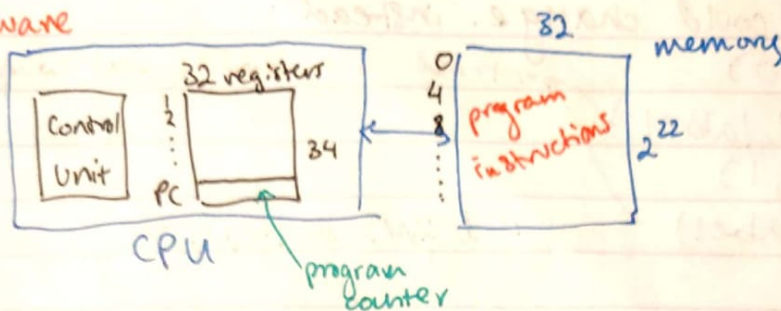


CS2412

Hardware

Sept 11, 2018



State: $\{0, 1\}^{32 \cdot 2^{22} + 32 \cdot 34}$

Control Unit: Implements a function from state \rightarrow state.
 $S_i := \text{step}(S_{i-1})$.

\rightarrow need a general purpose step fn.

$\text{step}(\text{state}) = \{$

instruction = state.mem(state.reg(PC)) // fetch instr.

state2 = state.setReg(PC, state.reg(PC) + 4) // PC += 4

instruction match $\{ \dots \}$ // decode/encode instr.

$\}$

Registers: 0th register is saved for quick access to 0 value.

Arithmetic: Same answer for add/sub no matter signed/unsigned
 \rightarrow not true for multi since you do mod 2^{64} over mod 2^{32}

OpCodes:

Sept 13, 2018

Word that represents a machine lang. instr.

\rightarrow ADD, JR, etc... first abstraction

(also gives you labels) \rightarrow Assembly is a lang. for writing m. lang programs using opcodes. An assembler translates assembly \rightarrow machine

Example:

Find abs of reg \$1.

0 SLT(2, 1, 0) // is \$1 < \$0 (always 0)? dest: \$2

4 BEQ(2, 0, 1) // skip 1 after next. (compare \$2 to \$0)

8 SUB(1, 0, 1) // put \$0 - \$1 in \$1

12 JR(31) // exit

$$\frac{12 - (4 + 4)}{4} = 1$$

Skip number could change. instead:

Words: 32 bit instructions (words = codes)

SLT(2,1,0)
 beg(2,0,label)
 SUB(1,0,1)
 Define(label) // defines a location
 JR(31)

these are codes, not words

How to eliminate labels?

A symbol table maps label names to meanings. (mem. addys)

pass 1) Build symbol table
 pass 2) Convert uses of each label to corresponding addy/offset
 Need 2 passes b/c can def. label after usage.

Example:

Sept 18, 2018

1) Define(p)

0 lis \$1

4 use(e) $\xrightarrow{\text{asm}}$

8 jr \$1

define(e)

12 jr \$31

label / addr

p 0

e 12

use(e)@4

lis \$1

12

jr \$1

jr \$31

Really, these are 32 bit binary (m. lang)

↑ gets changed during relocation too

Relocation and Linking:

Object File: contains machine lang w/ metadata (incl. symbol table)

lis \$1

use(p)

jalr \$1

TBC?

} calls above example as procedure. Assume assembled separately.

$\xrightarrow{\text{asm}}$

l/a

use(p)@4

lis \$1

0

jalr \$1

info on label defs and uses

Linking:

Process of combining obj. files into one program/lib.

1) Relocation

2) Connect labels from dif. obj files. "resolving"

```

0  lis $1
4  12
8  jalr $1
12 lis $1
16 12 24
20 jr $1
24 jr $31
    
```

Must adjust label values. "Relocation"

Variables:

Abstraction of storage location that can hold a value.

Extents:

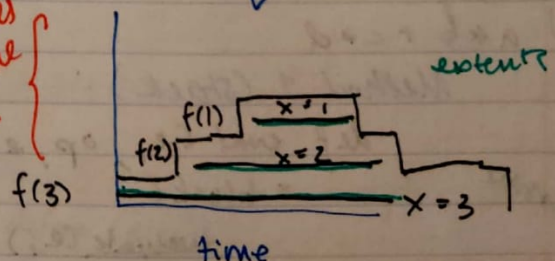
Extent of a var. instance is time interval where var accessible

	var kind	extent
fixed location	global	entire execution
stack	proc-local	one exec. of proc.
heap	field of object	obj creation → last use

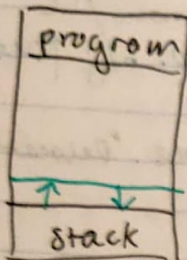
ex: fact(3)

$= \text{fact}(2) * 3$
 $= \text{fact}(1) * 2 * 3$
 $= 1 * 2 * 3$

many instances
of the same
variable.



Stack Implementation:



Designate reg \$30 to store addr of top of stack. "Stack ptr"
 push: -= 4 pop: += 4
 Can read vals not on top with lw (with offset).

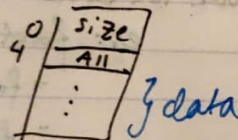
$lw(reg(c), 8, reg(30))$ \$30: 100
 // reads "c" ↑ 104
 108 a
 b
 c
 offset (8) is stored for each variable.

Frame Pointers:

Copy of stack ptr made at beginning of procedure (doesn't change)
 \$29 ↑

Memory:

Chunks.



block of consec. mem locations.
 offsets indexed by vars.

Example:

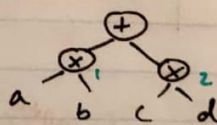
1) $a * b + c * d$

Method 1 (stack):

def eval(e_1 , op, e_2) {
 = block(
 evaluate(e_1)
 push \$3
 evaluate(e_2)
 pop \$4
 \$3 = \$4 op \$3
)
 }

recursive

general, easy
 x inefficient



read a into \$3
 push \$3
 *₁ { read b into \$3
 pop \$4
 \$3 = \$4 * \$3
 push \$3
 *₂ { same as *₁
 pop \$4
 \$3 = \$4 + \$3

Method 2: Variables

$t_1 = a \cdot b$ $t_2 = c \cdot d$ $t_3 = t_1 + t_2$

✓ easy to improve

x need reg's for ops

x many vars

def evaluate(e_1 , op, e_2): (code, variable) = {

(e_1 , v_1) = evaluate(e_1)

(e_2 , v_2) = evaluate(e_2)

$v_3 = \text{new Variable}(\text{"temp"})$

code = $c_1 + c_2$: + ($v_3 = v_1$ op v_2)

(code, v_3)

}

need

"register allocation"

Sept 25, 2018

Method 3: Hybrid (vars, operations on registers)

def evaluate(e_1 , op, e_2): Code {

$t_1 = \text{new Variable}(\text{"temp"})$

→ Scope(t_1 ,

block {

evaluate(e_1)

write(t_1 , $\$3$)

evaluate(e_2)

read($\$4$, t_1)

$\$3 = \4 op $\$3$

)

→

Scope: type of Code to keep track of used vars

If statements:

if (e_1 op e_2) T else E

evaluate(e_1)

write(t_1 , $\$3$)

evaluate(e_2)

read($\$4$, t_1)

bne($\$3$, $\$4$, else)

beg($\$0$, $\$0$, end)

→ define ("else")

E

define ("end")

* try:

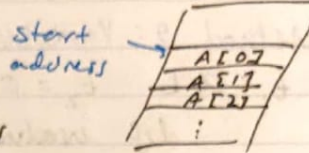
while loop

while (e_1 op e_2) body

can reuse evaluate ==

Arrays:

- Contiguous area of memory
- Compute offset from start address
- deref(address): put val at add in $\$3$. $\star(\text{address})$
 \hookrightarrow LW for assignment
- assignToAddr(address, code) $\star\text{address} = \text{code}$.
 \hookrightarrow SW



Register Allocation:

Sept 27, 2018

- Exam, but not assignments.
- Assigns registers/stack locations to variables.
- $a+b+c+d+e$:
 $\star 1 - t_1 = a+b$
 $\star 2 - t_2 = t_1 + c$
 $\star 3 - t_3 = t_2 + d$
 $\star 4 - t_4 = t_3 + e$

- A variable is "live" at program point p if the value at p may be read sometime after p . (watch for overwrite by read)
 \hookrightarrow at $\star 1$, t_1 is live, t_2 is not (overwrite)
 \hookrightarrow at $\star 2$, t_2 is live, t_1 isn't anymore (no more reads)
 \hookrightarrow at $\star 4$, t_4 is not live.
- 2 vars can share a reg if they're never both live at once.

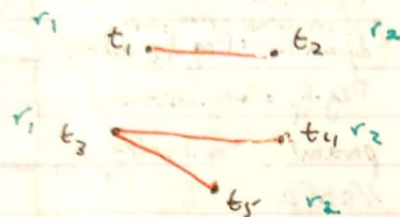
Example:

- $t_1 = a+b$ — t_1 live
 $t_2 = c+d$ — t_1, t_2 live
 $t_3 = t_1 + t_2$ — t_3 live
 $t_4 = e+f$ — t_3, t_4 live
 $t_5 = t_3 - t_4$ — t_5, t_3 live
 $g = t_3 + t_5$

r_1 for t_1, t_3
 r_2 for t_2, t_4, t_5

- Interference Graph:

- Variables are vertices.
- Edges iff vars are live at once.



- Graph Colouring:

- Assigns colour to each vertex where each edge connects dif. colours. \rightarrow Finding a minimal colouring for an arb. graph is NP hard. \therefore
- \rightarrow Greedy algos work ok.

for each vertex v ?

Valid, but not nec. minimal. colour v with the least colour not yet used by its neighbours

Procedures:

- Reusable seg [code].
- Calling code + procedure must agree on conventions.
 - Where in memory/registers to pass arguments + return val.
 - Who allocates space on stack?
 - Which registers the procedure may modify

"callee-save" - modify
"caller-save" - save

Calling Code

Procedure.

Oct 2, 2018

Define(proc)

Next page. \rightarrow

Conventions:

- callee save 'preserved' register - SP, FP, free param chunk, alloc/free frame.
- caller save modified registers - PC with JALR, allocate param chunk
 - passes param addr in reg. allocated.
 - Reg. allocated.
 - Return val in \$3
 - All other registers

Calling Code

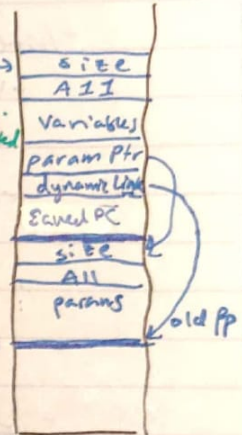
→ before call evaluate(args) into temp vars
stack.allocate(parameters)
param 1 = arg 1 (temp var)
param n = arg n (temp var)
LIS(Reg.targetPC)
Use(Proc)
JALR(Reg.TargetPC)

Need
reg. allocated
NOT FP

Procedure:

Define(proc) fp →
Reg.savedParamPtr = allocated
stack.allocate(Frame)
dyn.Link = Reg.FP
savedPC = Reg.savedPC
Reg.fP = Reg.allocated
paramPtr = Reg.savedPP
// stuff
Reg.savedPC = savedPC
Reg.fP = dynamic link
stack.push() // frame
stack.push() // params
JALR(Reg.savedPC)

Need
reg. allocated



eliminate Var Acc AS:

if v is Var:
access v in frame

else: // param
read paramPtr from frame to Reg.scratch
access v in param chunk ← base Reg + Reg.scratch

Dynamic Links:

Points to frame of caller.

Oct 4, 2018

Prologue/Epilogue:

Instrs at beg/end of proc that sets up/clears frame+reg's.

Static Link:

Points to frame that function is defined in

Nesting Depth:

depth(top) = 0 - if p is nested in p', depth(p) = depth(p') + 1
depth(static link) = depth(current) - 1

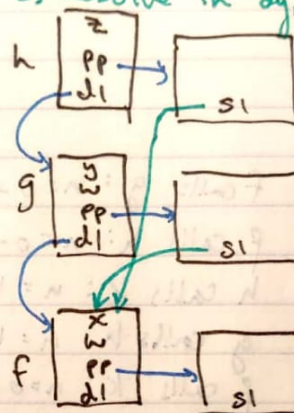
Nested Procedures:

nesting depth

```

def f() = {
  val x = 2
  val w = 5
  1 def g() = {
    val y = 3
    val w = 7
    x + y + h()
  }
  1 def h() = {
    val z = 4
    z + w
  }
  g()
}
    
```

- 1) h uses f's w: 5. Static scoping
- 2) h uses g's w: 7. Dynamic scoping.
 - 1) Resolve in statically enclosing proc.
 - 2) Resolve in dynamically calling proc.



To access variable v:

- $n = \text{depth}(\text{current}) - \text{depth}(\text{proc } w \text{ or } r)$
- Follow sl n times to get v.

f calls g:
g's sl: f's pp
g calls h:
h's sl: g's sl

check depth. ←
if ==, take →

While loop → nested procedure

```

def ml() = {
  var i = 0
  var j = 0
  def loop() = {
    if while (i < 10) {
      i = i + 1
      j = j + i
      loop()
    }
    loop()
  }
  i + j
}
    
```

To compute SL:

- $d(\text{SL}) = d(\text{current}) - 1$
- $n = \text{depth}(\text{caller}) - \text{depth}(\text{sl})$
- $= \text{depth}(\text{caller}) - \text{depth}(\text{curr}) + 1$

If $n = 0$, target sl = caller's pp
else, target sl = follows caller's sl. n times

1) f s o

h s 1

3

 $f(x)$

9 (1) 93

$$h(\gamma) \leq$$

S.V.

1005 E 3

3

3

falls $g: n = 0 - 1 + 1 = 0$

f calls h: $n = 0 - 1 + 1 = 0$

n = 1 - 2 + 1 = 0

g calls h : $n = 1 - 1 + 1 = 1$ h 's $SL = g$'s SL

f calls k: $n = 0 - 2 + 1 = -1$?? F can't call k

collee rollers
S.L. = FP

Oct 11, 2018

No name (lambdas)

increase = $\{ x \Rightarrow x+2 \}$

Undefined / not bound variable in an expression.

in $\{ x \rightarrow x + \text{increment} \}$:

↳ free

No free vars.

```
def increaseBy(inc: Int) {
```

def proc (x) = {x → x + inc} ← in LACS, this would be defined.

increase = increase by 8 \leftarrow call(proc)

increase (5) $118 + 5 = 123$

↑ call closure (closure: Code, ...)
 computes closure