

Coluna 1:

$X_i$	$f_i$	$F_i$	$h_i$	$F_h$	$X_i f_i$	$(X_i - \bar{x})^2 \cdot f_i$	$\bar{x} = 32/20 = 1,6$
0	3	3	15%	15%	0	$(0 - 1,6)^2 \cdot 3 = 10,8$	$Mo = 1$
1	6	9	30%	45%	6	$(1 - 1,6)^2 \cdot 6 = 4,8$	$MD = \frac{X_n + X_{n+1}}{2} = \frac{2+2}{2} = 2$
2	5	14	25%	70%	10	$(2 - 1,6)^2 \cdot 5 = 0,8$	$MD = 2$
3	2	16	10%	80%	6	$(3 - 1,6)^2 \cdot 2 = 4,2$	
4	4	20	20%	100%	16	$(4 - 1,6)^2 \cdot 4 = 17,6$	

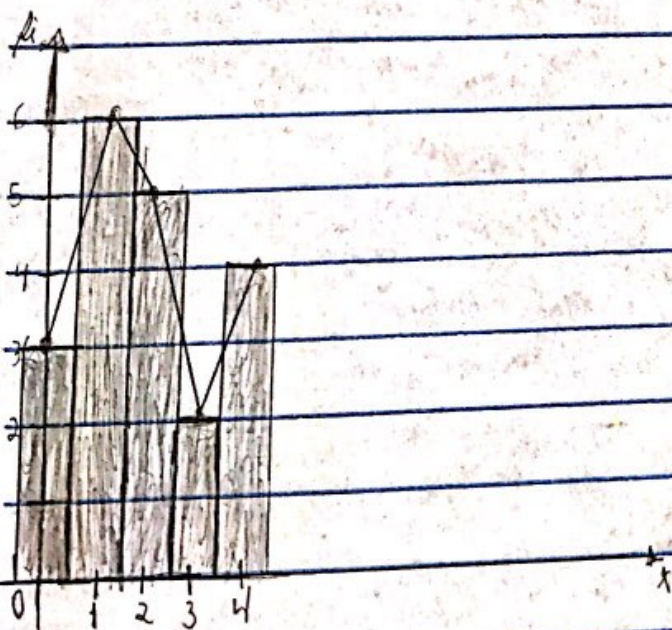
$$\sum X_i = 5 \quad \sum f_i = 20 \quad \sum h_i = 100\% \quad \sum (X_i \cdot h_i) = 38 \quad \sum (X_i - \bar{x})^2 \cdot f_i = 35,8$$

$$S_x^2 = \frac{\sum (X_i - \bar{x})^2 \cdot f_i}{n - 1}$$

$$S_x^2 = 1,88$$

$$S_x = \sqrt{\text{Variancia}}$$

$$S_x = 1,37$$





Coluna 2:

$X_i$	$p_i$	$F_i$	$h_i$	$F_n$	$X_i \cdot p_i$	$(X_i - \bar{X})^2 \cdot p_i$
160	20	20	25%	25%	3.200	$(160 - 161,66)^2 \cdot 20 = 55,11$
161	17	37	21,25%	46,25%	2.737	$(161 - 161,66)^2 \cdot 17 = 7,41$
162	19	56	23,75%	70%	3.078	$(162 - 161,66)^2 \cdot 19 = 2,2$
163	18	74	22,50%	92,5	2.934	$(163 - 161,66)^2 \cdot 18 = 32,32$
164	6	80	7,50%	100%	984	$(164 - 161,66)^2 \cdot 6 = 32,85$

$$\sum f_i (p_i)$$

$$\sum X_i p_i = 12.933$$

$$\sum (X_i - \bar{X})^2 p_i = 129,89$$

$$\bar{X} = 12.933 / 80 = 161,66$$

$$N_0 = 160$$

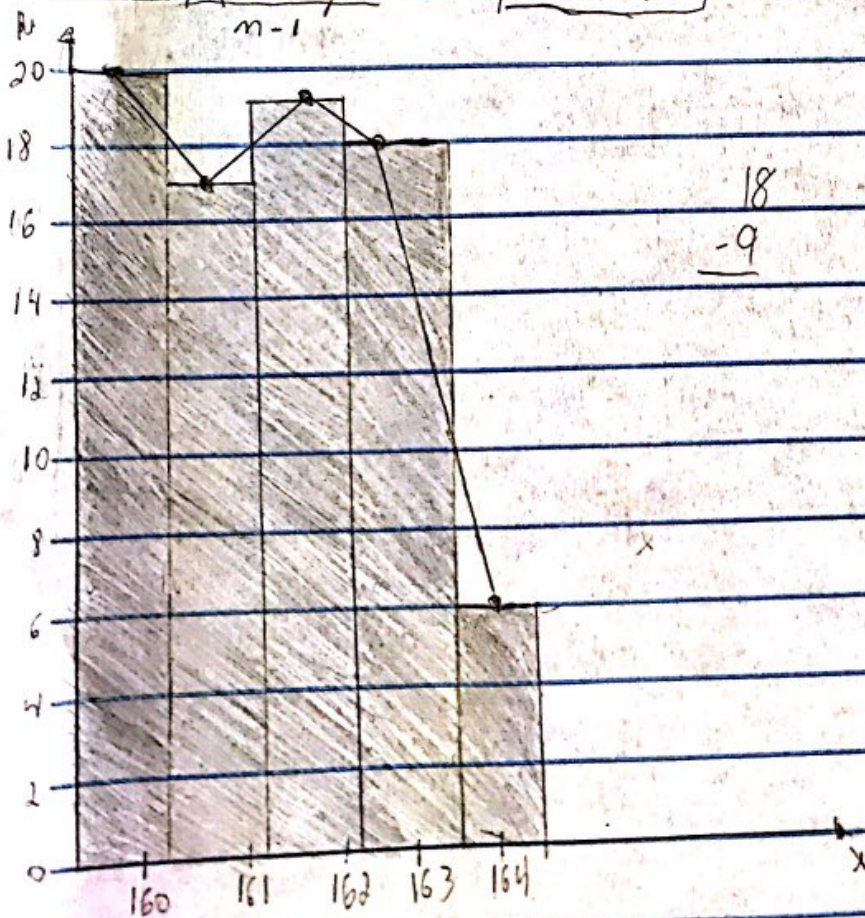
$$Md = \frac{X_{40} + X_{41}}{2} \rightarrow \frac{162 + 162}{2} \rightarrow Md = 162$$

Variancia Amostrai

Desvio Padrão

$$S_x = \frac{\sum (X_i - \bar{X})^2 \cdot p_i}{n-1} \rightarrow \boxed{S_x^2 = 1,64}$$

$$S_x = \sqrt{1,64} \rightarrow \boxed{S_x = 1,28}$$





Column 3:

$X_i$	$f_i$	$F_i$	$R_i$	$F_{ri}$	$X_i f_i$	$(X_i - \bar{X})^2 \cdot f_i$
0	3	3	6%	6%	0	$(0 - 9,74)^2 \cdot 3 = 284,6$
1	3	6	6%	12%	3	$(1 - 9,74)^2 \cdot 3 = 229,16$
2	3	9	6%	18%	6	$(2 - 9,74)^2 \cdot 3 = 179,72$
3	2	11	4%	22%	6	$(3 - 9,74)^2 \cdot 2 = 90,85$
4	3	14	6%	28%	12	$(4 - 9,74)^2 \cdot 3 = 98,84$
5	2	16	4%	32%	10	$(5 - 9,74)^2 \cdot 2 = 44,93$
6	2	18	4%	36%	12	$(6 - 9,74)^2 \cdot 2 = 27,97$
7	1	19	2%	38%	7	$(7 - 9,74)^2 \cdot 1 = 7,51$
8	2	21	4%	42%	16	$(8 - 9,74)^2 \cdot 2 = 6,06$
10	1	22	2%	44%	10	$(10 - 9,74)^2 \cdot 1 = 0,07$
11	6	28	12%	56%	66	$(11 - 9,74)^2 \cdot 6 = 9,53$
12	6	34	12%	68%	72	$(12 - 9,74)^2 \cdot 6 = 30,65$
13	2	36	4%	72%	26	$(13 - 9,74)^2 \cdot 2 = 21,26$
14	3	39	6%	78%	42	$(14 - 9,74)^2 \cdot 3 = 54,44$
15	1	40	2%	80%	15	$(15 - 9,74)^2 \cdot 1 = 27,67$
16	1	41	2%	82%	16	$(16 - 9,74)^2 \cdot 1 = 39,19$
17	3	44	6%	88%	51	$(17 - 9,74)^2 \cdot 3 = 158,12$
19	3	47	6%	94%	57	$(19 - 9,74)^2 \cdot 3 = 257,24$
20	3	50	6%	100%	60	$(20 - 9,74)^2 \cdot 3 = 315,80$
$\Sigma f_i (50)$		$\Sigma F_i (100\%)$				

$$\Sigma X_i f_i = 487$$

$$\Sigma (X_i - \bar{X})^2 \cdot f_i = 1823,64$$

$$\bar{X} = 487/50 \rightarrow \bar{X} = 9,74$$

$$M_0 = 11 \text{ e } 12$$

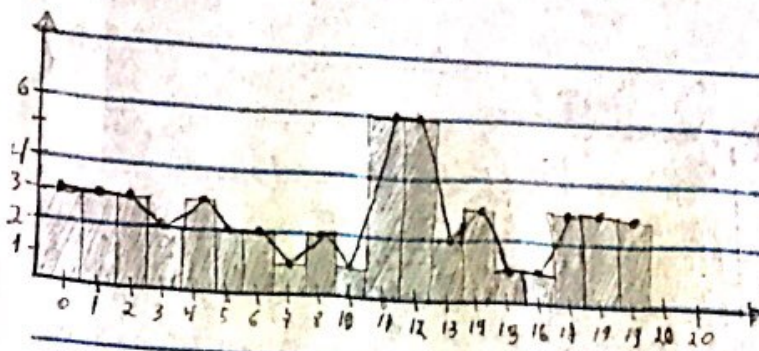
$$M_0 = X_{25} + X_{26} \rightarrow M_0 = 11 + 11 \rightarrow M_0 = 11 \text{ e } 12$$

$$S_{x^2} = \frac{\Sigma (X_i - \bar{X})^2 \cdot f_i}{n} = \frac{1823,64}{50} = 36,47$$

$$S_x = \sqrt{\frac{S_{x^2}}{n-1}} \rightarrow S_x = 6,20$$

MAXIMA





Column 4:

$X_i$	$n_i$	$F_i$	$h_i$	$F_n$	$X_i \cdot h_i$	$(X_i - \bar{X})^2 \cdot h_i$
50	3	3	5%	5%	150	$(50 - 59,3)^2 \cdot 3 = 259,47$
51	7	10	11,67%	16,67%	357	$(51 - 59,3)^2 \cdot 7 = 482,23$
52	3	13	5%	21,67%	156	$(52 - 59,3)^2 \cdot 3 = 159,87$
53	2	15	3,33%	25%	106	$(53 - 59,3)^2 \cdot 2 = 79,38$
54	3	18	5%	30%	162	$(54 - 59,3)^2 \cdot 3 = 84,27$
55	3	21	5%	35%	165	$(55 - 59,3)^2 \cdot 3 = 55,47$
56	3	24	5%	40%	168	$(56 - 59,3)^2 \cdot 3 = 32,67$
57	3	27	5%	45%	171	$(57 - 59,3)^2 \cdot 3 = 15,87$
58	3	30	5%	50%	174	$(58 - 59,3)^2 \cdot 3 = 9,07$
59	2	32	3,33%	53,33%	118	$(59 - 59,3)^2 \cdot 2 = 0,18$
60	2	34	3,33%	56,66%	120	$(60 - 59,3)^2 \cdot 2 = 0,98$
62	2	36	3,33%	59,99%	124	$(62 - 59,3)^2 \cdot 2 = 14,58$
63	5	41	8,33%	68,32%	315	$(63 - 59,3)^2 \cdot 5 = 68,45$
64	3	44	5%	73,32%	192	$(64 - 59,3)^2 \cdot 3 = 66,27$
65	3	47	5%	78,32%	195	$(65 - 59,3)^2 \cdot 3 = 97,47$
66	4	51	6,67%	84,99%	264	$(66 - 59,3)^2 \cdot 4 = 179,56$
67	1	52	1,67%	86,66%	67	$(67 - 59,3)^2 \cdot 1 = 59,29$
68	2	54	3,33%	89,99%	136	$(68 - 59,3)^2 \cdot 2 = 151,38$
69	2	56	3,33%	93,32%	138	$(69 - 59,3)^2 \cdot 2 = 188,18$
70	4	60	6,68%	100%	280	$(70 - 59,3)^2 \cdot 4 = 457,76$

$$\sum h_i = 60$$

$$\sum h_i = 99,99\% \rightarrow 100\%$$

$$\sum (X_i \cdot h_i) = 3.558$$

$$\sum (X_i - \bar{X})^2 \cdot h_i = 2458,6$$

$$\bar{X} = \frac{3558}{60} \rightarrow \bar{X} = 59,30$$

$$M_0 = 51$$

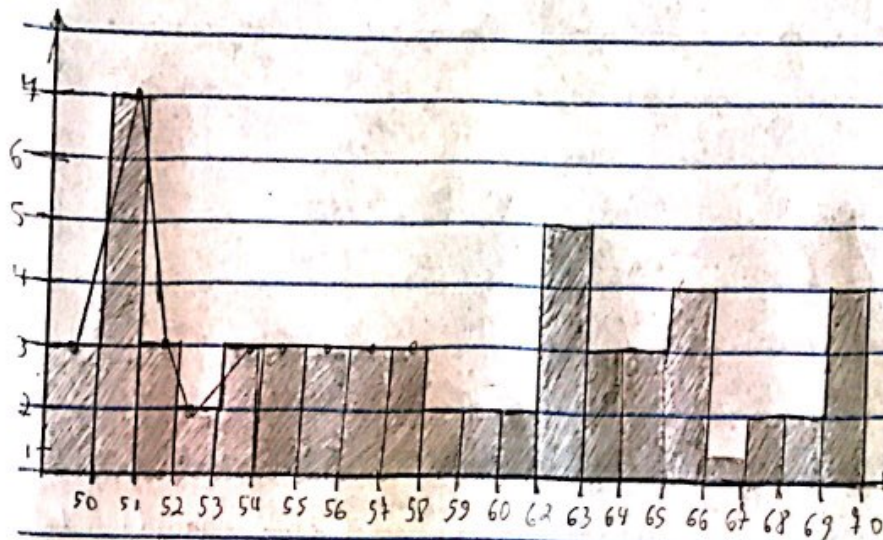
$$M_d = \frac{X_{50} + X_{51}}{2} = \frac{58 + 59}{2} = 58,5$$

$$S_{x^2} = \frac{2458,6}{60} + S_{x^2} = 41,69$$

$$S_x = 6,46$$

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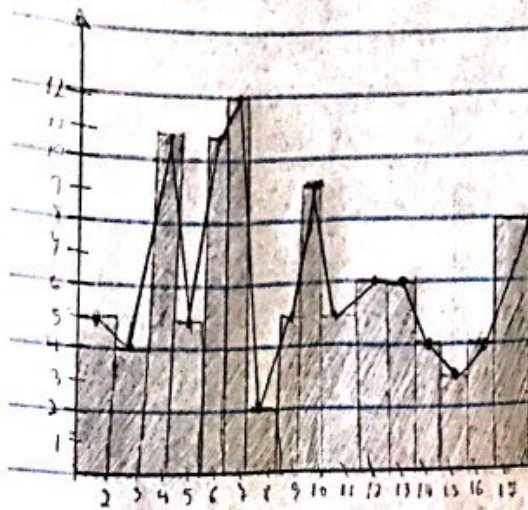
Column 5:

$X_i$	$f_i$	$F_i$	$h_i$	$F_i$	$X_i f_i$	$(X_i - \bar{X})^2 \cdot f_i$	
2	5	5	5%	5%	10	$(2 - 8,98)^2 \cdot 5 = 243,6$	$\bar{X} = \frac{898}{100} \rightarrow \bar{X} = 8,98$
3	4	9	4%	9%	12	$(3 - 8,98)^2 \cdot 4 = 143,04$	$h_i = 5$
4	11	20	11%	20%	44	$(4 - 8,98)^2 \cdot 11 = 292,8$	$MD = \frac{X_{50} + X_{51}}{2} = \frac{8+9}{2} = 8,5$
5	5	25	5%	25%	25	$(5 - 8,98)^2 \cdot 5 = 49,2$	
6	11	36	11%	36%	66	$(6 - 8,98)^2 \cdot 11 = 97,68$	$S_x^2 = \frac{1987,92}{99} \rightarrow S_x^2 = 20,08$
7	12	48	12%	48%	84	$(7 - 8,98)^2 \cdot 12 = 47,04$	$S_x = \sqrt{20,08} \rightarrow S_x = 4,48$
8	2	50	2%	50%	16	$(8 - 8,98)^2 \cdot 2 = 1,92$	
9	5	55	5%	55%	45	$(9 - 8,98)^2 \cdot 5 = 0$	
10	9	64	9%	64%	90	$(10 - 8,98)^2 \cdot 9 = 9,36$	
11	5	69	5%	69%	55	$(11 - 8,98)^2 \cdot 5 = 20,40$	
12	6	75	6%	75%	72	$(12 - 8,98)^2 \cdot 6 = 54$	
13	6	81	6%	81%	78	$(13 - 8,98)^2 \cdot 6 = 96,96$	
14	4	85	4%	85%	56	$(14 - 8,98)^2 \cdot 4 = 100,80$	
15	3	88	3%	88%	45	$(15 - 8,98)^2 \cdot 3 = 108,22$	
16	4	92	4%	92%	64	$(16 - 8,98)^2 \cdot 4 = 192,12$	
17	8	100	8%	100%	136	$(17 - 8,98)^2 \cdot 8 = 514,56$	
$\Sigma f_i = 100$		$\Sigma F_i = 100\%$	$\Sigma (X_i f_i) = 898$		$\Sigma (X_i - \bar{X})^2 \cdot f_i = 1987,92$		

MAXIMA

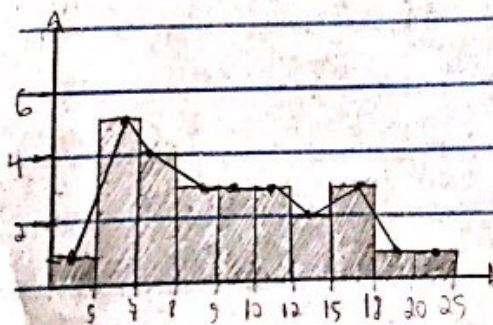
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Column 6:

$X_i$	$f_i$	$F_i$	$h_i$	$F_h$	$X_i f_i$	$(X_i - \bar{X})^2 h_i$	
5	1	1	3,85%	3,85%	5	$(5-11,23)^2 \cdot 1 = 38,81$	$\bar{X} = \frac{292}{26} = 11,23$
7	5	6	19,23%	23,08%	35	$(7-11,23)^2 \cdot 5 = 89,46$	$Mo = 7$
8	4	10	15,38%	38,46%	32	$(8-11,23)^2 \cdot 4 = 41,33$	$Md = \frac{X_n + X_{n+1}}{2} = \frac{9,5}{2}$
9	3	13	11,54%	50,00%	27	$(9-11,23)^2 \cdot 3 = 14,92$	
10	3	16	11,54%	61,54%	30	$(10-11,23)^2 \cdot 3 = 4,54$	$S_x^2 = 22,90$
12	3	19	11,54%	73,08%	36	$(12-11,23)^2 \cdot 3 = 1,98$	$S_x = \sqrt{22,90}$
15	2	21	7,69%	80,77%	30	$(15-11,23)^2 \cdot 2 = 28,43$	
18	3	24	11,54%	92,31%	54	$(18-11,23)^2 \cdot 3 = 137,50$	
20	1	25	3,85%	96,16%	20	$(20-11,23)^2 \cdot 1 = 76,91$	
25	1	26	3,85%	100,00%	23	$(25-11,23)^2 \cdot 1 = 138,53$	
$\Sigma f_i = 26$		$\Sigma F_i = 100\%$	$\Sigma X_i f_i = 292$		$\Sigma (X_i - \bar{X})^2 h_i = 572,61$		



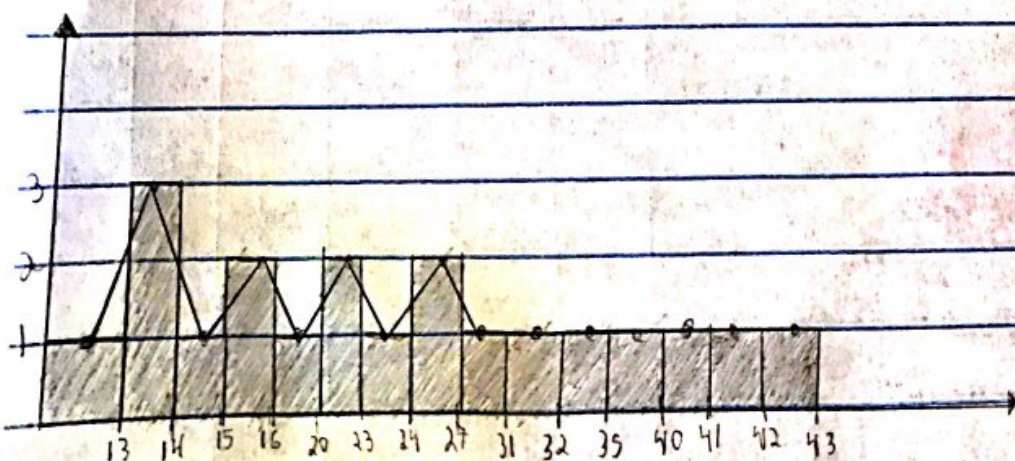
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Coluna 4:

$X_i$	$f_i$	$F_i$	$f_{\%}$	$F_{\%}$	$X_i \cdot f_i$	$(X_i - \bar{X})^2 \cdot f_i$	
13	1	1	5%	5%	13	$(13 - 25,5)^2 \cdot 1 = 156,25$	$\bar{X} = \frac{510}{20} = 25,5$
14	3	4	15%	20%	42	$(14 - 25,5)^2 \cdot 3 = 396,75$	
15	1	5	5%	25%	15	$(15 - 25,5)^2 \cdot 1 = 110,25$	$M_0 = 14$
16	2	7	10%	30%	32	$(16 - 25,5)^2 \cdot 2 = 180,50$	$M_d = \frac{X_{10} + X_{11}}{2} = 23,5$
20	1	8	5%	40%	20	$(20 - 25,5)^2 \cdot 1 = 30,25$	
23	2	10	10%	50%	46	$(23 - 25,5)^2 \cdot 2 = 12,50$	$S_x^2 = \frac{2085}{19} = 109,74$
24	1	11	5%	55%	24	$(24 - 25,5)^2 \cdot 1 = 2,25$	$S_x = \sqrt{109,74}$
27	2	13	10%	65%	54	$(27 - 25,5)^2 \cdot 2 = 4,50$	$S_x = 10,84$
31	1	14	5%	70%	31	$(31 - 25,5)^2 \cdot 1 = 30,25$	
32	1	15	5%	75%	32	$(32 - 25,5)^2 \cdot 1 = 42,25$	
35	1	16	5%	80%	35	$(35 - 25,5)^2 \cdot 1 = 90,25$	
40	1	17	5%	85%	40	$(40 - 25,5)^2 \cdot 1 = 210,25$	
41	1	18	5%	90%	41	$(41 - 25,5)^2 \cdot 1 = 240,25$	
42	1	19	5%	95%	42	$(42 - 25,5)^2 \cdot 1 = 292,25$	
43	1	20	5%	100%	43	$(43 - 25,5)^2 \cdot 1 = 306,25$	

$$\sum f_i = 20 \quad \sum f_i = 100\% \quad \sum X_i \cdot f_i = 510; \quad \sum (X_i - \bar{X})^2 \cdot f_i = 2.085$$

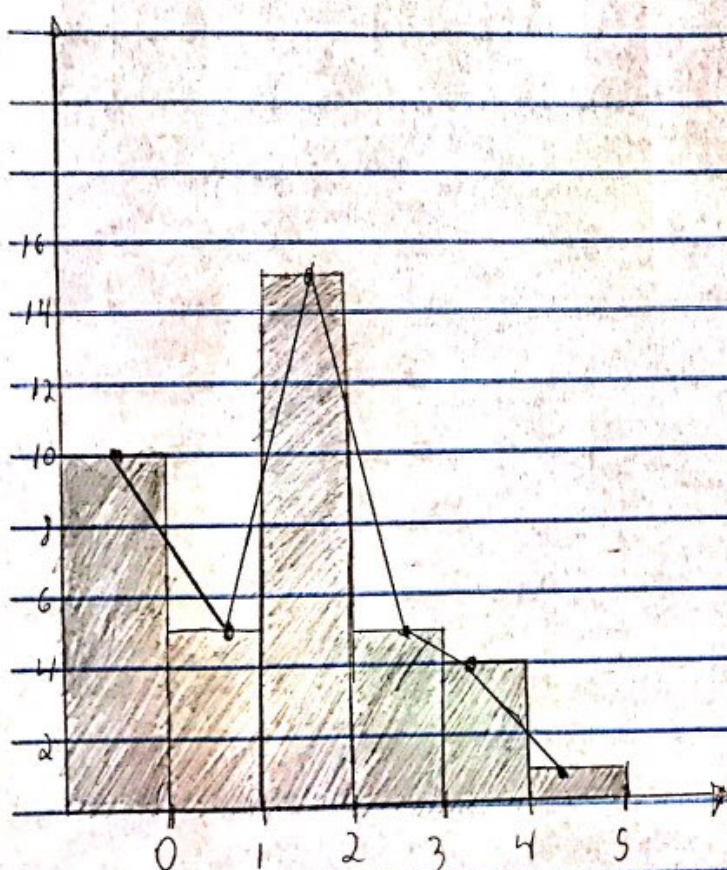




Column 8:

$X_i$	$f_i$	$F_i$	$f_n$	$F_n$	$X_i \cdot f_i$	$(X_i - \bar{X})^2 \cdot f_i$	
0	10	10	25%	25%	0	$(0 - 1,78)^2 \cdot 10 = 31,68$	$\bar{X} = \frac{71}{40} = 1,78$
1	5	15	12,50%	37,5%	5	$(1 - 1,78)^2 \cdot 5 = 5,04$	$M_0 = 2$
2	15	30	37,50%	75%	30	$(2 - 1,78)^2 \cdot 15 = 0,45$	$M_d = \frac{2+2}{2} = 2$
3	5	35	12,50%	87,5%	15	$(3 - 1,78)^2 \cdot 5 = 4,44$	$S_{x^2} = 1,92$
4	4	39	10%	97,5%	16	$(4 - 1,78)^2 \cdot 4 = 19,41$	$S_x = 1,39$
5	1	40	2,5%	100%	5	$(5 - 1,78)^2 \cdot 1 = 10,31$	

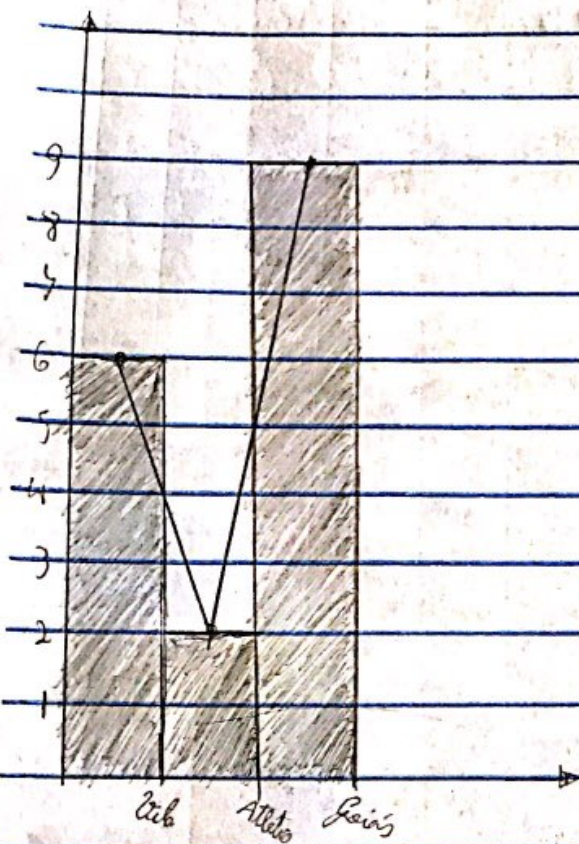
$$\sum f_i = 40; \quad \sum f_n = 100\% \quad \sum X_i \cdot f_i = 71 \quad \sum (X_i - \bar{X})^2 \cdot f_i = 74,91$$





Coluna 9:

$X_i$	$h_i$	$F_i$	$h_i$	$F_{ri}$
Vila	6	6	35,29%	35,29%
Aldeia	2	8	11,76%	47,05%
Grav	9	17	52,95%	100%
$\Sigma h_i = 17$			$\Sigma F_i = 99,99\% + 100\%$	





Coluna 10:

$X_i$	$h_i$	$F_i$	$h_i$	$F_i$	$X_i \cdot h_i$	$(X_i - \bar{X})^2 \cdot h_i$	
1	1	1	10%	10%	1	$(1-16)^2 \cdot 1 = 225$	$\bar{X} = 16$
5	1	2	10%	20%	5	$(5-16)^2 \cdot 1 = 121$	$M_0 = 7$
7	2	4	20%	40%	14	$(7-16)^2 \cdot 2 = 162$	$M = \frac{9+15}{2} = 12$
9	1	5	10%	50%	9	$(9-16)^2 \cdot 1 = 49$	
15	1	6	10%	60%	15	$(15-16)^2 \cdot 1 = 1$	$S_x^2 = 236,44$
17	1	7	10%	70%	17	$(17-16)^2 \cdot 1 = 1$	$S_x = 5,38$
18	1	8	10%	80%	18	$(18-16)^2 \cdot 1 = 4$	
27	1	9	10%	90%	27	$(27-16)^2 \cdot 1 = 121$	
54	1	10	10%	100%	54	$(54-16)^2 \cdot 1 = 1444$	

$$\sum p_i = 10 \quad \sum h_i = 100\% \quad \sum X_i \cdot h_i = 160 \quad \sum (X_i - \bar{X})^2 \cdot h_i = 2128$$

