

Given the in-order traversal of an arbitrary binary search tree, is it possible to reconstruct the original tree? If so, how? If not, why not?

Hint: Recall our discussion on AVL Trees from last week

Hint 2: Recall your lab on BST rotations

it is not possible because we do not know what the root value

Therefore, the function is not injective. QED.

No, because you cannot tell which nodes are children and which are parents.

n >= 2

Not possible. If we consider the function mapping BSTs to their in-order traversals, we see the function is not injective because multiple BSTs can map to a single in-order traversal.

the in order traversal of a BST will always return a sorted list, so it is impossible to reconstruct the original tree without more information

From looking at a BST, it isn't possible to create the exact same tree given arbitrary nodes. You'd know the structure, but you wouldn't know the original context of the nodes

Yes its "possible" but when you reconsturct it you cant know for certain its the same tree (this is just a guess)

No because we don't know what number the tree is balanced around

Given a sorted list of integers from 1 to $n, n \in \mathbb{N} \setminus \{0\}$, how do you construct a balanced binary search tree (i.e. height $\log(n)$) from this list? Outline the order of insertion, and explain why this works.

Divide list into 3 parts: [0:n//2], n//2, and [n//2 + 1:]. Place n//2 as root value, then recursively divide the two sublists. Left child is root of [0:n//2], right child is root of [n//2 + 1]

class BST: def
__init__(self, lst): mid
= len(lst)//2; self.root
= lst[mid]; if len(lst)
!= 1: {self.left =
BST(lst[:mid]);
self.right =
BST(lst[mid+1:]);}





Convert the following iterative function to a recursive function:

```
def ibranatchi_iterative(n: int) -> int:
 if n == 0:
   return 0
  elif n == 1:
   return 1
  elif n == 2:
   return 5
  sequence = [0, 1, 5]
 for i in range (3, n + 1):
    next_value = sequence[i - 1] * 2 * sequence[i - 2] - 5 *
   sequence[i - 3]
    sequence.append(next_value)
 return sequence [-1]
def ibranatchi_recursive(n: int) -> int:
 # TODO: Implement this recursively:
```

```
def ibranatchi_recursive(n: int) -> int:
    if 0 <= n <= 2:
        return [0, 1, 5][n]
    else:
        return (
            ibranatchi_recursive(n - 1)
        * 2
        * ibranatchi_recursive(n - 2) - 5
        * ibranatchi_recursive(n - 3)
    )</pre>
```

```
def ibranatchi_recursive(n: int) -> int:
    if n == 0:
        return 0
    elif n == 1:
        return 1
    elif n == 2:
        return 5
    else:
        return ibranatchi_recursive(n 1)+2*ibranatchi_recursive(n 2) 5*ibranatchi_recursive(n 3)
```

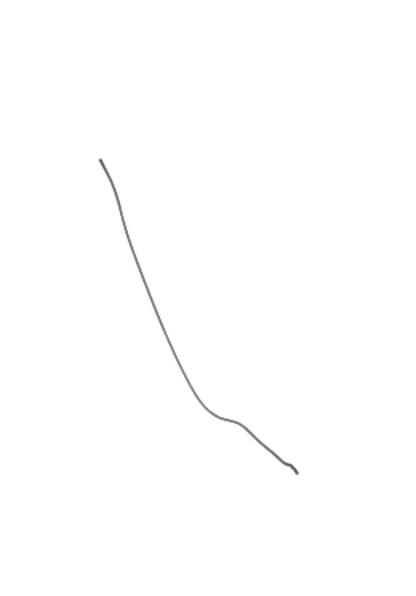
isnt it 0 for all n >= 2?

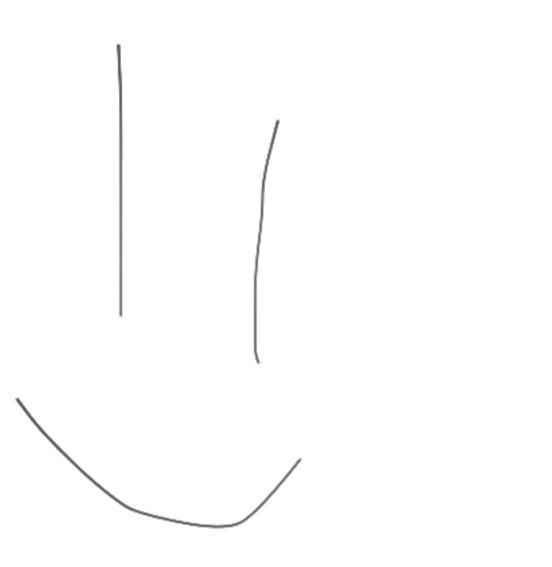
return
ibranatchi_iterative(n1)*2*ibranatchi_iterativ
e(n-2)-5*ibranatchi_ite
rative(n-3)

What is the output of the following list comprehension. If it throws an error, explain why:

```
[[x*y for x in range(4)] for y in range(7)]
```

what if we switch the ${\tt x}$ and ${\tt y}$ iterables?





secret treasure yeah