

Ex 5.1.1.

a.) $G = \{ \langle s \rangle, \{0,1\}, s, P \}$

dengan P adalah production rule ;

$$s \rightarrow 0s1 \mid 01$$

b.) Set $\{ a^i b^j c^k \mid i \neq j \text{ or } j \neq k \}$!

$$G = \{ \langle s, A, B, C, D, E \rangle, \{a, b, c\}, s, P \}$$

dgn P adalah :

$$s \rightarrow AB \mid CD$$

$$A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bBc \mid \epsilon \mid cD$$

$$C \rightarrow aCb \mid \epsilon \mid aA$$

$$D \rightarrow cD \mid \epsilon$$

$$E \rightarrow bE \mid b$$

c.) Set of all strings of a's and b's that are not of the form ww , that is, not equal to any string repeated.

$$G = \{ \langle s, T, A, B \rangle, \{a, b\}, s, P \}$$

P :

$$s \rightarrow AB \mid BA \mid T$$

$$T \rightarrow aTb \mid bTa \mid aTa \mid bTb \mid alb$$

$$A \rightarrow aAb \mid bAa \mid aAa \mid bAb \mid a$$

$$B \rightarrow aBb \mid bBa \mid aBa \mid bBb \mid b$$

d.) Set of all strings with twice as many 0's as 1's

$$G = \{ \langle s \rangle, \{0,1\}, s, P \}$$

P :

$$s \rightarrow \epsilon \mid ss \mid 00s1 \mid 1s00 \mid 01s0$$

Ex 5.1.2

following grammar generates the language of regular expression $0^*1(0+1)^*$

$$S \rightarrow A|B$$

$$A \rightarrow 0A|\epsilon$$

$$B \rightarrow 0B|1B|\epsilon$$

Give leftmost and rightmost derivations:

a) 00101

$$\begin{aligned} \text{LM: } S &\rightarrow AB \rightarrow 0AB \rightarrow 00AB \rightarrow 001B \rightarrow 0010B \\ &\rightarrow 00101B \rightarrow 00101 \end{aligned}$$

$$\text{RM: } S \rightarrow AB \rightarrow 0A10B \rightarrow 0A101B \rightarrow 0A101 \rightarrow 00A101 \rightarrow 00101$$

b.) 1001

$$\text{LM: } S \rightarrow AB \rightarrow 1B \rightarrow 10B \rightarrow 100B \rightarrow 1001B \rightarrow 1001$$

$$\text{RM: } S \rightarrow AB \rightarrow A10B \rightarrow A100B \rightarrow A1001B \rightarrow A1001 \rightarrow 1001$$

c.) 00011

$$\begin{aligned} \text{LM: } S &\rightarrow AB \rightarrow 0AB \rightarrow 00AB \rightarrow 000AB \rightarrow 0001B \\ &\rightarrow 00011B \rightarrow 00011 \end{aligned}$$

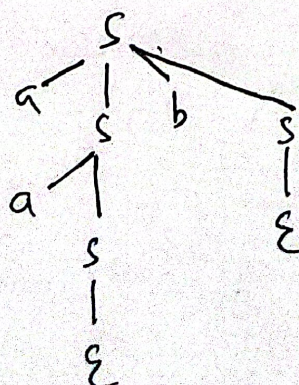
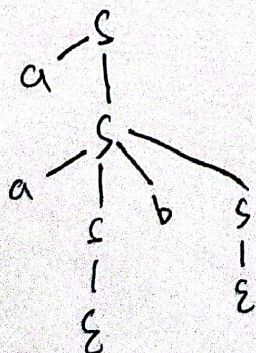
$$\begin{aligned} \text{RM: } S &\rightarrow AB \rightarrow A11B \rightarrow A11 \rightarrow 0A11 \rightarrow 00A11 \\ &\rightarrow 000A11 \rightarrow 00011 \end{aligned}$$

Ex 5.4.1

$$S \rightarrow aS | aSbS | \epsilon$$

This grammar is ambiguous. Show in particular that the string aab has two:

a.) Parse trees



Leftmost derivations

b.) #1 $S \rightarrow aS \rightarrow aasbs \rightarrow aab$

$S \rightarrow asbs \rightarrow aasbs \rightarrow aabs \rightarrow aab$

c.) Rightmost derivations

#1 $S \rightarrow aS \rightarrow aasbs \rightarrow aasb \rightarrow aab$

#2 $S \rightarrow asbs \rightarrow asb \rightarrow aasb \rightarrow aab$

EX 5-4.7

The following grammar generates prefix expressions with operands x and y and binary operators $+$, $-$, and $*$

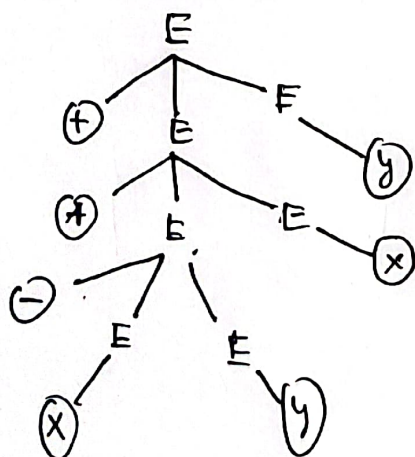
$$E \rightarrow +EE \mid *EE \mid -EE \mid x \mid y$$

a.) find LM RM derivations, and a derivation tree for the string $+*-xyxy$

LM : $E \rightarrow +EE \rightarrow +*EEE \rightarrow +*-EEEE \rightarrow +*-xEEE \rightarrow +*-xyEE \rightarrow +*-xyxE \rightarrow +*-xyxy$

RM : $E \rightarrow +EE \rightarrow +EY \rightarrow +*EEY \rightarrow +*EXY \rightarrow +*-EEXY \rightarrow +*-EyxY \rightarrow +*-xyxy$

Derivation tree :



b.) Pada grammar ini, setiap production rule memiliki awalan yg berbeda $(+, *, -, x, y)$. Untuk string yg termasuk dalam CFL ini, apabila diambil LM var. E , langkah berikutnya bergamung dengan simbol yg rugin dimunculkan dari w . Karena awalan tiap rule berbeda, maka dijamin hanya terdapat satu rule yg dapat diperoleh pada saat itu. Maka dijamin hanya ada satu LM derivatran untuk w dan grammar terbukti tidak ambigu.