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Image Classification with Convolutional Neural Networks: An Exploration with the CIFAR-10 Dataset

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1. Introduction

Convolutional Neural Networks (CNNs) have become a cornerstone of modern deep learning, particularly in the realm of computer vision. CNNs are meant to self-observe and self-learn the spatial hierarchies of features from large-scale Image data; therefore they are commonly applied in performing tasks such as image classification, object detection, facial recognition, and more. These abilities of processing the data with grid-like topology like the images, have placed the CNNs far ahead of the traditional Machine Learning models of data analysis.

One of the key reasons CNNs are so effective for image data is their ability to leverage local spatial correlations through convolutional layers. These layers place several filters upon the input image and are responsible for identifying low-level features such as edges, textures, and patterns. These learned features are progressively abstract through the addition of convolutional and pooling layers which result in high-level abstraction that discriminates complex objects or scenes. For instance, pooling layers are used to accomplish down sampling to minimize redundancy and increase efficiency, in addition to eliminating translation invariance.

A CNN model is composed of several types of layers: There are convolutional layers that learn features from images; the pooling layers that reduce image dimensions, and fully connected layers, which integrate the learned features for classification or regression tasks. Applying the architecture of successively more complex representations of the image data, the model is capable of surpassing many classical machine learning applications.

In this report, we explore the implementation of a CNN for the task of image classification using the CIFAR-10 dataset (online). We will walk through key stages including data preprocessing, model creation and assessment, and comparability analysis with other machine learning techniques such as Logistics Regression and k-Nearest Neighbors (k-NN). The goal is to demonstrate how CNNs effectively handle image data and how various techniques can be applied to optimize their performance.

2. Code Implementation

Step 1: Importing Libraries

We import libraries for data handling, CNN building, training, evaluation, and visualisation.

Python Script:

import tensorflow as tf

from tensorflow.keras import layers, models
import numpy as np
import matplotlib.pyplot as plt
import os
os.environ['TF_CPP_MIN_LOG_LEVEL'] = '3'
print("TensorFlow Version:", tf.__version__)

TensorFlow Version: 2.17.1

Step 2: Load and Explore the Dataset

In this step, I'll load a dataset suitable for training a CNN. I'll use the CIFAR-10 dataset, which contains 60,000 32x32 colour images across 10 classes (e.g., aeroplanes, cars, birds, etc.).

Python Script:

```
# Load the CIFAR-10 dataset from Keras datasets
from tensorflow.keras.datasets import cifar10
(train_images, train_labels), (test_images, test_labels) = cifar10.load_data()
# Print dataset shapes
print("Training data shape:", train_images.shape)
print("Training labels shape:", train_labels.shape)
print("Test data shape:", test_images.shape)
print("Test labels shape:", test_labels.shape)
# Display the first 5 labels
print("First 5 training labels:", train_labels[:5].flatten())
# Display a few sample images with their labels
class_names = ['airplane', 'automobile', 'bird', 'cat', 'deer',
          'dog', 'frog', 'horse', 'ship', 'truck']
                                                                   Training data shape: (50000, 32, 32, 3)
                                                                   Training labels shape: (50000, 1)
                                                                   Test data shape: (10000, 32, 32, 3)
                                                                   Test labels shape: (10000, 1)
                                                                   First 5 training labels: [6 9 9 4 1]
plt.figure(figsize=(5, 5))
                                                                                       truck
                                                                               truck
                                                                                                deer automobile
for i in range(10):
  plt.subplot(2, 5, i+1)
  plt.imshow(train_images[i])
  plt.title(class_names[train_labels[i][0]])
                                                                     automobile bird
  plt.axis('off')
plt.tight_layout()
plt.show()
```

Step 3: Preprocess the Data

In this step, I'll prepare the data for input into the CNN. Preprocessing ensures that the data is in a suitable format for training and can improve model performance.

Python Script:

Normalize pixel values to range 0-1 train_images = train_images / 255.0 test_images = test_images / 255.0

Convert labels to one-hot encoding

```
from tensorflow.keras.utils import to_categorical
train_labels = to_categorical(train_labels, num_classes=10)
test_labels = to_categorical(test_labels, num_classes=10)
# Print shapes after preprocessing
print("Normalized training images shape:", train_images.shape)
print("One-hot encoded training labels shape:", train_labels.shape)
                     Normalized training images shape: (50000, 32, 32, 3)
                     One-hot encoded training labels shape: (50000, 10)
Step 4: Build the CNN Model
```

In this step, we'll construct the architecture of the Convolutional Neural Network (CNN). The model will include convolutional layers, pooling layers, and fully connected (dense) layers to process and classify the image data.

```
Python Script:
from tensorflow.keras import layers, models
# Initialize a Sequential model
model = models.Sequential()
# Add convolutional layers followed by pooling layers
model.add(layers.Conv2D(32, (3, 3), activation='relu', input_shape=(32, 32, 3)))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(64, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(64, (3, 3), activation='relu'))
# Flatten the output from the convolutional layers
model.add(layers.Flatten())
# Add dense (fully connected) layers
model.add(layers.Dense(64, activation='relu'))
model.add(layers.Dense(10, activation='softmax')) # Output layer for 10 classes
model.summary()
```

Layer (type)	Output Shape	Param #
conv2d_12 (Conv2D)	(None, 30, 30, 32)	896
max_pooling2d_8 (MaxPooling2D)	(None, 15, 15, 32)	0
conv2d_13 (Conv2D)	(None, 13, 13, 64)	18,496
max_pooling2d_9 (MaxPooling2D)	(None, 6, 6, 64)	0
conv2d_14 (Conv2D)	(None, 4, 4, 64)	36,928
flatten_4 (Flatten)	(None, 1024)	0
dense_8 (Dense)	(None, 64)	65,600
dense_9 (Dense)	(None, 10)	650

Total params: 122,570 (478.79 KB) Trainable params: 122,570 (478.79 KB) Non-trainable params: 0 (0.00 B)

Step 5: Compile the Model

After building the CNN model, the next step is to compile it. Compilation specifies the optimizer, loss function, and evaluation metrics that the model will use during training.

Python Script:

```
# Compile the model
model.compile(
    optimizer='adam', # Optimizer for updating weights
    loss='categorical_crossentropy', # Loss function for multi-class classification
    metrics=['accuracy'] # Metric to evaluate during training and testing
)
# Display a confirmation message
print("Model compiled successfully!")

Model compiled successfully!
```

Step 6: Train the Model

Now that the CNN model is compiled, the next step is to train it using the training dataset. During training, the model will adjust its weights to minimize the loss function, improving its ability to classify images.

Python script:

```
train_labels,
                           # Training labels (one-hot encoded)
   epochs=10,
                             # Number of training epochs
   validation_data=(test_images, test_labels), # Validation data
                              # Batch size for gradient updates
   batch size=64,
   verbose=1
                            # Verbosity level for training output
)
# Display a confirmation message
print("Model training complete!")
      Epoch 1/10
      782/782
                               - 71s 88ms/step - accuracy: 0.3221 - loss: 1.8393 - val_accuracy: 0.5170 - val_loss: 1.3351
      Epoch 2/10
      782/782 -
                               - 81s 87ms/step - accuracy: 0.5329 - loss: 1.2978 - val_accuracy: 0.5574 - val_loss: 1.2282
      Epoch 3/10
      782/782 -
                               - 83s 88ms/step - accuracy: 0.6018 - loss: 1.1282 - val accuracy: 0.6259 - val loss: 1.0534
      Epoch 4/10
                                - 82s 88ms/step - accuracy: 0.6431 - loss: 1.0142 - val_accuracy: 0.6557 - val_loss: 0.9944
      782/782 ·
      Epoch 5/10
      782/782 -
                               - 83s 89ms/step - accuracy: 0.6760 - loss: 0.9269 - val accuracy: 0.6824 - val loss: 0.9209
      Epoch 6/10
      782/782 -
                               - 68s 87ms/step - accuracy: 0.7000 - loss: 0.8597 - val_accuracy: 0.6779 - val_loss: 0.9372
      Epoch 7/10
                               - 68s 86ms/step - accuracy: 0.7117 - loss: 0.8235 - val accuracy: 0.6893 - val loss: 0.8903
      782/782 -
```

Step 7: Visualizing Training Results

After training the model, it's important to visualize the training and validation accuracy and loss. This helps us understand how well the model is learning and identify potential issues like overfitting or underfitting.

- 82s 87ms/step - accuracy: 0.7325 - loss: 0.7672 - val accuracy: 0.6911 - val loss: 0.9087

- 72s 92ms/step - accuracy: 0.7443 - loss: 0.7291 - val accuracy: 0.6974 - val loss: 0.8832

- 80s 90ms/step - accuracy: 0.7572 - loss: 0.6929 - val_accuracy: 0.7004 - val_loss: 0.8669

Python script:

Epoch 8/10 782/782 ---

Epoch 9/10 782/782 ---

Epoch 10/10 782/782 ----

Model training complete!

```
import matplotlib.pyplot as plt

# Extract accuracy and loss from the training history
accuracy = history.history['accuracy']

val_accuracy = history.history['val_accuracy']

loss = history.history['loss']

val_loss = history.history['val_loss']

epochs = range(1, len(accuracy) + 1)

# Plot Training and Validation Accuracy

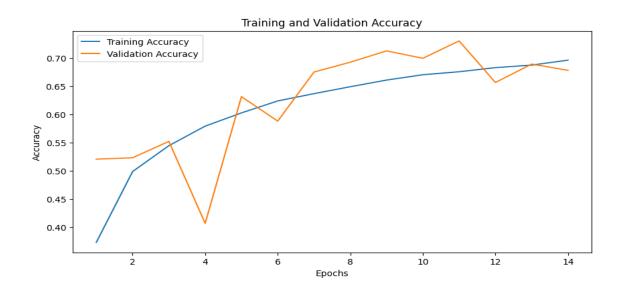
plt.figure(figsize=(10, 5))

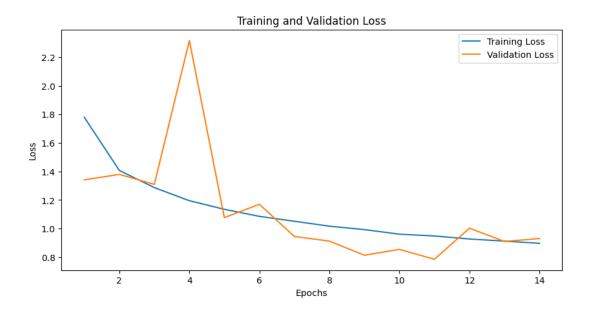
plt.plot(epochs, accuracy, label='Training Accuracy')
```

```
plt.plot(epochs, val_accuracy, label='Validation Accuracy')
plt.title('Training and Validation Accuracy')
plt.xlabel('Epochs')
plt.ylabel('Accuracy')
plt.legend()
plt.show()

# Plot Training and Validation Loss
plt.figure(figsize=(10, 5))
plt.plot(epochs, loss, label='Training Loss')
plt.plot(epochs, val_loss, label='Validation Loss')
plt.title('Training and Validation Loss')
plt.xlabel('Epochs')
plt.ylabel('Loss')
plt.legend()
```

plt.show()





Step 8: Evaluate Model Performance

Now that the model is trained, we need to evaluate its performance on the test dataset to see how well it generalizes to unseen data. This involves calculating the loss and accuracy of the test set and interpreting the results.

Python Script:

Evaluate the model on the test dataset

test_loss, test_accuracy = model.evaluate(test_images, test_labels, verbose=1)

Print the test results

print(f"Test Loss: {test_loss:.4f}")

print(f"Test Accuracy: {test_accuracy:.4f}")

Classification Report and Confusion Matrix

from sklearn.metrics import classification_report, confusion_matrix

import seaborn as sns

Predict the labels for the test dataset

predictions = model.predict(test_images)

predicted_labels = np.argmax(predictions, axis=1)

true_labels = np.argmax(test_labels, axis=1)

Generate the classification report

print("Classification Report:\n")

print(classification_report(true_labels, predicted_labels, target_names=class_names))

Generate the confusion matrix

conf_matrix = confusion_matrix(true_labels, predicted_labels)

Plot the confusion matrix

plt.figure(figsize=(10, 8))

sns.heatmap(conf_matrix, annot=True, fmt='d', cmap='Blues', xticklabels=class_names, yticklabels=class_names)

plt.xlabel('Predicted Labels')

plt.ylabel('True Labels')

plt.title('Confusion Matrix')

plt.show()

	precision	recall	f1-score	support	
airplane	0.77	0.71	0.74	1000	
automobile	0.79	0.84	0.82	1000	
bird	0.64	0.50	0.56	1000	
cat	0.54	0.49	0.51	1000	
deer	0.66	0.70	0.68	1000	
dog	0.52	0.71	0.60	1000	
frog	0.74	0.81	0.77	1000	
horse	0.81	0.69	0.75	1000	
ship	0.88	0.71	0.79	1000	
truck	0.74	0.84	0.79	1000	
accuracy			0.70	10000	
macro avg	0.71	0.70	0.70	10000	
weighted avg	0.71	0.70	0.70	10000	

Classification Report:



Step 9: Visualizing Model Predictions

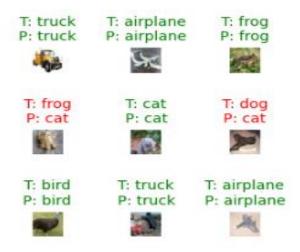
Visualizing the model's predictions helps us understand how it performs on individual test samples. We'll display a few test images along with their predicted and true labels.

```
Python Script:
```

```
import matplotlib.pyplot as plt
import numpy as np
# Predict the labels for the test dataset
predictions = model.predict(test_images)
predicted_labels = np.argmax(predictions, axis=1)
true_labels = np.argmax(test_labels, axis=1)
# Class names for CIFAR-10
class_names = ['airplane', 'automobile', 'bird', 'cat', 'deer',
         'dog', 'frog', 'horse', 'ship', 'truck']
# Select random test samples to visualize
num_samples = 9
indices = np.random.choice(len(test_images), num_samples, replace=False)
selected_images = test_images[indices]
                                                                                        Note
selected_true_labels = true_labels[indices]
                                                                             T: True label
selected_predicted_labels = predicted_labels[indices]
                                                                              P: Predicted label
                                                                             Green: Correct predictions.
# Plot the selected test images with predictions
                                                                             Red: Incorrect predictions.
plt.figure(figsize=(3, 3))
for i in range(num_samples):
  plt.subplot(3, 3, i + 1)
  plt.imshow(selected_images[i], interpolation='nearest')
  # Shorter titles with correct/incorrect coloring
  color = 'green' if selected_true_labels[i] == selected_predicted_labels[i] else 'red'
  plt.title(f"T: {class_names[selected_true_labels[i]]}\nP:
{class_names[selected_predicted_labels[i]]}",
        fontsize=10, color=color)
```

plt.axis('off') # Turn off axes for better visibility

plt.tight_layout(pad=2.0)
plt.show()



Step 10: Model Tuning and Optimization

To improve the model's performance, we can apply tuning and optimization techniques. These techniques include adjusting the model architecture, hyperparameters, and training strategies. The combined approach already integrates the key techniques (Dropout, Batch Normalization, Data Augmentation, and Early Stopping).

Python Script:

from tensorflow.keras import layers, models

from tensorflow.keras.callbacks import EarlyStopping

from tensorflow.keras.preprocessing.image import ImageDataGenerator

Define the CNN Model with Batch Normalization and Dropout

model = models.Sequential([

layers.Conv2D(32, (3, 3), activation='relu', input_shape=(32, 32, 3)),

layers.BatchNormalization(),

layers.MaxPooling2D((2, 2)),

layers.Conv2D(64, (3, 3), activation='relu'),

layers.BatchNormalization(),

layers.MaxPooling2D((2, 2)),

layers.Conv2D(64, (3, 3), activation='relu'),

layers.BatchNormalization(),

```
layers.Flatten(),
  layers.Dense(64, activation='relu'),
  layers.Dropout(0.5), # Dropout to prevent overfitting
  layers.Dense(10, activation='softmax') # Output layer
])
# Compile the Model
model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
# Define Early Stopping
early_stopping = EarlyStopping(monitor='val_loss', patience=3, restore_best_weights=True)
# Set Up Data Augmentation
datagen = ImageDataGenerator(
  rotation_range=15,
  width_shift_range=0.1,
  height_shift_range=0.1,
  horizontal_flip=True
)
datagen.fit(train_images)
# Train the Model with Data Augmentation and Early Stopping
history = model.fit(
  datagen.flow(train_images, train_labels, batch_size=64),
  epochs=20, # Early stopping will halt if no improvement
  validation_data=(test_images, test_labels),
  callbacks=[early_stopping]
)
And then
test_loss, test_accuracy = model.evaluate(test_images, test_labels)
print(f"Test Loss: {test_loss:.4f}")
print(f"Test Accuracy: {test_accuracy:.4f}")
```

```
313/313 ------ 7s 24ms/step - accuracy: 0.7300 - loss: 0.7856
```

Test Loss: 0.7856 Test Accuracy: 0.7298

Previous Test Loss: 0.8489
Previous Test Accuracy: 0.7004

New Test Loss: 0.7856New Test Accuracy: 0.7298

This indicates that the optimizations (Dropout, Batch Normalization, Data Augmentation, and Early Stopping) have helped the model generalize better.

Step 11: Compare CNN Performance with Other Models

To understand how well our CNN performs, it's useful to compare it with simpler models, such as Logistic Regression, k-Nearest Neighbors (k-NN), or Decision Trees. This step provides insights into whether CNN's complexity is justified based on the dataset and task.

Python Script:

target_names=class_names))

```
#Preprocess Data for Simpler Models
# Flatten the images for Logistic Regression and k-NN
train_images_flat = train_images.reshape(train_images.shape[0], -1)
test_images_flat = test_images.reshape(test_images.shape[0], -1)
print("Flattened training data shape:", train_images_flat.shape)
print("Flattened test data shape:", test_images_flat.shape)
#Logistic Regression
from sklearn.linear_model import LogisticRegression
from sklearn.metrics import accuracy_score, classification_report
# Train Logistic Regression
logistic_model = LogisticRegression(max_iter=100, solver='saga', multi_class='multinomial')
logistic_model.fit(train_images_flat, np.argmax(train_labels, axis=1))
# Predict and evaluate
logistic predictions = logistic model.predict(test images flat)
logistic_accuracy = accuracy_score(np.argmax(test_labels, axis=1), logistic_predictions)
print(f"Logistic Regression Test Accuracy: {logistic_accuracy:.4f}")
print("Logistic Regression Classification Report:")
print(classification_report(np.argmax(test_labels, axis=1), logistic_predictions,
```

#k-Nearest Neighbors (k-NN)

from sklearn.neighbors import KNeighborsClassifier

Train k-NN

knn_model = KNeighborsClassifier(n_neighbors=5) # You can experiment with different k values knn_model.fit(train_images_flat, np.argmax(train_labels, axis=1))

Predict and evaluate

knn_predictions = knn_model.predict(test_images_flat)

knn_accuracy = accuracy_score(np.argmax(test_labels, axis=1), knn_predictions)

print(f"k-NN Test Accuracy: {knn_accuracy:.4f}")

print("k-NN Classification Report:")

print(classification_report(np.argmax(test_labels, axis=1), knn_predictions, target_names=class_names))

Logistic Page	ossion Test /	\ccupac	0 1036							
Logistic Regr		-			k-NN Test Accuracy: 0.3398					
Logistic Regr					k-NN Classific	•				
	precision	recall	f1-score	support		precision		f1-score	support	
						precision	Lecall	11-50016	support	
airplane	0.46	0.49	0.47	1000	-11	0.30	0.54	0.45	4000	
automobile	0.47	0.47	0.47	1000	airplane	0.38	0.54	0.45	1000	
bird	0.33	0.29	0.31	1000	automobile	0.65	0.20	0.31	1000	
cat	0.28	0.26	0.27	1000	bird	0.23	0.45	0.30	1000	
					cat	0.29	0.22	0.25	1000	
deer	0.35	0.29	0.32	1000	deer	0.24	0.51	0.33	1000	
dog	0.33	0.33	0.33	1000	dog	0.39	0.22	0.28	1000	
frog	0.40	0.46	0.43	1000	frog	0.35	0.25	0.29	1000	
horse	0.45	0.44	0.44	1000	horse	0.68	0.21	0.32	1000	
ship	0.50	0.53	0.51	1000	ship	0.40	0.66	0.50	1000	
truck	0.43	0.46	0.45	1000	truck	0.70	0.14	0.23	1000	
					Lruck	0.70	0.14	0.25	1000	
accuracy			0.40	10000	accuracy			0.34	10000	
macro avg	0.40	0.40	0.40	10000	•	0.42	0.24			
weighted avg	0.40	0.40	0.40	10000	macro avg	0.43	0.34	0.33	10000	
merguren avg	0.40	0.40	0.40	10000	weighted avg	0.43	0.34	0.33	10000	

Model	Test Accuracy
Convolutional Neural Network (CNN)	72.98%
Logistic Regression	40.36%
k-Nearest Neighbors (k-NN)	33.98%

Note: The CNN outperforms both Logistic Regression (40.36%) and k-NN (33.98%) with an accuracy of 72.98%, highlighting its ability to effectively learn spatial features from images. Logistic Regression and k-NN struggle with high-dimensional data, making CNN the most suitable model for CIFAR-10 classification tasks.

3. Conclusion

This project presents a detailed study of CNNs for image classification using the CIFAR-10 dataset and an evaluation of their performance against other machine learning techniques such as Logistic

Regression and k-NN. We started by importing essential libraries and preparing the dataset, followed by data preprocessing and normalization, ensuring the images were ready for model training. We were able to train and design a CNN model inclusive of numerous convolutional and pooling layers sufficient to work spatial features of images and fine-tuning by the Adam optimizer. During training, we also assessed accuracy and loss, visualized the training, tested performance and model test using test accuracy, classification report, and confusion matrix. We then compared CNN performance with other models. Logistic Regression and k-NN achieved comparatively low accuracies of 40.36% and 33.98%, respectively, but the test accuracy of CNN was 72.98%. This demonstrated the advantages of CNNs in handling high-dimensional, image-based data. Thus, CNNs are very effective in image classification; moreover, the capacity to learn required features directly from the pixel data gives a huge advantage to CNNs compared to traditional machine learning algorithms. This project highlights the importance of model selection and optimization in achieving high performance in image classification tasks.

4. Key Take-Aways

- Convolutional Neural Networks (CNNs) excel in image classification tasks by learning spatial and hierarchical features, achieving 72.98% accuracy on the CIFAR-10 dataset.
- Techniques like Dropout, Data Augmentation, Batch Normalization, and Early Stopping improved CNN performance and generalization.
- Logistic Regression (40.36%) and k-Nearest Neighbors (33.98%) were outperformed by CNN due to their inability to handle high-dimensional image data effectively.
- Metrics such as accuracy, loss curves, classification reports, and confusion matrices were essential in assessing model performance.
- The results underscore the importance of selecting the right model and applying optimizations for complex datasets like CIFAR-10.

5. References

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GitHub Repository:

https://github.com/lbrahim22331/CNN-Model-Comparison-Report.git

Dataset line:

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