

Ex. 6.3.1

Convert the grammar to a PDA that accepts the same language by empty stack

$$\begin{aligned} S &\rightarrow 0S1 \mid A \\ A &\rightarrow 1A0 \mid S \mid \epsilon \end{aligned}$$

$$PDA : (Q, \Sigma, \Gamma, \delta, q, S)$$

$$\begin{aligned} \delta \rightarrow & \cdot \delta(q, \epsilon, S) = \{(q, 0S1), (q, A)\} \\ & \cdot \delta(q, \epsilon, A) = \{(q, 1A0), (q, S), (q, \epsilon)\} \\ & \cdot \delta(q, 0, 0) = \{(q, \epsilon)\} \\ & \cdot \delta(q, 1, 1) = \{(q, \epsilon)\} \end{aligned}$$

EX 6.3.2

Convert the grammar to a PDA that accepts the same language by empty stack.

$$\begin{aligned} S &\rightarrow aAA \\ A &\rightarrow aS \mid bS \mid a \end{aligned}$$

$$PDA : (Q, \Sigma, \Gamma, \delta, q, S)$$

$$\begin{aligned} \delta : & \cdot \delta(q, a, a) = \{(q, \epsilon)\} \\ & \cdot \delta(q, b, b) = \{(q, \epsilon)\} \\ & \cdot \delta(q, \epsilon, S) = \{(q, aAA)\} \\ & \cdot \delta(q, \epsilon, A) = \{(q, aS), (q, bS), (q, a)\} \end{aligned}$$

EX 6.3.3

Convert the PDA $P = (Q, \Sigma, \Gamma, \delta, q, z_0)$ to a CFG if δ is given

$$\begin{aligned} \cdot \delta(q, 1, z_0) &= \{(q, Xz_0)\} & \cdot \delta(q, \epsilon, X) &= \{(q, \epsilon)\} \\ \cdot \delta(q, 1, X) &= \{(q, XX)\} & \cdot \delta(P, 1, X) &= \{(P, \epsilon)\} \\ \cdot \delta(q, 0, X) &= \{(P, X)\} & \cdot \delta(P, 0, z_0) &= \{(q, z_0)\} \end{aligned}$$

S = start string, ϵ = empty string, $z = z_0$

$$\text{in } S \rightarrow [qzq] \mid [qzp]$$

$$\begin{aligned} (1) - [qzq] &\rightarrow 1 [qXq] [qzq] \\ &- [qzq] \rightarrow 1 [qXp] [pzq] \\ &- [qzp] \rightarrow 1 [qXq] [qzp] \\ &- [qzp] \rightarrow 1 [qXp] [pzp] \end{aligned}$$

$$\begin{aligned} (2) - [qXq] &\rightarrow 1 [qXq] [qXq] \\ &- [qXq] \rightarrow 1 [qXp] [pXq] \\ &- [qXp] \rightarrow 1 [qXq] [pXp] \\ &- [qXp] \rightarrow 1 [qXp] [pXp] \end{aligned}$$

$$(3) \quad -[q \times q] \rightarrow 0 [p \times q]$$

$$- [q \times p] \rightarrow 0 [p \times p]$$

$$(4) \quad - [q \times q] \rightarrow 6$$

$$(5) \quad - [p \times p] \rightarrow 1$$

$$(6) \quad - [p \times q] \rightarrow 0 [q \times q]$$

$$- [p \times p] \rightarrow 0 [q \times p]$$