

**Name:****UT EID:**

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An undirected graph is connected if each pair of vertices is connected by a path. Prove that the following two statements are equivalent:

1. An undirected graph  $G = (V, E)$  is disconnected
2. The vertices of the undirected graph  $G = (V, E)$  can be partitioned into two sets  $V_1, V_2$  such that there are no edges between any member of  $V_1$  and any member of  $V_2$ . A partition means that  $V_1 \cup V_2 = V$  and  $V_1 \cap V_2 = \emptyset$ .