

# GROUP 7

## Curve Fitting $y = ax^p$ Python Program

### Power Function Fit Using the Least Square Method

This Python program implements least square method to fit curve of type  $y = ax^p$ .

$$y = ax^p$$

$$\log y = \log ax^p$$

$$\log y = \log a + \log x^p$$

$$\log y = \log a + p \log x$$

$$\text{Let } Y = \log y,$$

$$X = \log x,$$

$$C = \log a$$

$$Y = pX + C$$

We first read  $n$  data points from user and then we implement curve fitting for  $y = ax^p$  using least square approach in Python programming language as follow:

```
In [1]: # -*- coding: utf-8 -*-
        """
        Created on Tue Nov  2 21:02:00 2021

        @author: OPEYEMI IBRAHIM
        """
        # Curve Fitting  $y = ax^p$  Python Program

        # This Python program implements Least square fit method to fit curve of type  $y = ax^p$ 

        #  $y = ax^p$ 
        #  $\log y = \log ax^p$ 
        #  $\log y = \log a + \log x^p$ 
        #  $\log y = \log a + p \log x$ 

        # Let  $Y = \log y$ ,
        #  $X = \log x$ ,
        #  $C = \log a$ 

        #  $Y = pX + C$ 

        # We first read  $n$  data points from user and then we implement curve fitting for  $y =$ 

        # Using the Least Square Fit (LSF) method

        # Fitting  $y = ax^p$  to given  $n$  data points
        import numpy as np

        # Reading value of  $n$ 
```

```

n = int(input("Please, enter number of data points, n = "))

# Creating numpy array x & y to store n data points;
x = np.zeros(n)
y = np.zeros(n)

# Reading data points for x and y;
print("Enter data points for x and y: ")
for i in range(n):
    x[i] = float(input("x["+str(i)+"]= "))
    y[i] = float(input("y["+str(i)+"]= "))

# Finding required sum for Least square methods
sumX, sumX2, sumY, sumXY = 0, 0, 0, 0

for i in range(n):
    sumX = sumX + np.log(x[i])
    sumY = sumY + np.log(y[i])
    sumX2 = sumX2 + np.log(x[i])*np.log(x[i])
    sumXY = sumXY + np.log(x[i])*np.log(y[i])

# Finding coefficients a and p

# Let D = denominator
D = (n*sumX2)-(sumX*sumX)

p = (n*sumXY-sumX*sumY)/D
C = (sumY - p*sumX)/n

# Obtaining a from C
a = np.exp(C)

print ('\nOUTPUT RESULT WHEN PROMPTING THE USER TO ENTER THE VALUES:\n')

# Displaying coefficients a, p & equation
print("\nCcoefficients are: ")
print("\na = %.3f" %(a))
print("\np = %.3f" %(p))

print("\nHence, y=%.3f(x)^%.3f" %(a, p))

print("\n'y = ax^p' is the best Power Fit method")

```

```

Please, enter number of data points, n = 6
Enter data points for x and y:
x[0]= 1
y[0]= 1200
x[1]= 2
y[1]= 900
x[2]= 3
y[2]= 600
x[3]= 4
y[3]= 200
x[4]= 5
y[4]= 110
x[5]= 6
y[5]= 50

```

OUTPUT RESULT WHEN PROMPTING THE USER TO ENTER THE VALUES:

Coefficients are:

a = 2033.966

p = -1.749

Hence,  $y=2033.966(x)^{-1.749}$

'y = ax<sup>p</sup>' is the best Power Fit method

## Method 2: By reading our values rigidly into our codes:

```
In [2]: # Using the Least Square Fit (LSF) method

# Fitting  $y = ax^p$  to given  $n$  data points
import numpy as np

# Reading value of  $n$ , i.e. number of data points
n = 6

# Creating numpy array  $x$  &  $y$  to store  $n$  data points;
x = np.zeros(n)
y = np.zeros(n)

# Reading data points for  $x$ ;
x = [1, 2, 3, 4, 5, 6]

# Reading data points for  $y$ ;
y = [0 for i in range(n)];
y[0] = 1200;
y[1] = 900;
y[2] = 600;
y[3] = 200;
y[4] = 110;
y[5] = 50;

# Finding required sum for least square methods
sumX, sumX2, sumY, sumXY = 0, 0, 0, 0

for i in range(n):
    sumX = sumX + np.log(x[i])
    sumY = sumY + np.log(y[i])
    sumX2 = sumX2 + np.log(x[i])*np.log(x[i])
    sumXY = sumXY + np.log(x[i])*np.log(y[i])

# Finding coefficients  $a$  and  $p$ 

# Let  $D$  = denominator
D = (n*sumX2)-(sumX*sumX)

p = (n*sumXY-sumX*sumY)/D
C = (sumY - p*sumX)/n

# Obtaining  $a$  from  $C$ 
a = np.exp(C)

print ('\nOUTPUT RESULT WHEN READING OUR VALUES RIGIDLY INTO OUR CODES:\n')

# Displaying coefficients  $a$ ,  $p$  & equation
print("\nCoefficients are: ")
print("\na = %.3f" %(a))
print("\np = %.3f" %(p))

print("\nHence,  $y=$ %.3f $x^$ %.3f" %(a, p))

print("\n'y = ax^p' is the best Power Fit method")
```

OUTPUT RESULT WHEN READING OUR VALUES RIGIDLY INTO OUR CODES:

Coefficients are:

$$a = 2033.966$$

$$p = -1.749$$

$$\text{Hence, } y = 2033.966x^{-1.749}$$

'y = ax<sup>p</sup>' is the best Power Fit method

In [ ]: