

# Task7

2019 年 6 月 19 日

## 1 图像处理 +180776+ 胡欣毅 (Python 版)

### 2 8 周课后

#### 2.1 1. 题目清单

1. 利用 Perona-Malik 算法改善图像清晰度
2. 利用 Gabor 算法改善图像清晰度

#### 2.2 Perona-Malik 算法

```
In [1]: import numpy as np
import cv2
import matplotlib.pyplot as plt
%matplotlib inline

In [2]: im = cv2.imread('../hudie/3.bmp')
im = cv2.cvtColor(im , cv2.COLOR_RGB2BGR)

gray = cv2.cvtColor(im , cv2.COLOR_RGB2GRAY).astype(float)
plt.imshow(gray,cmap='gray')
plt.axis("off")
plt.show()
gray.shape
```



Out [2]: (512, 768)

```
In [3]: def getImageVar(image):
        imageVar = cv2.Laplacian(image, cv2.CV_64F).var()
        return imageVar
```

```
In [4]: def g(s,k):
        return np.exp(-(s/k)**2)
```

```
In [5]: def get_c(grad_u,k):
        return g(abs(grad_u),k)
```

$$u(x, y, \Delta t) = u(x, y, 0) + \Delta t \frac{\partial u}{\partial t}$$

$$\frac{\partial u}{\partial t} = \nabla(c(x, y, t) \nabla u) = \nabla c(x, y, t) \nabla u + c(x, y, t) \Delta u$$

$$g(s) = \exp\left(-\left(\frac{s}{k}\right)^2\right)$$

$$c(x, y, t) = g(|\nabla u|)$$

## 2.2.1 方式一

```

In [6]: def PM1(src ,k = 12,lambd = .01 ):

    Ker_x = np.array([[ -1, 0, 1],
                      [ -1, 0, 1],
                      [ -1, 0, 1]])
    Ker_y = np.array([[ 1, 1, 1],
                      [ 0, 0, 0],
                      [-1,-1,-1]])

    # Laplace 扩展算子
    laplace = np.array([[ 1, 1, 1],
                        [ 1,-8, 1],
                        [ 1, 1, 1]])

    # grad_u
    grad_x = cv2.filter2D(src, -1 , Ker_x )
    grad_y = cv2.filter2D(src, -1 , Ker_y )
    grad_u = np.abs(grad_x) + np.abs(grad_y)

    # c
    c = get_c(grad_u,k = k)

    # grad_c
    grad_x_c = cv2.filter2D(src, -1 , Ker_x )
    grad_y_c = cv2.filter2D(src, -1 , Ker_y )
    grad_c = np.abs(grad_x_c) + np.abs(grad_y_c)

    # Laplace_u
    Laplace_u = cv2.filter2D(src, -1 , laplace )

    #
    im_out = (src + lambd*(grad_c * grad_u + c* Laplace_u ) )
    return im_out

In [7]: def PM2(src ,k = 12,lambd = .001 ):

    edge = - np.array([[ 1, 1, 1],
                       [ 1,-8, 1],
                       [ 1, 1, 1]])

    # grad_u
    grad_u = cv2.filter2D(src, -1 , edge )

    # c

```

```
c = get_c(grad_u, k = k)
# grad_c
grad_c = cv2.filter2D(src, -1, edge)

# Laplace_u
x = cv2.getGaussianKernel(3, 1.0) # 高斯滤波器
ker = x * x.T

Laplace_u = cv2.filter2D(src, -1, ker)
# out
im_out = (src + lambd*(grad_c * grad_u + c* Laplace_u))
return im_out
```

In [8]: # 迭代次数

```
step_num = 1
# copy
im_out1 = gray.astype(float)
im_out2 = gray.astype(float)
for t in range(step_num):
    im_out1 = PM1( im_out1, k = 12, lambd = .002)
    im_out2 = PM2( im_out2, k = 15, lambd = .003)
```

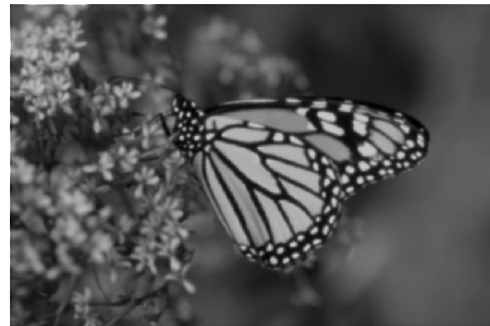
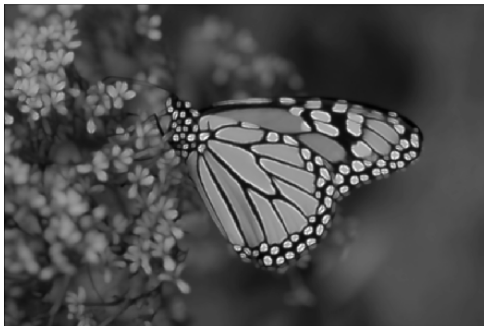
```
In [9]: print('原图: ', getImageVar(gray), '\n', 'PM 算法: ', \
            getImageVar(im_out1), getImageVar(im_out2))
```

原图: 24.55965163387333

PM 算法: 178.14737824894107 46.61359154302199

```
In [10]: plt.figure(figsize=(18,12))
plt.subplot(221)
plt.imshow(gray,cmap='gray')
plt.axis("off")
plt.subplot(223)
plt.imshow(im_out1,cmap='gray')
plt.axis("off")
plt.subplot(224)
plt.imshow(im_out2,cmap='gray')
```

```
plt.axis("off")  
plt.show()
```



### 2.2.2 方式二

```
In [11]: def f(s,k):  
         return 1.0 / (1.0 + (s / k) ** 2)  
  
In [12]: def Perona_Malik(src , times =30,dt=.01 ,kappa =12, option = 1 ):  
         ny,nx = src.shape  
         src = src.astype('float')  
         # copy  
         res = src  
         tmp = src  
  
         # 迭代次数  
         for t in range(times):  
             # 一次迭代  
             for i in range(ny):
```

```

for j in range(nx):
    # 位置信息 边界处理
    iUp = max(0,i - 1)
    iDown = min(ny-1,i + 1)
    jLeft = max(0,j - 1)
    jRight = min(nx-1,j + 1)

    # 书本 page216 先计算 deta_u
    deltaN = tmp[iUp,j] - tmp[i,j]
    deltaS = tmp[iDown,j] - tmp[i,j]
    deltaE = tmp[i,jRight] - tmp[i,j]
    deltaW = tmp[i,jLeft] - tmp[i,j]
    delta_u = np.array([deltaN , deltaS , deltaE , deltaW ])
    #print(delta_u)

    # 计算 c
    if (option == 1):
        c = g(np.abs(delta_u),kappa)
    elif (option == 2):
        c = f(np.abs(delta_u),kappa)
    # 相乘相加 加权赋值
    res[i,j] += dt * (sum(c * delta_u) )

tmp = res
return res

```

```

In [13]: res = Perona_Malik(src= gray, times =40,dt=.002 ,kappa = 14, option = 1)
         print('原图: ', getImageVar(gray),'\n','PM 算法: ',getImageVar(res))

```

原图: 24.55965163387333

PM 算法: 23.54068568433893

```

In [14]: plt.figure(figsize=(18,15))
         plt.subplot(121)
         plt.imshow(gray,cmap='gray')
         plt.axis("off")
         plt.subplot(122)
         plt.imshow(res,cmap='gray')

```

```
plt.axis("off")
plt.show()
```



## 2.3 Gabor 算法

### 2.3.1 Gabor 第一算法

$$f(x,y) = f(x,y) - t \frac{\partial^2 f}{\partial n^2}$$

```
In [15]: def gabor1(src,t):
    # 核 四个角度 一阶
    ker = np.zeros((3,3,4))
    ker[...,0] = np.array([[0,0,0],
                           [0,-1,1],
                           [0,0,0]])
    ker[...,1] = np.array([[0,0,1],
                           [0,-1,0],
                           [0,0,0]])
    ker[...,2] = np.array([[0,1,0],
                           [0,-1,0],
                           [0,0,0]])
    ker[...,3] = np.array([[1,0,0],
                           [0,-1,0],
                           [0,0,0]])

    # 核 四个角度 二阶
    ker2 = np.zeros((3,3,4))
```

```

ker2[...,0] = np.array([[0, 0,0],
                        [1,-2,1],
                        [0, 0,0]])
ker2[...,1] = np.array([[0, 0,1],
                        [0,-2,0],
                        [1, 0,0]])
ker2[...,2] = np.array([[0, 1,0],
                        [0,-2,0],
                        [0, 1,0]])
ker2[...,3] = np.array([[1, 0,0],
                        [0,-2,0],
                        [0, 0,1]])

# 四个角度的差分
d = np.zeros(src.shape +(4,))
dd = np.zeros(src.shape +(4,))
for i in range(4):
    d[...,i] = cv2.filter2D(src, -1 , ker[...,i])
    dd[...,i] = cv2.filter2D(src, -1 , ker2[...,i])

n_f = np.ones_like(src)
for row in range(src.shape[0]):
    for col in range(src.shape[1]):
        # 法向
        n = np.where( np.abs(d[row,col,:]) ==\
                        np.max(np.abs(d[row,col,:])) )[0][0]

        n_f[row,col] = dd[row,col,n]
    return src - t * n_f

gabor = gabor1(gray,0.5)

```

```
In [16]: print('原图: ', getImageVar(gray),'\n','PM 算法: ',getImageVar(gabor))
```

原图: 24.55965163387333

PM 算法: 88.80644580193461

```
In [17]: plt.figure(figsize=(18,15))
```



```
plt.subplot(121)
plt.imshow(gray,cmap='gray')
plt.axis("off")
plt.subplot(122)
plt.imshow(gabor,cmap='gray')
plt.axis("off")
plt.show()
```



### 2.3.2 Gabor 第二算法

$$f(x,y) = f(x,y) - t(\frac{\partial^2 f}{\partial n^2} - \frac{1}{3} \frac{\partial^2 f}{\partial s^2})$$

```
In [18]: def gabor2(src,t):
    # 核 四个角度 一阶
    ker = np.zeros((3,3,4))
    ker[...,0] = np.array([[0,0,0],
                           [0,-1,1],
                           [0,0,0]])
    ker[...,1] = np.array([[0,0,1],
                           [0,-1,0],
                           [0,0,0]])
    ker[...,2] = np.array([[0,1,0],
                           [0,-1,0],
                           [0,0,0]])
    ker[...,3] = np.array([[1,0,0],
                           [0,-1,0],
```

```

                                [0,0,0]))

# 核 四个角度 二阶
ker2 = np.zeros((3,3,4))
ker2[...,0] = np.array([[0, 0,0],
                        [1,-2,1],
                        [0, 0,0]])
ker2[...,1] = np.array([[0, 0,1],
                        [0,-2,0],
                        [1, 0,0]])
ker2[...,2] = np.array([[0, 1,0],
                        [0,-2,0],
                        [0, 1,0]])
ker2[...,3] = np.array([[1, 0,0],
                        [0,-2,0],
                        [0, 0,1]])

# 四个角度的差分
d = np.zeros(src.shape +(4,))
dd = np.zeros(src.shape +(4,))
for i in range(4):
    d[...,i] = cv2.filter2D(src, -1 , ker[...,i])
    dd[...,i] = cv2.filter2D(src, -1 , ker2[...,i])

n_f = np.ones_like(src)
s_f = np.ones_like(src)
for row in range(src.shape[0]):
    for col in range(src.shape[1]):
        # 法向
        n = np.where( np.abs(d[row,col,:]) ==\
                        np.max(np.abs(d[row,col,:])) )[0][0]

        # 切向
        s = (n+2)%4
        n_f[row,col] = dd[row,col,n]
        s_f[row,col] = dd[row,col,s]
    return src - t * (n_f - s_f /3 )

gabor = gabor2(gray,0.5)

```

```
In [19]: print('原图: ', getImageVar(gray), '\n', 'PM 算法: ', getImageVar(gabor))
```

原图: 24.55965163387333

PM 算法: 77.50446275135562

```
In [20]: plt.figure(figsize=(18,15))
plt.subplot(121)
plt.imshow(gray, cmap='gray')
plt.axis("off")
plt.subplot(122)
plt.imshow(gabor, cmap='gray')
plt.axis("off")
plt.show()
```



参考网上

```
In [21]: def gabor_fn(sigma, theta, Lambda, psi, gamma):
    sigma_x = sigma
    sigma_y = float(sigma) / gamma

    # -----这部分内容是为了确定卷积核的大小-----
    # Bounding box
    nstds = 3 # Number of standard deviation sigma
    xmax = max(abs(nstds * sigma_x * np.cos(theta)), \
               abs(nstds * sigma_y * np.sin(theta)))
    xmax = np.ceil(max(1, xmax))
    ymax = max(abs(nstds * sigma_x * np.sin(theta)), \
```

```

        abs(nstds * sigma_y * np.cos(theta)))

ymax = np.ceil(max(1, ymax))
xmin = -xmax
ymin = -ymax
(y, x) = np.meshgrid(np.arange(ymin, ymax + 1), np.arange(xmin, xmax + 1))
# -----这部分内容是为了确定卷积核的大小-----

# Rotation
x_theta = x * np.cos(theta) + y * np.sin(theta)
y_theta = -x * np.sin(theta) + y * np.cos(theta)

# -----这部分正是上面的公式-----
gb = np.exp(-.5 * (x_theta ** 2 / sigma_x ** 2 + y_theta ** 2 / sigma_y ** 2)) \
      * np.cos(2 * np.pi / Lambda * x_theta + psi)

return gb

```

In [22]: # 构建 Gabor 滤波器

# cv2.getGaborKernel(ksize, sigma, theta, lambda, gamma, psi, ktype) 参数说明

```

def build_filter():
    ksize = (5,5)
    lamda = np.pi/2.0 # 波长
    direction = 8
    out = np.zeros(ksize)

    for i,theta in enumerate(np.arange(0, np.pi, np.pi / direction)):
        # gabor 方向, 0 度, 22.5 度, 45 度, 67.5 度, 90 度,
        # 112.5 度, 135 度, 157.5 度 共 8 个
        kern = cv2.getGaborKernel(ksize,.7,theta,lamda,\
                                   gamma = 0.5, psi= 0, ktype=cv2.CV_32F)
        #np.maximum(out,kern,out)
        out += kern
    out /= out.sum()
    return out

```

In [23]: res = cv2.filter2D(gray,-1,build\_filter())

print('原图: ', getImageVar(gray),'\n','PM 算法: ',getImageVar(res))

原图: 24.55965163387333

PM 算法: 48.52537066073149

```
In [24]: plt.figure(figsize=(18,15))  
         plt.subplot(121)  
         plt.imshow(gray,cmap='gray')  
         plt.axis("off")  
         plt.subplot(122)  
         plt.imshow(res,cmap='gray')  
         plt.axis("off")  
         plt.show()
```



### 3 图像处理 +180776+ 胡欣毅 (C++ 版)

c++1 、 c++2