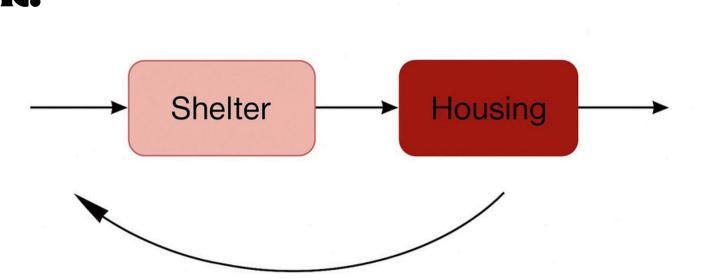
DISCRETEEVENTSIMULATIONANMETAMODELS

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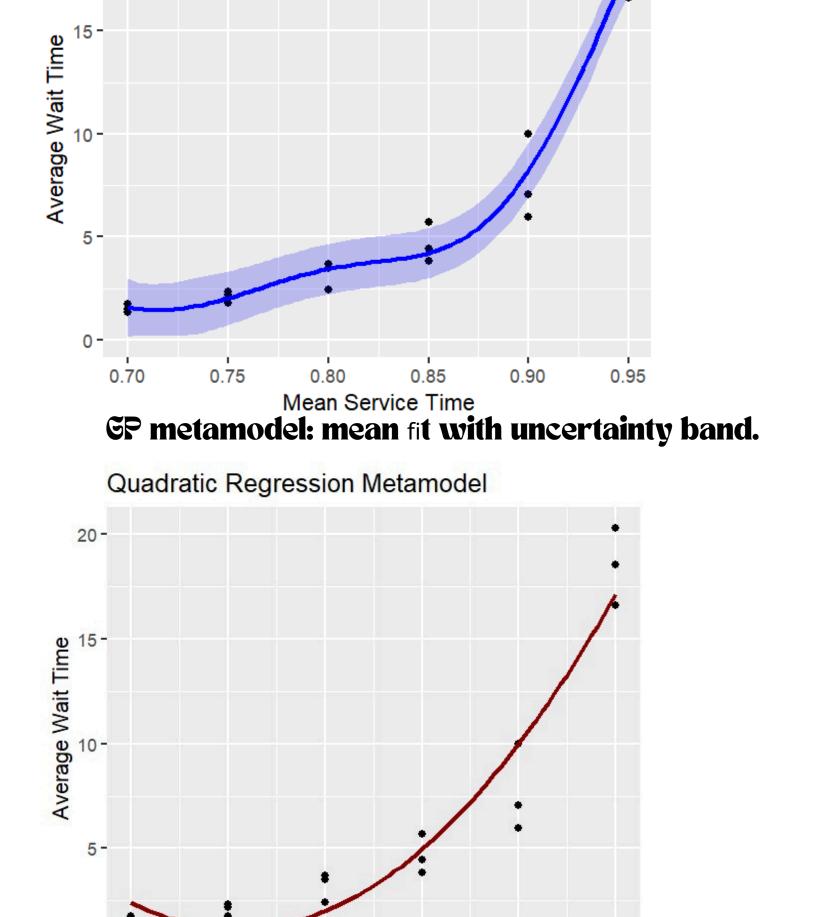
Introduction

Discrete-Event Simulation (DES) is a powerful tool for modelling complex systems where changes oc-cur at discrete points in time, such as in healthcare, manufacturing, housing. While DES provides detailed insights, it can be computationally expen-sive when many replications are required. To ad- dress this, metamodels researchers use simplified statistical or mathematical approximations of the simulation that provide faster predictions while pre-serving key system behaviour. To build accurate metamodels, it is essential to cover the model input space efficiently with a number of simulation runs. As the number of input dimensions grows, this hespinesvincies singly difficult; atin Hypercubes an dresses this by ensuring usual coverage the whole style with femons and metamodels. A single-server queue was used for hospital waiting times, where individuals remain in a single line until ser-vice is received, and the mean waiting time is the key measure. A tandem queue was used for home-lessness: the first state represents waiting for shelter, and the second represents waiting for perma- nent housing after leaving This layered short-term shelter captures both housing demand and long-term outcomes within the same framework.



Metamodel Results

We evaluate metamodels for predicting mean hos- pital waiting time in a single-server queue (M/M/I-type) DES. Ginear and Quadratic regressions cap- ture broad trends but struggle near high utilisation. Gaussian Process (EP) metamodels achieved the lowest MSE by adapting to curvature; however, EPs can appear to overfit local noise (especially with a small nugget) and are more computationally expensive than simple regressions.



Quadratic metamodel: smooth trend but underfits extremes.

MSE Comparison (lower is better)

Metamodel
GaussianProcest1328
Quadratic Regression 2.7552
GinearRegression

LinearRegression

LinearRe

MSE computed on DES outputs: n(yì-ŷ2i.

Constructing One-DimensionaHomelessness DES

Metamodels

We simulate a tandem queue with a To generate the metamodel plots we used that loop from Housing back to approaches in R.

We simulate a tandem queue with a that the plots we used the plots we used that the plots we used the plot

For the Gaussian Process (GP) model, we used the housing), 5 (extra shelter), Mh mlegp package. A GP assumes outputs followean hous-

ing service time), Ms (mean shelter service time), Ms (mean shelter service time), A (arrival rate), and R (re-entry probability). Bases case (no extra probability). Bases hown below, where vacion cavitism and the diagonal nugget with ith diagonal elements applicing stochast

withithdiagonalelementerpuring stochas unsheltered queue over 5 years: tic simulation noise. For deterministic outputs N=0; for constant noise N = \sigma 2\epsilon l. mlegp allows N to \frac{\text{be}}{\text{constant}}. \text{specified exactly or up to a multiplicative constant.} For the kinear and Quadratic regression metamodels, we used standard polynomial regression in \text{R}:

 $y = \beta_0 + \beta_1 x$, $y = \beta_0 + \beta_1 x + \beta_2 x^2$. These were fitted using lm() with polynomial terms in service time, providing simpler benchmarks $\frac{100}{0}$ $\frac{1}{1}$ $\frac{1}{2}$ $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{5}$ against the GP.

Together, these approaches allow comparts own fying these inputs we assess simple polynomial regressions with the minpacts blen un-sheltered queueing EP model.

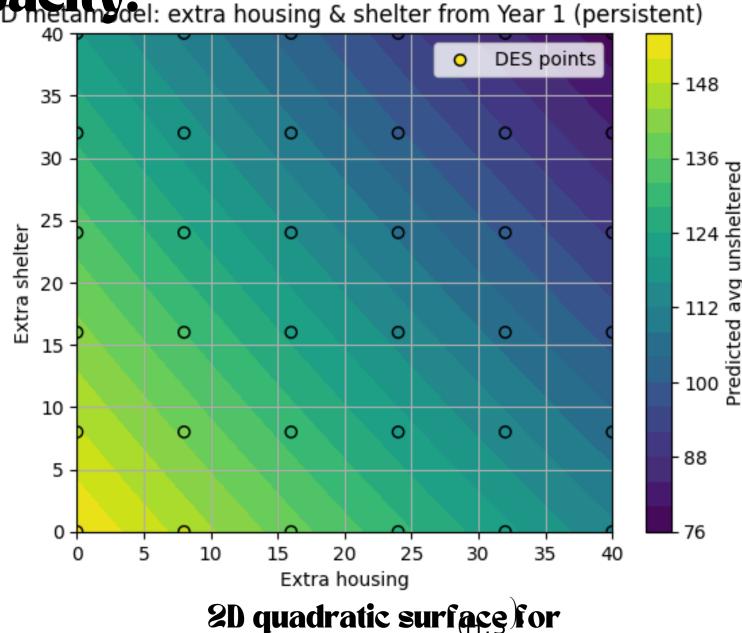
times; we then build metamod-els to approximate these DES outputs

approxima efficiently.

Higher Dimensional Metamod

2D(H, S): For two dimensions, we tested the im-pact of adding extra housing (H) versus shelter (S) capacity.

Capacity (S) shelter from Year 1 (persistent)



The fitted quadratic response surface is

 $\hat{y} = 155.8 - 1.17 \text{ H} - 0.93 \text{ S} + 0.0025 \text{ H} 2 + 0.001 \text{ S} 2 + 0.000200 \text{ HS}.$

with MSE $_{1.485}$ and $_{8}^{2}$ = 0.996. Adding one unit of housing reduces the amount of un homelessness more than adding one unit ter since 0.93. Also, the quadratic is stronger in H (coefficient on H2 is 0.00) in 5 (coefficient on 52 is 0.001), i.e., as hou creases further, the quadratic effect is g 4D(H, S, A, R): We then expanded to four by adding the arrival rate (A) and re-entr ity (R). A full-factorial design was used ar quadratic (squares + pairwise interaction ted to capture curvature and key interac 6D(H, S, Mh, Ms, A, R): Full factorial design become computationally expensive in six sions. We therefore used katin Hypercub achieve good space-filling coverage with runs, then fitted a quadratic with selected tions. Finally, we applied stepAIC, anothe age in R, to automatically remove negligil Akaike Information Criterion-based step lection), yielding a concise metamodel wi predictive accuracy.

Conclusions

·DES + Metamodels = fast, accurate what-ifs. GP gave the lowest MSE vs. linear/quadratic but is more computationally expensive housing

reduces the unsheltered homelessness estightly more compared to adding shelt • Scaling up: Latin Hypercube • stepAIC et a concise 6D model with far fewer runs factorial.