Ícaro Nunes - ICPC Library

Lembretes:

- Ler com cuidado

- Observar se arrays/segs/etc estão com tamanho de acordo com as constraints dadas e calculadas

- Checar se um grafo de entrada pode ter arestas repetidas

- Revisar assumptions feitas

- Observar casos base/edge

Formulas:

- Expected value of geometric distribution (expected number of failed Bernoulli trials before the first success, where p is the probability of a single success) $= \frac{1-p}{p}$

- Sum of arithemtic sequence:

  - $n \times \frac{(a_1 + a_n)}{2}$
  - $\frac{n}{2} \times [2a_1 + (n-1) \times d]$
  - Where: $a_1 =$ first term, $d =$ common difference, $n =$ number of terms in the range

- Law of sines:

  - $\frac{sin(A)}{a} = \frac{sin(B)}{b} = \frac{sin(C)}{c}$
  - Where $x =$ length of side opposed to angle X

- Law of cosines:

  - $a^2 = b^2 + c^2 - 2bc \times cos(A)$
  - Where $a =$ length of side opposed to angle A

Contents

1 Data Structures

1.1 Union-Find

```
// union find code
int parent[1123456];
int ranks[1123456];

int disjoint = 0;

// the use of ct and newSet()
// is useful in problems
// where the initial number
// of disjoint sets is unknown
// such as in Hoshen-Kopelman
int ct = 0;
int newSet() {
  ct++;
  disjoint++;
  parent[ct] = ct;
  ranks[ct] = 1;

  return ct;
}

// for "regular" disjoint-sets problems
// one must use this function to
// initialize the union_find
inline void init_union_find(int sz) {
  disjoint = sz;

  for(int i=1; i<=sz; i++) {
    parent[i] = i;
    ranks[i] = 1;
  }
}

// find using compression
int find(const int& v) {
  int root = parent[v];

  while(root != parent[root]) {
    parent[root] = parent[parent[root]];
    root = parent[root];
  }

  parent[v] = root;

  return root;
}

// merge using ranks
void merge(const int& a, const int& b) {
  int root_a = find(a);
  int root_b = find(b);

  if(root_a == root_b)
```

```
        return;

    if(ranks[root_b] > ranks[root_a]) {
        parent[root_a] = root_b;
        ranks[root_b] += ranks[root_a];
    } else {
        parent[root_b] = root_a;
        ranks[root_a] += ranks[root_b];
    }

    disjoint--;
}
// end union find code
```

1.2 Iterative Segment Tree

```
#include <vector>
#include <optional>

// Hash ef87f6
// segment tree - 0 indexed !
// space: 4n
// time:
// - range query: O(logn)
// - lower_bound: O(logn)
// - update: O(logn)
template<typename T, class Op>
struct STree {
        int size;

        // treesize -> smallest power
        // of 2 that is >= size
        // (the actual space taken by
        // the tree is 2*treesize)
        int ts;

        // items -> pointer to the
        // start of the leaves of
        // the segtree (implemented
        // as a perfect binary tree)
        T* it;

        // nodes -> pointer to the
        // whole tree, with an extra
        // unused node (nd[0])
        T* nd;

        // operation struct, must be
        // implemented as:
        // struct Op {
        //   T neutral;
        //   T operator()(const T& a, const T& b) {}
        // }
        Op op;

        STree(const std::vector<T>& from) {
                ts=1;

                while(ts < from.size())
                        ts <<=1;

                this->size = from.size();
                nd = new T[2*ts];
                it = nd+ts;

                for(int i=0; i<2*ts; i++)
                        nd[i] = op.neutral;

                for(int i=0; i<size; i++)
                        it[i] = from[i];

                for(int i=2*ts-1; i>1; i--)
                        nd[i>>1] = op(nd[i], nd[i>>1]);
        }

        void update(int idx, T val) {
                int i = ts+idx;

                nd[i] = val;
                i = i>>1;

                while(i>0) {
                        nd[i] = op(nd[i<<1], nd[(i<<1)+1]);
                        i>>=1;
                }
```

```
}

    T query(int l, int r) {
            T resl = op.neutral;
            T resr = op.neutral;

            r++;

            for(l += ts, r += ts; l<r; l>>=1, r>>=1) {
                    if(l&1) resl = op(resl, nd[l++]);
                    if(r&1) resr = op(nd[--r], resr);
            }

            return op(resl, resr);
    }

    ~STree() {
            delete nd;
    }

    // search for first ocurrence to the right of strt
    // of a value greater than or equal to v
    int lower_boundr(int strt, T v) {
            int i=ts+strt;

            // accumulated value
            T acc=nd[i];

            while(i>1 and !(acc >= v)) {
                    if(!(i&1) and op(acc, nd[i+1])>=v) break;
                    if(!(i&1)) acc = op(acc, nd[i+1]);
                    i>>=1;
            }

            if(i==1) return size;
            if(!(acc >= v)) i++;

            while(i<ts) {
                    if(op(acc, nd[i<<1])>=v) i <<= 1;
                    else acc = op(acc, nd[i<<1]), i = (i<<1) + 1;
            }

            return i-ts;
    }
};
```

1.3 SparseTable/RMQ

```
using namespace std;

// Hash 5a9566
// SparseTable:
// - construction O(nlogn)
// - query O(logn)
template<typename T, class Op>
struct SparseTable {
        const static int LOG = 23;
        vector<T> st[LOG];
        Op op;

        SparseTable(const vector<T>& f) {
                const int& n = f.size();

                st[0] = f;

                for(int c=1,l=1; (c << 1) <= n; c<<=1, l++) {
                        st[l].resize(n);

                        for(int i=0; i<n; i++)
                                st[l][i] = (i+c<n) ? op(st[l-1][i], st[l-1][i+c]) : st[l-1][i];
                }
        }

        virtual T query(int l, int r) {
                T res = op.neutral;

                while(l<=r) {
                        int len = r-l+1;
                        int log = 32 - __builtin_clz(len) - 1;
                        res = op(res, st[log][l]);
                        l += (1 << log);
                }

                return res;
        }
}
```

```
};

// Hash 501b00
// RMQ struct
// - range queries in O(1)
// - works for Operations that allow juxtaposition,
//   like min, max and gcd (idempotent functions)
template<typename T, class Op>
struct RMQ: SparseTable<T,Op> {
        RMQ(const vector<T>& f): SparseTable<T,Op> (f) {}

        T query(int l, int r) override {
                int len = r-l+1;
                int log = 32 - __builtin_clz(len) - 1;
                auto& opp = this->op; auto& stt = this->st;
                return opp(stt[log][l], stt[log][r-(1 << log)+1]);
        }
};


// example minimizer for numeric types
template<typename T>
struct Min {
        T neutral = numeric_limits<T>::max();
        T operator()(const T& a, const T& b) {
                return min(a, b);
        }
};
```

1.4 Mo's Algorithm

```
#include <vector>
using namespace std;

const int BLKSIZE=1e2;


// Hash 319b09
// OPTIONAL
inline int64_t hilbertOrder(int x, int y, int pow, int rotate) {
        if (pow == 0) {
                return 0;
        }
        int hpow = 1 << (pow-1);
        int seg = (x < hpow) ? (
                (y < hpow) ? 0 : 3
        ) : (
                (y < hpow) ? 1 : 2
        );
        seg = (seg + rotate) & 3;
        const int rotateDelta[4] = {3, 0, 0, 1};
        int nx = x & (x ^ hpow), ny = y & (y ^ hpow);
        int nrot = (rotate + rotateDelta[seg]) & 3;
        int64_t subSquareSize = int64_t(1) << (2*pow - 2);
        int64_t ans = seg * subSquareSize;
        int64_t add = hilbertOrder(nx, ny, pow-1, nrot);
        ans += (seg == 1 || seg == 2) ? add : (subSquareSize - add - 1);
        return ans;
}
//------------

// Hash d56199
struct Query {
        int l, r, idx;
        int64_t ord;

        Query(int l, int r, int idx) : l(l), r(r), idx(idx) {
                ord = hilbertOrder(l, r, 21, 0);
        }

        bool operator < (const Query& other) const {
                // return ord < other.ord;
                int i1 = l/BLKSIZE, i2 = other.l/BLKSIZE;
                if(i1 == i2) return (i1%2 ? r > other.r : r < other.r);
                return i1 < i2;
        }
};

int add(int i) {
        // TODO
}
```

```
int remove(int i) {
        // TODO
}


void process(const vector<Query>& queries) {
        vector<int> res(queries.size());

        for(const auto& query: queries) {
                while(l > query.l)
                        add(--l);

                while(r < query.r)
                        add(++r);

                while(l < query.l)
                        remove(l++);

                while(r > query.r)
                        remove(r--);

                res[query.idx] = ans;
        }
}
```

2 Graph

2.1 Dijkstra

```
#include <algorithm>
#include <limits>
#include <queue>
#include <stack>
#include <vector>


template<typename T>
void dijkstra(const std::vector<std::pair<T, int>>* graph, bool* visited, T* dist, int* parent, int root
        , int n) {
    for(int i=1; i<=n; i++)
        dist[i] = std::numeric_limits<T>::max();

    std::priority_queue<std::pair<T, int>, std::vector<std::pair<T, int>>, std::greater<std::pair<T, int
        >>> pq;

    pq.push({ 0, root });
    dist[root] = 0;
    parent[root] = root;

    while(!pq.empty()) {
        auto [dst, node] = pq.top();
        pq.pop();

        if(visited[node])
            continue;

        visited[node] = true;

        const std::vector<std::pair<T, int>>& adj = graph[node];

        for(const auto& [c_dst, child]: adj) {
            if(visited[child])
                continue;

            T newdst = dist[node] + c_dst;

            if(dist[child] > newdst) {
                dist[child] = newdst;
                pq.push({ newdst, child });
            }
        }
    }
}


// retrieve_path SEEMS TO BE NOT WORKING
//
// std::vector<int> retrieve_path(int tgt, int* parent) {
//    std::vector<int> ans;
//    int curr = tgt;
//    ans.push_back(tgt);
//
//    while(curr != parent[curr]) {
//      ans.push_back(parent[curr]);
//      curr = parent[curr];
```

```
//    }
//
//    std::reverse(ans.begin(), ans.end());
//
//    return ans;
// }
```

2.2 Toposort

```
#include <vector>
#include <stack>
#include <queue>

bool dfs(const std::vector<int>* graph, bool* visited, int* currtrav, std::stack<int>& ans, int node) {
        visited[node] = true;

        const std::vector<int>& adj = graph[node];

        bool poss = true;

        for(const int& child: adj) {
                if(currtrav[child] == currtrav[node]) {
                        poss = false;
                        break;
                }

                if(!visited[child]) {
                        currtrav[child] = currtrav[node];

                        if(!dfs(graph, visited, currtrav, ans, child)) {
                                poss = false;
                                break;
                        }
                }
        }

        if(!poss)
                return false;

        currtrav[node] = -1;
        ans.push(node);
        return true;
}

// dfs-based toposort
// returns an empty vector in case it finds a cycle
// (which means there is no valid topological order
// for the graph)
//
// PS. the array currtrav representes the origin node
// for the current traversal,it will be useful for
// finding if there are cycles
//
// PS2. removed std::optional since it only compiles on
// C++17 above, and judges such as SPOJ only supports up
// to C++14
std::vector<int> tarjan(const std::vector<int>* graph, bool* visited, int* currtrav, int n) {
        for(int i=1; i<=n; i++)
                currtrav[i] = -1;

        bool poss = true;

  std::stack<int> ans;

        for(int i=1; i<=n; i++) {
                if(visited[i])
                        continue;

                currtrav[i] = i;

                if(!dfs(graph, visited, currtrav, ans, i)) {
                        poss = false;
                        break;
                }
        }

        if(poss) {
                std::vector<int> v;

                while(!ans.empty()) {
                        v.push_back(ans.top());
                        ans.pop();
                }

                return v;
```

```
        } else
                return std::vector<int>();
}


// "bfs-based" toposort
// returns an empty vector in case it finds a cycle
// (which means there is no valid topological order
// for the graph)
//
// PS. removed std::optional since it only compiles on
// C++17 above, and judges such as SPOJ only supports up
// to C++14
std::vector<int> kahn(const std::vector<int>* graph, bool* visited, int* indeg, int n) {
  std::queue<int> q;

  for(int i=1; i<=n; i++) {
    if(indeg[i] == 0)
      q.push(i);
  }

  std::vector<int> ans;

  while(!q.empty()) {
    int node = q.front();
    q.pop();

    if(visited[node])
      continue;

    visited[node] = true;
    ans.push_back(node);

    const std::vector<int>& adj = graph[node];

    for(const int& child: adj) {
      indeg[child]--;

      if(indeg[child] == 0)
        q.push(child);
    }
  }

  if(ans.size() == n)
    return ans;
  else
    return std::vector<int>();
}
```

2.3 Prim/Kruskal

```
#include <queue>
#include <vector>
#include "../data-structure/union_find/union_find.h"

template<typename T>
T prim(const std::vector<std::pair<T, int>>* graph, bool* visited, int root) {
  using pTi = std::pair<T, int>;
  std::priority_queue<pTi, std::vector<pTi>, std::greater<pTi>> pq;

  T total = 0;

  pq.push({0, root});

  while(!pq.empty()) {
    auto [cost, node] = pq.top();
    pq.pop();

    if(visited[node])
      continue;

    visited[node] = true;
    total += cost;

    const std::vector<pTi>& adj = graph[node];

    for(const auto& [c_dist, child]: adj) {
      if(visited[child])
        continue;

      pq.push({c_dist, child});
    }
  }
}
```

```
  return total;
}


// for kruskal
template<typename T>
struct edge {
  int a, b;
  T c;

  bool operator<(const edge<T>& other) const {
    return c < other.c;
  }
};

template<typename T>
T kruskal(std::vector<edge<T>>& edges, int n) {

  init_union_find(n);

  sort(edges.begin(), edges.end());

  T total = 0;

  for(const edge<T>& e: edges) {
    int root_a = find(e.a);
    int root_b = find(e.b);

    if(root_a != root_b) {
      total += e.c;
      merge(root_a, root_b);
    }
  }

  return total;
}
```

2.4 Floyd-Warshall

```
#include <cstddef>
#include <limits>

template<typename T, std::size_t N, std::size_t M>
using Matrix = T[N][M];

// the adjacency matrix passed to floyd-warshall must contain
// weight of INF (numeric_limits<T>::max()) on pairs of nodes
// that are not adjacent, and 0 on the main diagonal
template<typename T, std::size_t N, std::size_t M>
void floydWarshall(const Matrix<T, N, M>& graph, Matrix<T, N, M>& dist, int n) {
  const T INF = std::numeric_limits<T>::max();

  for(int i=1; i<=n; i++)
    for(int j=1; j<=n; j++)
      dist[i][j] = graph[i][j];

  // k -> intermediate node
  for(int k=1; k<=n; k++) {
    // i -> source
    for(int i=1; i<=n; i++) {
      // j -> target
      for(int j=1; j<=n; j++) {
        T newdist;

        if(dist[i][k] == INF || dist[k][j] == INF)
          newdist = INF;
        else
          newdist = dist[i][k] + dist[k][j];

        dist[i][j] = min(dist[i][j], newdist);
      }
    }
  }
}
```

3 Math

3.1 FFT (recursive)

```
#include <iostream>
#include <math>

const long double PI = std::arccos(-1);
```

```
template<typename T>
struct Complex {
    T a, b;

    Complex(T a, T b) {
        this->a = a;
        this->b = b;
    }

    Complex(T a) {
        this->a = a;
        this->b = 0;
    }

    Complex operator+(const Complex& other) const {
        return Complex(a+other.a, b+other.b);
    }

    Complex operator-(const Complex& other) const {
        return Complex(a-other.a, b-other.b);
    }

    Complex operator*(const T& real) const {
        return Complex(a*real, b*real);
    }

    Complex operator*(const Complex& other) const {
        return Complex(a*other.a - b*other.b, a*other.b + b*other.a);
    }
};


// works for a power of 2 sized vector
// T must be a floating point type because
// of the trigonometric operations
template<typename T>
vector<Complex<T>> fft(const vector<T>& p) {
    int n = p.size();

    vector<Complex<T>> ans(n);

    if(n == 1) {
        ans[0] = Complex<T>(p[0]);
        return ans;
    }

    T angle = (2*PI)/n;
    Complex<T> w = Complex<T>(std::cos(angle), std::sin(angle));

    vector<T> pe(n/2), po(n/2);
    for(int i=0; i<=n-2; i+=2)
        pe[i/2] = p[i], po[i/2] = p[i+1];

    vector<Complex<T>> ye = fft(pe), yo = fft(po);

    Complex<T> w_i = Complex<T>(T(1));

    for(int i=0; i<n/2; i++) {
        ans[i] = ye[i] + w_i*yo[i];
        ans[i+n/2] = ye[i] - w_i*yo[i];
        w_i = w_i*w;
    }

    return ans;
}


// works for a power of 2 sized vector
// T must be a floating point type because
// of the trigonometric operations
template<typename T>
vector<Complex<T>> ifft(const vector<Complex<T>>& p) {
    int n = p.size();

    vector<Complex<T>> ans(n);

    if(n == 1) {
        ans[0] = Complex<T>(p[0]);
        return ans;
    }

    T angle = (2*PI)/n;
    Complex<T> w = (1/double(n)) * Complex<T>(std::cos(-angle), std::sin(-angle));
```

```cpp
        vector<T> pe(n/2), po(n/2);
        for(int i=0; i<=n-2; i+=2)
                pe[i/2] = p[i], po[i/2] = p[i+1];

        vector<Complex<T>> ye = ifft(pe), yo = ifft(po);

        Complex<T> w_i = Complex<T>(T(1));

        for(int i=0; i<n/2; i++) {
                ans[i] = ye[i] + w_i*yo[i];
                ans[i+n/2] = ye[i] - w_i*yo[i];
                w_i = w_i*w;
        }

        return ans;
}



std::ostream& operator<<(std::ostream& os, const Complex<T>& c) {
        os << "Complex(" << c.a << ", " << c.b << ")";
        return os;
}
```

3.2   FFT (in-place)

```cpp
using ld = long double;
using cd = complex<ld>;
const ld PI = acos(-1);

// Hash 7436b9
int reverse(int num, int lg_n) {
    int res = 0;
    for (int i = 0; i < lg_n; i++) {
        if (num & (1 << i))
            res |= 1 << (lg_n - 1 - i);
    }
    return res;
}

// Hash 6a7da6
void fft(vector<cd> & a, bool invert) {
    int n = a.size();
    int lg_n = 0;
    while ((1 << lg_n) < n)
        lg_n++;

    for (int i = 0; i < n; i++) {
        if (i < reverse(i, lg_n))
            swap(a[i], a[reverse(i, lg_n)]);
    }

    for (int len = 2; len <= n; len <<= 1) {
        ld ang = 2 * PI / len * (invert ? -1 : 1);
        cd wlen(cos(ang), sin(ang));
        for (int i = 0; i < n; i += len) {
            cd w(1);
            for (int j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
    }

    if (invert) {
        for (cd & x : a)
            x /= n;
    }
}
```

3.3   Matrix Multiplication

```cpp
#include <cstddef>


template<typename T, std::size_t N>
using Matrix = T[N][N];

template<typename T, std::size_t N>
void cp(const Matrix<T, N>& src, Matrix<T, N>& tgt) {
  for(int i=0; i<N; i++)
```

```cpp
        for(int j=0; j<N; j++)
            tgt[i][j] = src[i][j];
}

template<typename T, std::size_t N>
void matmul(const Matrix<T, N>& a, const Matrix<T, N>& b, Matrix<T, N>& dst, const int MOD) {
  Matrix<T, N> tmp;

  for(int i=0; i<N; i++) {
    for(int j=0; j<N; j++) {
      T sum = 0;

      for(int l=0; l<N; l++) {
        sum += (a[i][l]*b[l][j])%MOD;
        sum %= MOD;
      }

      tmp[i][j] = sum;
    }
  }

  cp(tmp, dst);
}
```

4   Geometry

4.1   Point2D

```cpp
#include <bits/stdc++.h>
using namespace std;
using ll=long long;

template<typename T>
struct Point {
        T x,y;

        Point() = default;
        Point(T x, T y) : x(x), y(y) {}

        bool operator<(const Point& o) const {
                if(x == o.x) return y<o.y;
                return x<o.x;
        }

        // Point operator
        Point operator+(const Point& o) const {
                return Point(x+o.x, y+o.y);
        }

        Point operator-(const Point& o) const {
                return Point(x-o.x, y-o.y);
        }
};

template<typename T>
T dot(const Point<T>& a, const Point<T>& b) {
        return a.x*b.x + a.y*b.y;
}

template<typename T>
T cross(const Point<T>& a, const Point<T>& b) {
        return a.x*b.y - a.y*b.x;
}

using point = Point<ll>;
```

4.2   Convex Hull

```cpp
#include <bits/stdc++.h>
#include <point.h>
using namespace std;

// Convex Hull, runs in O(n) for sorted list
// pts must be vector of at least 3 points
// SORTED with pair sort
// Returns: points of convex hull in ccw order
vector<point> convex_hull(const vector<point>& pts) {
        const int& n = pts.size();

        vector<point> hull = { pts[0], pts[1] };

        for(int i=2; i<n; i++) {
                while(hull.size() > 1 and cross(pts[i] - hull[hull.size()-2], hull.back() - hull[hull.
                        size()-2]) < 0)
```

```
                hull.pop_back();
            hull.push_back(pts[i]);
    }

    int lhsize = hull.size();
    hull.push_back(pts[n-2]);

    for(int i=n-3; i>=0; i--) {
        while(hull.size() > 1 and cross(pts[i] - hull[hull.size()-2], hull.back() - hull[hull.
                size()-2]) < 0)
            hull.pop_back();
        hull.push_back(pts[i]);
    }
    hull.pop_back();

    return hull;
}
```

5 Number Theory

5.1 Divisors

```
#include <bits/stdc++.h>

// regular implementation
// - time complexity: O(sqrt(n))
// - space complexity: O(sqrt(n))
template<typename Integer>
std::vector<Integer> find_divisors(Integer val) {
    std::vector<Integer> v;
    std::stack<Integer> finals;

    Integer root = sqrt(val);

    // this less than or equal to is important
    // to avoid edge case like in find_divisors(20),
    // where sqrt(20) == 4, and therefore, in a
    // mistake I previously made, my algorithm was
    // checking "root" separately, only to check
    // if the square root was exact. Even though
    // 4 is not the exact square root of 20, it is
    // still a divisor of 20, and that version of
    // the algorithm would output { 1, 2, 10, 20 }
    // instead of { 1, 2, 4, 5, 10, 20 }. Another
    // fix was to keep the separate check, but
    // using ceil-rounded (instead of floor-rounded)
    // square root.
    for(Integer i=1; i<=root; i++) {
        if(val%i == 0) {
            v.push_back(i);

            Integer div = val/i;

            if(div != i)
                finals.push(div);
        }
    }

    while(!finals.empty()) {
        v.push_back(finals.top());
        finals.pop();
    }

    return v;
}
```

5.2 Fexp/Modular Inverse

```
template<typename T>
T fexp(T x, T exp, const T MOD) {
    T cursor = 1;
    T ans = 1;
    T currpow = x;

    while(cursor <= exp) {
        if(cursor & exp)
            ans = (ans%MOD) * (currpow%MOD) %MOD;

        cursor <<= 1;
        currpow = currpow%MOD;
        currpow = (currpow*currpow)%MOD;
    }

    return ans;
}

template<typename T>
T inv(T x, const T MOD) {
    return fexp(x, MOD-2, MOD);
}
```

5.3 Gcd/Lcm

```
template<typename T>
T gcd(T a, T b) {
    if(a == b)
        return a;

    if(b > a)
        return gcd(b, a);

    if(!b) return a;
    return gcd(b, a%b);
}

template<typename T>
T lcm(T a, T b) {
    return a*b/gcd(a, b);
}
```

5.4 Sieve/Factors

```
#include <cmath>
#include <vector>

void sieve(bool* prime, std::vector<int>& primes, const int MAX_V) {
    for(int i=2; i<MAX_V; i++) {
        prime[i] = true;
    }

    int root = std::sqrt(MAX_V);

    for(int i=2; i<=root; i++) {
        if(!prime[i])
            continue;

        primes.push_back(i);

        for(int j=i; j <= MAX_V; j+=i) {
            prime[j] = false;
        }
    }

    for(int i=root; i<MAX_V; i++) {
        if(prime[i])
            primes.push_back(i);
    }
}

std::vector<std::pair<int, int>> factors(const int& x, const std::vector<int>& primes) {
    std::vector<std::pair<int, int>> res;

    int rem = x;

    for(const int& p: primes) {
        if(p > rem)
            break;

        if(rem % p != 0)
            continue;

        int amt = 0;

        while(rem % p == 0) {
            rem /= p;
            amt++;
        }

        res.push_back(std::make_pair(p, amt));
    }

    return res;
}
```

6 Strings

6.1 Z Function

```cpp
#include <vector>
#include <string>

// Hash abda49
std::vector<int> zstring(const std::string& s) {
        std::vector<int> z(s.size(), 0);

        int left = 0, right = 0;

        for(int k=1; k < s.size(); k++) {
                if(k > right) {
                        left = right = k;

                        while(right < s.size() && s[right] == s[right - left])
                                right++;

                        z[k] = right - left;

                        right--;
                } else /* k <= right */ {
                        int k1 = k - left;

                        if(z[k1] < right - k) {
                                z[k] = z[k1];
                        } else {
                                left = k;

                                while(right < s.size() && s[right] == s[right - left])
                                        right++;

                                z[k] = right - left;
                                right--;
                        }
                }
        }

        return z;
}

// Hash 756625
std::vector<int> match(const std::string& s, const std::string& pattern) {
        std::string pt = pattern + "$" + s;
        std::vector<int> z = zstring(pt);
        std::vector<int> res;

        for(int i=pattern.size() + 1; i < pt.size(); i++) {
                if(z[i] == pattern.size())
                        res.push_back(i - pattern.size() - 1);
        }

        return res;
}
```

6.2 Suffix Array

```cpp
#include <utility>
#include <string>
#include <vector>
#include <algorithm>
using namespace std;

// Hash dc9083
struct SuffixArray {
        int n;
        vector<int> p, lcp;
        string v;

        SuffixArray(const string& s) {
                n=s.size()+1, v=s+'\0';
                build();
                build_lcp();
        }

        // build suffix array of s
        // complexity: O(n*logn)
        void build() {
                p = vector<int>(n);
                vector<int> b(n),bp(n),bc(n),g(n),g_(n);

                for(int i=0; i<n; i++) p[i] = i;

                auto cmp=[&](int a, int b) {
```

```cpp
                        return v[a] < v[b];
                };
                sort(begin(p), end(p), cmp);

                g[p[0]]=0, bc[0]=1;
                for(int i=1,ct=0; i<n; i++)
                        if(v[p[i]] == v[p[i-1]]) g[p[i]]=ct, bc[ct]++;
                        else g[p[i]]=++ct, bc[ct]=1;

                for(int c=1,k=0; c<n; c<<=1,k++) {
                        auto& gg = (k&1) ? g_ : g;
                        auto& gg_ = (k&1) ? g : g_;

                        for(int i=0,sum=0; i<n; i++) bp[i]=sum,sum+=bc[i],bc[i]=bp[i];
                        for(int i=0; i<n; i++) b[bc[gg[(p[i]+c)%n]]++] = p[i];
                        for(int i=0; i<n; i++) p[bp[gg[b[i]]]++] = b[i];

                        gg_[p[0]]=0, bc[0]=1;
                        for(int i=1,ct=0; i<n; i++)
                                if(make_pair(gg[p[i]], gg[(p[i]+c)%n]) == make_pair(gg[p[i-1]], gg[(p[i
                                        -1]+c)%n]))
                                        gg_[p[i]]=ct, bc[ct]++;
                                else
                                        gg_[p[i]]=++ct, bc[ct]=1;
                }
        }

        void build_lcp() {
                lcp = vector<int>(n);
                vector<int> pos(n);
                for(int i=0; i<n; i++) pos[p[i]] = i;
                int k=0;
                for(int i=0, len=n-1; len>0; i++,len--,k=max(0,k-1)) {
                        int prv=p[pos[i]-1];
                        while(k<len)
                                if(v[i+k] == v[(prv+k)%n]) k++;
                                else break;
                        lcp[pos[i]] = k;
                }
        }
};
```

7 Others

7.1 Kadane

```cpp
template<typename T>
T kadane(T* arr, int n) {
  T curr = arr[0];
  T best = curr;

  for(int i=1; i<n; i++) {
    curr = max(arr[i], curr + arr[i]);
    best = max(best, curr);
  }

  return best;
}
```

8 Utils

8.1 Tester

```python
import random
import subprocess

MAX_N = 100


def gen_case() -> str:
    return f"1\n"

random.seed((1 << 9) | 31)

for i in range(100):
    print()
    print()
    case = gen_case()
    print(f"Test #{i+1}: ")
    print(case)
    # test bruteforce
```

```python
bf = subprocess.run(['out/b'], input=case, encoding='ascii', capture_output=True)
# test solution
sol = subprocess.run(['out/m'], input=case, encoding='ascii', capture_output=True)

bf_res = bf.stdout
sol_res = sol.stdout

print(f"bruteforce {bf_res}, solution {sol_res}")
```

```python
if bf_res == sol_res:
    print("accepted")
else:
    print("WA")
    break
```