

Name:

UT EID:

**Problem 1: Summing Integers**

Suppose you are given a collection  $A = \{a_1, a_2, \dots, a_n\}$  of  $n$  positive integers that add up to  $2Z$ . We want to design an  $O(nZ)$  time algorithm to decide if the set can be partitioned into two groups  $B$  and  $A - B$  such that:

$$\sum_{a_j \in B} a_j = \sum_{a_i \in (A-B)} a_i = Z,$$

in other words, there is a subset of  $A$  that adds up to  $Z$ .

- (a) Define an  $Z \times n$  array  $m$ , where  $m[z, i]$  is 1 if there exists a subset of  $A$ ,  $\{a_1, a_2, \dots, a_i\}$ , that sums to  $z$  and 0 otherwise. Write the dynamic equation formula for computing  $m[z, i]$ .
- (b) Write pseudocode that uses your dynamic equation formula to fill in the table  $m$ .
- (c) In English, describe how you would reconstruct the solution from the table  $m$  (describe how you would return the actual subset of numbers that sums to  $Z$  instead of just “yes” or “no”).