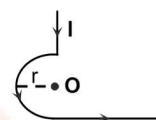


MAGNETIC EFFECT OF CURRENT & MAGNETISM

MULTIPLE CHOICE TYPE QUESTIONS

1. In the given figure, what is the magnetic field induction at point O?



- (A) $\frac{\mu_0 I}{4\pi r}$
- (B) $\frac{\mu_0 I}{4r} + \frac{\mu_0 I}{2\pi r}$
- (C) $\frac{\mu_0 I}{4r} + \frac{\mu_0 I}{4\pi r}$
- (D) $\frac{\mu_0 I}{4r} - \frac{\mu_0 I}{4\pi r}$

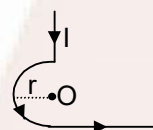
Sol. C

$$B_0 = |\vec{B}_1 + \vec{B}_2 + \vec{B}_3|$$

$$B_1 = 0 \Rightarrow B_0 = B_2 + B_3$$

$$\Rightarrow B_0 = \frac{1}{2} \left(\frac{\mu_0 I}{2r} \right) + \frac{1}{2} \left(\frac{\mu_0 I}{2\pi r} \right)$$

$$\Rightarrow B_0 = \frac{\mu_0 I}{4r} + \frac{\mu_0 I}{4\pi r}$$



2. Electrons at rest are accelerated by a potential of V volt. These electrons enter the region of space having a uniform, perpendicular magnetic induction field B. The radius of the path of the electrons inside the magnetic field is

(A) $\frac{1}{B} \sqrt{\frac{mV}{e}}$

(B) $\frac{1}{B} \sqrt{\frac{2mV}{e}}$

(C) $\frac{V}{B}$

(D) $\frac{1}{B} \sqrt{\frac{V}{e}}$

Sol. B

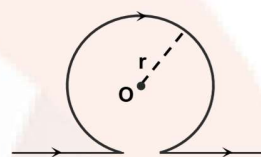
The gain in K.E. of the electron after moving through the potential difference

$$V = eV = \frac{1}{2}mv^2$$

$$\Rightarrow v = \sqrt{\frac{2eV}{m}}$$

$$\Rightarrow r = \frac{mv}{eB} = \frac{1}{B} \sqrt{\frac{2mV}{e}}$$

3. An infinitely long straight conductor is bent into shape as shown in figure. It carries a current I A. and the radius of circular loop is r metre. Then the magnetic induction at the centre of the circular loop is:



(A) 0

(B) ∞

(C) $\frac{\mu_0 i}{2\pi r}(\pi + 1)$

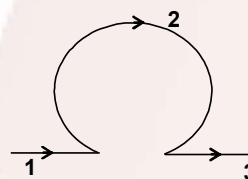
(D) $\frac{\mu_0 i}{2\pi r}(\pi - 1)$

Sol. **D**

$$B_0 = B_1 - B_2 + B_3$$

$$\Rightarrow B_0 = \frac{\mu_0 i}{4\pi r} - \frac{\mu_0 i}{2r} + \frac{\mu_0 i}{4\pi r}$$

$$\Rightarrow B_0 = \frac{\mu_0 i}{2\pi r}[\pi - 1].$$



4. In a hydrogen atom the electron is making 6.6×10^{15} revolutions per second in a circular orbit of radius 0.53 \AA .

The field of induction produced at the position of the nucleus is approximately (T - Tesla).

- (A) zero (B) $3\pi T$
(C) $4\pi T$ (D) $0.4\pi T$

Sol. C

$$B = \frac{\mu_0 i}{2R}, i = \frac{q\omega}{2\pi}$$

$$\omega = 2\pi \times 6.6 \times 10^{15}$$

$$B = \frac{4\pi \times 10^{-7} \times 1.6 \times 10^{-19} \times 6.6 \times 10^{15}}{2 \times 0.53 \times 10^{-10}} = 3.98\pi \approx 4\pi T$$

5. Alpha particles ($m = 6.7 \times 10^{-27}$ kg, $q = +2e$) are accelerated from rest through a potential difference of 6.7 kV. Then, they enter a magnetic field $B = 0.2$ T perpendicular to their direction of their motion. The radius of the path described by them is

- (A) 8.375 m (B) 8.375 cm
(C) infinity (D) none of these

Sol. B

$$r = \frac{mv}{qB}, v = \sqrt{\frac{2k}{m}}$$

$$\Rightarrow r = \frac{\sqrt{2km}}{qB}$$

$$= \frac{\sqrt{2 \times 6.7 \times 10^{-27} \times 2 \times 1.6 \times 10^{-19} \times 6.7 \times 10^3}}{2 \times 1.6 \times 10^{-19} \times 0.2}$$

$$= \frac{6.7}{8} \times 10^{-1} = 0.08375 \text{ m} = 8.375 \text{ cm}$$

6. A long straight wire along the z-axis carries a current I in the negative z direction. The magnetic vector field \vec{B} at a point having coordinates (x, y) in the $z = 0$ plane is

(A) $\frac{\mu_0 I}{2\pi} \frac{(y\hat{i} - x\hat{j})}{(x^2 + y^2)}$

(B) $\frac{\mu_0 I}{2\pi} \frac{(x\hat{i} + y\hat{j})}{(x^2 + y^2)}$

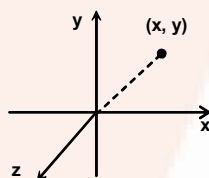
(C) $\frac{\mu_0 I}{2\pi} \frac{(x\hat{j} - y\hat{i})}{(x^2 + y^2)}$

(D) $\frac{\mu_0 I}{2\pi} \frac{(x\hat{i} - y\hat{j})}{(x^2 + y^2)}$

Sol. A

$$\vec{B} = d\vec{\ell} \times \vec{r} = -\frac{kx(x\hat{i} + y\hat{j})}{\sqrt{x^2 + y^2}}$$

$$\vec{B} = B\hat{B} = \frac{\mu_0 I}{2\pi} \frac{(y\hat{i} - x\hat{j})}{(x^2 + y^2)}$$



7. A circular coil of radius r carries a current I . If the same coil is now changed into a square loop carrying the same current, magnitude of its magnetic moment will

(A) increase

(B) decrease

(C) remain constant

(D) change depending upon the value of r

Sol. B

$$A_1 = \pi r^2$$

$$A_2 = L^2$$

$$2\pi r = 4L$$

$$L = \frac{\pi r}{2}$$

$$A_2 = \frac{\pi^2 r^2}{2}$$

$$\therefore A_2 > A_1$$

Hence, magnetic moment will increase.

8. Through two parallel wires A and B, 10 A and 2 A currents are passed, respectively, in opposite directions. If the wire A is infinitely long and the length of wire B is 2 m, then what will be the force on the conductor B which is situated 10 cm away from A?

(A) 6×10^{-5} N

(B) 9×10^{-5} N

(C) 8×10^{-5} N

(D) 10×10^{-5} N

Sol. C

$$F = \frac{\mu_0 I_1 I_2 \times \ell}{2\pi d} = \frac{4\pi \times 10^{-7} \times 10 \times 2 \times 2}{2\pi \times 10 \times 10^{-2}} = 8 \times 10^{-5}$$

N



9. An alpha particle and proton have same velocity when enter uniform magnetic field. The period of rotation of proton will be

(A) double of that of α particle

(B) four times that of α particle

(C) one half times that of α particle

(D) same as that of α particle.

Sol. C

$$T \propto r$$

$$r = \frac{mv}{qB}$$

$$\Rightarrow T \propto \frac{m}{q}$$

10. A magnetic field of $(0.004\hat{k})$ tesla exerts a force of $(4\hat{i} + 3\hat{j}) \times 10^{-10}\text{N}$ on a particle having charge of $1 \times 10^{-9}\text{C}$ and moving in $x - y$ plane. The velocity of particle is

- (A) $(75\hat{i} + 100\hat{j})\text{ms}^{-1}$ (B) $(75\hat{i} - 100\hat{j})\text{ms}^{-1}$
(C) $(-75\hat{i} + 100\hat{j})\text{ms}^{-1}$ (D) $(-75\hat{i} - 100\hat{j})\text{ms}^{-1}$

Sol. C

$$\vec{F} = q(\vec{v} \times \vec{B}) = [(4\hat{i} + 3\hat{j}) \times 10^{-10} = 1 \times 10^{-9}[(x\hat{i} + y\hat{j}) \times 0.004\hat{k}] =$$

$$1 \times 10^{-9}[-x \times 0.004\hat{j} + y \times 0.004\hat{i}]$$

$$3 \times 10^{-10} = -x \times 0.004 \times 10^{-9}$$

$$x = -\frac{3}{4} \times 100 = -75$$

$$y = 100$$

11. A proton, a deuteron and an α particle having same kinetic energy are moving in circular trajectories in a constant magnetic field. If r_p , r_d and r_α denote respectively the radii of trajectories of these particles, then,

- (A) $r_\alpha = r_p < r_d$ (B) $r_\alpha > r_p > r_d$
(C) $r_\alpha = r_d > r_p$ (D) $r_p = r_d = r_\alpha$

Sol. A

$$r = \frac{\sqrt{2km}}{qB}$$

$$r = \frac{\sqrt{m}}{q}$$

$$r_P \propto \frac{\sqrt{2m}}{q}$$

$$r_\alpha = \frac{\sqrt{4m}}{2q}$$

$$\Rightarrow r_P = r_\alpha < r_d$$

12. A circular loop of mass m and radius r is kept in a horizontal position (X-Y plane) on a table as shown in figure. A uniform magnetic field B is applied parallel to x-axis. The current I in the loop, so that its one point just lifts from the table, is:

- (A) $mg/\pi r^2 B$ (B) $mg/\pi r B$
(C) $mg/2\pi r B$ (D) $\pi r B/mg$

Sol. **B**

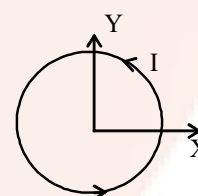
The magnetic moment of the loop is $\mu = \pi r^2 I$.

$$|\vec{\gamma}| = |\vec{\mu} \times \vec{B}|$$

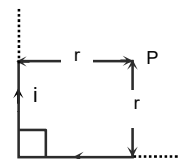
$$\Rightarrow \gamma = \pi r^2 IB.$$

For the loop to be just lifted,

$$mg r = \pi r^2 IB \Rightarrow I = \frac{mg}{\pi r B}.$$



13. The magnetic field strength at a point P distant r due to an infinite straight wire as shown in the figure carrying a current i is:



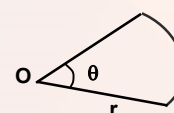
- (A) μ_0 (B) $\mu_0 i / 2\sqrt{2} r$
(C) $(\mu_0 i / \sqrt{2}\pi r)$ (D) $\frac{\mu_0 i}{4\pi r} [2 + \sqrt{2}]$

Sol. **D**

Magnetic field at P due to each of the straight wire will be directed inward and has the magnitude $\frac{\mu_0 i}{4\pi r} (\sin 45^\circ + \sin 90^\circ)$

Thus net field at P is $\frac{2\mu_0 i}{4\pi r} \left(1 + \frac{1}{\sqrt{2}}\right) = \frac{\mu_0 i}{4\pi r} (2 + \sqrt{2})$

14. A wire bent in the form of a sector of radius r subtending an angle θ° at centre, as shown in figure is carrying a current i. The magnetic field at O is:



- (A) $\frac{\mu_0 i}{2r} \theta$ (B) $\frac{\mu_0 i}{2r} (\theta / 180^\circ)$
(C) $\frac{\mu_0 i}{2r} (\theta / 360^\circ)$ (D) zero

Sol. **C**

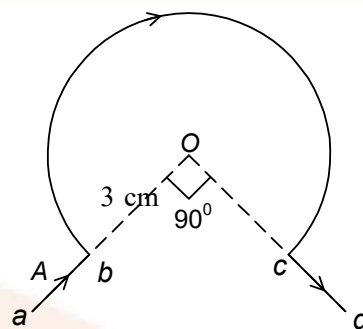
The magnetic field $B = \frac{\theta}{360^\circ} B_0$;

where $B_0 =$ magnetic field due to a circular loop $= \frac{\mu_0 i}{2r}$

$$\Rightarrow B = \frac{\theta}{360^\circ} \frac{\mu_0 i}{2r} = \frac{\mu_0 i}{2r} \left(\frac{\theta}{360^\circ} \right)$$

15. The conductor abcd carries a current of 4 A. The field at the centre O of the circular part of it is

- (a) $\frac{8\pi}{3} \times 10^{-5} \text{ T}$ (b) $2\pi \times 10^{-5} \text{ T}$
(c) $\frac{8\pi}{3} \times 10^{-4} \text{ T}$ (d) $2\pi \times 10^{-4} \text{ T}$



Sol. $B = \frac{\mu_0}{4\pi} \cdot \frac{2\pi ni}{r} = 10^{-7} \times \frac{2\pi \times \frac{3}{4} \times 4}{3 \times 10^{-2}} = 2\pi \times 10^{-5} \text{ T}$

\therefore (b)

16. A copper wire having resistance 0.01 ohm in each metre is used to wind a 400 turn solenoid of radius 1 cm and length 20 cm. Find the e.m.f of the battery which when connected across the solenoid will produce a magnetic field 1×10^{-2} tesla at the centre of solenoid.

- (a) 1 volt (b) 2 volts
(c) 2.5 volts (d) 3 volts

Sol. One turn has a length $= 2\pi r = 2\pi \times 1 \times 10^{-2} \text{ m}$

No. of turns = 400

\therefore Total length $= 400 \times 2\pi \times 10^{-2} \text{ m}$

Resistance (R) $= 400 \times 2\pi \times 10^{-2} \times 0.01 \text{ ohm}$

$= 800\pi \times 10^{-4} \text{ ohm}$

Magnetic field $= \mu_0 ni$

$$1 \times 10^{-2} = \mu_0 \times \frac{400}{20 \times 10^{-2}} \times i$$

$$\text{But } i = \frac{E}{R} = \frac{E}{8\pi \times 10^{-2}}$$

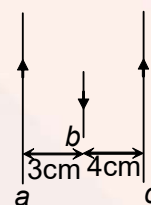
$$\frac{20 \times 10^{-2} \times 1 \times 10^{-2}}{400\mu_0} = \frac{E}{10^{-4} \times 800\pi}$$

$$E = \frac{800\pi \times 10^{-4} \times 20 \times 10^{-4}}{400 \times 4\pi \times 10^{-7}}$$

$$= 1 \text{ volt}$$

\therefore (a)

17. Currents of 3 A, 1 A and 2 A flow through the long, straight and parallel conductors a, b and c respectively as shown. A length 0.5 m of wire b experiences a force of



- (a) 10.0×10^{-6} N from right to left
- (b) 10.0×10^{-6} N from left to right
- (c) 5.0×10^{-6} N from right to left
- (d) 5.0×10^{-6} N from left to right

Sol. Force between the conductors a and b =

$$F_1 = \frac{\mu_0}{4\pi} \times \frac{2i_1 i_2}{r} \times 0.5 = 100 \times 10^{-7} \text{ N/m towards right.}$$

Force between the conductors c and b =

$$F_2 = \frac{\mu_0}{4\pi} \times \frac{2 \times 2 \times 1}{4 \times 10^{-2}} \times 0.5 = 50 \times 10^{-7} \text{ N/m towards left.}$$

$$(F_1 - F_2) = 50 \times 10^{-7} \text{ N/m towards right}$$

∴ (d)

18. Alpha particles ($m = 6.7 \times 10^{-27}$ kg, $q = + 2e$) are accelerated from rest through a potential difference of 6.7 kV. Then they enter a magnetic field $B = 0.2$ T perpendicular to their direction of motion. The radius of the path described by them is

(a) 8.375 m

(b) 8.375 cm

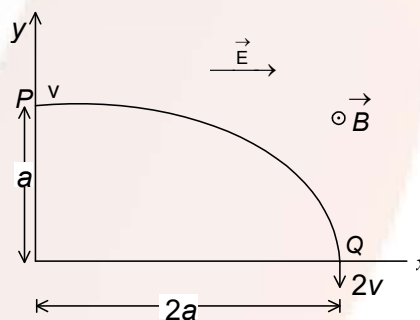
(c) infinity

(d) none of the above

Sol. $r = \frac{mv}{qB} = \frac{\sqrt{2Km}}{qB} = \frac{1}{B} \sqrt{\frac{2V}{q}} m = \frac{1}{0.2} \sqrt{\frac{2 \times 6.7 \times 10^3 \times 6.7 \times 10^{-27}}{2 \times 1.6 \times 10^{-19}}} = 8.375 \times 10^{-2}$ m

∴ (b)

19. A particle of charge $+q$ and mass m moving under the influence of a uniform electric field \vec{E} and a uniform magnetic field \vec{B} follows a trajectory from P to Q as shown in Figure.



The velocity at P and Q are $v\vec{i}$ and $-2v\vec{j}$. Which of the following statement/s is/are correct?

(a) $E = \frac{3}{4} \left(\frac{mv^2}{qa} \right)$

(b) Rate of work done by the electric field at P is $\frac{3}{4}\left(\frac{mv^3}{a}\right)$

(c) Rate of work done by the electric field at P is zero.

(d) Rate of work done by both of the fields at Q is different.

Sol. Work done by electric field = Gain in kinetic energy

$$\Rightarrow (qE) \times (2a) = \frac{1}{2}m[(2v)^2 - v^2]$$

$$\Rightarrow qE \times 2a = \frac{1}{2}m \times 3v^2 \Rightarrow E = \frac{3}{4}\left(\frac{mv^2}{qa}\right)$$

\therefore (a)

Rate of work done by electric field at P = $\vec{F} \cdot \vec{v} = (qE) \cdot v$

$$= qv \times \frac{3}{4}\left(\frac{mv^2}{qa}\right)$$

$$= \frac{3}{4}\left(\frac{mv^3}{a}\right)$$

\therefore (b)

20. A beam of charged particles of K.E. = 1 keV and $q = 1.6 \times 10^{-19}$ C and two masses 8×10^{-22} kg and 16×10^{-27} kg come out of an accelerator tube. And strike a plate at distance of 1 cm from the end of the tube, where the particles emerge perpendicularly. The value of the smallest magnetic field which can prevent the beam from striking the plate is

(a) 1.414 T

(b) 2.828 T

(c) 4.242 T

(d) 5.656 T

Sol. \vec{B} should be out of the paper. Let F be the magnetic force acting on the particles, where $F = (mv^2/r) = qvB$ since v is perpendicular to B . This force does not change the speed of the particles but it bends them into a circular arc of radius r , where $r = \left(\frac{mv}{qB}\right)$. The beam will not strike the plate, if the field is minimum, r is maximum. Hence

$$r_{\max} = \left(\frac{mv}{qB_{\min}}\right).$$

At the point A (see Figure), the beam is horizontal. Hence, the beam must describe a semi-circle, ABD with C as centre. Hence, $r_{\max} = 1.0 \text{ cm} = 10^{-2} \text{ m}$.

$$\therefore B_{\min} = \frac{mv}{q \times 10^{-2}} = \frac{mv}{(1.6 \times 10^{-19} \times 10^{-2})}$$

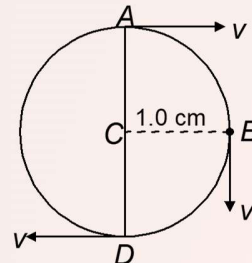
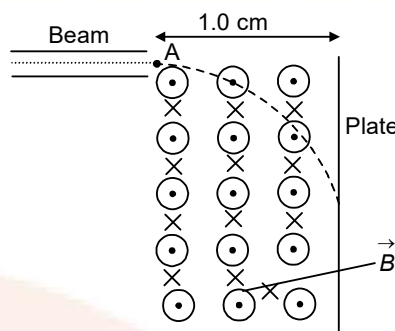
$$\text{Now } \frac{1}{2}mv^2 = \text{K.E.} = 1.0 \text{ keV}$$

$$= 10^3 \text{ eV}$$

$$= 10^3 \times 1.6 \times 10^{-19} \text{ J}$$

$$\text{or } v = (2 \times 10^3 \times 1.6 \times 10^{-19} \text{ J/m})^{1/2}.$$

$$B_{\min} = \frac{m \times \left(\frac{2 \times 10^3 \times 1.6 \times 10^{-19}}{m}\right)^{1/2}}{1.6 \times 10^{-19} \times 10^{-2}}$$



$$= \sqrt{m} \sqrt{\frac{2 \times 10^3 \times 1.6 \times 10^{-19}}{(1.6 \times 10^{-21})^2}} = \sqrt{m} \left[\frac{3.2 \times 10^{-16}}{2.56 \times 10^{-42}} \right]^{1/2}$$

$$= \sqrt{m} \times (1.25 \times 10^{26})^{1/2} = \sqrt{m} \times 1.1 \times 10^{13}$$

Hence, B_{\min} is more if m is more. The higher mass can be prevented from striking the plate, if

$$B_{\min} = \sqrt{16 \times 10^{-27}} \sqrt{1.25 \times 10^{13}}$$

$$= (\sqrt{1.6 \times 1.25}) = (\sqrt{2}) \text{ T} = 1.414 \text{ T}$$

\therefore (a)

21. A wire of length l carrying a current i is bent into a circle and placed in a magnetic field B . If the coil has only one turn, the maximum torque (τ) is

(a) $2l^2i B/\pi$

(b) $l^2i B/2\pi$

(c) $l^2i B/4\pi$

(d) $l^2i B/\pi$

Sol. A current carrying closed loop has a magnetic moment, $\mu = iA$ associated with it, where A = area of the coil.

$$l = 2\pi r \text{ or } r = \left(\frac{l}{2\pi} \right)$$

$$\text{Hence, } A = \pi r^2 = \frac{\pi l^2}{4\pi^2} = \left(\frac{l^2}{4\pi} \right)$$

$$\therefore \mu = iA = \frac{il^2}{4\pi}$$

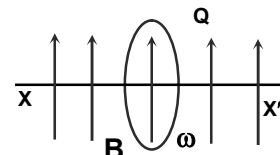
If the axis of the circular coil makes an angle θ with the field, torque = $\mu B \sin \theta$.

So maximum torque when $\theta = 90^\circ$,

$$\text{i.e., } \mu B = \frac{il^2 B}{4\pi}$$

\therefore (c)

22. A disc of mass m has a charge Q distributed on its surface. It is rotating about an XX' with a angular velocity ω . The force acting on the disc is, the magnetic field is B .

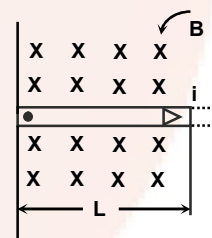


- (A) zero (B) $\omega RB/\pi$
(C) $2Q\omega BR$ (D) none of these

Sol. Since all the currents form closed loops in the uniform magnetic field, the force acting on the disc is zero.

\therefore (A)

23. A straight conductor of mass m and carrying a current i is hinged at one end and placed in a plane perpendicular to the magnetic field of intensity B as shown in the figure. At any moment if the conductor is let free, then the angular acceleration of the conductor will be (neglect gravity)



- (A) $\frac{2iB}{3m}$ (B) $\frac{3iB}{2m}$
(C) $\frac{iB}{2m}$ (D) $\frac{3i}{3mB}$

Sol. The force acting on the elementary portion of the current carrying conductor is given as,

$$dF = i(dr)B \sin 90^\circ$$

$$\Rightarrow dF = iBdr$$

The torque applied by dF about $O = d\tau = r dF$

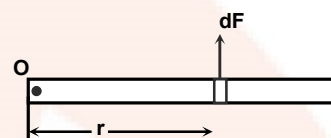
$$\Rightarrow \text{The total torque about } O = \tau = \int d\tau = \int r(iBdr)$$

$$\Rightarrow \tau = iB \int_0^L r dr = \frac{iBL^2}{2}$$

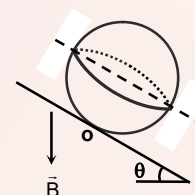
The angular acceleration $\alpha = \frac{\tau}{I}$

$$\Rightarrow \alpha = \left(\frac{iBL^2}{2} \right) / \left(\frac{mL^2}{3} \right) = \frac{3iB}{2m}$$

\therefore (B)



24. In the figure shown a coil of single turn is wound on a sphere of radius r and mass m . The plane of the coil is parallel to the inclined plane and lies in the equatorial plane of the sphere. If sphere is in rotational equilibrium the value of B is (current in the coil is i)



- (A) $\frac{mg}{\pi i r}$ (B) $\frac{mg \sin \theta}{\pi i}$
(C) $\frac{mgr \sin \theta}{\pi i}$ (D) none of these

Sol. The gravitational torque must be counter balanced by the magnetic torque about O, for equilibrium of the sphere. The gravitational torque

$$= \tau_{gr} = |\vec{mg} \times \vec{r}|$$

$$\Rightarrow \tau_{gr} = mgr \sin \theta$$

The magnetic torque $\vec{\tau}_m = \vec{\mu} \times \vec{B}$

Where the magnetic moment of the coil

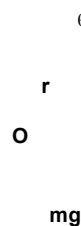
$$= \mu = (i \pi r^2)$$

$$\Rightarrow \tau_m = \pi i r^2 B \sin \theta$$

$$\pi i r^2 B \sin \theta = mgr \sin \theta$$

$$\Rightarrow B = \frac{mg}{\pi i r}$$

\therefore (A)

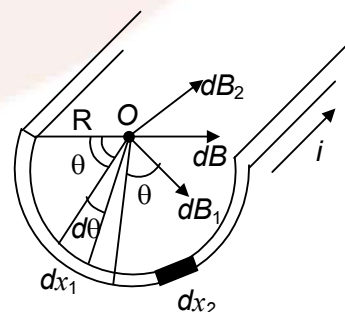


INTEGERS TYPE QUESTIONS

25. Find the magnetic induction B at a point on the axis due to an infinite thin conductor with semicircular cross-section of radius $R = 10$ cm carrying a uniform current $i = \pi$ amp.

Sol. Let R be the radius of semicircular cross-section and O, a point on the axis. Considering an element dx_1 carrying current di_1

$$di_1 = \frac{i dx_1}{\pi R}$$



Induction dB_1 at O due to di_1 is

$$dB_1 = \frac{\mu_o di}{2\pi R}$$

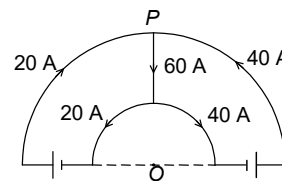
This is directed normal to line joining the element to O.

$$\begin{aligned} dB_1 &= \frac{\mu_o i}{2\pi R} \frac{dx_1}{\pi R} = \frac{\mu_o i}{2\pi^2 R^2} R d\theta \\ &= \frac{\mu_o i}{2\pi^2 R} d\theta \end{aligned}$$

Field dB_2 due to corresponding element dx_2 points in a direction shown. Resolving $d\vec{B}_1$ and $d\vec{B}_2$, $dB_1 \sin\theta$ and $dB_2 \sin\theta$ acting on same line and $dB_2 \cos\theta = dB_1 \cos\theta$ acting on opposite direction and hence cancelling each other.

$$\therefore B = \int_0^\pi dB_1 \sin\theta = \frac{\mu_o i}{2\pi^2 R} \int_0^\pi \sin\theta d\theta = \frac{\mu_o i}{\pi^2 R} = 4 \mu T$$

26. Two concentric coplanar semicircular conductors form part of two current loops as shown in the figure. If their radii are 11 cm and 4 cm calculate the magnetic induction at the centre.



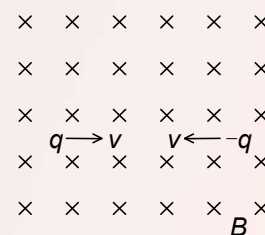
Sol. Magnetic induction at O = $\frac{1}{4} \frac{\mu_0}{2} \left(\frac{40}{r_1} - \frac{40}{r_2} \right) - \frac{1}{4} \frac{\mu_0}{2} \left(\frac{20}{r_1} - \frac{20}{r_2} \right)$

$$= \frac{4\pi \times 10^{-7}}{8} \left[20 \left(\frac{1}{r_1} - \frac{1}{r_2} \right) \right]$$

$$= \frac{4\pi \times 10^{-7}}{8} \left[20 \left(\frac{1}{4 \times 10^{-2}} - \frac{1}{11 \times 10^{-2}} \right) \right]$$

$$= 50 \mu \text{ weber/m}^2 \text{ (inward)}$$

27. Two particles P and Q, each having a mass $M = 1 \text{ mg}$ are placed at a separation $D = 4 \text{ m}$ in a uniform magnetic field $B = 1 \text{ T}$ as shown in figure. They have opposite charges of equal magnitude of $200 \mu\text{C}$. At time $t = 0$ the particles are projected towards each other, each with a speed v . Suppose the coulomb force between the charges is switched off. Find the maximum value v_m of the projection speed so that the two particles do not collide.



Sol. Force acting on P due to the magnetic field = Bqv .

This particle P will describe a circle in the clockwise direction whose radius is obtained from the equation

$$Bqv = \frac{mv^2}{r_1}$$

$$r_1 = \frac{mv}{qB}$$

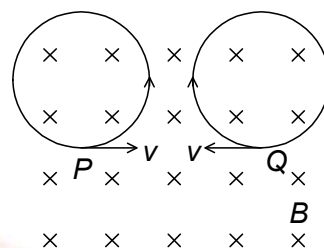
The particle Q will describe a circle in the anticlockwise direction $r_2 = \frac{mv}{qB}$

The two particles do not collide if $r_1 + r_2 \leq d$

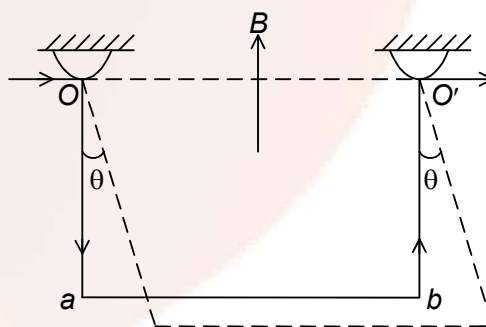
$$\frac{mv}{qB} + \frac{mv}{qB} \leq d$$

Maximum value of the projection speed,

$$v_{\max} = \frac{qBd}{2m} = 40 \text{ cm/s}$$

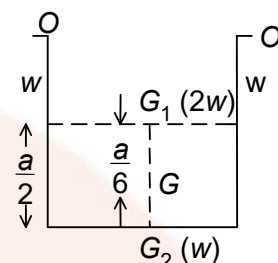


28. A copper wire with cross-sectional area 2.5 mm^2 and bent to make three sides of a square can turn about a horizontal axis OO' . The wire is located in a uniform vertical magnetic field. Find the magnetic induction, if on passing a current $I = 16 \text{ A}$ deflects by an angle



$\theta = 20^\circ$ (Specific gravity of copper = 8.9).

Sol. The deflection of the system is due to the force on the wire, due to the magnetic field B and the force is given by $= B I a$, where a is the side of the square and this force acts in the horizontal direction.



The moment of the force about the axis of rotation OO' =

$$B I a \times a \cos \theta = B I a^2 \cos \theta$$

where $\theta = 20^\circ$.

The weight of the wire is mg and this acts through the centre of gravity of the wire, G lying at a distance of $\frac{a}{2} + \frac{a}{6} = \frac{2a}{3}$ from OO' .

$$\therefore \text{moment of the weight about } OO' = mg \cdot \frac{2}{3} a \sin \theta$$

For the equilibrium of the system

$$\frac{2}{3} mg a \sin \theta = B I a^2 \cos \theta$$

$$\text{or } B = \frac{2 mg a \sin \theta}{3 I a^2 \cos \theta} = \frac{2 mg}{3 I a} \tan \theta$$

The mass m of the wire is given by

$$m = \text{Length of the wire} \times \text{cross-section} \times \text{density}$$

$$= 3a \times (2.5 \times 10^{-6} \text{ m}^2) (8900 \text{ kg/m}^3)$$

$$\therefore B = \frac{2}{3} \frac{3a(2.5 \times 10^{-6})(8900)(9.8)}{16 \times a} \tan 20^\circ$$

$$= 9900 \mu\text{T}$$

29. A beam of protons with a velocity $4 \times 10^5 \text{ m/sec}$ enters a uniform magnetic field of 0.3 Tesla at an angle of 60° to the magnetic field. Find the radius of the helical path taken by the proton beam. Also find the pitch of the helix, which is the distance travelled by a proton in the beam parallel to the magnetic field during one period of rotation.

[Mass of proton = $1.67 \times 10^{-27} \text{ Kg}$, charge on proton = $1.6 \times 10^{-19} \text{ C}$]

Sol. The velocity of particle can be resolved into two components $v \cos 60^\circ$, parallel and $v \sin 60^\circ$ perpendicular to direction of B.

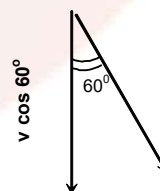
Due to parallel component of velocity ($= v \cos 60^\circ$), Lorentz force on proton is zero.

$$[F = q (v \cos 60^\circ) B \sin 0^\circ = 0]$$

Due to perpendicular component of velocity ($= v \sin 60^\circ$), Lorentz force on proton is

$$F = q (v \sin 60^\circ) B \sin 90^\circ = qv B \sin 60^\circ.$$

This force is \perp to the plane of paper, directed into it. Due to this force, proton will move on a circular path, having axis



along the direction of magnetic field. The radius of this circular path is given by

$$r = \frac{m(v \sin 60^\circ)}{qB} \quad \left[\therefore \frac{m(v \sin 60^\circ)^2}{r} = q(v \sin 60^\circ) B \right]$$

Due to simultaneous linear motion of proton along the direction of magnetic field, the proton will also move forward along the direction of B i.e. proton will spiral around the direction of \vec{B} .

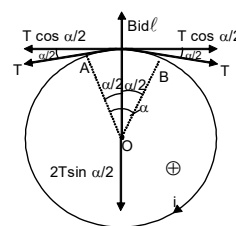
Hence, the radius of spiral or helical path is

$$\begin{aligned} r &= \frac{mv \sin 60^\circ}{qB} \\ &= \frac{(1.67 \times 10^{-27}) \times 4 \times 10^5 \times (\sqrt{3}/2)}{(1.6 \times 10^{-19}) \times 0.3} \\ &= 1.205 \times 10^{-2} \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Pitch of the helix} &= v \cos 60^\circ \times T = v \cos 60^\circ \times 2\pi r / v \sin 60^\circ \\ &= 2\pi r \cot 60^\circ = 2 \times 3.14 \times 1.205 \times 10^{-2} \times \frac{1}{\sqrt{3}} = 4.4 \text{ cm.} \end{aligned}$$

30. A loop of flexible conducting wire of length 0.5 m lies in a magnetic field of 1.0T perpendicular to the plane of the loop. Show that when a current is passed through the loop, it opens into a circle. Also calculate the tension developed in the wire if the current is 1.57 amp.

Sol. Consider small elemental length $d\ell$ of the loop when a current is passed through the loop in clock-wise direction and loop is placed in a downward magnetic field, then



force on each element will be directed radially outward and \perp to the element. Hence the loop opens into a circle.

Consider an element AB of length $d\ell$ of the circle of radius r subtending an angle α at the centre O. If T is the tension in the wire,

then force towards the centre will be equal to $2T \sin(\alpha/2)$ which is balanced by outward magnetic force on the current carrying element ($= Bid\ell$)

$$\text{i.e. } 2T \sin(\alpha/2) = Bid\ell$$

For small angle α , $\sin(\alpha/2) = \alpha/2$

$$\therefore 2T \frac{\alpha}{2} = Bid\ell \quad \text{or} \quad T = \frac{Bid\ell}{\alpha} = Bir, \quad \text{Putting } \alpha = \frac{d\ell}{r},$$

$$\text{we get } T = Bi \left(\frac{\ell}{2\pi} \right) = 1.57 \times 1.0 \times \left(\frac{0.5}{2 \times 3.14} \right) = \frac{1}{8} = 0.125\text{N}.$$