

PHYSICAL CONSTANTS

Speed of Light $c = 3 \times 10^8 \text{ m/s}$

Plank constant $\hbar = 6.63 \times 10^{-34} \text{ Js}$ $hc = 1242 \text{ eV} \cdot \text{nm}$

Gravitation constant $G = 6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2$

Boltzmann constant $k = 1.38 \times 10^{-23} \text{ J/K}$

Molar gas constant $R = 8.314 \text{ J/mol K}$

Avogadro's number $N_A = 6.023 \times 10^{23}/\text{mol}$

Charge of electron $e = 1.602 \times 10^{-19} \text{ C}$

Permeability of vacuum $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$

Permittivity of vacuum $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$

Coulomb constant $1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N m}^2/\text{C}^2$

Faraday constant $F = 96485 \text{ C/mol}$

Mass of electron $m_e = 9.1 \times 10^{-31} \text{ kg}$

Mass of proton $m_p = 1.6726 \times 10^{-27} \text{ kg}$

Mass of neutron $m_n = 1.6749 \times 10^{-27} \text{ kg}$

Atomic mass unit $u = 1.66 \times 10^{-27} \text{ kg}$

Stefan-Boltzmann constant $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4$

Rydberg constant $R_\infty = 1.097 \times 10^7 \text{ m}$

Bohr magneton $\mu_B = 9.27 \times 10^{-24} \text{ J/T}$

Bohr radius $a_0 = 0.529 \times 10^{-10} \text{ m}$

Standard atmosphere $atm = 1.01325 \times 10^5 \text{ Pa}$

Wien displacement constant $b = 2.9 \times 10^{-3} \text{ mK}$

VECTORS

$$\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k} \quad |\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$$

$$\text{DOT PRODUCT } \vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z = ab \cos \theta$$

$$\text{CROSS PRODUCT } \vec{a} \times \vec{b} = ab \sin \theta$$

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = (a_y b_z - b_y a_z) \hat{i} - (a_x b_z - b_x a_z) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$$

DON'T FORGET AREA

KINEMATICS

$$\vec{V}_{avg} = \Delta \vec{s} / \Delta t \quad \vec{V}_{inst} = d\vec{s} / dt$$

$$\vec{a}_{avg} = \Delta \vec{v} / \Delta t \quad \vec{a}_{inst} = d\vec{v} / dt$$

$$s = ut + \frac{1}{2}at^2$$

$$v = u + at$$

$$v^2 = u^2 + 2as$$

$$\text{RELATIVE VELOCITY} \quad v_{A/B} = V_A - V_B$$

PROJECTILE MOTION

$$u_x = u \cos \theta \quad u_y = u \sin \theta$$

$$\text{Time of Flight} = 2u_y/g \Rightarrow T = 2u \sin \theta / g$$

$$\text{Range} = u_x \cdot T \Rightarrow R = u^2 \sin 2\theta / g$$

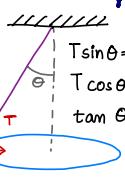
$$y = u \sin \theta \cdot t - \frac{1}{2} g t^2$$

LAWS OF MOTION

1st LAW: INERTIA $F = d\vec{P}/dt = ma$ 2nd LAW: Action \Rightarrow Reaction

Friction: $f_{static,maximum} = \mu_s N \quad f_{kinetic} = \mu_k N$

$$\text{Centripetal force} = \frac{mv^2}{r} = m\omega^2 r$$



$$\text{CURVED BANKING}$$

$$\frac{v^2}{rg} = \tan \theta \quad \frac{v^2}{rg} = \frac{\mu + \tan \theta}{1 - \mu \tan \theta}$$



WORK, POWER & ENERGY

$$\text{WORK} = \vec{F} \cdot \vec{s} = FS \cos \theta \quad KE = \frac{1}{2} mv^2 \quad \text{POTENTIAL ENERGY (U)}$$

$$\oint \vec{F} \cdot d\vec{s} = 0 \quad \left\{ \begin{array}{l} \text{Work by Conservative} \\ \text{force in a closed path} \end{array} \right.$$

$$\text{POWER} = dw/dt = \vec{F} \cdot \vec{v}$$

$$\text{WORK-ENERGY THEOREM}$$

$$W_{net} = \Delta K$$

$$U_g = mgh \quad \vec{F} = -\frac{dU}{dx}$$

$$U_{spring} = \frac{1}{2} kx^2 \quad \text{FOR CONSERVATIVE FORCES}$$

$$K+U = \text{Conserved}$$

CENTER OF MASS

$$x_{cm} = \frac{\sum x_i m_i}{\sum m_i} = \frac{\int x dm}{\int dm}$$

$$\vec{v}_{cm} = \frac{\sum m_i \vec{v}_i}{\sum m_i} \quad \vec{F} = m \vec{a}_{cm}$$

$$\text{HOLLOW CONE} = h/3 \quad \text{SOLID CONE} = h/4$$

$$\text{HOLLOW} \quad R/2$$

$$\text{SOLID} \quad 3R/8$$

COLLISION

$$m_1 \quad m_2 \quad m_1 \quad m_2$$

$$u_1 \quad u_2 \quad v_1 \quad v_2$$

MOMENTUM CONSERVATION {Always?}

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

$$m_1 > m_2$$

$m_1 \rightarrow$ Undisturbed motion

Solve using CoR in m_1 frame

$$\text{ELASTIC} \quad \text{INELASTIC}$$

$$\text{CAN BE NON ZERO}$$

$$CoR = e = \frac{V_{SEPARATION}}{V_{APPROACH}} = \frac{V_2 - V_1}{U_1 - U_2}$$

ENERGY CONSERVATION {Elastic}

$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

$$m_1 = m_2$$

Velocity Exchange for Elastic

RIGID BODY DYNAMICS

$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{d\theta}{dt} \quad \alpha = \frac{\Delta \omega}{\Delta t} = \frac{d\omega}{dt} \quad \vec{v} = \vec{\omega} \times \vec{r} \quad \vec{a}_{tan} = \vec{r} \times \vec{\alpha}$$

$$\vec{a}_{centri} = \omega^2 \vec{r}$$

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2 \quad \vec{l} = \vec{r} \times \vec{p} = mv \vec{\alpha}$$

$$\omega = \omega_0 + \alpha t \quad \vec{z} = I \vec{\alpha} = d\vec{l}/dt$$

$$\vec{a} = \vec{r} \times \vec{F} = \vec{r}_\perp F = \gamma F \sin \theta$$

EQUILIBRIUM: $F_{net} = 0 = Z_{net}$

$$\omega = 2\pi f \quad T = 1/f$$

MOMENT OF INERTIA

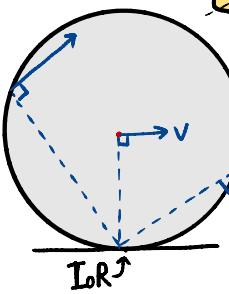
$$\begin{aligned} \text{RECTANGLE} &= \frac{ml^2}{12} \\ \text{RECTANGLE} &= \frac{m(a^2+b^2)}{12} \\ I = \sum m_i r_i^2 & \\ I = \int r^2 dm & \quad R_{\text{GYRATION}} = \sqrt{\frac{I}{M}} \end{aligned}$$

KINETIC ENERGY

$$K = \frac{1}{2}mv_c^2 + \frac{1}{2}I_c\omega^2$$

$$K = \frac{1}{2}I_H\omega^2 \quad \text{About Hinge or IOR}$$

$$a = \frac{g \sin \theta}{\left[1 + \frac{I}{mr^2}\right]} \quad v = \sqrt{\frac{2gH}{1 + \frac{I}{mr^2}}}$$



AXIS THEOREMS

$$I_z = I_x + I_y$$

$$\text{PERPENDICULAR}$$

$$\begin{aligned} \text{PARALLEL} & \\ I_{\parallel} &= I_{cm} + md^2 \end{aligned}$$

ROLLING MOTION

$$V = \omega r \quad (\text{no slip condition})$$

$$\begin{aligned} \text{IOR} & \text{ INSTANTANEOUS} \\ & \text{AXIS OF ROTATION} \\ \vec{V} &= \vec{\omega} \times \vec{r} \end{aligned}$$

$$\begin{aligned} t &= \frac{\pi w_0}{\mu g \left[1 + \frac{I}{mr^2}\right]} \\ t &= \frac{V_0}{\mu g \left[1 + \frac{I}{mr^2}\right]} \end{aligned}$$

GRAVITATION

$$F = G \frac{Mm}{R^2} \quad \text{POT. ENERGY (U)} = -G \frac{Mm}{R}$$

$$g = G \frac{M}{R^2} \quad g' = g \left[1 - \frac{1}{R_e}\right] \quad g' \approx g \left[1 - \frac{2h}{R_e}\right]$$

$$\begin{aligned} V_{\text{ORBITAL}} &= \sqrt{GM/R} \\ V_{\text{ESCAPE}} &= \sqrt{2GM/R} \\ g' &= g - \omega^2 R_e \cos^2 \theta \end{aligned}$$

KEPLER'S LAWS

- 1st Elliptical Orbits, Sun @ foci
- 2nd Equal Area in Equal time (ℓ^2)
- 3rd $T^2 \propto a^3$ [semi major axis]

SIM

$$\begin{aligned} \text{HOODLE'S LAW} & F = -kx \\ x &= A \sin(\omega t + \phi) \\ v &= Aw \cos(\omega t + \phi) \\ a &= -\omega^2 x = -kx/m \\ T &= \frac{2\pi}{\omega} = 2\pi \sqrt{m/k} \end{aligned}$$

$$\begin{aligned} T &= 2\pi \sqrt{l/g} \\ T &= 2\pi \sqrt{\frac{I}{mgL}} \end{aligned}$$

$$\begin{aligned} K &= \frac{1}{2}mv^2 \\ U &= \frac{1}{2}kx^2 \\ E &= K+U = \frac{1}{2}KA^2 = \frac{1}{2}m\omega^2A^2 \end{aligned}$$

$$\begin{aligned} \sigma &= k\theta \\ T &= 2\pi \sqrt{\frac{I}{K}} \end{aligned}$$

$$\begin{aligned} x_1 &= A_1 \sin(\omega t) \\ x_2 &= A_2 \sin(\omega t + \phi) \\ x &= x_1 + x_2 = A \sin(\omega t + \epsilon) \\ A &= \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \phi} \end{aligned}$$

$$\begin{aligned} \text{SERIES} & \quad \frac{1}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2} \\ \text{PARALLEL} & \quad K_{eq} = K_1 + K_2 \end{aligned}$$

PROPERTIES OF MATTER

$$\text{YOUNG'S MODULUS (Y)} = \frac{F/A}{\Delta L/L}$$

$$\text{BULK MODULUS (B)} = -V \frac{\Delta P}{\Delta V}$$

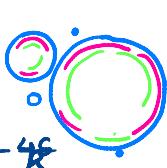
$$\text{POISSON'S RATIO (G)} = \frac{\text{LATERAL STRAIN}}{\text{LONGITUDINAL STRAIN}} = \frac{\Delta D/D}{\Delta L/L}$$

$$\text{ELASTIC ENERGY (U)} = \frac{1}{2} \text{STRESS} \times \text{STRAIN} \times \text{VOLUME}$$

$$\text{SURFACE TENSION (S)} = F/l$$

$$\text{SURFACE ENERGY (U)} = S \cdot \text{AREA}$$

$$\Delta_{\text{EXCESS}} = \Delta_{\text{PAIR}} - \frac{2S}{R} \quad \Delta_{\text{BOND}} = 4F$$



$$h = \frac{2S \cos \theta}{\rho g r}$$

$$P_{\text{HYDROSTATIC}} = \rho gh \quad F_{\text{BUOYANT}} = \rho g V$$

$$\text{CONTINUITY} \quad A_1 V_1 = A_2 V_2 \quad \frac{A_1 V_1}{A_2 V_2}$$

$$\text{BERNOULLI'S} \quad P + \rho gh + \frac{1}{2} \rho v^2 = \text{Const}$$

$$F_{\text{VISCOUS}} = -\eta A \frac{dv}{dx}$$

$$\text{TORRICELLI'S} \quad V_{\text{EFFLUX}} = \sqrt{2gh} \quad V_{\text{EFFLUX}} = \sqrt{2gh}$$

$$\text{STOKE'S LAW} \quad F = 6\pi\eta rv \quad V_{\text{TERMINAL}} = \frac{2r^2(\rho - \sigma)g}{9\eta}$$

$$\text{POISEUILLE'S EQUATION} \quad \text{VOLUME FLOW} = \frac{\pi r^4 \Delta P}{8\eta L}$$

WAVES

$y_1 = A \sin(kx - \omega t)$ $y_2 = A \sin(kx + \omega t)$

$$Y = A \sin(kx - \omega t) + A_2 \sin(kx - \omega t + \phi)$$

$$\phi = 2n\pi \text{ (even)} : \text{constructive}$$

$$= (2n+1)\pi \text{ (odd)} : \text{destructive}$$

$$\tan E = \frac{A_2 \sin \phi}{A + A_2 \cos \phi}$$

$$V = \sqrt{\frac{1}{\mu}}$$

$$P_{\text{avg}} = 2\pi^2 \mu D A V^2$$

$T = \frac{1}{V} = \frac{2\pi}{\omega}$ $V = \lambda f$ WAVE NUMBER (k) = $\frac{2\pi}{\lambda}$

STANDING WAVES

$y_1 = A \sin(kx - \omega t)$ $y_2 = A \sin(kx + \omega t)$

$Y = 2A \cos(kx) \sin \omega t$ Node if y is zero $\Rightarrow x = (n + \frac{1}{2})\lambda$

$L = n \cdot \lambda / 2$ $D = \frac{n}{2L} \sqrt{\frac{1}{\mu}}$ SONOMETER

$L = (2n+1) \frac{\lambda}{4}$ $D = \frac{2n+1}{4L} \sqrt{\frac{1}{\mu}}$

OPEN \Rightarrow ANTI NODE

SOUND WAVES

$$S = S_0 \sin[\omega(t - x/v)]$$

$$V_{\text{solid}} = \sqrt{Y/\rho}$$

$$P = P_0 \cos[\omega(t - x/v)]$$

$$V_{\text{liq}} = \sqrt{B/\rho}$$

$$P_0 = \left[\frac{B C \omega}{V} \right] S_0$$

$$V_{\text{gas}} = \sqrt{\kappa P / \rho}$$

$$I = \frac{2\pi^2 B S_0 V^2}{V} = \frac{P_0^2 V}{2\rho} = \frac{P_0}{2\rho V}$$

STANDING LONGITUDINAL WAVES

$$P_1 = P_0 \sin[\omega(t - x/v)]$$

$$P_2 = \sin[\omega(t + x/v)]$$

$$P = P_1 + P_2 = 2P_0 \cos kx \sin \omega t$$

CLOSED ORGAN PIPE

$$L = (2n+1) \frac{\lambda}{4}$$

$$\nu = (2n+1) \frac{V}{4L}$$

OPEN ORGAN PIPE

$$L = n \frac{\lambda}{2}$$

$$\nu = n \frac{V}{2L}$$

RESONANCE COLUMN

$$L_1 + d = \frac{\lambda}{2}$$

$$L_2 + d = \frac{3\lambda}{2}$$

$$V = 2(L_2 - L_1) \nu$$

BEATS (if $\omega_1 \approx \omega_2$)

$$P_1 = P_0 \sin \omega_1 (t - x/v)$$

$$P_2 = P_0 \sin \omega_2 (t - x/v)$$

$$P = 2P_0 \cos \Delta \omega (t - x/v) \sin \omega_1 (t - x/v)$$

$$\omega = (\omega_1 + \omega_2) / 2$$

Beats $\rightarrow \Delta \omega = \omega_1 - \omega_2$

DOPPLER

$$\nu = \frac{V + V_o}{V - V_s} \nu_0$$

LIGHT WAVES

PLANE WAVES $E = E_0 \sin \omega(t - x/v)$; $I = I_0$

SPHERICAL WAVES $E = \frac{a E_0}{r} \sin \omega(t - r/v)$; $I = \frac{I_0}{r^2}$

DIFFRACTION

$$\Delta x = b \sin \theta \approx b \theta$$

$$\theta \sim \tan \theta = y/D$$

$$\text{Minima } b\theta = n\lambda$$

$$\text{Resolution } \sin \theta = \frac{1.22\lambda}{b}$$

YOUNG'S DOUBLE SLIT EXPERIMENT

$$\text{Path diff: } \Delta x = y \frac{d}{D}$$

$$\text{Phase diff: } \delta = \frac{2\pi}{\lambda} \Delta x$$

CONSTRUCTIVE $\delta = 2n\pi$; $\Delta x = n\lambda$

DESTRUCTIVE $\delta = (2n+1)\lambda$; $\Delta x = (n + \frac{1}{2})\lambda$

$$\text{Intensity } I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

$$I_{\text{max/min}} = (\sqrt{I_1} \pm \sqrt{I_2})^2$$

$$\text{Fringe Width } \omega = \frac{D}{a}$$

$$\text{Optical Path } \Delta x = \mu \Delta x$$

$$\text{LAW of MALUS}$$

$$I = I_0 \cos^2 \theta$$

$$\text{INTERFERENCE THROUGH THIN FILM}$$

$$\Delta x = 2nd = \frac{n\lambda}{(2n+1)\lambda/2}$$

OPTICS

REFLECTION

$$(i) i = r$$

(ii) i, r & normal in same plane

$$f = R/2$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\text{Magnification } m = -\frac{v}{u}$$

MICROSCOPE

$$\text{Simple } m = D/f$$

Compound

$$m = \frac{v}{u} \frac{D}{f_e}$$

Resolving Pow $R = \frac{1}{\Delta \theta} = \frac{2 \mu \sin \theta}{\lambda}$

DISPERSION

$$\text{Cauchy's } \mu = \mu_0 + A/x \quad A > 0$$

For small A & i

$$\text{mean deviation } S_y = (\mu_y - 1)A$$

$$\text{Angular dispersion } \theta = (\mu_y - \mu_r)A$$

Dispersive Power

$$(\omega - \omega') \mu \sim \theta$$

REFRACTION

$$\mu = \frac{C}{V} = \frac{(\text{vacuum})}{(\text{medium})}$$

$$\text{SNAIL'S LAW } \mu_1 \sin i = \mu_2 \sin r$$

$$\text{APPARENT DEPTH } d' = d/u$$

$$\text{TIR CRITICAL ANGLE}$$

$$\mu \sin \theta_c = \frac{\sin 90^\circ}{\mu_c}$$

$$\mu \sin \theta_c = 1$$

TELESCOPE

$$m = -\frac{f_o}{f_e}$$

$$L = f_o + f_e$$

$$R = \frac{1}{\Delta \theta} = \frac{1}{1.22\lambda}$$

SPHERICAL SURFACE

$$\frac{\mu_2 - \mu_1}{V} = \frac{\mu_2 - \mu_1}{R}$$

$$m = \frac{\mu_1 V}{\mu_2 u}$$

$$\text{LEN'S MAKER'S } \frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\text{LEN'S FORMULA } \frac{1}{v} - \frac{1}{u} = \frac{1}{f}; m = \frac{v}{u}$$

$$\text{POWER } P = \frac{1}{f}$$

$$\text{THIN LENSES } \frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

PRISM

$$S = i + r - A$$

$$\mu = \frac{\sin \left(\frac{A + S_{\min}}{2} \right)}{\sin \left(\frac{A}{2} \right)}$$

$$S_{\min} = (\mu - 1)A$$

For small 'A'

$$S_m = \frac{(\mu - 1)A}{2}$$

HEAT AND TEMP

$$F = 32 + \frac{9}{5}C$$

$$K = C + 273.16$$

$$\text{Ideal Gas} \rightarrow PV = nRT$$

van der Waals

$$(P + \frac{a}{V^2})(V - b) = nRT$$

$$L = L_0(1 + \alpha \Delta T)$$

$$A = A_0(1 + 2\alpha \Delta T)$$

$$V = V_0(1 + 3\alpha \Delta T)$$

THERMAL STRESS

$$\frac{F}{A} = Y \frac{\Delta L}{L}$$

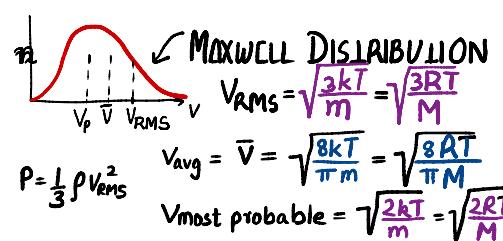
KINETIC THEORY

EQUIPARTITION OF ENERGY

$$K = \frac{1}{2}kT \text{ for each DoF}$$

$$K = \frac{F}{2}kT \text{ for } F \text{ Degrees of freedom}$$

$$\text{Internal Energy } U = \frac{F}{2}nRT$$



$$F = 3 \text{ (monatomic)}; 5 \text{ (diatomic)}$$

SPECIFIC HEAT

$$\text{Specific heat } S = \frac{Q}{m \Delta T}$$

$$\text{Latent heat } L = Q/m$$

$$C_v = \frac{F}{2}R \quad C_p = C_v + R \quad r = C_p/C_v$$

$$C_v = \frac{n_1 C_{v1} + n_2 C_{v2}}{n_1 + n_2} \quad r = \frac{n_1 C_{p1} + n_2 C_{p2}}{n_1 C_{v1} + n_2 C_{v2}}$$

THERMODYNAMICS

$$1^{\text{st}} \text{ LAW } \Delta Q = \Delta U + W \quad W = \int P dV$$

$$\text{ADIABATIC } W = \frac{P_1 V_1 - P_2 V_2}{r-1}$$

$$\text{ISOTHERMAL } W = nRT \ln\left(\frac{V_2}{V_1}\right)$$

$$\text{ISOBARIC } W = P(V_2 - V_1)$$

$$\text{ADIABATIC: } \Delta Q = 0; \quad PV^r = \text{Const}$$

$$\eta = \frac{W}{Q_1} = 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1} \quad \text{CoP} = \frac{Q_2}{W} = \frac{T_{cold}}{\Delta T}$$

$$2^{\text{nd}} \text{ LAW } \text{ENTROPY } dS = \frac{dQ}{T}$$

HEAT TRANSFER

$$\text{CONDUCTION } \frac{\Delta Q}{\Delta t} = -KA \frac{\Delta T}{x}$$

$$\text{Thermal Resistance} = \frac{x}{KA}$$

$$\text{SERIES } R = R_1 + R_2 = \frac{x_1}{k_1 A_1} + \frac{x_2}{k_2 A_2}$$

$$\text{PARALLEL } \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\text{KIRCHHOFF'S LAW } \frac{\text{Emmisive Power}}{\text{Absorptive Power}} = \frac{E_{body}}{a_{body}} = E_{blackbody}$$

$$\text{WIEN'S DISPLACEMENT } \lambda_m T = b$$

$$\text{STEFAN-BOLTZMANN } \Delta \theta / \Delta t = \sigma e A T^4$$

$$\text{NEWTON'S COOLING } \frac{dT}{dt} = -bA(T - T_0)$$

ELECTROSTATICS

$$\text{COULOMB'S LAW } F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$\vec{E} = \vec{F}/q = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$\text{POTENTIAL (V)} = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$PE(U) = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} \quad \vec{E} = -\frac{dV}{dr}$$

DIPOLE MOMENT

$$\vec{p} = q \vec{d}$$

$$\frac{1}{4\pi\epsilon_0} \cdot \frac{p \cos \theta}{r^2} = V(r)$$

DIPOLE IN FIELD

$$\vec{U} = \vec{p} \cdot \vec{E}$$

$$E_r = \frac{1}{4\pi\epsilon_0} \frac{2p \cos \theta}{r^3}$$

$$E_\theta = \frac{1}{4\pi\epsilon_0} \frac{p \sin \theta}{r^3}$$

UNIFORMLY CHARGED SPHERE

$$\frac{1}{4\pi\epsilon_0} \frac{Q}{R^3} \cdot \frac{1}{r^2}$$

UNIFORM SHELL

$$\frac{1}{4\pi\epsilon_0} \frac{Q}{R^2}$$

$$\text{LINE CHARGE } E = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\infty\text{-sheet } E = \frac{\sigma}{2\epsilon_0}$$

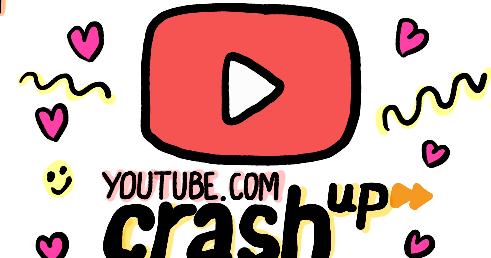
$$\vec{E} \text{ near } \text{CONDUCTING SURFACE } E = \frac{\sigma}{\epsilon_0}$$

GAUSS'S LAW

$$\phi = q_{in}/\epsilon_0$$

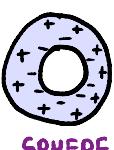
$$\text{FLUX } \phi = \vec{\phi} \cdot \vec{dS}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \cos \theta$$



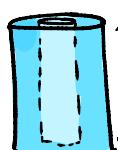
CAPACITORS

$$C = q/V \quad C = \epsilon_0 A/d$$



$$C = 4\pi\epsilon_0 \frac{Y_1 Y_2}{Y_2 - Y_1}$$

$$C = \frac{2\pi\epsilon_0 L}{\ln(Y_2/Y_1)}$$



$$\text{PARALLEL } C_{eq} = C_1 + C_2$$

$$\text{SERIES } \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\text{WITH DIELECTRIC } C = \frac{\epsilon_0 K A}{d}$$

$$\text{Force b/w plates} = \frac{Q^2}{2A\epsilon_0}$$

$$U = \frac{1}{2} CV^2 = \frac{Q^2}{2C} = \frac{1}{2} QV$$

CURRENT ELECTRICITY

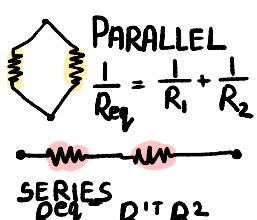
$$\text{DENSITY } j = i/A = \sigma E$$

$$V_{drift} = \frac{1}{2} \frac{eE\tau}{m} = \frac{i}{neA}$$

$$R_{WIRE} = \rho L/A \quad \rho = \frac{1}{\sigma}$$

$$R = R_0(1 + \alpha \Delta T)$$

$$\text{OHM'S LAW } V = IR$$



KIRCHHOFF'S LAWS

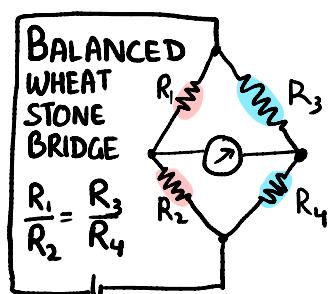
$$*\text{ JUNCTION LAW } \sum I_i = 0$$

Sum of all i towards a node = 0

$$*\text{ LOOP LAW } \sum \Delta V = 0$$

Sum of all ΔV in closed loop = 0

$$\text{POWER} - i^2R - V^2/R - iV$$



GALVANOMETER
 $i_g G = (i - i_g) S$
Voltmeter
 $V_{AB} = i_g(R + G)$

CAPACITOR
 Charging
 $q(t) = CV(1 - e^{-t/RC})$
 Discharging
 $q(t) = q_0 e^{-(t/RC)}$
 Time Constant $\tau = RC$

MAGNETISM
 $F_{LORENTZ} = qv \times \vec{B} + qE$
 $qvB = mv^2/r$
 $T = \frac{2\pi m}{qB}$

MAGNETIC DIPOLE
 $\mu = iA/\text{area}$
 $\vec{B} = \vec{\mu}/\mu_0$
 $U = -\vec{\mu} \cdot \vec{B}$

HALL EFFECT
 $V_H = \frac{Bi}{ned}$

PELTIER EFFECT
 $\text{emf } e = \frac{\Delta H}{\Delta T}$

THOMSON EFFECT
 $\text{emf } e = \frac{\Delta H}{\Delta T} = \sigma \Delta T$

FARADAY'S LAW OF ELECTROLYSIS
 $m = Zit = \frac{1}{F} Eit$
 $E = \text{Chem equivalent}$
 $Z = \text{Electro Chem eq}$
 $F = 96485 \text{ C/g}$

SEEBACK EFFECT
 $e = aT + \frac{1}{2} bT^2$
 $T_{\text{neutral}} = -a/b$
 $T_{\text{inversion}} = -2a/b$

BIOT-SAWART LAW
 $d\vec{B} = \frac{\mu_0}{4\pi} i \frac{dl \times \vec{r}}{r^3}$

STRAIGHT CONDUCTOR
 $B_{00} = \frac{\mu_0 i}{2\pi d}$
 $B = \frac{\mu_0 i}{4\pi d} [\cos \theta_2 - \cos \theta_1]$

WIRING
 $i_1 i_2 \frac{dF}{dl} = \frac{\mu_0 i_1 i_2}{2\pi d}$

AXIS OF RING
 $B_p = \frac{\mu_0 i_1 r^2}{2(a^2 + d^2)^{3/2}}$

CENTER OF ARC
 $\theta : B = \frac{\mu_0 i_1 \theta}{4\pi r}$
 $B = \mu_0 i_1 n/2r$ (ring)

SOLENOID
 $m m m m$
 $B = \mu_0 n i$

TOROID
 $B = \mu_0 n i$
 $n = N/2\pi r_2$

AMPERE'S LAW
 $\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{in}}$

BAR MAGNET

$B_1 = \frac{\mu_0 2M}{4\pi d^3}$
 $B_2 = \frac{\mu_0 M}{4\pi d^3}$

ANGLE OF DIP

$B_h = B \cos \delta$

$B_v = B \sin \delta$



TANGENT GALVANOMETER
 $B_n \tan \theta = \mu_0 n i/2r \quad |i| = k \tan \theta$

PERMEABILITY
 $\vec{B} = \mu \vec{H}$

MAGNETOMETER
 $T = 2\pi \sqrt{I/M B_h}$

ELECTROMAGNETIC INDUCTION

MAGNETIC FLUX $\Phi = \vec{\phi} \cdot \vec{B} \cdot d\vec{s}$ **FARADAY'S LAW** $e = -\frac{d\Phi}{dt}$

LENZ'S LAW: Induced current produces \vec{B} that opposes change in Φ

ALTERNATING CURRENT

$i = i_0 \sin(\omega t + \phi)$
 $i_{\text{rms}} = i_0 / \sqrt{2}$
 POWER = $i^2_{\text{rms}} \cdot R$

REACTANCE

CAPACITIVE $X_C = 1/\omega C$
 INDUCTIVE $X_L = \omega L$
 IMPEDANCE $Z = \sqrt{R^2 + X^2}$

RC-CIRCUIT

$\frac{1}{\omega C} \rightarrow V$
 $\tan \phi = \frac{1}{\omega CR}$
 $Z = \sqrt{R^2 + X_C^2}$
 $X_C = \frac{1}{\omega R}$

LR-CIRCUIT

$\omega L \rightarrow V$
 $\tan \phi = \frac{\omega L}{R}$
 $Z = \sqrt{R^2 + X_L^2}$
 $X_L = \omega L$

LCR-CIRCUIT

$\tan \phi = \frac{X_C - X_L}{R}$
 $Z = \sqrt{R^2 + (X_C - X_L)^2}$
 $P = P_{\text{rms}} i_{\text{rms}} \cos \phi$
 POWER FACTOR \rightarrow
 $(X_C = X_L)$

SELF INDUCTANCE

$\Phi = Li$
 $e = -L \frac{di}{dt}$
SOLENOID $L = \mu_0 n^2 \pi r^2 l$
MUTUAL INDUCTANCE $\Phi = Mi$, $e = -M \frac{di}{dt}$

GROWTH

$i = \frac{V}{R} [1 - e^{-t/R}]$

DECAY

$i = i_0 e^{-t/LR}$



Time Const. $\beta = L/R$

ENERGY $U = \frac{1}{2} L I^2$

ENERGY DENSITY OF B-FIELD

$u = \frac{U}{V} = \frac{B^2}{2\mu_0}$

ROTATING COIL $e = NAB\omega \sin \omega t$

TRANSFORMER $\frac{N_1}{N_2} = \frac{e_1}{e_2}$

$C = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$

MODERN PHYSICS

$E = h\nu = hc/\lambda$ $p = h/\lambda = E/c$ $E = mc^2$

Ejected photo-electron $K_{\text{max}} = h\nu - \phi$

THRESHOLD $V_0 = \phi/h$

STOPPING $V_b = \frac{hc(1 - \frac{\phi}{E})}{e(\lambda - \phi)}$
 de Broglie $\lambda = h/p$

BOHR'S ATOM

$E_n = -\frac{m_e^2 c^4}{8\epsilon_0^2 h^2 n^2} = -\frac{13.6 Z^2}{n^2} \text{ eV}$
 $\gamma_n = \frac{E_n h^2 n^2}{mc^2} = \frac{0.529 n^2 A^2}{z^2}$

$E_{\text{TRANSITION}} = 13.6 Z^2 \left(\frac{1}{n^2} - \frac{1}{m^2} \right) A^0$

HEISENBERG $\Delta x \Delta p \geq h/2\pi$ $\Delta E \Delta t \geq \hbar/2\pi$

MOSLEY'S LAW $\frac{1}{\lambda} = \frac{a(z-b)}{x^2} n \theta$

NUCLEUS

$R = R_o A^{1/3}$; $R_o = 1.1 \times 10^{-15} \text{ m}$

RADIOACTIVE DECAY

$\frac{dN}{dt} = -\lambda N$ $N = N_0 e^{-\lambda t}$

HALF LIFE $t_{1/2} = 0.693/\lambda$

Avg LIFE $t_{\text{avg}} = 1/\lambda$

Mass DEFECT

$\Delta M = [Z m_p + (A-Z)m_n] - M$

BINDING E = $\Delta M \cdot c^2$

Q-VALUE $Q = U_i - U_f$

SEMICONDUCTORS

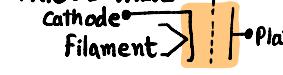
HALF WAVE RECTIFIER



FULL WAVE RECTIFIER



TRIODE VALVE



TRIODE

Plate Resistance $r_p = \frac{\Delta V_p}{\Delta i_p} \mid \Delta V_g = 0$

Trans-conductance $g_m = \frac{\Delta i_p}{\Delta V_g} \mid \Delta V_p = 0$

Amplification $u = -\frac{\Delta V_p}{\Delta V_g} \mid \Delta i_p = 0$

$\mu = r_p \times g_m$

TRANSISTOR

$I_e = I_b + I_c$

$\alpha = \frac{I_c}{I_e} \quad \beta = \frac{I_c}{I_b} \quad \beta = \frac{\alpha}{1-\alpha}$

Transconductance $g_m = \frac{\Delta I_c}{\Delta V_{be}}$

LOGIC GATES

AND	NAND	OR	NOR
A B	AB	A+B	A+B
0 0	0	1	0
0 1	0	1	1
1 0	0	1	0
1 1	0	1	0

NOW YOU'RE ONE STEP CLOSER TO YOUR GOAL