2 * p}{s} + 1 \quad (1)$$

$$O_{\text{pooling}} = \frac{I - p_s}{s} + 1 \quad (2)$$

where  $I$  is the input shape,  $k$  is the kernel size,  $p$  is the padding size,  $s$  is the stride, and  $p_s$  is the pooling size.

#### 4.1.3 Second CNN architecture (HMB2)

Table 4 and Fig. 6 show a summary of the design of the second CNN architecture. The configuration of the convolutional, max-pooling, batch normalization, and dropout layers is the same as HMB1 architecture. The main difference is the number and size of hidden layers. HMB1 is more complex and has more trainable parameters than HMB2. However, L2 regularization [49] with a value of  $10^{-4}$  is applied to the different convolutional layers. This will help to study the effect and relation between overfitting, regularization, and architecture complexity.

#### 4.1.4 Training parameters

ReLU [50] was used as the activation function for the hidden layers and SoftMax [51] for the output layer. The number of epochs was 50, and the batch size was 32. Different weights initializers [52] were applied: they were LeCun [53–55] normal and uniform initializer, Xavier (Glorot) [56] normal and uniform initializers, and He [57] normal and uniform initializers.

Different optimizers were applied to overcome the overfitting common problem and reach a higher accuracy faster: they were Adam [58, 59] (A Method for Stochastic Optimization), AdaDelta [60] (An Adaptive Learning Rate

Method), AdaMax, AdaGrad [61], and stochastic gradient descent (SGD) [62].

The learning rate was 0.01 for AdaGrad and SGD, 0.002 for AdaMax, 0.001 for Adam, and 1.0 for AdaDelta. All code were written in Python programming language with the help of the Python DL library, Keras [63]. The training used Google Colab [64] and a Graphical Processing Unit.

#### 4.1.5 Performance parameters

Performance metrics were accuracy, precision, recall (sensitivity), and F1 values for training and testing phases. **Accuracy** is the ratio of correctly predicted observation to the total observations. It is the most intuitive performance metric; as it shows whether architecture is being correctly trained and how it will perform [65]. Hence, the best architecture is selected according to the highest validation accuracy, from all of the epochs results.

$$\text{Accuracy} = \frac{T_p + T_n}{T_p + T_n + F_p + F_n + \varepsilon} \quad (3)$$

The **precision** is the ratio of correctly predicted positive observations to the total predicted positive observations [66]. It shows how often positive predications occur. The **recall** is the ratio of correctly predicted positive observations to all observations in a specific class. It helps when false negative values are high [67]. The **F1 Score** is the weighted average of precision and recall [68].

$$\text{Precision} = \frac{T_p}{T_p + F_p + \varepsilon} \quad (4)$$

$$\text{Recall} = \frac{T_p}{T_p + F_n + \varepsilon} \quad (5)$$

$$F1 = 2 * \frac{\text{Precision} * \text{Recall}}{\text{Precision} + \text{Recall}} \quad (6)$$

The previous four equations from 3 to 6 [69, 70] demonstrate the different metrics where  $T_p$ ,  $T_n$ ,  $F_p$ , and  $F_n$  are the true positive, true negative, false positive, and false negative values, respectively. Equation 7 demonstrates the loss function. For multi-class classification, categorical

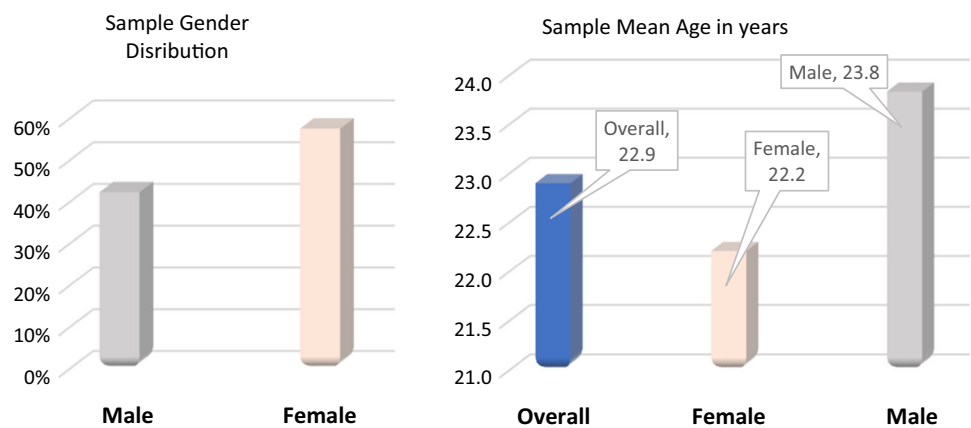


**Fig. 7** Sample from the seven pages template (the first page)

| Volunteer Information |  |  |          |
|-----------------------|--|--|----------|
| Full Name             |  |  |          |
| Gender                | O Male   |  | O Female |
| Age                   |  |  |          |
| Mobile Number         |  |  |          |
| Email Address         |  |  |          |
| Agreement             | By signing this, I fully agree that, my information and my following handwritten data can be used in a scientific and/or an academic approach(es) (i.e. researches). |  |          |
| Signature             |  |  |          |

Please, fill in the squares with the required character. Please, avoid writing on the boundaries of the squares.

|   |   |   |   |
|---|---|---|---|
| ا | ل | ل | ا |
|   |   |   |   |
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| ب | ب | ب | ب |
|   |   |   |   |
|   |   |   |   |
|   |   |   |   |

**Fig. 8** The age and gender of the sharing persons

cross-entropy (SoftMax loss function) is used. The lower the value, the more favorable [15, 71].

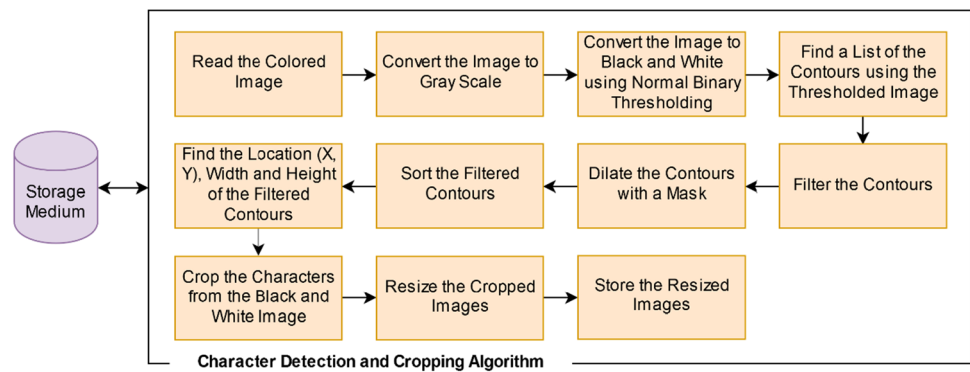
$$\text{SoftMax Loss function} = - \sum_{i=1}^N y_i * \log(\hat{y}_i) \quad (7)$$

where  $N$  is the number of records in the dataset,  $y_i$  is the accurate output value, and  $\hat{y}_i$  is the architecture predicted value. Epsilon ( $\epsilon$ : a very small value) can be added in the denominators to avoid the division by zero.

## 4.2 Data collection

### 4.2.1 Tool production

A seven-page dataset template is constructed from the different Arabic characters and numbers; where the characters are drawn so that, the users can mimic them. Taking in consideration, they have different drawings, according to their positions in the word such as: isolated, middle, begin

**Fig. 9** Character detection and cropping algorithm**Algorithm 2:** Character Detection and Cropping Algorithm

```

1 Data: Images dataset
2 Result: Manipulated characters
3 parameters initializations;
4 for  $j = 1$  to  $numOfImages$  do
5    $cImg = readColorImage(imagePath);$ 
6    $gImg = convertGray(cImg);$ 
7    $bImg = binarizeImage(gImg);$ 
8    $contours = findContours(bImg);$ 
9    $filtered = filterContours(contours);$ 
10   $dilated = dilateContours(filtered);$ 
11   $sorted = sortContours(dilated);$ 
12   $locations = locateContours(sorted);$ 
13   $characters = cropCharacters(locations);$ 
14   $resized = resizeCharacters(characters);$ 
15   $storeCharacters(resized);$ 
16 end
  
```

**Fig. 10** Character detection and cropping algorithm

and end [72]; the constructed template has 116 characters and numerals (digits), and each element has four squares for writing, so, there are 464 squares. One character is duplicated; hence, the total unique elements are 115. (An example subpage from the seven pages is shown in Fig. 7).

#### 4.2.2 Sample

Different persons are invited on a voluntary basis to share in this phase of the study. The aim and study design are well-explained to them. 155 volunteers accepted to share. The “seven-page dataset” is printed and distributed to the study sample. The dataset is collected from 125 persons (81% if the invited sample). The sample age and gender are shown in Fig. 8. The age has a range of 9 to 82 years,

**Fig. 11** Left image: one of the input images. Right image: the corresponding output of that image

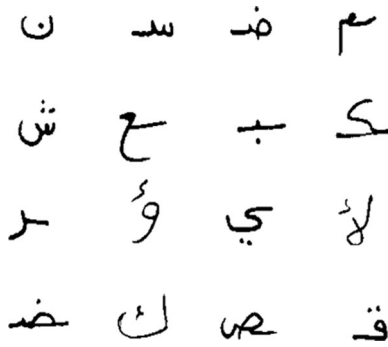


Fig. 12 16 different output characters

and the mean value  $\pm$  Standard Deviation is 22.9 years  $\pm$  8.8.

#### 4.2.3 Data identification

The pages are collected from the volunteers after completion. Each volunteer has a separate unique identifier on the form “AHCR\_xxxxx”. The “Xs” are replaced with a unique identifier code starting from 00001.

**Table 5** Generated pickle files with different configurations

| Image size       | Applied data augmentation? | No. of output images | File name               | File size |
|------------------|----------------------------|----------------------|-------------------------|-----------|
| 32 $\times$ 32   | No                         | 54,115               | HMBD_NO_AUG_32_54115.p  | 214 MB    |
| 64 $\times$ 64   | No                         | 54,115               | HMBD_NO_AUG_64_54115.p  | 848 MB    |
| 32 $\times$ 32   | Yes (1:4)                  | 216,460              | HMBD_AUG_32_216460.p    | 940 MB    |
| 32 $\times$ 32   | Yes (1:6)                  | 324,690              | HMBD_AUG_32_324690.p    | 1.25 GB   |
| 128 $\times$ 128 | No                         | 54,115               | HMBD_NO_AUG_128_54115.p | 3.30 GB   |
| 32 $\times$ 32   | Yes (1:16)                 | 865,840              | HMBD_AUG_32_865840.p    | 3.60 GB   |

**Table 6** Study experiments and their configurations

| Experiment | Architecture | Dataset | Size    | Augmented? | Image Size     |
|------------|--------------|---------|---------|------------|----------------|
| 1          | HMB1         | HMBD    | 54,115  | No         | 32 $\times$ 32 |
| 2          | HMB2         | HMBD    | 54,115  | No         | 32 $\times$ 32 |
| 3          | HMB1         | HMBD    | 54,115  | No         | 64 $\times$ 64 |
| 4          | HMB2         | HMBD    | 54,115  | No         | 64 $\times$ 64 |
| 5          | HMB1         | HMBD    | 216,460 | Yes        | 32 $\times$ 32 |
| 6          | HMB2         | HMBD    | 216,460 | Yes        | 32 $\times$ 32 |
| 7          | HMB1         | HMBD    | 865,840 | Yes        | 32 $\times$ 32 |
| 8          | HMB2         | HMBD    | 865,840 | Yes        | 32 $\times$ 32 |
| 9          | HMB1         | CMATER  | 3000    | No         | 32 $\times$ 32 |
| 10         | HMB2         | CMATER  | 3000    | No         | 32 $\times$ 32 |
| 11         | HMB1         | CMATER  | 30,000  | Yes        | 32 $\times$ 32 |
| 12         | HMB2         | CMATER  | 30,000  | Yes        | 32 $\times$ 32 |
| 13         | HMB1         | AIA9k   | 8974    | No         | 32 $\times$ 32 |
| 14         | HMB2         | AIA9k   | 8974    | No         | 32 $\times$ 32 |
| 15         | HMB1         | AIA9k   | 89,740  | Yes        | 32 $\times$ 32 |
| 16         | HMB2         | AIA9k   | 89,740  | Yes        | 32 $\times$ 32 |

#### 4.2.4 Data re-coding

The collected pages are scanned using the “HP Scanjet Pro 3000 s2” scanner (company name, and data, take from the back of the scanner). The received file identifiers are re-coded on the form to “AHCR\_xxxx\_Dy”; where, the “y” indicates the dataset page number from 1 to 7.

### 4.3 Dataset production

#### 4.3.1 Character detection

After applying the annotation on the images and collecting them together, each page was passed through a set of layers as shown in the block diagram in Fig. 9.

#### 4.3.2 The algorithm

The algorithm block diagram uses black and white image conversion, finding contours, filtering them, dilating them, sorting them, finding the (x, y) coordinates, width and height of them after sorting, cropping the characters,

resizing them and storing the resized images in the corresponding folder on a storage medium (i.e., hard disk, or cloud storage). The output of the algorithm is the manipulated characters. The algorithm pseudocode for a single input image is presented in Algorithm 2 (Fig. 10).

## 4.4 Dataset processing and representation

### 4.4.1 Image processing

Figure 11 shows one of the inputs images before and after processing. Figure 12 shows 16 different characters of the output characters. The total number of collected characters is 58,000 characters. After removing the unwritten, unclear, or bad characters manually, the remaining number is 54,115 characters. The ratio of these filtered images to the total number of unfiltered characters is 93.30%.

### 4.4.2 Data augmentation

The dataset files are compiled multiple times, with different configurations and stored in Python pickle files to be easily used later in the training process or further working. Images were optionally transformed by  $15^\circ$  rotations, 0.1 width and height shifts, 0.2 shears relative to size and zoom factors of 0.2. These configurations are selected to add only a small change on the images to save it from distortions or to be changed to another letter (i.e., “v” and “v”). Table 5 shows the different overall configurations and sizes of output pickle files. The table rows were sorted by the file size ascendingly.

(1 :  $x$ ) in the table means that each input image has another “ $x - 1$ ” augmented images, so the overall number of each input image is “ $x$ .” The filename is initialized by “HMBD” which is the name of the presented dataset. “AUG”, or “NO\_AUG” follows the dataset name which indicates if a data augmentation is applied or not, respectively. The image size followed by the number of images terminates the filename. The “p” extension indicates that it is a pickle Python file.

**Table 7** The design of the CNN architecture in [24]

| Layer type             | Output shape | Layer type    | Output shape |
|------------------------|--------------|---------------|--------------|
| 2D convolutional layer | (28, 28, 80) | Flatten layer | (1600)       |
| 2D max-pooling layer   | (14, 14, 80) | Dense layer   | (1024)       |
| Batch normalization    | (14, 14, 80) | Dropout layer | (1024)       |
| 2D convolutional layer | (10, 10, 64) | Dense layer   | (512)        |
| 2D max-pooling layer   | (5, 5, 64)   | Dropout layer | (1024)       |
| Batch normalization    | (5, 5, 64)   | Dense layer   | (115)        |

**Table 8** Cross-validation experiments and their configurations

| Phase | Architecture | Dataset    | Size   | Image size     |
|-------|--------------|------------|--------|----------------|
| 1     | [24]         | HMBD       | 54,114 | $32 \times 32$ |
| 2     | HMB1         | AHCD1 [24] | 16,800 | $32 \times 32$ |
|       | HMB2         | AHCD1 [24] | 16,800 | $32 \times 32$ |

## 4.5 Validation of the AHCR-DLS with datasets

HMBD, CMATER, and AIA9k datasets were used to validate the AHCR-DLS using the two presented architectures in the current study to validate them and see if the system can work and generalize for different datasets. Table 6 shows the different experiments and their configurations that will be performed. Categorical cross-entropy, ReLU, and SoftMax were the common loss function, hidden activation function, and output activation function, respectively. 64, and 32 were the common number of epochs and batch size, respectively. The used datasets were split into: 95% for training and validation (split internally into 95% for training and 5% for validation) and 5% for testing. Different optimizers (Adam, AdaDelta, SGD, AdaMax, and AdaGrad) and weight initializers (He Normal, He Uniform, Glorot Normal, Glorot Uniform, LeCun Normal and LeCun Uniform) were applied.

## 4.6 Cross-validation testing

Cross-validation was performed between the presented study architectures and datasets and versus a selected control architecture and a dataset presented in [24] in two phases. The first phase was to test the presented dataset HMBD versus their architecture generalization. The second phase was to test the presented architectures’ generalization on their dataset.

**Table 9** Comparing HMBD with different AHCR datasets

| Database              | Data type                           | No. of tested writers | Dataset size |
|-----------------------|-------------------------------------|-----------------------|--------------|
| HMBD                  | 115 (105 Characters and 10 Numbers) | 125                   | 54,115       |
| AHCD [24, 28]         | 28 Characters                       | 700                   | 16,800       |
| AIA9K [27]            | 28 Characters                       | 107                   | 8737         |
| ADBase & MADBase [73] | 10 Numbers                          | 60                    | 70,000       |

**Table 10** Training and testing reported results of Experiment 1

| Weight initializer      | Optimizer       | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal               | Adam            | 0.04           | 99.1        | 0.99        | 99.2        | 99.1        | 0.56          | 90.1        | 0.90        | 90.4        | 89.8        | 2301        |
|                         | AdaDelta        | 0.05           | 99.3        | 0.99        | 99.3        | 99.3        | 0.67          | 90.5        | 0.91        | 90.9        | 90.4        | 2480        |
|                         | SGD             | 0.05           | 98.6        | 0.99        | 98.7        | 98.5        | 0.49          | 88.6        | 0.89        | 89.7        | 88.1        | 1838        |
|                         | AdaMax          | 0.05           | 98.6        | 0.99        | 98.6        | 98.5        | 0.52          | 88.8        | 0.89        | 89.2        | 88.5        | 2209        |
|                         | AdaGrad         | 0.04           | 98.9        | 0.99        | 99.0        | 98.9        | 0.50          | 88.4        | 0.89        | 89.4        | 87.8        | 2080        |
| <b>He Uniform</b>       | Adam            | 0.05           | 98.7        | 0.99        | 98.7        | 98.7        | 0.52          | 89.8        | 0.90        | 90.4        | 89.5        | 2356        |
|                         | <b>AdaDelta</b> | <b>0.05</b>    | <b>99.2</b> | <b>0.99</b> | <b>99.2</b> | <b>99.2</b> | <b>0.69</b>   | <b>90.7</b> | <b>0.91</b> | <b>91.0</b> | <b>90.5</b> | <b>2555</b> |
|                         | SGD             | 0.05           | 98.9        | 0.99        | 98.9        | 98.8        | 0.57          | 87.7        | 0.88        | 88.5        | 87.3        | 1934        |
|                         | AdaMax          | 0.04           | 99.4        | 0.99        | 99.4        | 99.4        | 0.59          | 90.0        | 0.90        | 90.2        | 89.8        | 2180        |
|                         | AdaGrad         | 0.04           | 99.4        | 0.99        | 99.4        | 99.3        | 0.51          | 89.1        | 0.89        | 89.7        | 88.7        | 2078        |
| Glorot (Xavier) Normal  | Adam            | 0.04           | 99.1        | 0.99        | 99.1        | 99.1        | 0.57          | 90.2        | 0.90        | 90.6        | 90.0        | 2337        |
|                         | AdaDelta        | 0.05           | 99.0        | 0.99        | 99.0        | 99.0        | 0.63          | 90.3        | 0.90        | 90.5        | 90.1        | 2539        |
|                         | SGD             | 0.12           | 95.9        | 0.96        | 96.4        | 95.5        | 0.43          | 88.2        | 0.89        | 89.7        | 87.3        | 1904        |
|                         | AdaMax          | 0.04           | 99.3        | 0.99        | 99.3        | 99.3        | 0.58          | 90.2        | 0.90        | 90.5        | 90.0        | 2160        |
|                         | AdaGrad         | 0.04           | 99.1        | 0.99        | 99.1        | 99.1        | 0.47          | 89.2        | 0.90        | 90.1        | 88.9        | 2111        |
| Glorot (Xavier) Uniform | Adam            | 0.04           | 99.1        | 0.99        | 99.2        | 99.1        | 0.55          | 89.6        | 0.90        | 89.9        | 89.4        | 1738        |
|                         | AdaDelta        | 0.05           | 99.2        | 0.99        | 99.2        | 99.2        | 0.71          | 89.9        | 0.90        | 90.3        | 89.7        | 1907        |
|                         | SGD             | 0.03           | 99.2        | 0.99        | 99.2        | 99.1        | 0.49          | 89.1        | 0.89        | 89.8        | 88.8        | 1458        |
|                         | AdaMax          | 0.04           | 99.2        | 0.99        | 99.2        | 99.2        | 0.58          | 89.7        | 0.90        | 90.1        | 89.3        | 1694        |
|                         | AdaGrad         | 0.04           | 99.4        | 0.99        | 99.4        | 99.3        | 0.54          | 89.1        | 0.89        | 89.5        | 88.8        | 1622        |
| LeCun Normal            | Adam            | 0.04           | 98.9        | 0.99        | 99.0        | 98.9        | 0.55          | 89.5        | 0.90        | 89.9        | 89.4        | 1815        |
|                         | AdaDelta        | 0.04           | 99.2        | 0.99        | 99.2        | 99.2        | 0.63          | 90.1        | 0.90        | 90.6        | 90.0        | 1999        |
|                         | SGD             | 0.04           | 98.9        | 0.99        | 98.9        | 98.8        | 0.52          | 88.8        | 0.89        | 89.4        | 88.5        | 1523        |
|                         | AdaMax          | 0.04           | 99.1        | 0.99        | 99.1        | 99.1        | 0.56          | 89.6        | 0.90        | 90.1        | 89.5        | 1730        |
|                         | AdaGrad         | 0.03           | 99.4        | 0.99        | 99.5        | 99.4        | 0.57          | 89.0        | 0.89        | 89.5        | 88.7        | 1690        |
| LeCun Uniform           | Adam            | 0.04           | 99.1        | 0.99        | 99.2        | 99.1        | 0.53          | 90.5        | 0.91        | 90.9        | 90.2        | 1897        |
|                         | AdaDelta        | 0.07           | 97.7        | 0.98        | 97.8        | 97.6        | 0.54          | 89.2        | 0.89        | 90.0        | 88.9        | 2023        |
|                         | SGD             | 0.05           | 98.7        | 0.99        | 98.7        | 98.6        | 0.48          | 88.4        | 0.89        | 89.6        | 88.1        | 1591        |
|                         | AdaMax          | 0.04           | 98.9        | 0.99        | 99.0        | 98.9        | 0.53          | 89.9        | 0.90        | 90.3        | 89.5        | 1773        |
|                         | AdaGrad         | 0.04           | 98.9        | 0.99        | 99.0        | 98.9        | 0.48          | 89.1        | 0.89        | 89.5        | 88.6        | 1708        |

#### 4.6.1 Phase 1

The architecture in [24] was compiled and tested on HMBD without data augmentation using a dataset pickle file named: “HMBD\_NO\_AUG\_32\_54115.p”. Their

architecture has a design shown in Table 7. The number of classes in the dense output layer was modified from 28 to 115 to match HMBD’ classes. They used SoftMax as an output activation function and ReLU as an activation function for the hidden layers. They applied L2



**Table 11** Training and testing reported results of Experiment 2

| Weight initializer      | Optimizer     | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|---------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |               | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal               | Adam          | 0.34           | 94.9        | 0.95        | 95.6        | 94.3        | 0.60          | 87.8        | 0.88        | 89.0        | 86.8        | 1143        |
|                         | AdaDelta      | 0.26           | 97.6        | 0.98        | 97.8        | 97.4        | 0.62          | 89.2        | 0.90        | 90.7        | 88.4        | 1211        |
|                         | SGD           | 0.10           | 98.6        | 0.99        | 98.7        | 98.6        | 0.48          | 89.2        | 0.89        | 89.9        | 88.9        | 988         |
|                         | AdaMax        | 0.17           | 98.5        | 0.99        | 98.6        | 98.4        | 0.59          | 88.8        | 0.89        | 89.8        | 88.5        | 1115        |
|                         | AdaGrad       | 0.14           | 97.4        | 0.97        | 97.8        | 97.0        | 0.45          | 88.1        | 0.88        | 89.6        | 87.1        | 1046        |
| He Uniform              | Adam          | 0.29           | 96.4        | 0.96        | 96.8        | 96.1        | 0.63          | 88.2        | 0.88        | 89.3        | 87.1        | 1249        |
|                         | AdaDelta      | 0.26           | 97.5        | 0.97        | 97.7        | 97.2        | 0.62          | 88.4        | 0.89        | 90.3        | 87.3        | 1341        |
|                         | SGD           | 0.11           | 98.2        | 0.98        | 98.3        | 98.1        | 0.48          | 88.7        | 0.89        | 89.5        | 88.1        | 1074        |
|                         | AdaMax        | 0.17           | 98.2        | 0.98        | 98.3        | 98.1        | 0.60          | 88.5        | 0.89        | 89.2        | 88.2        | 1207        |
|                         | AdaGrad       | 0.14           | 97.2        | 0.97        | 97.6        | 96.8        | 0.47          | 87.9        | 0.88        | 89.3        | 86.8        | 1145        |
| Glorot (Xavier) Normal  | Adam          | 0.27           | 97.2        | 0.97        | 97.4        | 97.0        | 0.64          | 88.2        | 0.88        | 89.3        | 87.5        | 1283        |
|                         | AdaDelta      | 0.28           | 96.8        | 0.97        | 97.1        | 96.4        | 0.63          | 88.1        | 0.88        | 89.4        | 87.2        | 1384        |
|                         | SGD           | 0.11           | 98.2        | 0.98        | 98.3        | 98.0        | 0.51          | 87.9        | 0.88        | 88.8        | 87.3        | 1098        |
|                         | AdaMax        | 0.17           | 98.3        | 0.98        | 98.4        | 98.3        | 0.60          | 88.4        | 0.89        | 89.0        | 88.1        | 1233        |
|                         | AdaGrad       | 0.14           | 97.4        | 0.97        | 97.7        | 97.1        | 0.48          | 87.7        | 0.88        | 88.6        | 87.0        | 1187        |
| Glorot (Xavier) Uniform | Adam          | 0.29           | 96.5        | 0.97        | 96.9        | 96.2        | 0.63          | 88.6        | 0.89        | 90.0        | 87.8        | 1320        |
|                         | AdaDelta      | 0.27           | 97.1        | 0.97        | 97.3        | 96.9        | 0.63          | 88.4        | 0.89        | 89.8        | 87.8        | 1419        |
|                         | SGD           | 0.11           | 98.2        | 0.98        | 98.3        | 98.0        | 0.50          | 88.2        | 0.89        | 89.3        | 87.8        | 1135        |
|                         | AdaMax        | 0.17           | 98.4        | 0.98        | 98.5        | 98.4        | 0.65          | 88.1        | 0.88        | 88.7        | 87.7        | 1276        |
|                         | AdaGrad       | 0.13           | 97.7        | 0.98        | 97.9        | 97.4        | 0.48          | 87.7        | 0.88        | 89.0        | 86.9        | 1227        |
| <b>LeCun Normal</b>     | Adam          | 0.26           | 97.4        | 0.97        | 97.6        | 97.2        | 0.63          | 88.5        | 0.89        | 89.6        | 88.1        | 1354        |
|                         | AdaDelta      | 0.26           | 97.3        | 0.97        | 97.5        | 97.1        | 0.65          | 88.5        | 0.89        | 90.0        | 87.7        | 1442        |
|                         | SGD           | 0.10           | 98.5        | 0.99        | 98.6        | 98.4        | 0.51          | 88.7        | 0.89        | 89.6        | 88.2        | 1183        |
|                         | <b>AdaMax</b> | <b>0.17</b>    | <b>98.5</b> | <b>0.99</b> | <b>98.5</b> | <b>98.4</b> | <b>0.58</b>   | <b>89.3</b> | <b>0.90</b> | <b>90.1</b> | <b>88.9</b> | <b>1304</b> |
|                         | AdaGrad       | 0.15           | 97.0        | 0.97        | 97.4        | 96.6        | 0.48          | 88.4        | 0.89        | 89.7        | 87.4        | 1305        |
| LeCun Uniform           | Adam          | 0.29           | 96.7        | 0.97        | 97.0        | 96.4        | 0.64          | 87.8        | 0.88        | 89.1        | 87.0        | 1299        |
|                         | AdaDelta      | 0.31           | 95.8        | 0.96        | 96.5        | 95.1        | 0.64          | 87.3        | 0.88        | 89.4        | 85.7        | 1383        |
|                         | SGD           | 0.10           | 98.5        | 0.99        | 98.6        | 98.4        | 0.47          | 89.1        | 0.89        | 90.1        | 88.7        | 1074        |
|                         | AdaMax        | 0.17           | 98.4        | 0.98        | 98.5        | 98.3        | 0.65          | 88.1        | 0.88        | 89.0        | 87.7        | 1224        |
|                         | AdaGrad       | 0.18           | 96.4        | 0.96        | 97.0        | 95.9        | 0.49          | 87.7        | 0.88        | 89.1        | 86.9        | 1192        |

regularization with a value of 0.001 and used the SGD optimizer with a learning rate  $\alpha$  equals 0.01 and a momentum  $\gamma$  equals 0.1.

#### 4.6.2 Phase 2

The dataset in [24] was composed of 16,800 handwritten characters written by 60 participants with an age range of 19 to 40 years old and 90% of them were right-handed. The dataset was rescaled to  $32 \times 32$ . This dataset was used with this study described architecture.

Table 8 summarizes the two phases of experiments with their configurations. Categorical cross-entropy, ReLU, and SoftMax were the common loss function, hidden activation function, and output activation function, respectively. 64 and 32 were the common number of epochs and batch size,

respectively. The used datasets were split into: 95% for training and validation (split internally into 95% for training and 5% for validation) and 5% for testing. For the second phase only, different optimizers (Adam, AdaDelta, SGD, AdaMax, and AdaGrad) and weight initializers (He Normal, He Uniform, Glorot Normal, Glorot Uniform, LeCun Normal and LeCun Uniform) were applied.

## 5 Experiments results and discussion

### 5.1 Comparison of the newly presented dataset with the previous datasets

The presented dataset, HMBD, in the current research captures the different positions of the characters; isolated,

**Table 12** Training and testing reported results of Experiment 3

| Weight initializer      | Optimizer     | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|---------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |               | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| <b>He Normal</b>        | Adam          | 0.03           | 99.2        | 0.99        | 99.2        | 99.1        | 0.58          | 88.7        | 0.89        | 89.3        | 88.4        | 3518        |
|                         | AdaDelta      | 0.04           | 99.3        | 0.99        | 99.4        | 99.3        | 0.73          | 89.4        | 0.90        | 90.0        | 89.4        | 3851        |
|                         | SGD           | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.58          | 88.9        | 0.89        | 89.4        | 88.4        | 3027        |
|                         | <b>AdaMax</b> | <b>0.03</b>    | <b>99.4</b> | <b>0.99</b> | <b>99.5</b> | <b>99.4</b> | <b>0.64</b>   | <b>89.8</b> | <b>0.90</b> | <b>90.1</b> | <b>89.5</b> | <b>3361</b> |
|                         | AdaGrad       | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.54          | 88.1        | 0.88        | 88.8        | 87.6        | 3160        |
| He Uniform              | Adam          | 0.05           | 98.6        | 0.99        | 98.7        | 98.6        | 0.57          | 88.5        | 0.89        | 89.1        | 88.1        | 3513        |
|                         | AdaDelta      | 0.04           | 99.2        | 0.99        | 99.2        | 99.2        | 0.68          | 89.0        | 0.89        | 89.6        | 88.8        | 3770        |
|                         | SGD           | 0.32           | 89.7        | 0.90        | 91.4        | 88.2        | 0.84          | 79.3        | 0.80        | 82.1        | 77.5        | 2987        |
|                         | AdaMax        | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.69          | 89.5        | 0.90        | 89.8        | 89.3        | 3370        |
|                         | AdaGrad       | 0.04           | 99.1        | 0.99        | 99.2        | 99.0        | 0.50          | 88.3        | 0.89        | 89.2        | 87.9        | 3316        |
| Glorot (Xavier) Normal  | Adam          | 0.04           | 98.8        | 0.99        | 98.9        | 98.8        | 0.53          | 89.6        | 0.90        | 90.2        | 89.4        | 3148        |
|                         | AdaDelta      | 0.04           | 98.9        | 0.99        | 99.0        | 98.9        | 0.61          | 89.0        | 0.89        | 89.6        | 88.7        | 3423        |
|                         | SGD           | 0.04           | 99.0        | 0.99        | 99.1        | 98.9        | 0.50          | 88.6        | 0.89        | 89.5        | 88.0        | 2621        |
|                         | AdaMax        | 0.07           | 97.6        | 0.98        | 97.7        | 97.5        | 0.43          | 88.9        | 0.89        | 89.8        | 88.2        | 2930        |
|                         | AdaGrad       | 0.09           | 97.3        | 0.97        | 97.5        | 97.0        | 0.41          | 88.1        | 0.88        | 89.6        | 87.0        | 2861        |
| Glorot (Xavier) Uniform | Adam          | 0.04           | 98.9        | 0.99        | 98.9        | 98.9        | 0.58          | 88.3        | 0.89        | 88.9        | 88.1        | 3531        |
|                         | AdaDelta      | 0.04           | 99.4        | 0.99        | 99.4        | 99.4        | 0.78          | 88.8        | 0.89        | 89.2        | 88.5        | 3787        |
|                         | SGD           | 0.05           | 98.9        | 0.99        | 98.9        | 98.8        | 0.59          | 88.6        | 0.89        | 89.3        | 88.2        | 3031        |
|                         | AdaMax        | 0.03           | 99.5        | 1.00        | 99.5        | 99.5        | 0.68          | 89.1        | 0.89        | 89.5        | 89.1        | 3412        |
|                         | AdaGrad       | 0.03           | 99.4        | 0.99        | 99.4        | 99.4        | 0.54          | 89.3        | 0.89        | 89.6        | 88.8        | 3294        |
| LeCun Normal            | Adam          | 0.03           | 99.4        | 0.99        | 99.4        | 99.3        | 0.64          | 89.0        | 0.89        | 89.5        | 88.7        | 3614        |
|                         | AdaDelta      | 0.04           | 98.9        | 0.99        | 98.9        | 98.9        | 0.59          | 89.2        | 0.89        | 89.8        | 88.9        | 3890        |
|                         | SGD           | 0.04           | 99.1        | 0.99        | 99.1        | 99.0        | 0.51          | 88.9        | 0.89        | 89.5        | 88.6        | 3056        |
|                         | AdaMax        | 0.03           | 99.4        | 0.99        | 99.4        | 99.4        | 0.64          | 88.9        | 0.89        | 89.3        | 88.6        | 3392        |
|                         | AdaGrad       | 0.03           | 99.2        | 0.99        | 99.3        | 99.2        | 0.50          | 88.3        | 0.89        | 89.1        | 87.9        | 3248        |
| LeCun Uniform           | Adam          | 0.04           | 99.1        | 0.99        | 99.2        | 99.1        | 0.63          | 88.5        | 0.89        | 88.9        | 88.2        | 3128        |
|                         | AdaDelta      | 0.04           | 99.3        | 0.99        | 99.3        | 99.2        | 0.73          | 89.0        | 0.89        | 89.3        | 88.8        | 11,734      |
|                         | SGD           | 0.05           | 98.3        | 0.98        | 98.4        | 98.3        | 0.47          | 88.3        | 0.89        | 89.4        | 87.8        | 8428        |
|                         | AdaMax        | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.63          | 89.3        | 0.90        | 90.0        | 89.1        | 9858        |
|                         | AdaGrad       | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.55          | 88.8        | 0.89        | 89.4        | 88.6        | 3225        |

beginning, middle, and end; besides, the numbers. The size of the dataset is larger than those available datasets. Table 9 shows a comparison between the HMBD dataset that is presented in this study and the previously prepared datasets by other authors [24, 28]. Most of the currently available datasets deal with the numbers (from 0 to 9), or the 28 characters in the Arabic language (from “ا” to “ي”) [28, 27, 24].

## 5.2 Experimenting the AHCR-DLS with datasets

Tables 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25 and 26 show the corresponding results of the different experiments mentioned in Table 6, respectively. They show the loss, accuracy, F1, precision, and recall

values for training and testing phases. The training time is reported in seconds. The best results (concerning the testing accuracy) are in bold.

Table 10 shows that the AdaDelta optimizer and He Uniform weight initializer report the highest testing accuracy in experiment 1. The testing accuracy reached 90.7% with a loss value of 0.69. The average training time is 1974 s. The average training and testing accuracies are 98.9%, and 89.4%, respectively. The average training and testing losses are 0.05, and 0.55, respectively. Figure 13 shows the experiment training and testing accuracies curves with their trendlines. Figure 14 shows the training time curve with its trendline. The *x*-axis refers to the corresponding experiment rows, and the *y*-axis refers to the

**Table 13** Training and testing reported results of Experiment 4

| Weight initializer      | Optimizer      | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |                | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal               | Adam           | 0.25           | 95.6        | 0.96        | 96.2        | 95.0        | 0.81          | 83.1        | 0.84        | 85.1        | 82.0        | 1558        |
|                         | AdaDelta       | 0.23           | 96.7        | 0.97        | 97.1        | 96.5        | 0.99          | 83.2        | 0.84        | 85.4        | 82.5        | 1630        |
|                         | SGD            | 0.15           | 96.8        | 0.97        | 97.1        | 96.5        | 0.91          | 82.6        | 0.83        | 83.6        | 81.9        | 1476        |
|                         | AdaMax         | 0.24           | 94.9        | 0.95        | 95.7        | 94.1        | 0.67          | 85.1        | 0.86        | 87.0        | 84.1        | 1557        |
|                         | AdaGrad        | 0.09           | 98.8        | 0.99        | 98.9        | 98.7        | 0.65          | 85.4        | 0.86        | 87.0        | 84.3        | 1519        |
| He Uniform              | Adam           | 0.23           | 96.0        | 0.96        | 96.3        | 95.7        | 0.87          | 83.9        | 0.84        | 85.2        | 83.3        | 1623        |
|                         | AdaDelta       | 0.24           | 96.2        | 0.96        | 96.7        | 95.9        | 0.97          | 82.3        | 0.83        | 84.2        | 81.6        | 1689        |
|                         | SGD            | 0.24           | 94.0        | 0.94        | 94.6        | 93.6        | 1.17          | 80.3        | 0.81        | 81.3        | 79.8        | 1500        |
|                         | AdaMax         | 0.11           | 99.0        | 0.99        | 99.0        | 98.9        | 0.92          | 85.4        | 0.86        | 86.1        | 84.9        | 1586        |
|                         | AdaGrad        | 0.11           | 98.5        | 0.99        | 98.6        | 98.4        | 0.66          | 85.7        | 0.86        | 86.6        | 85.2        | 1526        |
| Glorot (Xavier) Normal  | Adam           | 0.21           | 96.9        | 0.97        | 97.1        | 96.7        | 0.87          | 84.1        | 0.84        | 84.9        | 83.5        | 1667        |
|                         | AdaDelta       | 0.24           | 96.0        | 0.96        | 96.4        | 95.8        | 1.11          | 81.2        | 0.82        | 82.6        | 80.7        | 1589        |
|                         | SGD            | 0.16           | 96.1        | 0.96        | 96.5        | 95.8        | 0.79          | 82.9        | 0.83        | 84.6        | 82.2        | 1377        |
|                         | AdaMax         | 0.13           | 98.7        | 0.99        | 98.7        | 98.6        | 0.89          | 84.7        | 0.85        | 85.7        | 84.4        | 1469        |
|                         | AdaGrad        | 0.11           | 98.5        | 0.99        | 98.6        | 98.4        | 0.70          | 85.3        | 0.86        | 86.7        | 84.6        | 1424        |
| Glorot (Xavier) Uniform | Adam           | 0.18           | 97.4        | 0.97        | 97.5        | 97.2        | 0.83          | 84.0        | 0.85        | 85.3        | 83.7        | 1516        |
|                         | AdaDelta       | 0.25           | 95.8        | 0.96        | 96.6        | 95.2        | 0.77          | 84.3        | 0.85        | 86.5        | 83.3        | 1601        |
|                         | SGD            | 0.09           | 99.0        | 0.99        | 99.0        | 98.9        | 0.84          | 85.0        | 0.85        | 85.7        | 84.7        | 1421        |
|                         | AdaMax         | 0.15           | 97.9        | 0.98        | 98.0        | 97.8        | 0.96          | 83.7        | 0.84        | 84.9        | 83.4        | 1510        |
|                         | AdaGrad        | 0.13           | 97.5        | 0.98        | 97.9        | 97.2        | 0.63          | 84.7        | 0.85        | 86.4        | 83.4        | 1464        |
| <b>LeCun Normal</b>     | Adam           | 0.22           | 96.3        | 0.96        | 96.6        | 96.0        | 0.81          | 84.4        | 0.85        | 85.7        | 83.5        | 1534        |
|                         | AdaDelta       | 0.43           | 91.2        | 0.91        | 92.3        | 90.5        | 1.09          | 80.4        | 0.81        | 82.3        | 79.5        | 1606        |
|                         | SGD            | 0.13           | 97.3        | 0.97        | 97.6        | 96.9        | 0.73          | 84.5        | 0.85        | 86.1        | 83.5        | 1464        |
|                         | AdaMax         | 0.15           | 97.8        | 0.98        | 97.9        | 97.7        | 0.99          | 83.4        | 0.84        | 84.3        | 83.2        | 1565        |
|                         | <b>AdaGrad</b> | <b>0.10</b>    | <b>98.5</b> | <b>0.99</b> | <b>98.6</b> | <b>98.4</b> | <b>0.65</b>   | <b>86.0</b> | <b>0.86</b> | <b>87.2</b> | <b>85.3</b> | <b>1522</b> |
| LeCun Uniform           | Adam           | 0.17           | 97.9        | 0.98        | 97.9        | 97.8        | 0.89          | 84.0        | 0.84        | 84.8        | 83.5        | 1622        |
|                         | AdaDelta       | 0.31           | 93.9        | 0.94        | 94.8        | 93.1        | 0.73          | 84.8        | 0.85        | 87.2        | 83.2        | 1697        |
|                         | SGD            | 0.30           | 92.2        | 0.92        | 93.6        | 91.3        | 0.98          | 80.2        | 0.81        | 82.9        | 78.6        | 1397        |
|                         | AdaMax         | 0.15           | 97.9        | 0.98        | 98.1        | 97.7        | 0.83          | 84.4        | 0.85        | 85.5        | 83.9        | 1348        |
|                         | AdaGrad        | 0.10           | 98.5        | 0.99        | 98.6        | 98.4        | 0.68          | 84.9        | 0.85        | 86.2        | 84.4        | 1522        |

accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 11 shows that the AdaMax optimizer and LeCun Normal weight initializer report the highest testing accuracy in experiment 2. The testing accuracy reached 89.3% with a loss value of 0.58. The average training time is 1228 s. The average training and testing accuracies are 97.5%, and 88.3%, respectively. The average training and testing losses are 0.20, and 0.57, respectively. Figure 15 shows the experiment training and testing accuracies curves with their trendlines. Figure 16 shows the training time curve with its trendline. The *x*-axis refers to the corresponding experiment rows, and the *y*-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 12 shows that the AdaMax optimizer and He Normal weight initializer report the highest testing accuracy in experiment 3. The testing accuracy reached 89.8% with a loss value of 0.64. The average training time is 3983 s. The average training and testing accuracies are 98.7%, and 88.5%, respectively. The average training and testing losses are 0.05, and 0.60, respectively. Figure 17 shows the experiment training and testing accuracies curves with their trendlines. Figure 18 shows the training time curve with its trendline. The *x*-axis refers to the corresponding experiment rows, and the *y*-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 13 shows that AdaGrad optimizer and LeCun Normal weight initializer report the highest testing

**Table 14** Training and testing reported results of Experiment 5

| Weight initializer            | Optimizer       | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                               |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal                     | Adam            | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.34          | 93.2        | 0.93        | 93.3        | 93.1        | 10,224      |
|                               | AdaDelta        | 0.03           | 99.3        | 0.99        | 99.3        | 99.3        | 0.38          | 93.4        | 0.93        | 93.6        | 93.3        | 9893        |
|                               | SGD             | 0.03           | 99.3        | 0.99        | 99.3        | 99.3        | 0.35          | 92.0        | 0.92        | 92.3        | 91.8        | 7564        |
|                               | AdaMax          | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.34          | 93.5        | 0.94        | 93.7        | 93.5        | 6505        |
|                               | AdaGrad         | 0.02           | 99.6        | 1.00        | 99.6        | 99.5        | 0.44          | 92.0        | 0.92        | 92.2        | 91.8        | 6133        |
| He Uniform                    | Adam            | 0.02           | 99.4        | 1.00        | 99.5        | 99.4        | 0.30          | 93.6        | 0.94        | 93.8        | 93.5        | 6872        |
|                               | AdaDelta        | 0.03           | 99.5        | 1.00        | 99.5        | 99.5        | 0.42          | 93.2        | 0.93        | 93.4        | 93.1        | 7467        |
|                               | SGD             | 0.03           | 99.3        | 0.99        | 99.3        | 99.2        | 0.37          | 91.9        | 0.92        | 92.2        | 91.7        | 5720        |
|                               | AdaMax          | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.36          | 93.4        | 0.94        | 93.6        | 93.3        | 6536        |
|                               | AdaGrad         | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.40          | 92.4        | 0.93        | 92.7        | 92.3        | 7476        |
| <b>Glorot (Xavier) Normal</b> | Adam            | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.33          | 93.7        | 0.94        | 93.9        | 93.7        | 8387        |
|                               | <b>AdaDelta</b> | <b>0.02</b>    | <b>99.6</b> | <b>1.00</b> | <b>99.6</b> | <b>99.6</b> | <b>0.41</b>   | <b>93.8</b> | <b>0.94</b> | <b>94.0</b> | <b>93.7</b> | <b>7485</b> |
|                               | SGD             | 0.02           | 99.4        | 0.99        | 99.4        | 99.4        | 0.35          | 92.9        | 0.93        | 93.1        | 92.9        | 5866        |
|                               | AdaMax          | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.36          | 93.5        | 0.94        | 93.6        | 93.4        | 6489        |
|                               | AdaGrad         | 0.02           | 99.6        | 1.00        | 99.6        | 99.5        | 0.44          | 91.7        | 0.92        | 91.8        | 91.5        | 6162        |
| Glorot (Xavier) Uniform       | Adam            | 0.02           | 99.4        | 0.99        | 99.4        | 99.4        | 0.32          | 93.2        | 0.93        | 93.5        | 93.2        | 6937        |
|                               | AdaDelta        | 0.03           | 99.5        | 1.00        | 99.5        | 99.5        | 0.42          | 93.3        | 0.93        | 93.5        | 93.2        | 7435        |
|                               | SGD             | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.33          | 93.2        | 0.93        | 93.4        | 93.1        | 5625        |
|                               | AdaMax          | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.32          | 93.7        | 0.94        | 93.9        | 93.6        | 7857        |
|                               | AdaGrad         | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.40          | 92.1        | 0.92        | 92.3        | 91.9        | 7556        |
| LeCun Normal                  | Adam            | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.31          | 93.7        | 0.94        | 93.9        | 93.6        | 6976        |
|                               | AdaDelta        | 0.03           | 99.5        | 1.00        | 99.5        | 99.5        | 0.42          | 93.5        | 0.94        | 93.7        | 93.4        | 7755        |
|                               | SGD             | 0.02           | 99.4        | 1.00        | 99.5        | 99.4        | 0.35          | 92.7        | 0.93        | 93.0        | 92.6        | 5757        |
|                               | AdaMax          | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.35          | 93.4        | 0.93        | 93.6        | 93.3        | 6431        |
|                               | AdaGrad         | 0.02           | 99.5        | 1.00        | 99.6        | 99.5        | 0.41          | 92.0        | 0.92        | 92.2        | 91.8        | 6045        |
| LeCun Uniform                 | Adam            | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.32          | 93.6        | 0.94        | 93.7        | 93.5        | 6753        |
|                               | AdaDelta        | 0.02           | 99.5        | 1.00        | 99.6        | 99.5        | 0.42          | 93.3        | 0.93        | 93.5        | 93.2        | 7360        |
|                               | SGD             | 0.03           | 99.3        | 0.99        | 99.3        | 99.3        | 0.34          | 93.0        | 0.93        | 93.2        | 92.9        | 5701        |
|                               | AdaMax          | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.34          | 93.7        | 0.94        | 93.8        | 93.6        | 6578        |
|                               | AdaGrad         | 0.02           | 99.5        | 1.00        | 99.6        | 99.5        | 0.41          | 92.0        | 0.92        | 92.2        | 91.9        | 6281        |

accuracy in experiment 4. The testing accuracy reached 86.0% with a loss value of 0.65. The average training time is 1533 s. The average training and testing accuracies are 96.7%, and 83.8%, respectively. The average training and testing losses are 0.19, and 0.85, respectively. Figure 19 shows the experiment training and testing accuracies curves with their trendlines. Figure 20 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 14 shows that the AdaDelta optimizer and Glorot Normal weight initializer report the highest testing accuracy in experiment 5. The testing accuracy reached 93.8% with a loss value of 0.41. The average training time is

6449 s. The average training and testing accuracies are 99.5%, and 93.0%, respectively. The average training and testing losses are 0.02, and 0.37, respectively. Figure 21 shows the experiment training and testing accuracies curves with their trendlines. Figure 22 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 15 shows that the SGD optimizer and LeCun Uniform weight initializer report the highest testing accuracy in experiment 6. The testing accuracy reached 92.2% with a loss value of 0.30. The average training time is 3996 s. The average training and testing accuracies are 94.8%, and 90.7%, respectively. The average training and

**Table 15** Training and testing reported results of Experiment 6

| Weight Initializer      | Optimizer  | Training Phase |             |             |             |             | Testing Phase |             |             |             |             | Time        |
|-------------------------|------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |            | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal               | Adam       | 0.36           | 93.1        | 0.93        | 94.1        | 92.2        | 0.47          | 89.9        | 0.90        | 91.3        | 88.7        | 3842        |
|                         | AdaDelta   | 0.43           | 92.6        | 0.93        | 93.6        | 91.4        | 0.55          | 89.6        | 0.90        | 91.2        | 88.2        | 4167        |
|                         | SGD        | 0.14           | 97.3        | 0.97        | 97.6        | 97.1        | 0.32          | 91.7        | 0.92        | 92.4        | 91.1        | 3276        |
|                         | AdaMax     | 0.24           | 95.8        | 0.96        | 96.2        | 95.4        | 0.37          | 91.6        | 0.92        | 92.3        | 91.0        | 3867        |
|                         | AdaGrad    | 0.18           | 95.1        | 0.95        | 95.8        | 94.4        | 0.31          | 90.6        | 0.91        | 91.9        | 89.5        | 3632        |
| He Uniform              | Adam       | 0.35           | 93.6        | 0.94        | 94.4        | 92.8        | 0.46          | 90.2        | 0.90        | 91.4        | 89.1        | 4147        |
|                         | AdaDelta   | 0.43           | 92.6        | 0.93        | 93.8        | 91.2        | 0.55          | 89.5        | 0.90        | 91.3        | 87.9        | 4083        |
|                         | SGD        | 0.15           | 96.7        | 0.97        | 97.0        | 96.4        | 0.31          | 91.4        | 0.92        | 92.2        | 90.8        | 3295        |
|                         | AdaMax     | 0.24           | 96.0        | 0.96        | 96.4        | 95.7        | 0.38          | 91.6        | 0.92        | 92.6        | 91.0        | 3732        |
|                         | AdaGrad    | 0.17           | 95.6        | 0.96        | 96.2        | 94.9        | 0.32          | 90.7        | 0.91        | 91.9        | 89.7        | 3491        |
| Glorot (Xavier) Normal  | Adam       | 0.36           | 93.3        | 0.93        | 94.3        | 92.3        | 0.47          | 89.8        | 0.90        | 91.2        | 88.5        | 3915        |
|                         | AdaDelta   | 0.42           | 92.7        | 0.93        | 93.8        | 91.6        | 0.54          | 89.9        | 0.90        | 91.6        | 88.5        | 4172        |
|                         | SGD        | 0.15           | 96.7        | 0.97        | 97.1        | 96.4        | 0.31          | 91.4        | 0.91        | 92.2        | 90.6        | 3234        |
|                         | AdaMax     | 0.24           | 95.8        | 0.96        | 96.2        | 95.4        | 0.38          | 91.6        | 0.92        | 92.4        | 90.9        | 3508        |
|                         | AdaGrad    | 0.16           | 96.0        | 0.96        | 96.5        | 95.5        | 0.30          | 91.2        | 0.91        | 92.2        | 90.3        | 3343        |
| Glorot (Xavier) Uniform | Adam       | 0.33           | 93.9        | 0.94        | 94.6        | 93.1        | 0.45          | 90.8        | 0.91        | 91.8        | 89.8        | 3726        |
|                         | AdaDelta   | 0.43           | 92.3        | 0.92        | 93.5        | 91.1        | 0.55          | 89.4        | 0.89        | 91.0        | 88.0        | 4236        |
|                         | SGD        | 0.14           | 97.0        | 0.97        | 97.3        | 96.7        | 0.32          | 91.6        | 0.92        | 92.6        | 91.0        | 3235        |
|                         | AdaMax     | 0.25           | 95.5        | 0.95        | 96.0        | 95.0        | 0.38          | 91.3        | 0.91        | 92.3        | 90.5        | 4914        |
|                         | AdaGrad    | 0.42           | 92.6        | 0.93        | 93.8        | 91.3        | 0.54          | 89.4        | 0.89        | 91.0        | 87.7        | 4050        |
| LeCun Normal            | Adam       | 0.36           | 93.3        | 0.93        | 94.2        | 92.4        | 0.47          | 90.1        | 0.90        | 91.3        | 89.0        | 4026        |
|                         | AdaDelta   | 0.42           | 92.6        | 0.93        | 93.8        | 91.3        | 0.53          | 89.8        | 0.90        | 91.3        | 88.3        | 4316        |
|                         | SGD        | 0.15           | 96.8        | 0.97        | 97.1        | 96.5        | 0.33          | 91.5        | 0.92        | 92.3        | 90.9        | 3380        |
|                         | AdaMax     | 0.25           | 95.5        | 0.96        | 95.9        | 95.1        | 0.39          | 91.5        | 0.92        | 92.4        | 90.9        | 3829        |
|                         | AdaGrad    | 0.18           | 95.4        | 0.95        | 96.1        | 94.8        | 0.31          | 91.0        | 0.91        | 92.1        | 89.8        | 4435        |
| <b>LeCun Uniform</b>    | Adam       | 0.34           | 93.7        | 0.94        | 94.5        | 92.9        | 0.47          | 89.8        | 0.90        | 91.1        | 88.8        | 4976        |
|                         | AdaDelta   | 0.43           | 92.4        | 0.92        | 93.8        | 91.1        | 0.54          | 89.6        | 0.90        | 91.3        | 87.8        | 5374        |
|                         | <b>SGD</b> | <b>0.13</b>    | <b>97.7</b> | <b>0.98</b> | <b>97.9</b> | <b>97.5</b> | <b>0.30</b>   | <b>92.2</b> | <b>0.92</b> | <b>92.8</b> | <b>91.7</b> | <b>4266</b> |
|                         | AdaMax     | 0.24           | 95.8        | 0.96        | 96.2        | 95.4        | 0.38          | 91.1        | 0.91        | 91.9        | 90.5        | 4824        |
|                         | AdaGrad    | 0.14           | 96.7        | 0.97        | 97.2        | 96.3        | 0.30          | 91.3        | 0.91        | 92.4        | 90.4        | 4596        |

testing losses are 0.27, and 0.41, respectively. Figure 23 shows the experiment training and testing accuracies curves with their trendlines. Figure 24 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 16 shows that Adam optimizer and LeCun Uniform weight initializer report the highest testing accuracy in experiment 7. The testing accuracy reached 98.4% with a loss value of 0.07. The average training time is 28,595 s. The average training and testing accuracies are 99.8%, and 97.8%, respectively. The average training and testing losses are 0.01, and 0.10, respectively. Figure 25 shows the experiment training and testing accuracies curves with their

trendlines. Figure 26 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 17 shows that SGD and He Uniform weight initializer report the highest testing accuracy in experiment 8. The testing accuracy reached 95.4% with a loss value of 0.18. The average training time is 16,245 s. The average training and testing accuracies are 94.3%, and 93.2%, respectively. The average training and testing losses are 0.27, and 0.30, respectively. Figure 27 shows the experiment training and testing accuracies curves with their trendlines. Figure 28 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding



**Table 16** Training and testing reported results of Experiment 7

| Weight initializer      | Optimizer   | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time          |
|-------------------------|-------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|---------------|
|                         |             | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |               |
| He Normal               | Adam        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.2        | 0.98        | 98.3        | 98.2        | 35,194        |
|                         | AdaDelta    | 0.01           | 99.7        | 1.00        | 99.8        | 99.7        | 0.10          | 98.0        | 0.98        | 98.1        | 98.0        | 31,005        |
|                         | SGD         | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.09          | 97.7        | 0.98        | 97.8        | 97.7        | 28,300        |
|                         | AdaMax      | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.3        | 0.98        | 98.3        | 98.3        | 25,521        |
|                         | AdaGrad     | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.16          | 96.6        | 0.97        | 96.6        | 96.6        | 24,206        |
| He Uniform              | Adam        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.2        | 0.98        | 98.3        | 98.2        | 27,081        |
|                         | AdaDelta    | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 98.1        | 0.98        | 98.2        | 98.1        | 30,401        |
|                         | SGD         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 97.8        | 0.98        | 97.8        | 97.7        | 23,078        |
|                         | AdaMax      | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.2        | 0.98        | 98.2        | 98.1        | 34,270        |
|                         | AdaGrad     | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.13          | 96.9        | 0.97        | 97.0        | 96.9        | 25,048        |
| Glorot (Xavier) Normal  | Adam        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.3        | 0.98        | 98.3        | 98.3        | 28,252        |
|                         | AdaDelta    | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.09          | 98.1        | 0.98        | 98.1        | 98.1        | 26,334        |
|                         | SGD         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 97.7        | 0.98        | 97.8        | 97.7        | 22,849        |
|                         | AdaMax      | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.3        | 0.98        | 98.3        | 98.3        | 26,581        |
|                         | AdaGrad     | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.15          | 96.7        | 0.97        | 96.8        | 96.7        | 24,868        |
| Glorot (Xavier) Uniform | Adam        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.1        | 0.98        | 98.2        | 98.1        | 25,827        |
|                         | AdaDelta    | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.1        | 0.98        | 98.2        | 98.1        | 30,129        |
|                         | SGD         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 97.8        | 0.98        | 97.9        | 97.8        | 29,349        |
|                         | AdaMax      | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.3        | 0.98        | 98.3        | 98.2        | 25,901        |
|                         | AdaGrad     | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.14          | 96.8        | 0.97        | 96.8        | 96.7        | 31,701        |
| LeCun Normal            | Adam        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.2        | 0.98        | 98.2        | 98.1        | 33,002        |
|                         | AdaDelta    | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.11          | 98.0        | 0.98        | 98.1        | 98.0        | 29,398        |
|                         | SGD         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 97.7        | 0.98        | 97.8        | 97.7        | 23,725        |
|                         | AdaMax      | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.3        | 0.98        | 98.3        | 98.3        | 33,528        |
|                         | AdaGrad     | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.16          | 96.6        | 0.97        | 96.7        | 96.6        | 32,193        |
| <b>LeCun Uniform</b>    | <b>Adam</b> | <b>0.01</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.07</b>   | <b>98.4</b> | <b>0.98</b> | <b>98.4</b> | <b>98.4</b> | <b>34,729</b> |
|                         | AdaDelta    | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 98.1        | 0.98        | 98.1        | 98.1        | 28,113        |
|                         | SGD         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 97.7        | 0.98        | 97.7        | 97.7        | 28,772        |
|                         | AdaMax      | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.2        | 0.98        | 98.3        | 98.2        | 34,266        |
|                         | AdaGrad     | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.12          | 97.1        | 0.97        | 97.2        | 97.0        | 24,234        |

experiment rows, and the y-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 18 shows that two scenarios in experiment 9 reach 100% testing accuracies, but AdaDelta optimizer and Glorot (Xavier) Uniform weight initializer report the highest training and testing accuracies. The testing accuracy reached 100% with a loss value of 0. The average training time is 141 s. The average training and testing accuracies are 99.6%, and 97.9%, respectively. The average training and testing losses are 0.02, and 0.07, respectively. Figure 29 shows the experiment training and testing accuracies curves with their trendlines. Figure 30 shows the training time curve with its trendline. The x-axis refers to the corresponding experiment rows, and the y-axis refers to

the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 19 shows that Adam optimizer and LeCun Uniform weight initializer report the highest testing accuracy in experiment 10. The testing accuracy reached 100% with a loss value of 0.05. The average training time is 142 s. The average training and testing accuracies are 99.7%, and 98.3%, respectively. The average training and testing losses are 0.06, and 0.09, respectively. Figure 31 shows the experiment training and testing accuracies curves with their trendlines. Figure 32 shows the training time curve with its trendline. The x-axis refers to the corresponding experiment rows, and the y-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

**Table 17** Training and testing reported results of Experiment 8

| Weight initializer      | Optimizer  | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time          |
|-------------------------|------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|---------------|
|                         |            | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |               |
| He Normal               | Adam       | 0.40           | 91.7        | 0.92        | 92.7        | 90.8        | 0.42          | 90.8        | 0.91        | 92.0        | 89.9        | 20,889        |
|                         | AdaDelta   | 0.47           | 91.2        | 0.91        | 92.7        | 89.5        | 0.49          | 90.7        | 0.91        | 92.2        | 88.9        | 20,611        |
|                         | SGD        | 0.15           | 96.9        | 0.97        | 97.1        | 96.6        | 0.18          | 95.4        | 0.96        | 95.8        | 95.1        | 17,437        |
|                         | AdaMax     | 0.28           | 94.1        | 0.94        | 94.8        | 93.5        | 0.31          | 93.1        | 0.93        | 94.0        | 92.4        | 19,322        |
|                         | AdaGrad    | 0.12           | 96.8        | 0.97        | 97.1        | 96.5        | 0.16          | 95.0        | 0.95        | 95.5        | 94.6        | 14,118        |
| <b>He Uniform</b>       | Adam       | 0.39           | 91.6        | 0.92        | 92.9        | 90.5        | 0.42          | 90.9        | 0.91        | 92.3        | 89.7        | 16,365        |
|                         | AdaDelta   | 0.48           | 90.6        | 0.91        | 92.4        | 88.7        | 0.51          | 89.9        | 0.90        | 91.9        | 88.1        | 17,909        |
|                         | <b>SGD</b> | <b>0.14</b>    | <b>96.9</b> | <b>0.97</b> | <b>97.1</b> | <b>96.7</b> | <b>0.18</b>   | <b>95.4</b> | <b>0.96</b> | <b>95.8</b> | <b>95.1</b> | <b>13,268</b> |
|                         | AdaMax     | 0.28           | 94.1        | 0.94        | 94.7        | 93.6        | 0.31          | 93.0        | 0.93        | 93.7        | 92.5        | 19,555        |
|                         | AdaGrad    | 0.12           | 96.9        | 0.97        | 97.2        | 96.6        | 0.16          | 95.2        | 0.95        | 95.7        | 94.9        | 13,702        |
| Glorot (Xavier) Normal  | Adam       | 0.39           | 91.8        | 0.92        | 93.1        | 90.6        | 0.41          | 91.1        | 0.91        | 92.5        | 89.8        | 15,415        |
|                         | AdaDelta   | 0.47           | 91.1        | 0.91        | 92.4        | 89.8        | 0.49          | 90.6        | 0.91        | 92.0        | 89.3        | 16,169        |
|                         | SGD        | 0.14           | 96.8        | 0.97        | 97.0        | 96.6        | 0.19          | 95.3        | 0.95        | 95.7        | 95.0        | 16,564        |
|                         | AdaMax     | 0.27           | 94.6        | 0.95        | 95.2        | 94.0        | 0.30          | 93.7        | 0.94        | 94.3        | 93.0        | 19,878        |
|                         | AdaGrad    | 0.12           | 96.8        | 0.97        | 97.2        | 96.5        | 0.16          | 95.1        | 0.95        | 95.6        | 94.7        | 18,325        |
| Glorot (Xavier) Uniform | Adam       | 0.48           | 90.9        | 0.91        | 92.4        | 89.5        | 0.50          | 90.3        | 0.90        | 91.7        | 88.9        | 16,485        |
|                         | AdaDelta   | 0.14           | 96.9        | 0.97        | 97.2        | 96.7        | 0.18          | 95.4        | 0.95        | 95.8        | 95.1        | 13,203        |
|                         | SGD        | 0.27           | 94.3        | 0.94        | 94.9        | 93.7        | 0.30          | 93.3        | 0.93        | 94.1        | 92.6        | 19,922        |
|                         | AdaMax     | 0.13           | 96.5        | 0.97        | 96.8        | 96.2        | 0.17          | 94.9        | 0.95        | 95.4        | 94.5        | 13,465        |
|                         | AdaGrad    | 0.12           | 96.9        | 0.97        | 97.2        | 96.6        | 0.16          | 95.1        | 0.95        | 95.6        | 94.7        | 13,929        |
| LeCun Normal            | Adam       | 0.38           | 91.9        | 0.92        | 93.0        | 91.0        | 0.41          | 91.2        | 0.91        | 92.2        | 90.3        | 15,449        |
|                         | AdaDelta   | 0.47           | 91.1        | 0.91        | 92.5        | 89.8        | 0.49          | 90.6        | 0.91        | 92.2        | 89.3        | 17,164        |
|                         | SGD        | 0.17           | 96.1        | 0.96        | 96.5        | 95.8        | 0.21          | 94.8        | 0.95        | 95.3        | 94.4        | 12,632        |
|                         | AdaMax     | 0.28           | 94.2        | 0.94        | 94.8        | 93.5        | 0.31          | 93.2        | 0.93        | 94.0        | 92.6        | 14,252        |
|                         | AdaGrad    | 0.12           | 96.8        | 0.97        | 97.1        | 96.5        | 0.16          | 95.1        | 0.95        | 95.5        | 94.6        | 17,546        |
| LeCun Uniform           | Adam       | 0.38           | 92.2        | 0.92        | 93.2        | 91.2        | 0.40          | 91.4        | 0.92        | 92.6        | 90.4        | 15,879        |
|                         | AdaDelta   | 0.47           | 91.0        | 0.91        | 92.6        | 89.4        | 0.49          | 90.5        | 0.90        | 92.2        | 88.8        | 17,055        |
|                         | SGD        | 0.15           | 96.8        | 0.97        | 97.1        | 96.5        | 0.19          | 95.4        | 0.95        | 95.8        | 95.0        | 13,181        |
|                         | AdaMax     | 0.27           | 94.3        | 0.94        | 95.0        | 93.7        | 0.31          | 93.3        | 0.93        | 94.1        | 92.7        | 14,094        |
|                         | AdaGrad    | 0.12           | 96.9        | 0.97        | 97.2        | 96.6        | 0.17          | 95.1        | 0.95        | 95.5        | 94.7        | 13,569        |

Table 20 shows that the AdaDelta optimizer and Glorot (Xavier) Uniform weight initializer report the highest testing accuracy in experiment 11. The testing accuracy reached 99.4% with a loss value of 0.05. The average training time is 1000 s. The average training and testing accuracies are 99.8%, and 98.9%, respectively. The average training and testing losses are 0.01, and 0.05, respectively. Figure 33 shows the experiment training and testing accuracies curves with their trendlines. Figure 34 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 21 shows that the AdaMax optimizer and LeCun Uniform weight initializer report the highest testing

accuracy in experiment 12. The testing accuracy reached 99.2% with a loss value of 0.06. The average training time is 751 s. The average training and testing accuracies are 99.8%, and 98.8%, respectively. The average training and testing losses are 0.05, and 0.08, respectively. Figure 35 shows the experiment training and testing accuracies curves with their trendlines. Figure 36 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

From experiments (9 to 12), accuracy, precision, and recall values are above (or equal) 99.2%, loss values are below (or equal) 0.06 and F1 values are above (or equal) 0.99. HMB1 reports better results than HMB2. Table 22

**Table 18** Training and testing reported results of Experiment 9

| Weight initializer             | Optimizer       | Training phase |             |             |             |             | Testing phase |              |             |              |              | Time       |
|--------------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|--------------|-------------|--------------|--------------|------------|
|                                |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy     | F1          | Precision    | Recall       |            |
| He Normal                      | Adam            | 0.03           | 99.2        | 0.99        | 99.3        | 99.1        | 0.14          | 96.7         | 0.97        | 97.3         | 96.7         | 113        |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.04          | 99.3         | 0.99        | 99.3         | 98.7         | 117        |
|                                | SGD             | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.03          | 98.7         | 0.99        | 99.3         | 98.7         | 94         |
|                                | AdaMax          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.0         | 0.98        | 98.0         | 98.0         | 109        |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.8        | 0.07          | 97.3         | 0.97        | 97.3         | 96.7         | 104        |
| He Uniform                     | Adam            | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.14          | 95.3         | 0.95        | 95.3         | 95.3         | 117        |
|                                | AdaDelta        | 0.05           | 98.7        | 0.99        | 98.9        | 98.6        | 0.06          | 97.3         | 0.98        | 98.0         | 97.3         | 128        |
|                                | SGD             | 0.02           | 99.7        | 1.00        | 99.7        | 99.6        | 0.07          | 97.3         | 0.97        | 97.3         | 97.3         | 103        |
|                                | AdaMax          | 0.02           | 99.7        | 1.00        | 99.7        | 99.7        | 0.05          | 98.7         | 0.98        | 98.7         | 98.0         | 119        |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 97.3         | 0.97        | 97.3         | 97.3         | 118        |
| Glorot (Xavier) Normal         | Adam            | 0.01           | 99.5        | 1.00        | 99.5        | 99.5        | 0.02          | 99.3         | 1.00        | 100.0        | 99.3         | 131        |
|                                | AdaDelta        | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.01          | 100.0        | 1.00        | 100.0        | 100.0        | 141        |
|                                | SGD             | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.03          | 99.3         | 0.99        | 99.3         | 98.7         | 124        |
|                                | AdaMax          | 0.03           | 98.9        | 0.99        | 99.1        | 98.9        | 0.09          | 96.7         | 0.97        | 96.7         | 96.7         | 135        |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.13          | 95.3         | 0.96        | 96.0         | 95.3         | 131        |
| <b>Glorot (Xavier) Uniform</b> | Adam            | 0.01           | 99.6        | 1.00        | 99.6        | 99.6        | 0.02          | 98.7         | 0.99        | 98.7         | 98.7         | 149        |
|                                | <b>AdaDelta</b> | <b>0.01</b>    | <b>99.8</b> | <b>1.00</b> | <b>99.8</b> | <b>99.8</b> | <b>0.00</b>   | <b>100.0</b> | <b>1.00</b> | <b>100.0</b> | <b>100.0</b> | <b>159</b> |
|                                | SGD             | 0.02           | 99.6        | 1.00        | 99.6        | 99.4        | 0.05          | 98.7         | 0.99        | 99.3         | 98.0         | 133        |
|                                | AdaMax          | 0.06           | 98.6        | 0.99        | 98.8        | 98.3        | 0.16          | 95.3         | 0.95        | 95.3         | 95.3         | 150        |
|                                | AdaGrad         | 0.02           | 99.7        | 1.00        | 99.7        | 99.7        | 0.08          | 96.0         | 0.96        | 96.7         | 96.0         | 146        |
| LeCun Normal                   | Adam            | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.7         | 0.99        | 98.7         | 98.7         | 164        |
|                                | AdaDelta        | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.15          | 96.7         | 0.97        | 97.3         | 96.7         | 170        |
|                                | SGD             | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.03          | 99.3         | 0.99        | 99.3         | 98.7         | 152        |
|                                | AdaMax          | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.03          | 98.0         | 0.98        | 98.6         | 98.0         | 170        |
|                                | AdaGrad         | 0.03           | 99.3        | 0.99        | 99.4        | 99.3        | 0.04          | 98.7         | 0.99        | 98.7         | 98.7         | 160        |
| LeCun Uniform                  | Adam            | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.03          | 98.7         | 0.99        | 98.7         | 98.7         | 179        |
|                                | AdaDelta        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.7         | 0.99        | 98.7         | 98.7         | 185        |
|                                | SGD             | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.03          | 98.7         | 0.98        | 98.6         | 98.0         | 164        |
|                                | AdaMax          | 0.01           | 99.8        | 1.00        | 99.9        | 99.8        | 0.03          | 98.0         | 0.98        | 98.0         | 98.0         | 181        |
|                                | AdaGrad         | 0.03           | 99.3        | 0.99        | 99.3        | 99.2        | 0.13          | 96.0         | 0.96        | 96.7         | 95.3         | 175        |

shows a comparison between the study reported accuracies, and other authors (researches) reported accuracies:

Figure 37 shows the confusion matrices (top left, top right, bottom left, and bottom right) of the last four experiments (9 to 12), respectively.

Table 23 shows that the AdaDelta optimizer and He Uniform weight initializer report the highest testing accuracy in experiment 13. The testing accuracy reached 92.7% with a loss value of 0.42. The average training time is 334 s. The average training and testing accuracies are 92.6%, and 86.6%, respectively. The average training and testing losses are 0.24, and 0.48, respectively. Figure 38 shows the experiment training and testing accuracies curves with their trendlines. Figure 39 shows the training time curve with its trendline. The  $x$ -axis refers to the

corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 24 shows that two scenarios in experiment 14 reach 93.3% testing accuracies, but AdaGrad optimizer and He Uniform weight initializer report the highest training and testing accuracies. The testing accuracy reached 93.3% with a loss value of 0.38. The average training time is 179 s. The average training and testing accuracies are 99.4%, and 91.9%, respectively. The average training and testing losses are 0.09, and 0.47, respectively. Figure 40 shows the experiment training and testing accuracies curves with their trendlines. Figure 41 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a

**Table 19** Training and testing reported results of Experiment 10

| Weight initializer      | Optimizer   | Training phase |             |             |             |             | Testing phase |              |             |              |              | Time       |
|-------------------------|-------------|----------------|-------------|-------------|-------------|-------------|---------------|--------------|-------------|--------------|--------------|------------|
|                         |             | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy     | F1          | Precision    | Recall       |            |
| He Normal               | Adam        | 0.09           | 99.3        | 0.99        | 99.3        | 99.3        | 0.12          | 98.7         | 0.99        | 98.7         | 98.7         | 124        |
|                         | AdaDelta    | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.7         | 0.99        | 98.7         | 98.7         | 129        |
|                         | SGD         | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 98.7         | 0.99        | 99.3         | 98.7         | 113        |
|                         | AdaMax      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 96.7         | 0.97        | 96.7         | 96.7         | 125        |
|                         | AdaGrad     | 0.06           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.0         | 0.98        | 98.0         | 98.0         | 118        |
| He Uniform              | Adam        | 0.07           | 99.8        | 1.00        | 99.8        | 99.8        | 0.12          | 98.0         | 0.98        | 98.0         | 98.0         | 133        |
|                         | AdaDelta    | 0.06           | 99.7        | 1.00        | 99.7        | 99.7        | 0.08          | 99.3         | 0.99        | 99.3         | 99.3         | 135        |
|                         | SGD         | 0.06           | 99.7        | 1.00        | 99.7        | 99.7        | 0.12          | 98.0         | 0.98        | 98.0         | 98.0         | 121        |
|                         | AdaMax      | 0.05           | 99.9        | 1.00        | 99.9        | 99.8        | 0.08          | 99.3         | 0.99        | 99.3         | 99.3         | 133        |
|                         | AdaGrad     | 0.06           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.7         | 0.99        | 98.7         | 98.7         | 127        |
| Glorot (Xavier) Normal  | Adam        | 0.06           | 99.8        | 1.00        | 99.8        | 99.8        | 0.12          | 98.7         | 0.99        | 98.7         | 98.7         | 141        |
|                         | AdaDelta    | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.11          | 98.0         | 0.98        | 98.0         | 98.0         | 146        |
|                         | SGD         | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 97.3         | 0.97        | 97.3         | 97.3         | 128        |
|                         | AdaMax      | 0.07           | 99.5        | 1.00        | 99.5        | 99.5        | 0.15          | 94.7         | 0.95        | 94.7         | 94.7         | 141        |
|                         | AdaGrad     | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.04          | 99.3         | 0.99        | 99.3         | 99.3         | 134        |
| Glorot (Xavier) Uniform | Adam        | 0.07           | 99.8        | 1.00        | 99.8        | 99.8        | 0.13          | 98.7         | 0.99        | 98.7         | 98.7         | 150        |
|                         | AdaDelta    | 0.10           | 98.4        | 0.98        | 98.5        | 98.3        | 0.10          | 97.3         | 0.98        | 98.0         | 97.3         | 151        |
|                         | SGD         | 0.07           | 99.3        | 0.99        | 99.4        | 99.3        | 0.08          | 98.0         | 0.98        | 98.7         | 98.0         | 136        |
|                         | AdaMax      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.11          | 96.7         | 0.97        | 96.7         | 96.7         | 149        |
|                         | AdaGrad     | 0.07           | 99.5        | 1.00        | 99.5        | 99.5        | 0.07          | 99.3         | 0.99        | 99.3         | 99.3         | 141        |
| LeCun Normal            | Adam        | 0.09           | 99.4        | 0.99        | 99.4        | 99.4        | 0.15          | 97.3         | 0.97        | 97.3         | 97.3         | 157        |
|                         | AdaDelta    | 0.07           | 99.5        | 1.00        | 99.5        | 99.5        | 0.06          | 99.3         | 0.99        | 99.3         | 99.3         | 160        |
|                         | SGD         | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 99.3         | 0.99        | 99.3         | 99.3         | 145        |
|                         | AdaMax      | 0.05           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 99.3         | 0.99        | 99.3         | 99.3         | 158        |
|                         | AdaGrad     | 0.07           | 99.6        | 1.00        | 99.7        | 99.6        | 0.10          | 97.3         | 0.97        | 97.3         | 97.3         | 148        |
| <b>LeCun Uniform</b>    | <b>Adam</b> | <b>0.06</b>    | <b>99.7</b> | <b>1.00</b> | <b>99.7</b> | <b>99.7</b> | <b>0.05</b>   | <b>100.0</b> | <b>1.00</b> | <b>100.0</b> | <b>100.0</b> | <b>166</b> |
|                         | AdaDelta    | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 99.3         | 0.99        | 99.3         | 99.3         | 166        |
|                         | SGD         | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.0         | 0.98        | 98.0         | 98.0         | 154        |
|                         | AdaMax      | 0.06           | 99.6        | 1.00        | 99.6        | 99.6        | 0.08          | 99.3         | 0.99        | 99.3         | 99.3         | 165        |
|                         | AdaGrad     | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.07          | 98.0         | 0.98        | 98.7         | 98.0         | 155        |

percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 25 shows that the AdaMax optimizer and He Uniform weight initializer report the highest testing accuracy in experiment 15. The testing accuracy reached 99.0% with a loss value of 0.06. The average training time is 3116 s. The average training and testing accuracies are 99.9%, and 98.6%, respectively. The average training and testing losses are 0.01, and 0.08, respectively. Figure 42 shows the experiment training and testing accuracies curves with their trendlines. Figure 43 shows the training time curve with its trendline. The *x*-axis refers to the corresponding experiment rows, and the *y*-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 26 shows that the SGD optimizer and He Normal weight initializer report the highest testing accuracy in experiment 16. The testing accuracy reached 98.4% with a loss value of 0.10. The average training time is 1764 s. The average training and testing accuracies are 99.4%, and 97.8%, respectively. The average training and testing losses are 0.08, and 0.13, respectively. Figure 44 shows the experiment training and testing accuracies curves with their trendlines. Figure 45 shows the training time curve with its trendline. The *x*-axis refers to the corresponding experiment rows, and the *y*-axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

From this finding, it can be concluded that the two newly presented architectures in the current study can be

**Table 20** Training and testing reported results of Experiment 11

| Weight initializer             | Optimizer       | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|--------------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                                |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal                      | Adam            | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.03          | 99.3        | 0.99        | 99.3        | 99.3        | 959         |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 99.2        | 0.99        | 99.2        | 99.2        | 1027        |
|                                | SGD             | 0.02           | 99.5        | 1.00        | 99.5        | 99.4        | 0.05          | 98.7        | 0.99        | 98.7        | 98.6        | 787         |
|                                | AdaMax          | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.8        | 0.99        | 98.8        | 98.8        | 910         |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.7        | 0.99        | 98.7        | 98.6        | 863         |
| He Uniform                     | Adam            | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 98.9        | 0.99        | 98.9        | 98.9        | 976         |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.04          | 99.1        | 0.99        | 99.1        | 99.1        | 1058        |
|                                | SGD             | 0.01           | 99.6        | 1.00        | 99.6        | 99.6        | 0.04          | 98.8        | 0.99        | 98.8        | 98.7        | 824         |
|                                | AdaMax          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.04          | 99.3        | 0.99        | 99.3        | 99.3        | 937         |
|                                | AdaGrad         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.04          | 98.8        | 0.99        | 98.8        | 98.7        | 902         |
| Glorot (Xavier) Normal         | Adam            | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.7        | 0.99        | 98.7        | 98.7        | 1016        |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 99.3        | 0.99        | 99.3        | 99.3        | 1093        |
|                                | SGD             | 0.02           | 99.5        | 1.00        | 99.5        | 99.5        | 0.05          | 98.7        | 0.99        | 98.8        | 98.7        | 857         |
|                                | AdaMax          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 98.8        | 0.99        | 98.9        | 98.8        | 980         |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.03          | 99.3        | 0.99        | 99.3        | 99.3        | 937         |
| <b>Glorot (Xavier) Uniform</b> | Adam            | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 98.9        | 0.99        | 98.9        | 98.9        | 1062        |
|                                | <b>AdaDelta</b> | <b>0.00</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.05</b>   | <b>99.4</b> | <b>0.99</b> | <b>99.4</b> | <b>99.4</b> | <b>1143</b> |
|                                | SGD             | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.05          | 98.6        | 0.99        | 98.6        | 98.6        | 907         |
|                                | AdaMax          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.04          | 98.8        | 0.99        | 98.9        | 98.8        | 1028        |
|                                | AdaGrad         | 0.01           | 99.6        | 1.00        | 99.7        | 99.6        | 0.05          | 98.6        | 0.99        | 98.6        | 98.6        | 983         |
| LeCun Normal                   | Adam            | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.03          | 99.1        | 0.99        | 99.1        | 99.1        | 1100        |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.8        | 0.99        | 98.8        | 98.8        | 1173        |
|                                | SGD             | 0.02           | 99.4        | 0.99        | 99.4        | 99.3        | 0.05          | 98.4        | 0.98        | 98.5        | 98.4        | 933         |
|                                | AdaMax          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.04          | 99.2        | 0.99        | 99.2        | 99.2        | 1061        |
|                                | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 98.6        | 0.99        | 98.6        | 98.6        | 1017        |
| LeCun Uniform                  | Adam            | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.05          | 98.8        | 0.99        | 98.8        | 98.8        | 1133        |
|                                | AdaDelta        | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 99.1        | 0.99        | 99.1        | 99.1        | 1227        |
|                                | SGD             | 0.02           | 99.6        | 1.00        | 99.6        | 99.5        | 0.04          | 98.8        | 0.99        | 98.8        | 98.8        | 965         |
|                                | AdaMax          | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.05          | 98.6        | 0.99        | 98.6        | 98.6        | 1097        |
|                                | AdaGrad         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.05          | 98.9        | 0.99        | 98.9        | 98.9        | 1058        |

used for different datasets, with a high-quality output. Besides that, they produce higher accuracies than two reported and published accuracies. As mentioned, the differences between the two described architectures are in the design of the hidden layers, such as the number and type of layers, the number and the size of kernels, and the size of strides. This concludes also two main things (from the hardware point of view): (i) HMB1 can achieve higher accuracy than HMB2 and can be used with devices with high-level hardware such as Gaming devices. (ii) HMB2 can achieve a bit lower accuracy than HMB2 and can be used with devices such as mobile phones (they contain low-level hardware compared with Gaming devices).

## 5.3 Cross-validation testing

### 5.3.1 Phase 1: (test HMBD versus the selected control architecture)

After training their architecture, the results are presented in Table 27.

### 5.3.2 Comments on the first phase

The training and testing accuracies reach max 51.0% and 47.7%, respectively. The losses are higher than 1.8, and the F1 scores are below 0.5. These values proved that their control architecture cannot generalize for the current study presented dataset. This may be due to the inability of the



**Table 21** Training and testing reported results of Experiment 12

| Weight initializer      | Optimizer     | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time       |
|-------------------------|---------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|------------|
|                         |               | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |            |
| He Normal               | Adam          | 0.07           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.9        | 0.99        | 98.9        | 98.9        | 728        |
|                         | AdaDelta      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 98.5        | 0.99        | 98.5        | 98.5        | 789        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.5        | 0.99        | 98.5        | 98.5        | 612        |
|                         | AdaMax        | 0.03           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.8        | 0.99        | 98.8        | 98.8        | 698        |
|                         | AdaGrad       | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.9        | 0.99        | 98.9        | 98.9        | 664        |
| He Uniform              | Adam          | 0.08           | 99.5        | 1.00        | 99.6        | 99.5        | 0.14          | 98.1        | 0.98        | 98.1        | 98.1        | 752        |
|                         | AdaDelta      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.08          | 99.1        | 0.99        | 99.1        | 99.1        | 825        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.8        | 0.99        | 98.8        | 98.8        | 631        |
|                         | AdaMax        | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.9        | 0.99        | 98.9        | 98.9        | 714        |
|                         | AdaGrad       | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.7        | 0.99        | 98.7        | 98.7        | 681        |
| Glorot (Xavier) Normal  | Adam          | 0.07           | 99.6        | 1.00        | 99.6        | 99.6        | 0.11          | 98.6        | 0.99        | 98.6        | 98.5        | 765        |
|                         | AdaDelta      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.6        | 0.99        | 98.7        | 98.5        | 819        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 99.0        | 0.99        | 99.1        | 99.0        | 651        |
|                         | AdaMax        | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 99.0        | 0.99        | 99.0        | 99.0        | 729        |
|                         | AdaGrad       | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 99.0        | 0.99        | 99.0        | 99.0        | 714        |
| Glorot (Xavier) Uniform | Adam          | 0.07           | 99.5        | 1.00        | 99.5        | 99.5        | 0.10          | 98.4        | 0.98        | 98.4        | 98.4        | 792        |
|                         | AdaDelta      | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 99.1        | 0.99        | 99.1        | 99.1        | 853        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.7        | 0.99        | 98.7        | 98.7        | 675        |
|                         | AdaMax        | 0.03           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.7        | 0.99        | 98.7        | 98.7        | 756        |
|                         | AdaGrad       | 0.03           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 99.1        | 0.99        | 99.1        | 99.1        | 727        |
| LeCun Normal            | Adam          | 0.07           | 99.7        | 1.00        | 99.7        | 99.7        | 0.10          | 98.9        | 0.99        | 98.9        | 98.9        | 818        |
|                         | AdaDelta      | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 99.0        | 0.99        | 99.0        | 99.0        | 870        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.8        | 0.08          | 98.9        | 0.99        | 98.9        | 98.8        | 702        |
|                         | AdaMax        | 0.04           | 99.9        | 1.00        | 99.9        | 99.8        | 0.08          | 99.0        | 0.99        | 99.1        | 98.9        | 788        |
|                         | AdaGrad       | 0.03           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 99.1        | 0.99        | 99.1        | 99.1        | 753        |
| <b>LeCun Uniform</b>    | Adam          | 0.06           | 99.7        | 1.00        | 99.7        | 99.7        | 0.09          | 98.8        | 0.99        | 98.8        | 98.8        | 835        |
|                         | AdaDelta      | 0.05           | 99.7        | 1.00        | 99.7        | 99.7        | 0.10          | 98.7        | 0.99        | 98.7        | 98.7        | 892        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.5        | 0.99        | 98.6        | 98.5        | 720        |
|                         | <b>AdaMax</b> | <b>0.03</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.06</b>   | <b>99.2</b> | <b>0.99</b> | <b>99.2</b> | <b>99.2</b> | <b>803</b> |
|                         | AdaGrad       | 0.03           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 99.1        | 0.99        | 99.1        | 99.1        | 772        |

**Table 22** Comparing current study and other authors reported accuracies using CMATER dataset

| Authors       | Testing accuracy  |
|---------------|---|
| Current Study | 100% (with the HMB1 architecture)<br>99.2% and 99.4% (with the HMB2 architecture) |
| [74]          | 98.59%  |
| [75]          | 97.40%  |

control architecture to work with the study larger and more complex datasets.

### 5.3.3 Phase 2 (test the described architectures' generalization versus the control dataset)

Tables 28 and 29 show the corresponding results of the different experiments mentioned in Table 6, respectively. They show the loss, accuracy, F1, precision, and recall values for training and testing phases. The training time is reported in seconds. The best results are in bold.

Table 28 shows that the AdaDelta optimizer and LeCun Uniform weight initializer report the highest testing accuracy which is 97.3% using HMB1 in phase two from the cross-validation testing. The average training time is 740 s. The average training and testing accuracies are 99.8%, and 96.1%, respectively. The average training and testing losses are 0.01, and 0.18, respectively. Figure 46 shows the

**Table 23** Training and testing reported results of Experiment 13

| Weight initializer      | Optimizer       | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time       |
|-------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|------------|
|                         |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |            |
| He Normal               | Adam            | 0.18           | 94.4        | 0.94        | 95.3        | 93.4        | 0.42          | 89.1        | 0.89        | 90.2        | 88.0        | 303        |
|                         | AdaDelta        | 0.02           | 99.6        | 1.00        | 99.6        | 99.5        | 0.45          | 91.5        | 0.92        | 91.7        | 91.3        | 324        |
|                         | SGD             | 0.65           | 78.8        | 0.78        | 85.7        | 71.2        | 0.75          | 74.4        | 0.73        | 80.2        | 66.8        | 249        |
|                         | AdaMax          | 0.11           | 96.7        | 0.97        | 97.3        | 96.2        | 0.45          | 88.2        | 0.88        | 89.9        | 86.6        | 289        |
|                         | AdaGrad         | 0.19           | 94.2        | 0.94        | 95.3        | 93.2        | 0.38          | 88.6        | 0.88        | 89.5        | 85.7        | 277        |
| <b>He Uniform</b>       | Adam            | 0.17           | 95.0        | 0.95        | 95.9        | 94.1        | 0.44          | 89.5        | 0.90        | 91.3        | 88.2        | 310        |
|                         | <b>AdaDelta</b> | <b>0.02</b>    | <b>99.5</b> | <b>1.00</b> | <b>99.5</b> | <b>99.5</b> | <b>0.42</b>   | <b>92.7</b> | <b>0.93</b> | <b>92.9</b> | <b>92.7</b> | <b>343</b> |
|                         | SGD             | 0.76           | 79.0        | 0.78        | 86.1        | 70.7        | 0.89          | 75.1        | 0.75        | 82.8        | 68.4        | 270        |
|                         | AdaMax          | 0.10           | 96.9        | 0.97        | 97.3        | 96.6        | 0.43          | 91.8        | 0.92        | 92.7        | 91.3        | 306        |
|                         | AdaGrad         | 0.19           | 94.1        | 0.94        | 95.2        | 93.2        | 0.40          | 88.9        | 0.88        | 89.8        | 86.9        | 293        |
| Glorot (Xavier) Normal  | Adam            | 0.19           | 94.0        | 0.94        | 95.1        | 92.9        | 0.43          | 87.1        | 0.87        | 89.2        | 85.7        | 332        |
|                         | AdaDelta        | 0.03           | 99.4        | 0.99        | 99.4        | 99.3        | 0.45          | 90.4        | 0.91        | 91.4        | 90.0        | 360        |
|                         | SGD             | 0.58           | 81.1        | 0.80        | 86.7        | 74.8        | 0.70          | 75.7        | 0.76        | 81.0        | 71.5        | 292        |
|                         | AdaMax          | 0.14           | 95.7        | 0.96        | 96.3        | 95.2        | 0.34          | 90.2        | 0.91        | 92.4        | 88.9        | 329        |
|                         | AdaGrad         | 0.22           | 93.1        | 0.93        | 94.5        | 91.7        | 0.48          | 84.6        | 0.85        | 87.5        | 82.4        | 314        |
| Glorot (Xavier) Uniform | Adam            | 0.30           | 89.8        | 0.90        | 92.0        | 87.8        | 0.50          | 83.1        | 0.83        | 85.9        | 80.0        | 354        |
|                         | AdaDelta        | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.40          | 92.2        | 0.92        | 92.4        | 92.0        | 381        |
|                         | SGD             | 0.58           | 82.6        | 0.82        | 88.9        | 75.8        | 0.68          | 79.1        | 0.77        | 83.6        | 71.3        | 308        |
|                         | AdaMax          | 0.12           | 96.1        | 0.96        | 96.6        | 95.4        | 0.36          | 91.3        | 0.92        | 93.8        | 90.4        | 351        |
|                         | AdaGrad         | 0.17           | 95.0        | 0.95        | 96.1        | 94.1        | 0.38          | 89.5        | 0.90        | 91.0        | 88.4        | 331        |
| LeCun Normal            | Adam            | 0.25           | 92.0        | 0.92        | 93.5        | 90.6        | 0.45          | 85.1        | 0.85        | 86.8        | 82.9        | 369        |
|                         | AdaDelta        | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.44          | 92.4        | 0.92        | 92.8        | 92.0        | 396        |
|                         | SGD             | 0.61           | 80.2        | 0.79        | 86.2        | 73.3        | 0.72          | 76.4        | 0.77        | 83.8        | 71.7        | 323        |
|                         | AdaMax          | 0.10           | 96.9        | 0.97        | 97.2        | 96.6        | 0.33          | 92.0        | 0.92        | 92.6        | 90.6        | 367        |
|                         | AdaGrad         | 0.24           | 92.6        | 0.93        | 94.4        | 91.1        | 0.43          | 86.0        | 0.87        | 88.5        | 84.9        | 349        |
| LeCun Uniform           | Adam            | 0.30           | 90.1        | 0.90        | 92.0        | 88.4        | 0.46          | 84.2        | 0.85        | 87.3        | 82.2        | 387        |
|                         | AdaDelta        | 0.02           | 99.8        | 1.00        | 99.8        | 99.8        | 0.47          | 92.4        | 0.93        | 93.2        | 92.2        | 415        |
|                         | SGD             | 0.47           | 85.3        | 0.85        | 89.2        | 80.9        | 0.61          | 81.5        | 0.81        | 86.1        | 76.6        | 348        |
|                         | AdaMax          | 0.13           | 96.2        | 0.96        | 96.6        | 95.6        | 0.38          | 89.5        | 0.90        | 90.6        | 89.1        | 390        |
|                         | AdaGrad         | 0.32           | 90.1        | 0.90        | 92.5        | 87.4        | 0.47          | 86.6        | 0.86        | 89.1        | 83.5        | 369        |

experiment training and testing accuracies curves with their trendlines. Figure 47 shows the training time curve with its trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

Table 29 shows that the AdaMax optimizer and LeCun Uniform weight initializer report the highest testing accuracy which is 96.8% using HMB2 in phase two from the cross-validation testing. The average training time is 402 s. The average training and testing accuracies are 99.7%, and 96.1%, respectively. The average training and testing losses are 0.08, and 0.24, respectively. Figure 48 shows the experiment training and testing accuracies curves with their trendlines. Figure 49 shows the training time curve with its

trendline. The  $x$ -axis refers to the corresponding experiment rows, and the  $y$ -axis refers to the accuracy as a percentage (in the accuracies figure) and refers to the time in seconds (in the time figure).

### 5.3.4 Comments on the second phase

From the obtained results, the study described architectures generalize for the control dataset and have higher accuracies, than the reported accuracy in the selected control study for the different comparing tests.

Table 30 summarizes the obtained results in the two phases.

**Table 24** Training and testing reported results of Experiment 14

| Weight initializer      | Optimizer      | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time       |
|-------------------------|----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|------------|
|                         |                | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |            |
| He Normal               | Adam           | 0.15           | 99.0        | 0.99        | 99.0        | 99.0        | 0.61          | 92.0        | 0.92        | 92.0        | 92.0        | 161        |
|                         | AdaDelta       | 0.08           | 99.6        | 1.00        | 99.6        | 99.6        | 0.47          | 92.9        | 0.93        | 93.1        | 92.9        | 152        |
|                         | SGD            | 0.06           | 99.5        | 1.00        | 99.5        | 99.5        | 0.41          | 91.8        | 0.92        | 92.3        | 91.3        | 171        |
|                         | AdaMax         | 0.08           | 99.5        | 1.00        | 99.5        | 99.5        | 0.48          | 92.7        | 0.93        | 92.8        | 92.4        | 182        |
|                         | AdaGrad        | 0.06           | 99.7        | 1.00        | 99.7        | 99.6        | 0.41          | 92.0        | 0.92        | 92.8        | 92.0        | 150        |
| <b>He Uniform</b>       | Adam           | 0.14           | 99.2        | 0.99        | 99.2        | 99.1        | 0.60          | 92.2        | 0.92        | 92.4        | 91.8        | 164        |
|                         | AdaDelta       | 0.08           | 99.7        | 1.00        | 99.7        | 99.7        | 0.58          | 92.0        | 0.92        | 92.4        | 92.0        | 159        |
|                         | SGD            | 0.05           | 99.7        | 1.00        | 99.7        | 99.6        | 0.40          | 91.3        | 0.91        | 91.3        | 90.9        | 177        |
|                         | AdaMax         | 0.07           | 99.7        | 1.00        | 99.7        | 99.6        | 0.47          | 91.5        | 0.92        | 91.7        | 91.3        | 188        |
|                         | <b>AdaGrad</b> | <b>0.06</b>    | <b>99.7</b> | <b>1.00</b> | <b>99.7</b> | <b>99.7</b> | <b>0.38</b>   | <b>93.3</b> | <b>0.93</b> | <b>93.5</b> | <b>93.1</b> | <b>157</b> |
| Glorot (Xavier) Normal  | Adam           | 0.15           | 99.3        | 0.99        | 99.3        | 99.2        | 0.59          | 93.3        | 0.94        | 93.7        | 93.3        | 175        |
|                         | AdaDelta       | 0.08           | 99.6        | 1.00        | 99.7        | 99.6        | 0.44          | 92.0        | 0.92        | 92.2        | 92.0        | 166        |
|                         | SGD            | 0.06           | 99.6        | 1.00        | 99.7        | 99.6        | 0.37          | 92.4        | 0.92        | 92.5        | 92.0        | 188        |
|                         | AdaMax         | 0.07           | 99.7        | 1.00        | 99.7        | 99.7        | 0.46          | 92.0        | 0.92        | 92.4        | 92.0        | 198        |
|                         | AdaGrad        | 0.06           | 99.7        | 1.00        | 99.7        | 99.7        | 0.41          | 91.8        | 0.92        | 92.0        | 91.8        | 167        |
| Glorot (Xavier) Uniform | Adam           | 0.16           | 98.7        | 0.99        | 98.7        | 98.6        | 0.62          | 90.6        | 0.91        | 90.8        | 90.6        | 183        |
|                         | AdaDelta       | 0.07           | 99.6        | 1.00        | 99.6        | 99.6        | 0.59          | 91.5        | 0.92        | 91.9        | 91.5        | 175        |
|                         | SGD            | 0.06           | 99.5        | 1.00        | 99.5        | 99.5        | 0.41          | 91.3        | 0.91        | 91.9        | 90.6        | 196        |
|                         | AdaMax         | 0.17           | 96.2        | 0.96        | 96.8        | 95.7        | 0.38          | 91.3        | 0.91        | 92.0        | 90.6        | 208        |
|                         | AdaGrad        | 0.07           | 99.6        | 1.00        | 99.6        | 99.5        | 0.38          | 91.1        | 0.91        | 91.1        | 91.1        | 177        |
| LeCun Normal            | Adam           | 0.13           | 99.0        | 0.99        | 99.0        | 98.9        | 0.58          | 91.3        | 0.92        | 92.3        | 91.1        | 193        |
|                         | AdaDelta       | 0.07           | 99.6        | 1.00        | 99.6        | 99.6        | 0.51          | 91.3        | 0.91        | 91.3        | 91.3        | 187        |
|                         | SGD            | 0.06           | 99.4        | 0.99        | 99.4        | 99.3        | 0.36          | 91.3        | 0.92        | 91.9        | 91.1        | 207        |
|                         | AdaMax         | 0.07           | 99.6        | 1.00        | 99.6        | 99.5        | 0.46          | 91.3        | 0.92        | 92.1        | 91.1        | 219        |
|                         | AdaGrad        | 0.06           | 99.6        | 1.00        | 99.7        | 99.6        | 0.38          | 92.9        | 0.93        | 93.1        | 92.9        | 186        |
| LeCun Uniform           | Adam           | 0.15           | 99.5        | 1.00        | 99.5        | 99.5        | 0.62          | 91.8        | 0.92        | 92.2        | 91.8        | 205        |
|                         | AdaDelta       | 0.07           | 99.7        | 1.00        | 99.7        | 99.7        | 0.49          | 92.7        | 0.93        | 93.6        | 92.2        | 195        |
|                         | SGD            | 0.06           | 99.6        | 1.00        | 99.6        | 99.5        | 0.38          | 91.5        | 0.92        | 92.1        | 91.1        | 161        |
|                         | AdaMax         | 0.07           | 99.6        | 1.00        | 99.7        | 99.6        | 0.41          | 92.0        | 0.92        | 92.3        | 92.0        | 152        |
|                         | AdaGrad        | 0.06           | 99.7        | 1.00        | 99.7        | 99.7        | 0.39          | 91.3        | 0.91        | 91.7        | 90.6        | 171        |

## 6 Conclusions

The current research presented a valid system for Arabic handwritten character recognition with the ability to select between two CNN architectures, with a large, and complex dataset for the AHCR problem. The reason for presenting two CNN architectures was to study the effects of changing the architecture complexity. As discussed in Sect. 4.1, HMB1 was more complex (more trainable parameters) than HMB2. However, HMB2 used regularization to study

the effect of reducing the complexity with the application of the overfitting reduction technique (regularization). Table 31 summarizes the different 16 experiments with the highest testing accuracies with the corresponding best weights initializers and optimizers.

From the obtained results, we can conclude that data augmentation helped to improve the testing accuracy and decrease the overfitting. Data augmentation increased the number of inputs data and hence the architectures learned and trained on more data. HMB1 reported higher

**Table 25** Training and testing reported results of Experiment 15

| Weight initializer      | Optimizer     | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|---------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |               | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| He Normal               | Adam          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.05          | 98.7        | 0.99        | 98.7        | 98.7        | 3152        |
|                         | AdaDelta      | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.7        | 0.99        | 98.7        | 98.7        | 2956        |
|                         | SGD           | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.2        | 0.98        | 98.2        | 98.1        | 3270        |
|                         | AdaMax        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.6        | 0.99        | 98.6        | 98.6        | 3315        |
|                         | AdaGrad       | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.11          | 98.0        | 0.98        | 98.1        | 98.0        | 2582        |
| <b>He Uniform</b>       | Adam          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.8        | 0.99        | 98.9        | 98.8        | 2924        |
|                         | AdaDelta      | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.9        | 0.99        | 99.0        | 98.9        | 2656        |
|                         | SGD           | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.2        | 0.98        | 98.3        | 98.2        | 2938        |
|                         | <b>AdaMax</b> | <b>0.00</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.06</b>   | <b>99.0</b> | <b>0.99</b> | <b>99.0</b> | <b>99.0</b> | <b>3240</b> |
|                         | AdaGrad       | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.10          | 98.4        | 0.98        | 98.4        | 98.3        | 2565        |
| Glorot (Xavier) Normal  | Adam          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.6        | 0.99        | 98.6        | 98.6        | 2946        |
|                         | AdaDelta      | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.9        | 0.99        | 98.9        | 98.9        | 3178        |
|                         | SGD           | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.4        | 0.98        | 98.4        | 98.4        | 3630        |
|                         | AdaMax        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.8        | 0.99        | 98.9        | 98.8        | 3881        |
|                         | AdaGrad       | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.4        | 0.98        | 98.4        | 98.4        | 3027        |
| Glorot (Xavier) Uniform | Adam          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.6        | 0.99        | 98.6        | 98.6        | 3424        |
|                         | AdaDelta      | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.8        | 0.99        | 98.8        | 98.7        | 3293        |
|                         | SGD           | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.3        | 0.98        | 98.4        | 98.3        | 3690        |
|                         | AdaMax        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.8        | 0.99        | 98.8        | 98.8        | 3122        |
|                         | AdaGrad       | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.4        | 0.98        | 98.4        | 98.4        | 2395        |
| LeCun Normal            | Adam          | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.7        | 0.99        | 98.7        | 98.6        | 2829        |
|                         | AdaDelta      | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.8        | 0.99        | 98.9        | 98.8        | 2725        |
|                         | SGD           | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.09          | 98.2        | 0.98        | 98.2        | 98.2        | 3074        |
|                         | AdaMax        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.8        | 0.99        | 98.8        | 98.7        | 3842        |
|                         | AdaGrad       | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.4        | 0.98        | 98.5        | 98.4        | 2942        |
| LeCun Uniform           | Adam          | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.06          | 98.7        | 0.99        | 98.8        | 98.7        | 3334        |
|                         | AdaDelta      | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.07          | 98.9        | 0.99        | 98.9        | 98.9        | 3160        |
|                         | SGD           | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.4        | 0.98        | 98.4        | 98.4        | 3152        |
|                         | AdaMax        | 0.00           | 99.9        | 1.00        | 99.9        | 99.9        | 0.06          | 98.7        | 0.99        | 98.7        | 98.6        | 2956        |
|                         | AdaGrad       | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.08          | 98.4        | 0.98        | 98.4        | 98.4        | 3270        |

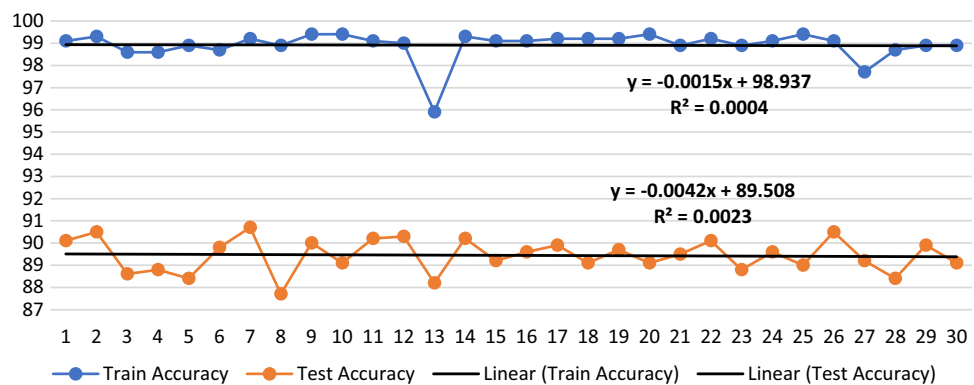
accuracies (but not very high) than HMB2 as the first one's architecture is more complex and has more parameters than the later one but requires more time to train. Regularization helped to decrease the overfitting in HMB2 although the architecture is less complex. By increasing the dataset width and height, lead to more parameters and less accuracy and this concludes that, the more the parameters, the more the required data. He Uniform reported the best accuracies in 6 experiments and hence can be considered as a suitable weight initializer to use. AdaDelta optimizer

reported the best accuracies in 5 experiments and hence can be considered as a suitable optimizer to use. The average time in each experiment (from 1 to 16) is calculated and plotted in Fig. 50. Experiment 7 had the longest time between the different experiments because it worked on 865,840 elements using the HMBD dataset and HMB1 architecture.

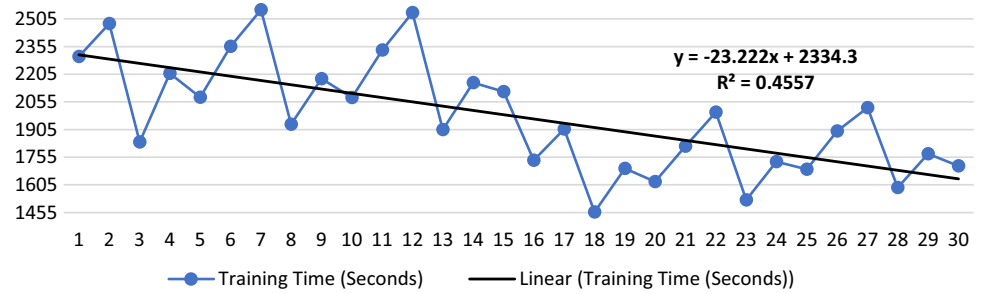
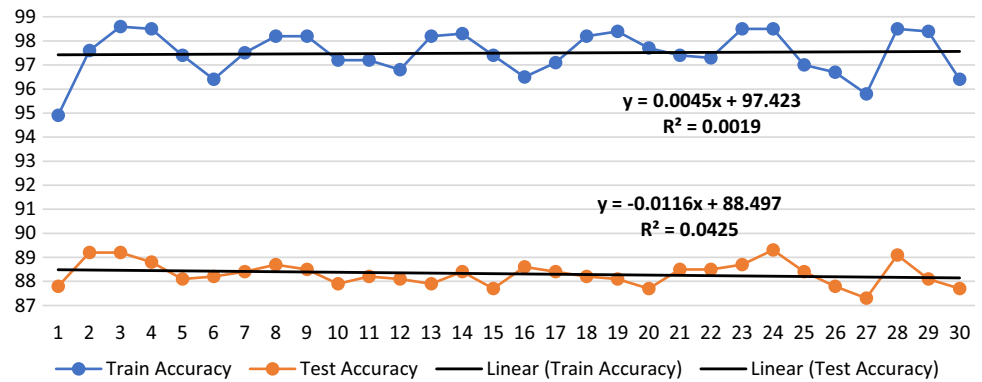
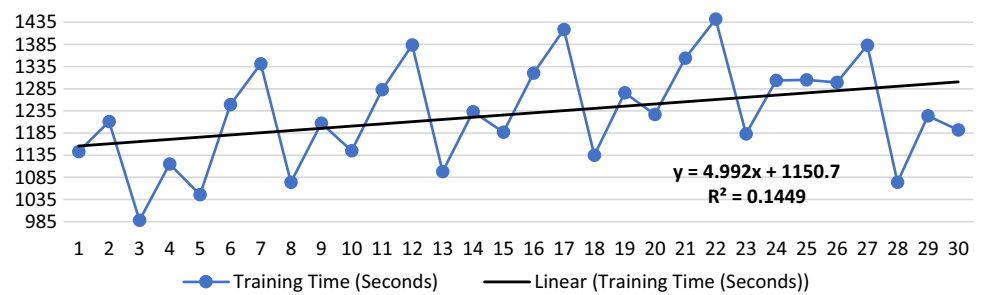
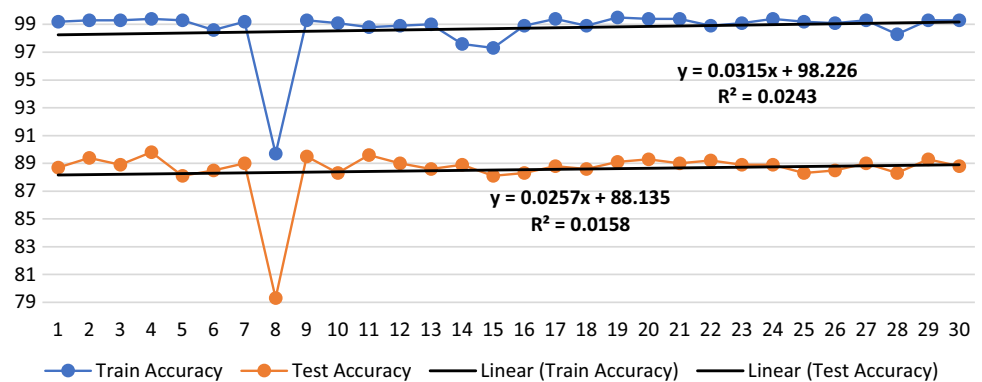
The two described architectures achieved more than 99.2% and 100% using CMATER dataset with and without data augmentation, respectively. HMB1 and HMB2

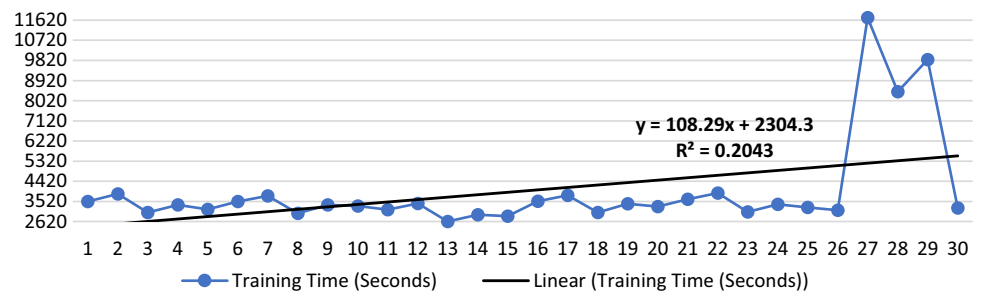
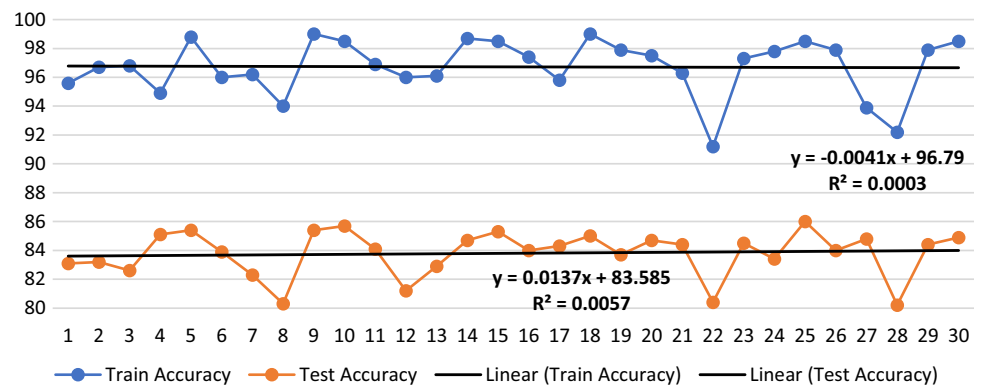
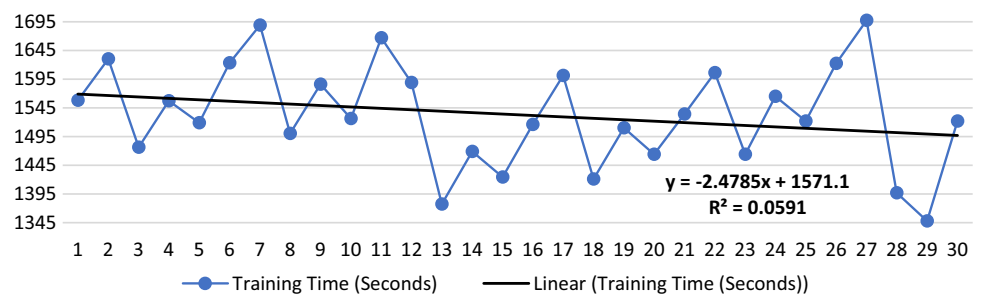
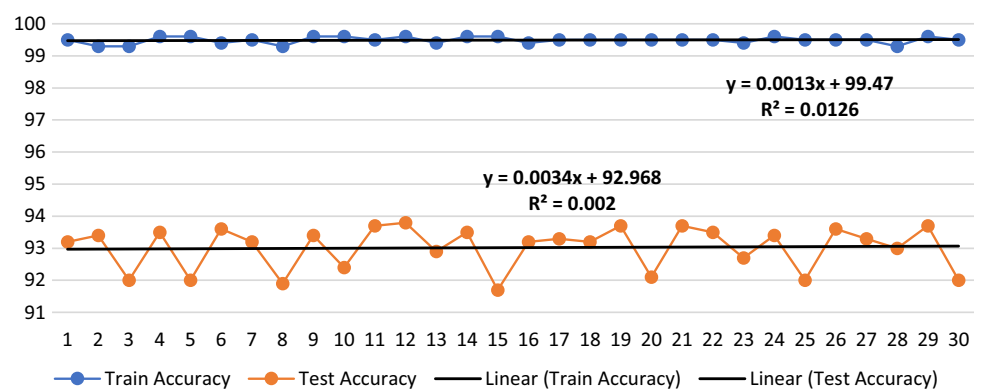
**Table 26** Training and testing reported results of Experiment 16

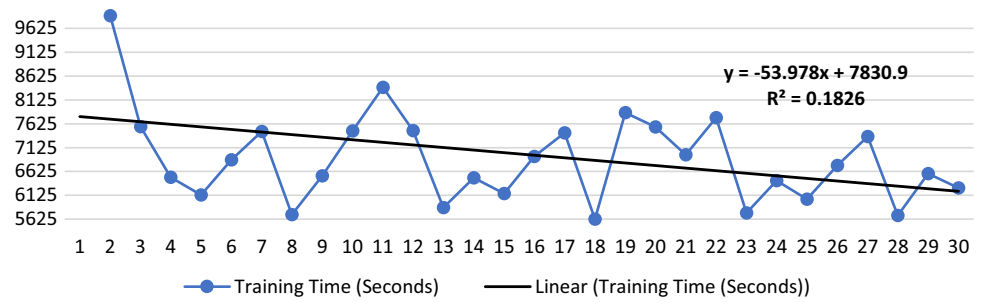
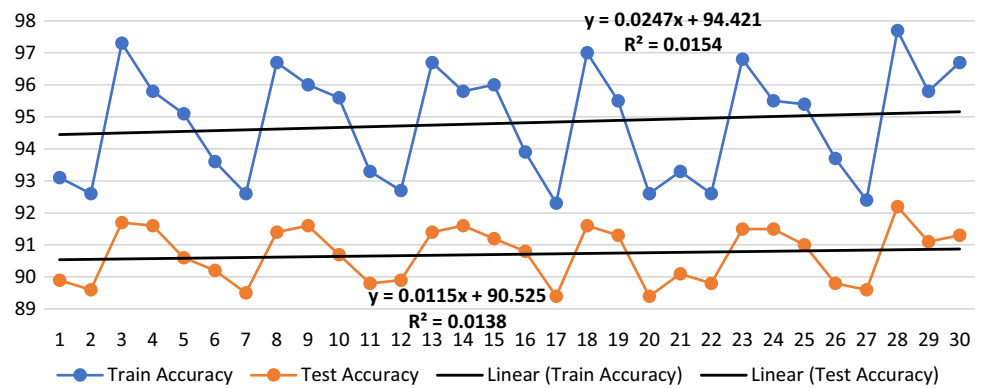
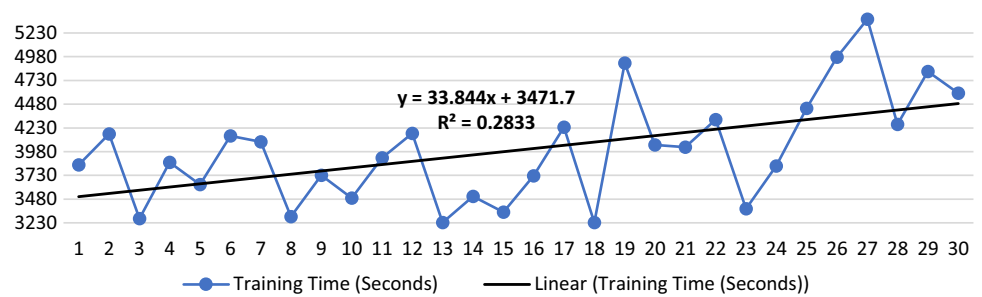
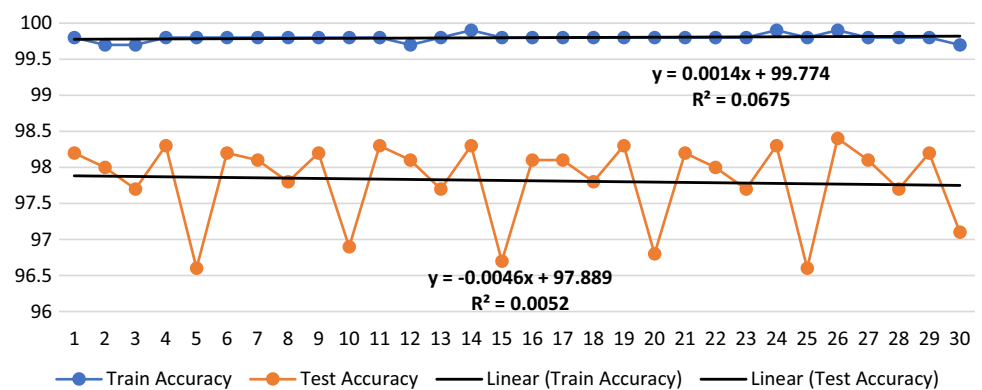
| Weight initializer      | Optimizer  | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time        |
|-------------------------|------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|-------------|
|                         |            | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |             |
| <b>He Normal</b>        | Adam       | 0.13           | 98.6        | 0.99        | 98.7        | 98.5        | 0.17          | 97.3        | 0.97        | 97.6        | 97.2        | 1972        |
|                         | AdaDelta   | 0.11           | 99.2        | 0.99        | 99.2        | 99.1        | 0.15          | 97.9        | 0.98        | 98.1        | 97.7        | 1897        |
|                         | <b>SGD</b> | <b>0.04</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.10</b>   | <b>98.4</b> | <b>0.98</b> | <b>98.5</b> | <b>98.4</b> | <b>2105</b> |
|                         | AdaMax     | 0.07           | 99.6        | 1.00        | 99.7        | 99.6        | 0.13          | 98.2        | 0.98        | 98.3        | 98.0        | 2274        |
|                         | AdaGrad    | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.10          | 98.0        | 0.98        | 98.1        | 98.0        | 1796        |
| He Uniform              | Adam       | 0.13           | 98.6        | 0.99        | 98.7        | 98.6        | 0.17          | 97.3        | 0.97        | 97.5        | 97.1        | 1585        |
|                         | AdaDelta   | 0.13           | 98.7        | 0.99        | 98.7        | 98.6        | 0.18          | 97.3        | 0.97        | 97.5        | 97.2        | 1510        |
|                         | SGD        | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.09          | 98.3        | 0.98        | 98.4        | 98.2        | 1717        |
|                         | AdaMax     | 0.08           | 99.6        | 1.00        | 99.6        | 99.6        | 0.13          | 98.0        | 0.98        | 98.0        | 98.0        | 1846        |
|                         | AdaGrad    | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.2        | 0.98        | 98.3        | 98.0        | 1454        |
| Glorot (Xavier) Normal  | Adam       | 0.13           | 98.5        | 0.99        | 98.5        | 98.4        | 0.18          | 97.3        | 0.97        | 97.5        | 97.2        | 1626        |
|                         | AdaDelta   | 0.12           | 98.9        | 0.99        | 99.0        | 98.8        | 0.17          | 97.2        | 0.97        | 97.5        | 97.0        | 1554        |
|                         | SGD        | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.2        | 0.98        | 98.3        | 98.1        | 1696        |
|                         | AdaMax     | 0.08           | 99.5        | 1.00        | 99.5        | 99.5        | 0.12          | 98.2        | 0.98        | 98.3        | 98.2        | 1801        |
|                         | AdaGrad    | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.10          | 98.1        | 0.98        | 98.1        | 98.0        | 1435        |
| Glorot (Xavier) Uniform | Adam       | 0.13           | 98.7        | 0.99        | 98.8        | 98.6        | 0.18          | 97.1        | 0.97        | 97.3        | 97.0        | 1584        |
|                         | AdaDelta   | 0.11           | 99.2        | 0.99        | 99.2        | 99.1        | 0.16          | 97.7        | 0.98        | 97.9        | 97.6        | 1528        |
|                         | SGD        | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.10          | 98.1        | 0.98        | 98.1        | 98.0        | 1688        |
|                         | AdaMax     | 0.08           | 99.4        | 0.99        | 99.4        | 99.4        | 0.13          | 97.7        | 0.98        | 97.7        | 97.7        | 1811        |
|                         | AdaGrad    | 0.04           | 99.9        | 1.00        | 99.9        | 99.9        | 0.10          | 97.9        | 0.98        | 98.0        | 97.9        | 1474        |
| LeCun Normal            | Adam       | 0.13           | 98.5        | 0.99        | 98.6        | 98.5        | 0.18          | 97.0        | 0.97        | 97.1        | 96.9        | 1674        |
|                         | AdaDelta   | 0.11           | 99.1        | 0.99        | 99.2        | 99.1        | 0.16          | 97.7        | 0.98        | 97.9        | 97.7        | 1595        |
|                         | SGD        | 0.04           | 99.8        | 1.00        | 99.9        | 99.8        | 0.11          | 98.0        | 0.98        | 98.0        | 97.9        | 1780        |
|                         | AdaMax     | 0.07           | 99.7        | 1.00        | 99.7        | 99.6        | 0.13          | 98.1        | 0.98        | 98.2        | 98.1        | 1921        |
|                         | AdaGrad    | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.11          | 97.5        | 0.98        | 97.6        | 97.5        | 1737        |
| LeCun Uniform           | Adam       | 0.13           | 98.5        | 0.99        | 98.6        | 98.4        | 0.17          | 97.4        | 0.98        | 97.6        | 97.3        | 1939        |
|                         | AdaDelta   | 0.12           | 99.0        | 0.99        | 99.0        | 98.9        | 0.17          | 97.6        | 0.98        | 97.7        | 97.5        | 1940        |
|                         | SGD        | 0.04           | 99.7        | 1.00        | 99.8        | 99.7        | 0.11          | 98.0        | 0.98        | 98.2        | 97.9        | 1972        |
|                         | AdaMax     | 0.07           | 99.6        | 1.00        | 99.6        | 99.6        | 0.13          | 98.0        | 0.98        | 98.1        | 98.0        | 1897        |
|                         | AdaGrad    | 0.04           | 99.9        | 1.00        | 99.9        | 99.8        | 0.10          | 98.0        | 0.98        | 98.1        | 98.0        | 2105        |

**Fig. 13** Experiment 1 training and testing accuracies curves with their trendlines

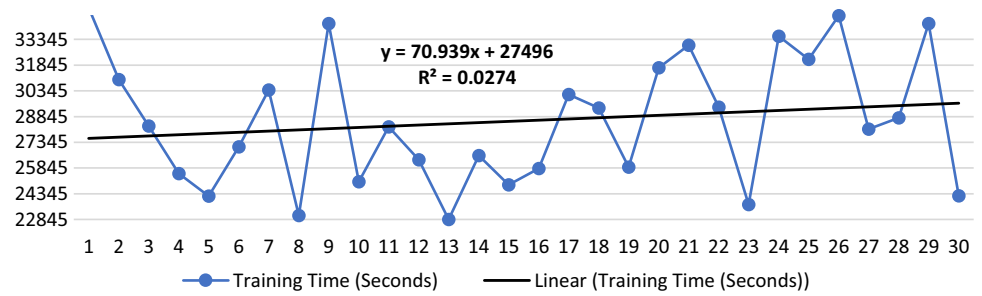


**Fig. 14** Experiment 1 Training Time Curve with its Trendline**Fig. 15** Experiment 2 training and testing accuracies curves with their trendlines**Fig. 16** Experiment 2 training time curve with its trendline**Fig. 17** Experiment 3 training and testing accuracies curves with their trendlines

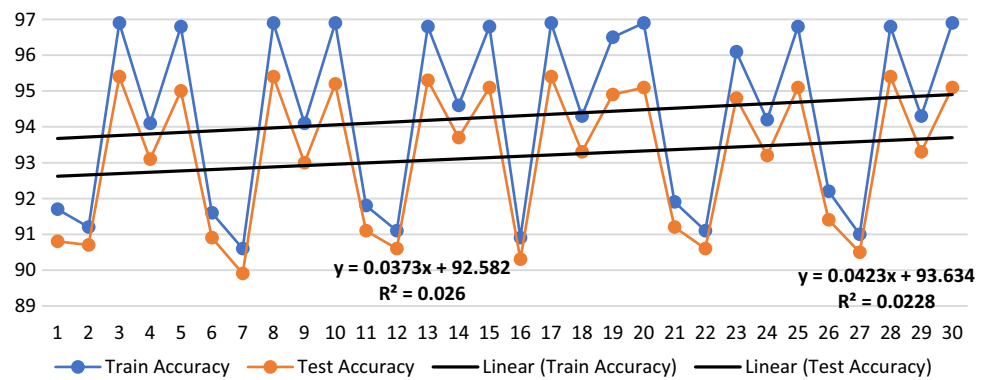
**Fig. 18** Experiment 3 training time curve with its trendline**Fig. 19** Experiment 4 training and testing accuracies curves with their trendlines**Fig. 20** Experiment 4 training time curve with its trendline**Fig. 21** Experiment 5 training and testing accuracies curves with their trendlines

**Fig. 22** Experiment 5 training time curve with its trendline**Fig. 23** Experiment 6 training and testing accuracies curves with their trendlines**Fig. 24** Experiment 6 training time curve with its trendline**Fig. 25** Experiment 7 training and testing accuracies curves with their trendlines

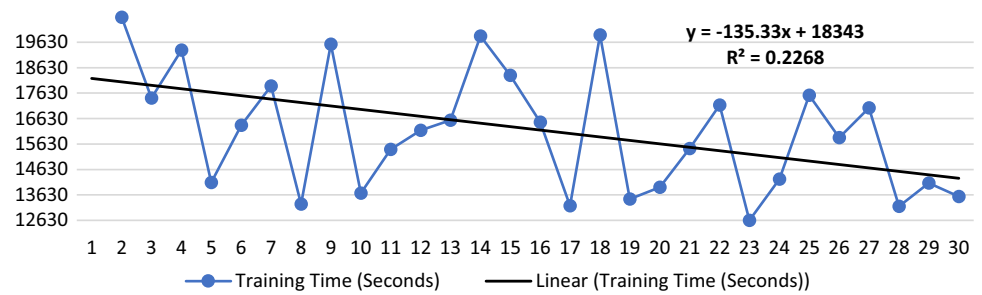
**Fig. 26** Experiment 7 training time curve with its trendline



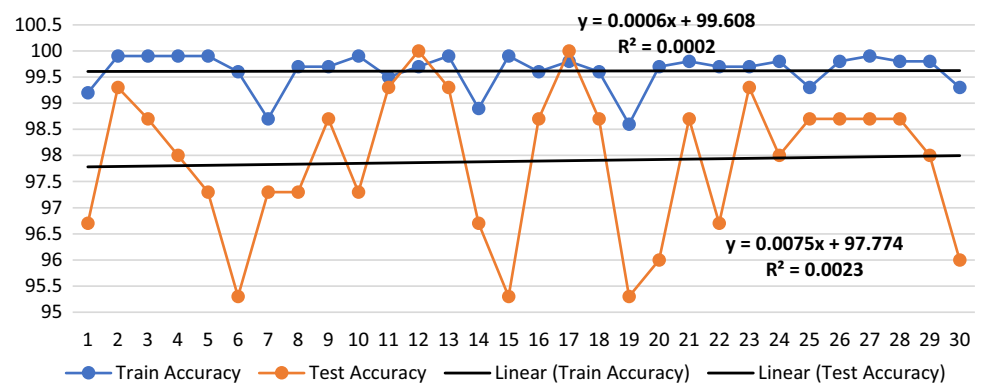
**Fig. 27** Experiment 8 training and testing accuracies curves with their trendlines

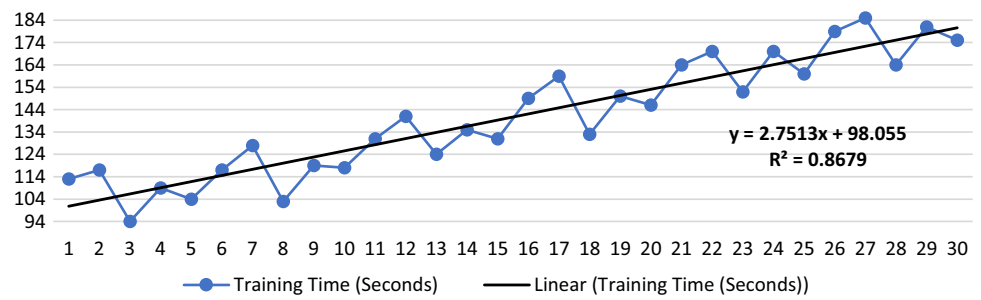
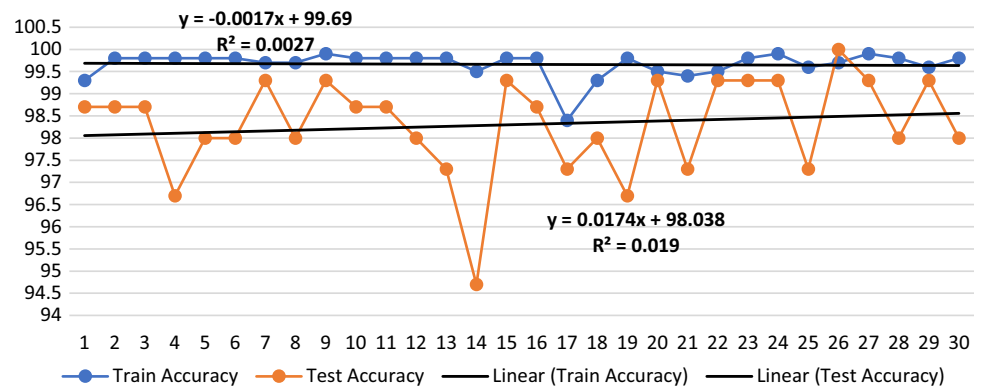
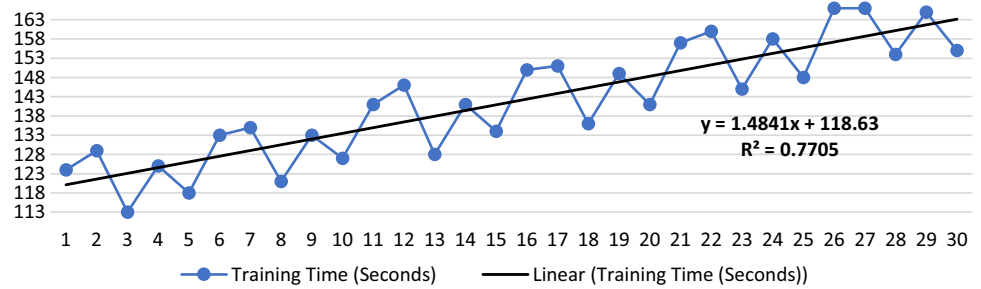
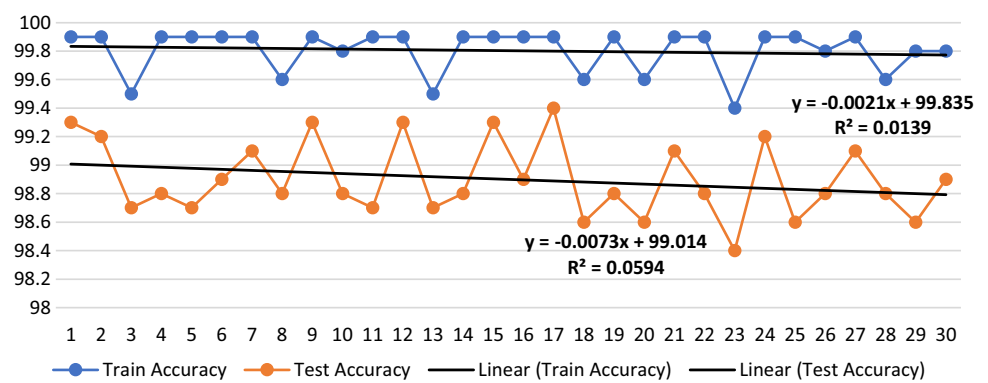


**Fig. 28** Experiment 8 training time curve with its trendline

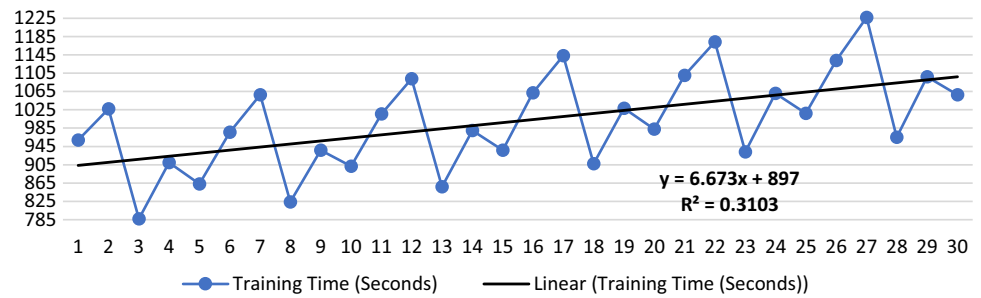
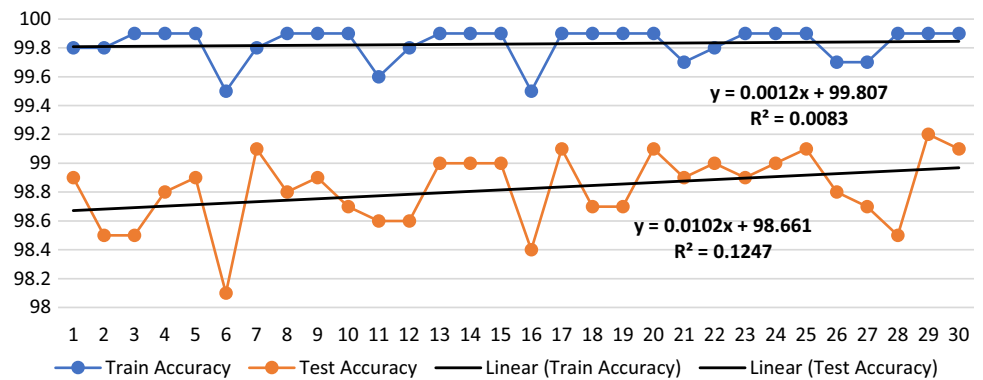
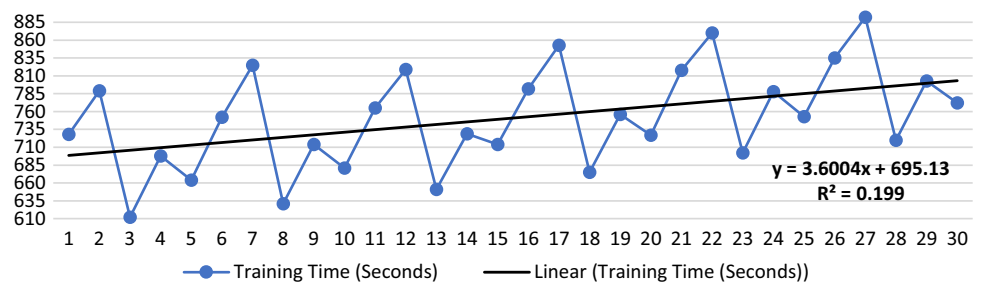


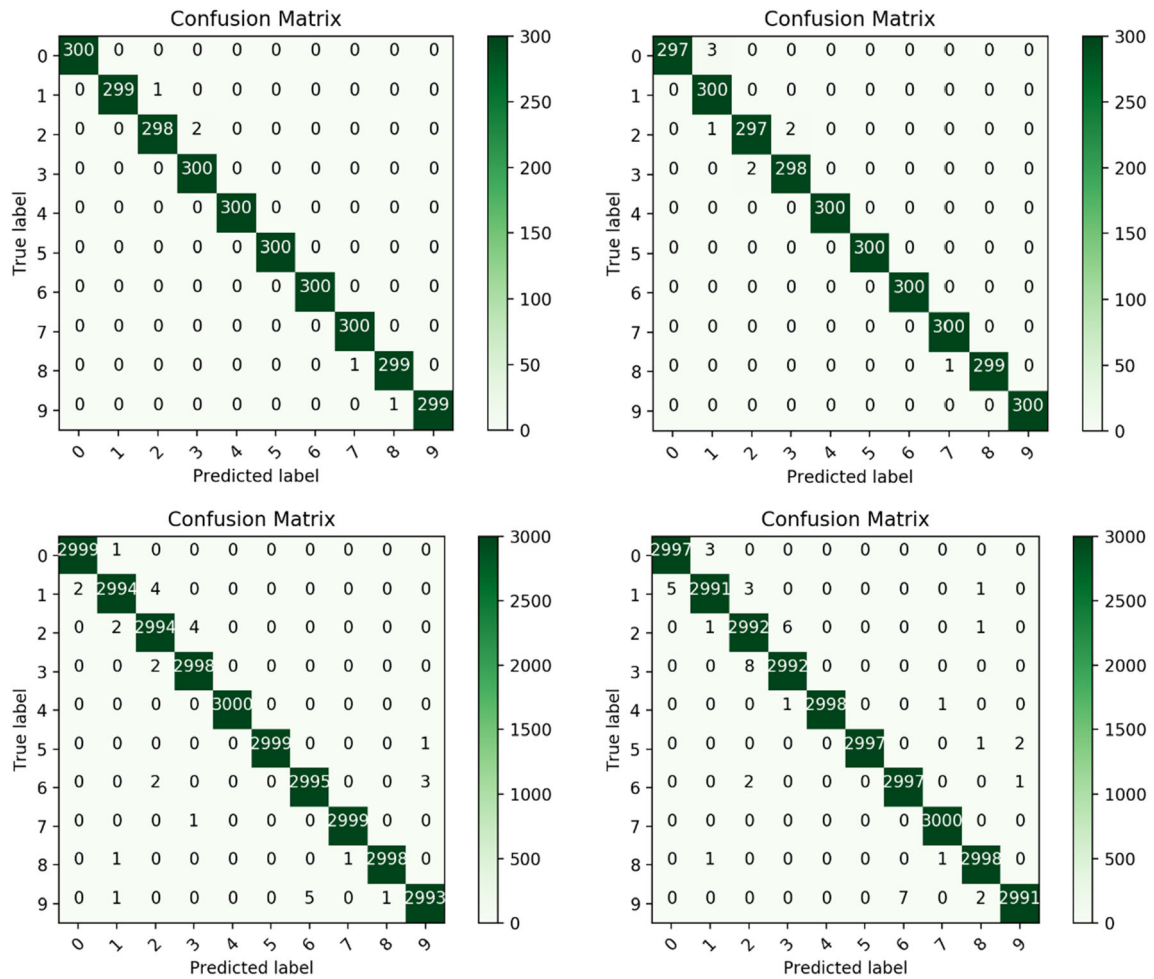
**Fig. 29** Experiment 9 training and testing accuracies curves with their trendlines



**Fig. 30** Experiment 9 training time curve with its trendline**Fig. 31** Experiment 10 training and testing accuracies curves with their trendlines**Fig. 32** Experiment 10 training time curve with its trendline**Fig. 33** Experiment 11 training and testing accuracies curves with their trendlines

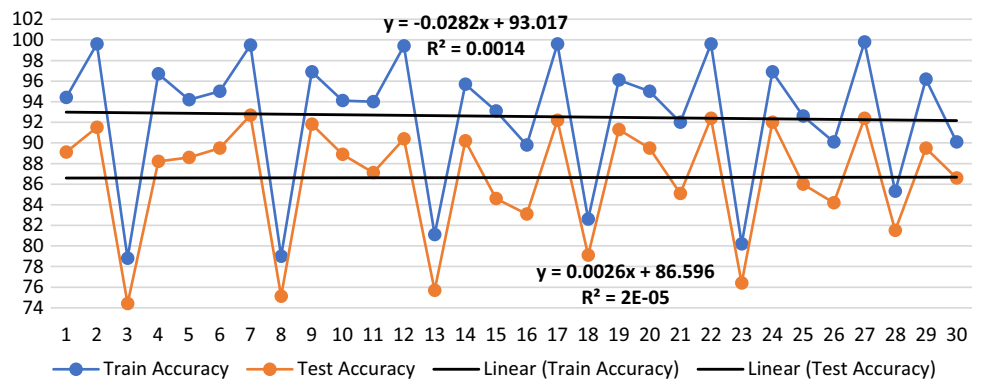


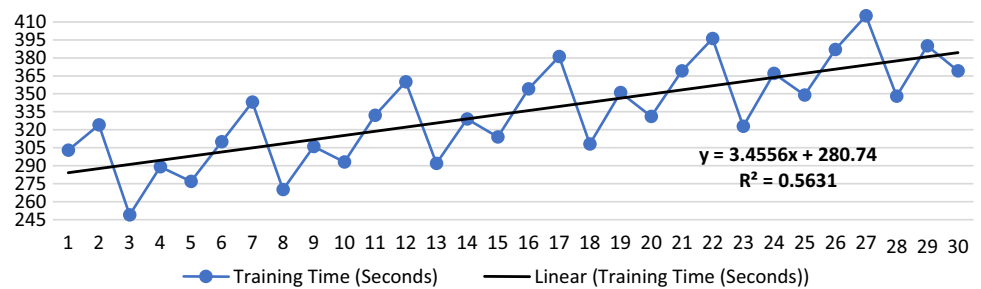
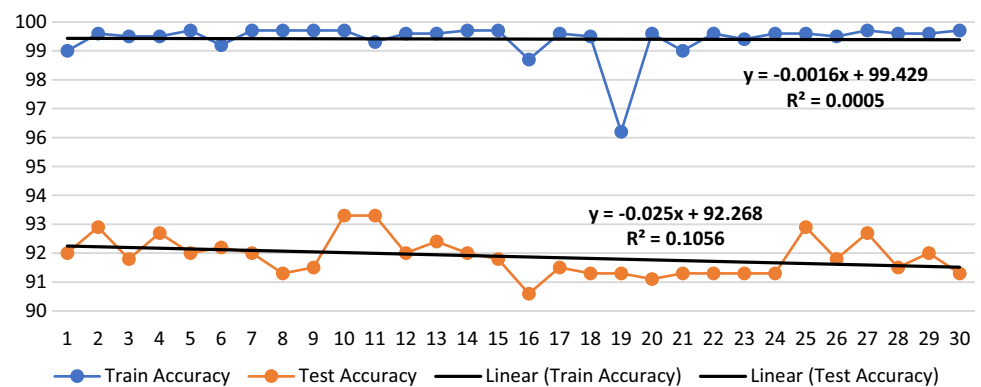
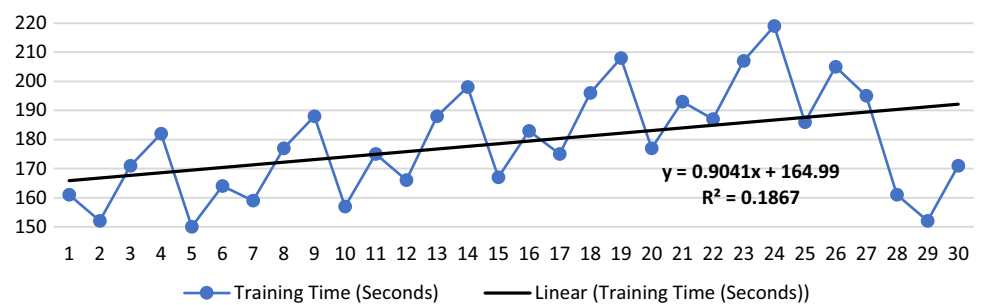
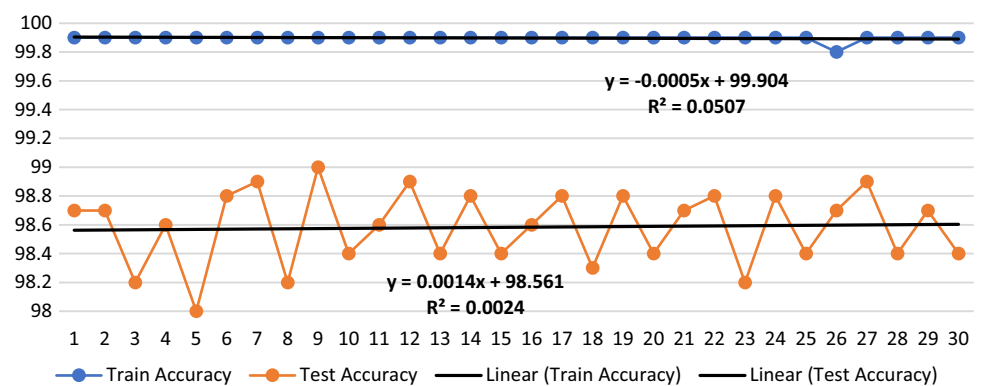
**Fig. 34** Experiment 11 training time curve with its trendline**Fig. 35** Experiment 12 training and testing accuracies curves with their trendlines**Fig. 36** Experiment 12 training time curve with its trendline

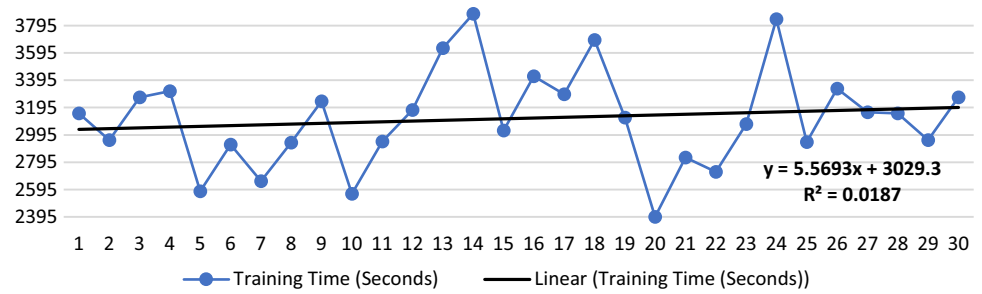
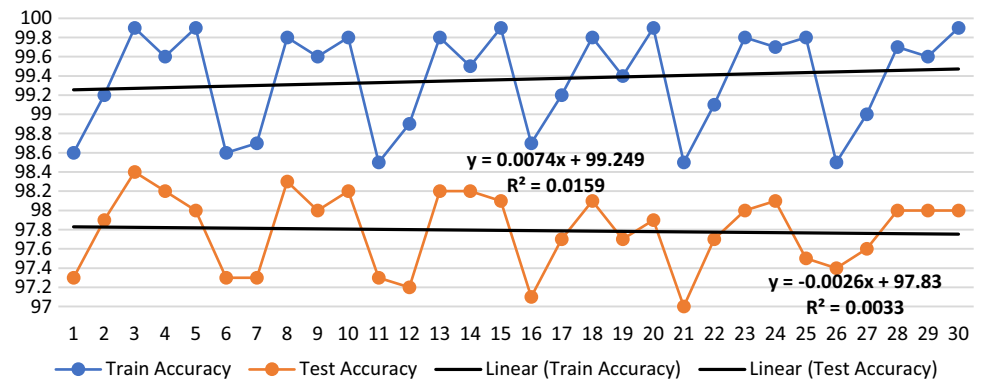
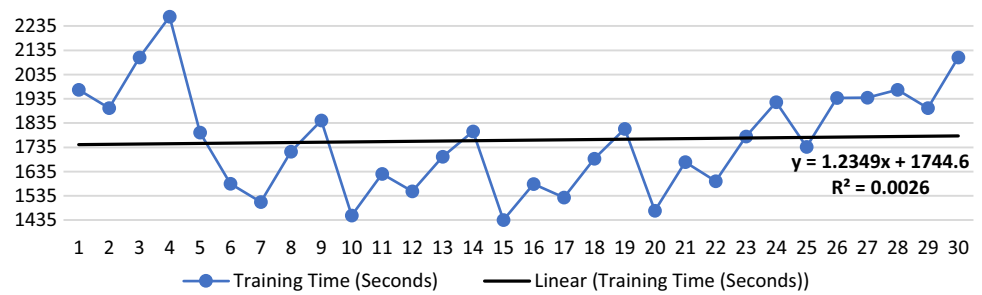


**Fig. 37** Confusion matrices (top left, top right, bottom left, and bottom right) for Experiments 9 to 12, respectively

**Fig. 38** Experiment 13 training and testing accuracies curves with their trendlines



**Fig. 39** Experiment 13 training time curve with its trendline**Fig. 40** Experiment 14 training and testing accuracies curves with their trendlines**Fig. 41** Experiment 14 training time curve with its trendline**Fig. 42** Experiment 15 training and testing accuracies curves with their trendlines

**Fig. 43** Experiment 15 training time curve with its trendline**Fig. 44** Experiment 16 training and testing accuracies curves with their trendlines**Fig. 45** Experiment 16 training time curve with its trendline**Table 27** Results obtained from testing the described architecture in [27] on the presented dataset

| Weight initializer             | Training phase |             |             |             |             | Testing phase |             |             |             |             |
|--------------------------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|
|                                | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |
| He Normal                      | 2.39           | 41.5        | 0.39        | 63.2        | 28.2        | 2.52          | 39.2        | 0.37        | 60.3        | 26.8        |
| He Uniform                     | 2.14           | 47.6        | 0.44        | 63.5        | 34.0        | 2.25          | 44.9        | 0.42        | 60.7        | 32.2        |
| Glorot (Xavier) Normal         | 2.12           | 43.5        | 0.38        | 72.7        | 25.9        | 2.25          | 39.9        | 0.34        | 68.2        | 22.9        |
| <b>Glorot (Xavier) Uniform</b> | <b>1.84</b>    | <b>51.0</b> | <b>0.49</b> | <b>72.5</b> | <b>37.2</b> | <b>2.03</b>   | <b>47.7</b> | <b>0.46</b> | <b>67.8</b> | <b>35.0</b> |
| LeCun Normal                   | 2.93           | 36.8        | 0.35        | 51.4        | 26.5        | 3.03          | 35.5        | 0.33        | 49.5        | 25.0        |
| LeCun Uniform                  | 2.56           | 42.4        | 0.42        | 56.1        | 33.9        | 2.76          | 40.5        | 0.40        | 53.3        | 31.9        |

**Table 28** Phase 2 results using the described HMB1 and their control dataset

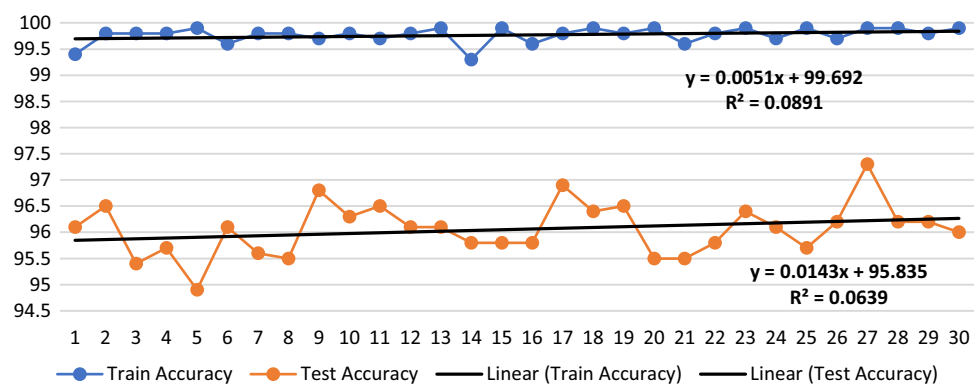
| Weight initializer      | Optimizer       | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time       |
|-------------------------|-----------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|------------|
|                         |                 | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |            |
| He Normal               | Adam            | 0.02           | 99.4        | 0.99        | 99.4        | 99.4        | 0.17          | 96.1        | 0.96        | 96.3        | 96.1        | 671        |
|                         | AdaDelta        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.18          | 96.5        | 0.97        | 96.5        | 96.4        | 640        |
|                         | SGD             | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.21          | 95.4        | 0.95        | 95.8        | 94.9        | 719        |
|                         | AdaMax          | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.18          | 95.7        | 0.96        | 95.8        | 95.6        | 779        |
|                         | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.21          | 94.9        | 0.95        | 94.9        | 94.9        | 630        |
| He Uniform              | Adam            | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.21          | 96.1        | 0.96        | 96.3        | 96.0        | 693        |
|                         | AdaDelta        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.23          | 95.6        | 0.96        | 95.6        | 95.5        | 665        |
|                         | SGD             | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.22          | 95.5        | 0.96        | 95.8        | 95.4        | 744        |
|                         | AdaMax          | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.16          | 96.8        | 0.97        | 96.8        | 96.8        | 786        |
|                         | AdaGrad         | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.16          | 96.3        | 0.97        | 97.0        | 96.1        | 651        |
| Glorot (Xavier) Normal  | Adam            | 0.02           | 99.7        | 1.00        | 99.7        | 99.7        | 0.18          | 96.5        | 0.97        | 96.7        | 96.5        | 722        |
|                         | AdaDelta        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.19          | 96.1        | 0.96        | 96.3        | 96.0        | 695        |
|                         | SGD             | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.18          | 96.1        | 0.96        | 96.2        | 96.0        | 782        |
|                         | AdaMax          | 0.02           | 99.3        | 0.99        | 99.3        | 99.2        | 0.15          | 95.8        | 0.96        | 96.1        | 95.6        | 833        |
|                         | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.21          | 95.8        | 0.96        | 95.8        | 95.8        | 691        |
| Glorot (Xavier) Uniform | Adam            | 0.02           | 99.6        | 1.00        | 99.6        | 99.6        | 0.18          | 95.8        | 0.96        | 96.0        | 95.6        | 761        |
|                         | AdaDelta        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.15          | 96.9        | 0.97        | 97.4        | 96.8        | 731        |
|                         | SGD             | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.15          | 96.4        | 0.97        | 96.9        | 96.4        | 810        |
|                         | AdaMax          | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.18          | 96.5        | 0.97        | 96.5        | 96.4        | 857        |
|                         | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.8        | 0.20          | 95.5        | 0.96        | 95.9        | 95.4        | 713        |
| LeCun Normal            | Adam            | 0.01           | 99.6        | 1.00        | 99.6        | 99.6        | 0.21          | 95.5        | 0.96        | 95.8        | 95.4        | 784        |
|                         | AdaDelta        | 0.01           | 99.8        | 1.00        | 99.8        | 99.8        | 0.21          | 95.8        | 0.96        | 96.1        | 95.8        | 747        |
|                         | SGD             | 0.01           | 99.9        | 1.00        | 99.9        | 99.8        | 0.15          | 96.4        | 0.97        | 96.8        | 96.3        | 826        |
|                         | AdaMax          | 0.01           | 99.7        | 1.00        | 99.7        | 99.6        | 0.17          | 96.1        | 0.96        | 96.2        | 95.7        | 881        |
|                         | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.19          | 95.7        | 0.96        | 96.2        | 95.5        | 736        |
| <b>LeCun Uniform</b>    | Adam            | 0.01           | 99.7        | 1.00        | 99.7        | 99.7        | 0.17          | 96.2        | 0.96        | 96.2        | 96.2        | 821        |
|                         | <b>AdaDelta</b> | <b>0.01</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.16</b>   | <b>97.3</b> | <b>0.97</b> | <b>97.4</b> | <b>97.0</b> | <b>793</b> |
|                         | SGD             | 0.01           | 99.9        | 1.00        | 99.9        | 99.8        | 0.19          | 96.2        | 0.96        | 96.6        | 96.1        | 671        |
|                         | AdaMax          | 0.01           | 99.8        | 1.00        | 99.8        | 99.7        | 0.19          | 96.2        | 0.96        | 96.6        | 96.2        | 640        |
|                         | AdaGrad         | 0.01           | 99.9        | 1.00        | 99.9        | 99.9        | 0.19          | 96.0        | 0.96        | 96.2        | 96.0        | 719        |

achieved also more than 92.7% and 98.4% using the AIA9k dataset with and without data augmentation, respectively. The AIA9k dataset achieved less accuracy than the CMATER dataset because of the nature of the

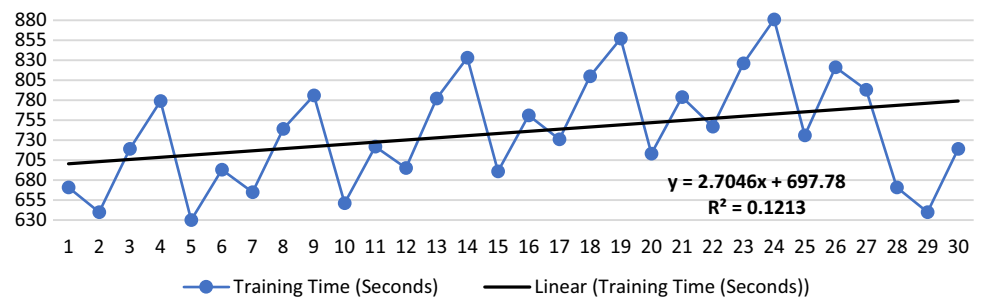
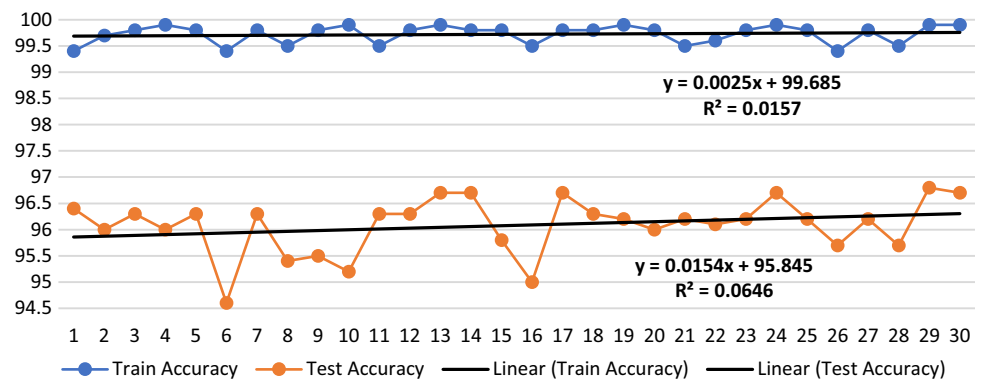
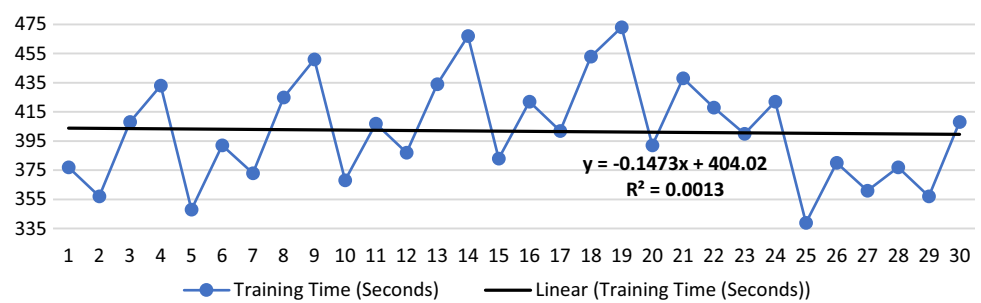
input data. The AIA9k dataset included the characters while CMATER dataset included the digits. This reduction can be increased by applying more data augmentation, more regularization, and more training iterations (epochs).

**Table 29** Phase 2 results using the described HMB2 and their control dataset

| Weight initializer      | Optimizer     | Training phase |             |             |             |             | Testing phase |             |             |             |             | Time       |
|-------------------------|---------------|----------------|-------------|-------------|-------------|-------------|---------------|-------------|-------------|-------------|-------------|------------|
|                         |               | Loss           | Accuracy    | F1          | Precision   | Recall      | Loss          | Accuracy    | F1          | Precision   | Recall      |            |
| He Normal               | Adam          | 0.16           | 99.4        | 0.99        | 99.4        | 99.4        | 0.29          | 96.4        | 0.96        | 96.7        | 96.2        | 377        |
|                         | AdaDelta      | 0.09           | 99.7        | 1.00        | 99.7        | 99.7        | 0.24          | 96.0        | 0.96        | 96.1        | 95.6        | 357        |
|                         | SGD           | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.21          | 96.3        | 0.96        | 96.4        | 96.2        | 408        |
|                         | AdaMax        | 0.06           | 99.9        | 1.00        | 99.9        | 99.9        | 0.23          | 96.0        | 0.96        | 95.9        | 95.8        | 433        |
|                         | AdaGrad       | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.21          | 96.3        | 0.96        | 96.5        | 96.2        | 348        |
| He Uniform              | Adam          | 0.15           | 99.4        | 0.99        | 99.5        | 99.4        | 0.34          | 94.6        | 0.95        | 95.0        | 94.6        | 392        |
|                         | AdaDelta      | 0.08           | 99.8        | 1.00        | 99.8        | 99.8        | 0.26          | 96.3        | 0.96        | 96.7        | 96.2        | 373        |
|                         | SGD           | 0.05           | 99.5        | 1.00        | 99.5        | 99.5        | 0.22          | 95.4        | 0.96        | 95.6        | 95.4        | 425        |
|                         | AdaMax        | 0.06           | 99.8        | 1.00        | 99.8        | 99.8        | 0.24          | 95.5        | 0.96        | 95.7        | 95.4        | 451        |
|                         | AdaGrad       | 0.05           | 99.9        | 1.00        | 99.9        | 99.9        | 0.19          | 95.2        | 0.95        | 95.6        | 95.2        | 368        |
| Glorot (Xavier) Normal  | Adam          | 0.14           | 99.5        | 1.00        | 99.5        | 99.5        | 0.32          | 96.3        | 0.96        | 96.3        | 96.1        | 407        |
|                         | AdaDelta      | 0.08           | 99.8        | 1.00        | 99.8        | 99.8        | 0.24          | 96.3        | 0.96        | 96.8        | 96.0        | 387        |
|                         | SGD           | 0.04           | 99.9        | 1.00        | 99.9        | 99.8        | 0.21          | 96.7        | 0.97        | 96.8        | 96.4        | 434        |
|                         | AdaMax        | 0.07           | 99.8        | 1.00        | 99.8        | 99.8        | 0.19          | 96.7        | 0.97        | 96.8        | 96.5        | 467        |
|                         | AdaGrad       | 0.06           | 99.8        | 1.00        | 99.8        | 99.8        | 0.20          | 95.8        | 0.96        | 96.1        | 95.8        | 383        |
| Glorot (Xavier) Uniform | Adam          | 0.15           | 99.5        | 1.00        | 99.6        | 99.5        | 0.36          | 95.0        | 0.95        | 95.4        | 94.8        | 422        |
|                         | AdaDelta      | 0.08           | 99.8        | 1.00        | 99.8        | 99.8        | 0.23          | 96.7        | 0.97        | 96.7        | 96.5        | 402        |
|                         | SGD           | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.20          | 96.3        | 0.96        | 96.5        | 96.1        | 453        |
|                         | AdaMax        | 0.06           | 99.9        | 1.00        | 99.8        | 99.8        | 0.26          | 96.2        | 0.96        | 96.3        | 96.1        | 473        |
|                         | AdaGrad       | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.22          | 96.0        | 0.96        | 96.1        | 95.8        | 392        |
| LeCun Normal            | Adam          | 0.16           | 99.5        | 1.00        | 99.5        | 99.5        | 0.29          | 96.2        | 0.96        | 96.4        | 95.8        | 438        |
|                         | AdaDelta      | 0.09           | 99.6        | 1.00        | 99.6        | 99.6        | 0.27          | 96.1        | 0.96        | 96.3        | 96.0        | 418        |
|                         | SGD           | 0.04           | 99.8        | 1.00        | 99.8        | 99.8        | 0.18          | 96.2        | 0.96        | 96.5        | 96.1        | 400        |
|                         | AdaMax        | 0.06           | 99.9        | 1.00        | 99.9        | 99.9        | 0.22          | 96.7        | 0.97        | 97.0        | 96.5        | 422        |
|                         | AdaGrad       | 0.05           | 99.8        | 1.00        | 99.8        | 99.8        | 0.19          | 96.2        | 0.96        | 96.6        | 95.8        | 339        |
| <b>LeCun Uniform</b>    | Adam          | 0.16           | 99.4        | 0.99        | 99.4        | 99.3        | 0.33          | 95.7        | 0.96        | 95.9        | 95.6        | 380        |
|                         | AdaDelta      | 0.08           | 99.8        | 1.00        | 99.8        | 99.8        | 0.25          | 96.2        | 0.96        | 96.5        | 96.2        | 361        |
|                         | SGD           | 0.06           | 99.5        | 1.00        | 99.5        | 99.4        | 0.20          | 95.7        | 0.96        | 96.0        | 95.5        | 377        |
|                         | <b>AdaMax</b> | <b>0.06</b>    | <b>99.9</b> | <b>1.00</b> | <b>99.9</b> | <b>99.9</b> | <b>0.22</b>   | <b>96.8</b> | <b>0.97</b> | <b>96.9</b> | <b>96.7</b> | <b>357</b> |
|                         | AdaGrad       | 0.05           | 99.9        | 1.00        | 99.9        | 99.9        | 0.19          | 96.7        | 0.97        | 97.0        | 96.7        | 408        |

**Fig. 46** Phase 2 training and testing accuracies curves with their trendlines using HMB1

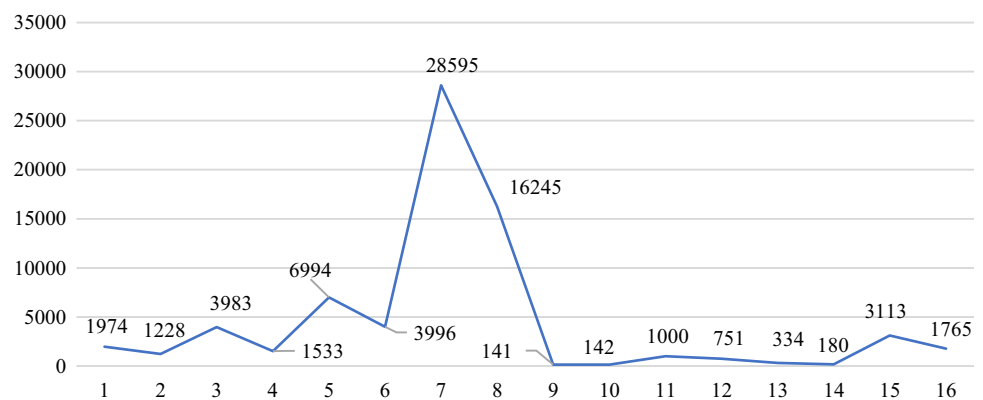


**Fig. 47** Phase 2 training time curve with its trendline using HMB1**Fig. 48** Phase 2 training and testing accuracies curves with their trendlines using HMB2**Fig. 49** Phase 2 training time curve with its trendline using HMB1**Table 30** Summarization of the obtained results in the two phases

| Phase | Architecture    | Dataset    | Size   | Weight initializer      | Optimizer | Testing accuracy (%) |
|-------|-----------------|------------|--------|-------------------------|-----------|----------------------|
| 1     | [24]            | HMBD       | 54,114 | Glorot (Xavier) Uniform | SGD       | 47.7                 |
|       | HMB1            |            |        | He Uniform              | AdaDelta  | 90.7                 |
|       | HMB2            |            |        | LeCun Normal            | AdaMax    | 89.3                 |
| 2     | [24] (Reported) | AHCD1 [24] | 16,800 | —                       | SGD       | 94.9                 |
|       | HMB1            |            |        | LeCun Uniform           | AdaDelta  | 97.3                 |
|       | HMB2            |            |        | LeCun Uniform           | AdaMax    | 96.8                 |

**Table 31** Summary of the different performed 16 Experiments

| #  | Arch. | Dataset | Size    | Image Size | Weight initializer      | Optimizer       | Train accuracy | Test accuracy | Difference (%) |
|----|-------|---------|---------|------------|-------------------------|-----------------|----------------|---------------|----------------|
| 1  | HMB1  | HMBD    | 54,114  | 32 × 32    | <b>He Uniform</b>       | <b>AdaDelta</b> | 99.2           | 90.7          | 8.5            |
| 2  | HMB2  | HMBD    | 54,114  | 32 × 32    | LeCun Normal            | AdaMax          | 98.5           | 89.3          | 9.2            |
| 3  | HMB1  | HMBD    | 54,114  | 64 × 64    | <b>He Uniform</b>       | AdaMax          | 99.4           | 89.8          | 9.6            |
| 4  | HMB2  | HMBD    | 54,114  | 64 × 64    | LeCun Normal            | AdaGrad         | 98.5           | 86.0          | 12.4           |
| 5  | HMB1  | HMBD    | 216,460 | 32 × 32    | Glorot (Xavier) Normal  | <b>AdaDelta</b> | 99.6           | 93.8          | 5.8            |
| 6  | HMB2  | HMBD    | 216,460 | 32 × 32    | LeCun Uniform           | SGD             | 97.7           | 92.2          | 5.5            |
| 7  | HMB1  | HMBD    | 865,840 | 32 × 32    | LeCun Uniform           | Adam            | 99.9           | 98.4          | 1.5            |
| 8  | HMB2  | HMBD    | 865,840 | 32 × 32    | <b>He Uniform</b>       | SGD             | 96.9           | 95.4          | 1.4            |
| 9  | HMB1  | CMATER  | 3000    | 32 × 32    | Glorot (Xavier) Uniform | <b>AdaDelta</b> | 99.8           | 100.0         | −0.2           |
| 10 | HMB2  | CMATER  | 3000    | 32 × 32    | LeCun Uniform           | Adam            | 99.7           | 100.0         | −0.3           |
| 11 | HMB1  | CMATER  | 30,000  | 32 × 32    | Glorot (Xavier) Uniform | <b>AdaDelta</b> | 99.9           | 99.4          | 0.5            |
| 12 | HMB2  | CMATER  | 30,000  | 32 × 32    | LeCun Uniform           | AdaMax          | 99.9           | 99.2          | 0.7            |
| 13 | HMB1  | AIA9k   | 8974    | 32 × 32    | <b>He Uniform</b>       | <b>AdaDelta</b> | 99.5           | 92.7          | 6.8            |
| 14 | HMB2  | AIA9k   | 8974    | 32 × 32    | <b>He Uniform</b>       | AdaGrad         | 99.7           | 93.3          | 6.4            |
| 15 | HMB1  | AIA9k   | 89,740  | 32 × 32    | <b>He Uniform</b>       | AdaMax          | 99.9           | 99.0          | 1.0            |
| 16 | HMB2  | AIA9k   | 89,740  | 32 × 32    | He Normal               | SGD             | 99.9           | 98.4          | 1.4            |

**Fig. 50** Average training time in Experiments 1 to 16

From the cross-validation testing, the presented dataset was large enough, so that a previous small architecture could not generalize for it. The described architecture could generalize with a previously published dataset with higher accuracy metrics.

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