Deriving Via

or, How to Turn Hand-Written Instances into an Anti-Pattern

Baldur Blöndal

Andres Löh
Well-Typed LLP

Ryan Scott
Indiana University

Abstract

Haskell's `deriving` construct is a cheap and cheerful way to quickly generate instances of type classes that follow common patterns. But at present, there is only a subset of such type class patterns that `deriving` supports, and if a particular class lies outside of this subset, then one cannot derive it at all, with no alternative except for laboriously declaring the instances by hand.

To overcome this deficit, we introduce Deriving Via, an extension to `deriving` that enables programmers to compose instances from named programming patterns, thereby turning `deriving` into a high-level domain-specific language for defining instances. Deriving Via leverages newtypes—an already familiar tool of the Haskell trade—to declare recurring patterns in a way that both feels natural and allows a high degree of abstraction.

CCS Concepts • **Software and its engineering → Functional languages**; *Data types and structures*;

Keywords type classes, instances, deriving, Haskell, functional programming

ACM Reference Format:
Baldur Blöndal, Andres Löh, and Ryan Scott. 2018. Deriving Via: or, How to Turn Hand-Written Instances into an Anti-Pattern. In *Proceedings of the 11th ACM SIGPLAN International Haskell Symposium (Haskell '18), September 27–28, 2018, St. Louis, MO, USA.* ACM, New York, NY, USA, 13 pages. https://doi.org/10.1145/3242744.3242746

1 Introduction

In Haskell, type classes capture common interfaces. When defining class instances, we often discover repeated patterns where different instances have the same definition. For example, the following instances appear in the base library of the Glasgow Haskell Compiler (GHC):

```
instance Monoid a => Monoid (IO a) where
  mempty  = pure mempty
  mappend = liftA2 mappend
```

```
instance Monoid a => Monoid (ST s a) where
  mempty  = pure mempty
  mappend = liftA2 mappend
```

These have completely identical instance bodies. The underlying pattern works not only for `IO` and `ST s`, but for any applicative functor `f`.

It is tempting to avoid this obvious repetition by defining an instance for all such types in one fell swoop:

```
instance (Applicative f, Monoid a)
   => Monoid (f a) where
  mempty  = pure mempty
  mappend = liftA2 mappend
```

Unfortunately, this general instance is undesirable as it overlaps with all other `(f a)`-instances. Instance resolution will match the instance head first before considering the context, whether `f` is applicative or not. Once GHC has commited to an instance, it will never backtrack. Consider:

```
newtype Endo a = MkEndo (a -> a)   -- Data.Monoid
```

Here, `Endo` is not an applicative functor, but it still admits a perfectly valid `Monoid` instance that overlaps with the general instance above:

```
instance Monoid (Endo a) where
  mempty = MkEndo id
  mappend (MkEndo f) (MkEndo g) = MkEndo (f . g)
```

Moreover, even if we have an applicative functor `f` on our hands, there is no guarantee that this is the definition we want. Notably, lists are the *free monoid* (i.e, the most 'fundamental' monoid) but that instance does not coincide with the rule above and in particular, imposes no `(Monoid a)` constraint:

```
instance Monoid [a] where
  mempty  = []
  mappend = (++)
```

In fact, the monoid instance for lists is captured by a *different* rule based on `Alternative`:

```
instance Alternative f => Monoid (f a) where
  mempty  = empty
  mappend = (<|>)
```

Because instance resolution never backtracks, we cannot define these two distinct rules for `Monoid (f a)` at the same time, even with overlapping instances.

The only viable workaround using the Haskell type class system is to write the instances for each data type by hand, each one with an identical definition (like the instances for `IO a` and `ST s a`), which is extremely unsatisfactory:

- It is not obvious that we are instantiating a general principle.
- Because the general principle is not written down in code with a name and documentation, it has to be communicated through folklore or in comments and is difficult to discover and search for. Our code has lost a connection to its origin.
- There are many such rules, some quite obvious, but others more surprising and easy to overlook.
- While the work required to define instances manually for `Monoid`—which only has two methods—is perhaps acceptable, it quickly becomes extremely tedious and error-prone for classes with many methods.

As an illustration of the final point, consider `Num`. There is a way to lift a `Num` instance through any applicative functor:[1]

```
instance (Applicative f, Num a) => Num (f a) where
  (+) = liftA2 (+)
  (-) = liftA2 (-)
  (*) = liftA2 (*)
  negate = liftA negate
  abs    = liftA abs
  signum = liftA signum
  fromInteger = pure . fromInteger
```

Defining such boilerplate instances manually for concrete type constructors is so annoying that Conal Elliott introduced a preprocessor [8] for this particular use case several years ago.

1.1 Deriving

Readers familiar with Haskell's deriving mechanism may wonder why we cannot simply derive all the instances we just discussed. Unfortunately, our options are very limited.

To start, `Monoid` is not one of the few blessed type classes that GHC has built-in support to derive. It so happens that `(IO a)`, `(ST s a)` and `(Endo a)` are all newtypes, so they are in principle eligible for *generalized newtype deriving* (GND), in which their instances could be derived by reusing the instances of their underlying types [1]. However, this would give us the wrong definition in all three cases.

Our last hope is that the the `Monoid` type class has a suitable generic default implementation [11]. If that were the case, we could use a deriving clause in conjunction with the `DeriveAnyClass` extension, and thereby get the compiler to generate an instance for us.

However, there is no generic default for `Monoid`, a standard class from the base library (which would be difficult to change). But even if a generic instance existed, it would still capture a *single* rule over all others, so we couldn't ever use it to derive both the monoid instance for lists and that for `ST s a`.

We thus have no other choice but to write some instances by hand. This means that we have to provide explicit implementations of at least a minimal subset of the class methods. There is no middle ground here, and the additional work required compared to **deriving** can be drastic—especially if the class has many methods—so the option of using **deriving** remains an appealing alternative.

1.2 Introducing Deriving Via

We are now going to address this unfortunate lack of abstraction and try to bridge the gap between manually defined instances and the few available **deriving** mechanisms we have at our disposal.

Our approach has two parts:

1. We capture general rules for defining new instances using newtypes.
2. We introduce Deriving Via, a new language construct that allows us to use such newtypes to explain to the compiler exactly how to construct the instance without having to write it by hand.

As a result, we are no longer limited to a fixed set of predefined ways to define particular class instances, but can instead teach the compiler new rules for deriving instances, selecting the one we want using a high-level description.

Let us look at examples. For the *first part*, we revisit the rule that explains how to lift a monoid instance through an applicative functor. We can turn the problematic generic and overlapping instance for `Monoid (f a)` into an entirely unproblematic instance by defining a suitable adapter newtype [9] and wrapping the instance head in it:

```
newtype Ap f a = Ap (f a)
instance (Applicative f, Monoid a)
   => Monoid (Ap f a) where
  mempty = Ap (pure mempty)
  mappend (Ap f) (Ap g) = Ap (liftA2 mappend f g)
```

Since GHC 8.4, we also need a `Semigroup` instance, because it is now a superclass of `Monoid`[2]:

```
instance (Applicative f, Semigroup a)
   => Semigroup (Ap f a) where
  Ap f <> Ap g = Ap (liftA2 (<>) f g)
```

[1]Similarly for `Floating` and `Fractional`, numeric type classes with a combined total of 25 methods (15 for a minimal definition).

[2]See Section 4.4 for a more detailed discussion of this aspect.

The *second part* is to now use such a rule in our new form of **deriving** statement. We can do this when defining a new data type, such as in

```
data Maybe a = Nothing | Just a
  deriving Monoid via (Ap Maybe a)
```

This requires that we independently have an Applicative instance for Maybe, but then we obtain the desired Monoid instance nearly for free.

In the deriving clause, **via** is a new language construct that explains *how* GHC should derive the instance, namely by reusing the Monoid instance already available for the **via** type, Ap Maybe a. It should be easy to see why this works: due to the use of a newtype, Ap Maybe a has the same internal representation as Maybe a, and any instance available on one type can be made to work on the other by suitably wrapping or unwrapping a newtype. In more precise language, Ap Maybe a and Maybe a are representationally equal [1].

The Data.Monoid module defines many further adapters that can readily be used with Deriving Via. For example, the rule that obtains a Monoid instance from an Alternative instance is already available through the Alt newtype:

```
newtype Alt f a = Alt (f a)

instance Alternative f => Monoid (Alt f a) where
  mempty                = Alt empty
  mappend (Alt f) (Alt g) = Alt (f <|> g)

instance Alternative f => Semigroup (Alt f a) where
  (<>) = mappend
```

Note that while Alt has the same definition as Ap, its Monoid instance is different, and by naming the type in a **via** clause, we can explicitly select the instance we are interested in.

Using adapters such as Ap and Alt, a vast amount of Monoid instances that currently have to be defined by hand can instead be derived using the **via** construct.

1.3 Contributions and Structure of the Paper

Many hand-written instances that occur in Haskell code are in fact instantiations of similar rules as we have just shown, and can be replaced by Deriving Via. We argue that expressing an instance as the instantiation of a rule should be the norm, and using a hand-written instance when a rule could be used instead should be discouraged, or even be considered an anti-pattern.

Throughout the paper, we provide many additional examples of the use of Deriving Via, starting with a case study using the QuickCheck library (Section 2).

We also provide a detailed explanation of how to type-check and translate Deriving Via clauses (Section 3).

The idea of Deriving Via is surprisingly simple, yet it has a number of powerful and equally surprising properties:

- It further generalizes the *generalized newtype deriving* extension. (Section 3.2.1).
- It additionally generalizes the concept of *default signatures*. (Section 4.2).
- It provides a possible solution to the problem of introducing additional boilerplate code when introducing new superclasses (such as Applicative for Monad, Section 4.4).
- It allows for reusing instances not just between representationally equal types, but also between isomorphic or similarly related types (Section 4.3).

Our extension is fully implemented in GHC and will be present in version 8.6.

2 Case Study: QuickCheck

QuickCheck [3] is a well-known Haskell library for randomized property-based testing. At the core of QuickCheck's test-case generation functionality is the Arbitrary class. Its primary method is arbitrary, which describes how to generate suitable random values of a given size and type. It also has a method shrink that is used to try to shrink failing counterexamples of test properties.

Many standard Haskell types, such as Int and lists, are already instances of Arbitrary. This can be very convenient, because many properties involving these types can be quick-checked without any extra work.

On the other hand, there are often additional constraints imposed on the actual values of a type that are not sufficiently expressed in their types. Depending on the context and the situation, we might want to guarantee that we generate positive integers, or non-empty lists, or even sorted lists.

The QuickCheck library provides a number of newtype-based adapters (called *modifiers* in the library) for this purpose. As an example, QuickCheck defines:

```
newtype NonNegative a =
  NonNegative {getNonNegative :: a}
```

which comes with a predefined instance of the form

```
instance (Num a, Ord a, Arbitrary a)
   => Arbitrary (NonNegative a)
```

that explains how to generate and shrink non-negative numbers. A user who wants a non-negative integer can now use NonNegative Int rather than Int to make this obvious.

This approach, however, has a drastic disadvantage: we have to wrap each value in an extra constructor, and the newtype and constructor are QuickCheck-specific. An implementation detail (the choice of testing library) leaks into the data model of an application. While we might be willing to use domain-specific newtypes for added type safety, such as Age or Duration, we might not be eager to add QuickCheck modifiers everywhere. And what if we need more than one modifier? And what if other libraries export their own set of modifiers as well? We certainly do not want to change the actual definition of our data types (and corresponding code) whenever we start using a new library.

With Deriving Via, we have the option to reuse the existing infrastructure of modifiers without paying the price of cluttering up our data type definitions. We can choose an actual domain-specific newtype such as

```haskell
newtype Duration = Duration Int   -- in seconds
```

and now specify exactly how the `Arbitrary` should be derived for this:

```haskell
  deriving Arbitrary via (NonNegative Int)
```

This yields an `Arbitrary` instance that generates only non-negative integers. Only the deriving clause changes, not the data type itself. If we later decide we want only positive integers as durations, we replace `NonNegative` with `Positive` in the deriving clause. Again, the data type itself is unaffected. In particular, we do not have to change any constructor names anywhere in our code.

2.1 Composition

Multiple modifiers can be combined. For example, there is another modifier called `Large` that will scale up the size of integral values being produced by a generator. It is defined as

```haskell
newtype Large a = Large {getLarge :: a}
```

with a corresponding `Arbitrary` instance:

```haskell
instance (Integral a, Bounded a) => Arbitrary (Large a)
```

For our `Duration` type, we can easily write[3]

```haskell
  deriving Arbitrary via (NonNegative (Large Int))
```

and derive an instance which only generates `Duration` values that are both non-negative *and* large. This works because `Duration` still shares the same runtime representation as `NonNegative (Large Int)` (namely, that of `Int`), so the latter's `Arbitrary` instance can be reused.

2.2 Adding New Modifiers

Of course, we can add add our own modifiers if the set of predefined modifiers is not sufficient. For example, it is difficult to provide a completely generic `Arbitrary` instance that works for all data types, simply because there are too many assumptions about what makes good test data that need to be taken into account.

But for certain groups of data types, there are quite reasonable strategies of coming up with generic instances. For example, for enumeration types, one strategy is to desire a uniform distribution of the finite set of values. QuickCheck even offers such a generator, but it does not expose it as a newtype modifier:

```haskell
arbitraryBoundedEnum :: (Bounded a, Enum a) => Gen a
```

But from this, we can easily define our own:

```haskell
newtype BoundedEnum a = BoundedEnum a

instance (Bounded a, Enum a)
   => Arbitrary (BoundedEnum a) where
  arbitrary = BoundedEnum <$> arbitraryBoundedEnum
```

We can then use this functionality to derive `Arbitrary` for a new enumeration type:

```haskell
data Weekday = Mo | Tu | We | Th | Fr | Sa | Su
  deriving (Enum, Bounded)
  deriving Arbitrary via (BoundedEnum Weekday)
```

2.3 Parameterized Modifiers

Sometimes, we might want to parameterize a generator with extra data. We can do so by defining a modifier that has extra arguments and using those extra arguments in the associated `Arbitrary` instance.

An extreme case that also makes use of type-level programming features in GHC is a modifier that allows us to specify a lower and an upper bound of a generated natural number.

```haskell
newtype Between (l :: Nat) (u :: Nat) = Between Integer

instance (KnownNat l, KnownNat u)
   => Arbitrary (Between l u) where
  arbitrary = Between <$>
    choose (natVal @l Proxy, natVal @u Proxy)
```

(Note that this instance makes use of visible type application [7] in `natVal @l` and `natVal @u`.)

We can then equip an application-specific type for years with a generator that lies within a plausible range:

```haskell
newtype Year = Year Integer
  deriving Show
  deriving Arbitrary via (Between 1900 2100)
```

In general, we can use this technique of adding extra parameters to a newtype to support additional ways to configure the behavior of derived instances.

3 Typechecking and Translation

Seeing enough examples of Deriving Via can give the impression that it is a somewhat magical feature. In this section, we aim to explain the magic underlying Deriving Via by giving a more precise description of:

- how Deriving Via clauses are typechecked,
- what sort of code Deriving Via generates behind the scenes, and
- how to determine the scoping of type variables in Deriving Via clauses.

[3] Here and in many later places, we use **`deriving`** clauses in isolation, in order to highlight the part of the syntax we are focusing on and to not repeat **`data`** or **`newtype`** unnecessarily often. It is still understood that the **`deriving`** clause is syntactically attached to the data type declaration mentioned in the text – in this case, `Duration`. Our extension is also compatible with `StandaloneDeriving`, which is briefly discussed in Section 6.

To avoid clutter, we assume that all types have monomorphic kinds. However, it is easy to incorporate kind polymorphism [13], and our implementation of these ideas in GHC does so.

3.1 Well-Typed Uses of Deriving Via

Deriving Via grants the programmer the ability to put extra types in her programs, but the flip side to this is that it is possible for her to accidentally put total nonsense into a Deriving Via clause, such as:

```
newtype S = S Char
  deriving Eq via Maybe
```

In this section, we describe a general algorithm for when a Deriving Via clause should typecheck, which will allow us to reject ill-formed examples like the one above.

3.1.1 Aligning Kinds

Suppose we are deriving the following instance:

```
data D d₁ … dₘ
  deriving (C c₁ … cₙ) via (V v₁ … vₚ)
```

In order for this declaration to typecheck, we must check the *kinds* of each type. In particular, the following conditions must hold:

1. The type `C c₁ … cₙ` must be of kind `(k₁ -> … -> kᵣ -> *) -> Constraint` for some kinds `k₁, …, kᵣ`. The reason is that the instance [4] we must generate,

   ```
   instance C c₁ … cₙ (V v₁ … vₚ) =>
            C c₁ … cₙ (D d₁ … dᵢ) where …
   ```

   requires that we can apply `C c₁ … cₙ` to the types `V v₁ … vₚ` and `D d₁ … dᵢ` (where $i = m - r$, see Section 3.1.2). Therefore, it would be nonsense to try to derive an instance of `C c₁ … cₙ` if it had kind, say, `Constraint`, since it couldn't be applied as above.
2. The kinds of `V v₁ … vₚ` and `D d₁ … dᵢ`, and the kind of the argument to `C c₁ … cₙ` must all unify. This check rules out the above example of `deriving Eq via Maybe`, as it does not even make sense to talk about reusing the `Eq` instance for `Maybe`—which is of kind `(* -> *)`—as `Eq` instances can only exist for types of kind `*`.

3.1.2 Shaping the Data Type

Note that in the conditions above, we specify `D d₁ … dᵢ` (for some i), instead of `D d₁ … dₘ`. That is because in general, the kind of the argument to `C c₁ … cₙ` is allowed to be different from the kind of `D d₁ … dₘ`! For instance, the following example is perfectly legitimate:

[4]Technically, the context that is produced is not `C c₁ … cₙ (V v₁ … vₚ)`, but instead the residual constraints that are produced from GHC's constraint solver after simplifying that context. This is a property that Deriving Via shares with other forms of `deriving` as well.

```
class Functor (f :: * -> *) where …
data Foo a = Foo a a
  deriving Functor
```

despite the fact that `Foo a` has kind `*` and the argument to `Functor` has kind `(* -> *)`. This is because the code that actually gets generated has the following shape:

```
instance Functor Foo where …
```

To put it differently, we have dropped the `a` in `Foo a` before applying `Functor` to it. The power to drop variables from the data type is part of what makes deriving clauses so flexible.

To determine how many variables to drop, we must examine the kind of `C c₁ … cₙ`, which by condition (1) is of the form `((k₁ -> … -> kᵣ -> *) -> Constraint)` for some kinds `k₁, …, kᵣ`. Then the number of variables to drop is simply r, so to compute the i in `D d₁ … dᵢ`, we take $i = m - r$.

This is better explained by example, so consider the following two scenarios, both of which typecheck:

```
newtype A a = A a deriving Eq      via (Identity a)
newtype B b = B b deriving Functor via Identity
```

In the first example, we have the class `Eq`, which is of kind `* -> Constraint`. The argument to `Eq`, which is of kind `*`, does not require that we drop any variables. As a result, we check that `A a` is of kind `*`, which is the case.

In the second example, we have the class `Functor`, which is of kind `(* -> *) -> Constraint`. The argument to `Functor` is of kind `(* -> *)`, which requires that we drop one variable from `B b` to obtain `B`. We then check that `B` is kind of `(* -> *)`, which is true.

3.2 Code Generation

Once the typechecker has ascertained that a `via` type is fully compatible with the data type and the class for which an instance is being derived, GHC proceeds with generating the code for the instance itself. This generated code is then fed *back* into the typechecker, which acts as a final sanity check that GHC is doing the right thing under the hood.

3.2.1 Generalized Newtype Deriving (GND)

The process by which Deriving Via generates code is heavily based off of the approach that generalized newtype deriving (GND) takes, so it is informative to first explain how GND works. From there, Deriving Via is a straightforward generalization—so much so that Deriving Via can be thought of as “generalized GND”.

Our running example in this section will be the newtype `Age`, which is a simple wrapper around `Int` (which we will call the *representation type*):

```
newtype Age = MkAge Int
  deriving Enum
```

A naïve way to generate code would be to manually wrap and unwrap the `MkAge` constructor wherever necessary, such as in the code below:

```
instance Enum Age where
  toEnum i = MkAge (toEnum i)
  fromEnum (MkAge x) = fromEnum x
  enumFrom (MkAge x) = map MkAge (enumFrom x)
```

This works, but is somewhat unsatisfying. After all, a newtype is intended to be a zero-cost abstraction that acts identically to its representation type at runtime. Accordingly, any function that mentions a newtype in its type signature should be able to be converted to a new function with all occurrences of the newtype in the type signature replaced with the representation type, and moreover, that new function should behave identically to the old one at runtime.

Unfortunately, the implementation of `enumFrom` may not uphold this guarantee. While wrapping and unwrapping the `MkAge` constructor is certain to be a no-op, the `map` function is definitely *not* a no-op, as it must walk the length of a list. But the fact that we need to call `map` in the first place feels rather silly, as all we are doing is wrapping a newtype at each element.

Luckily, there is a convenient solution to this problem: the safe `coerce` function [1]:

```
coerce :: Coercible a b => a -> b
```

Operationally, `coerce` can be thought of as behaving like its wily cousin, `unsafeCoerce`, which takes a value of one type as casts it to a value at a another type. Unlike `unsafeCoerce`, which can break programs if used carelessly, `coerce` is completely type-safe due to its use of the `Coercible` constraint. We explain `Coercible` in more detail in Section 3.2.2, but for now, it suffices to say that a `Coercible a b` constraint witnesses the fact that two types `a` and `b` have the same representation at runtime, and thus any value of type `a` can be safely cast to type `b`.

Armed with `coerce`, we can show what code GND would actually generate for the `Enum Age` instance above:

```
instance Enum Age where
  toEnum =
    coerce @(Int -> Int) @(Int -> Age) toEnum
  fromEnum =
    coerce @(Int -> Int) @(Age -> Int) fromEnum
  enumFrom =
    coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Now we have a strong guarantee that the `Enum` instance for `Age` has exactly the same runtime characteristics as the instance for `Int`. As an added benefit, the code ends up being simpler as every method can be implemented as a straightforward application of `coerce`. The only interesting part is generating the two explicit type arguments [7] that are being used to specify the source type (using the representation type) and the target type (using the newtype) of `coerce`.

3.2.2 The `Coercible` Constraint

A `Coercible` constraint can be thought of as evidence that GHC can use to cast between two types. `Coercible` is not a type class, so it is impossible to write a `Coercible` instance by hand. Instead, GHC can generate and solve `Coercible` constraints automatically as part of its built-in constraint solver, much like it can solve equality constraints. (Indeed, `Coercible` can be thought of as a broader notion of equality among types.)

As mentioned in the previous section, a newtype can be safely cast to and from its representation type, so GHC treats them as inter-`Coercible`. Continuing our earlier example, this would mean that GHC would be able to conclude that:

```
instance Coercible Age Int
instance Coercible Int Age
```

But this is not all that `Coercible` is capable of. A key property is that GHC's constraint solver can look inside other type constructors when determining whether two types are inter-`Coercible`. For instance, both of these statements hold:

```
instance Coercible (Age -> [Age]) (Int -> [Int])
instance Coercible (Int -> [Int]) (Age -> [Age])
```

This demonstrates the ability to cast through the function and list type constructors. This ability is important, as our derived `enumFrom` instance would not typecheck otherwise!

Another crucial fact about `Coercible` that we rely on is that it is transitive: if `Coercible a b` and `Coercible b c` hold, then `Coercible a c` also holds. This is perhaps unsurprising if one views `Coercible` as an equivalence relation, but it is a fact that is worth highlighting, as the transitivity of `Coercible` is what allows us to `coerce` *between newtypes*. For instance, if we have these two newtypes:

```
newtype A a = A [a]
newtype B   = B [Int]
```

then GHC is able to conclude that `Coercible (A Int) B` holds, because we have the following `Coercible` rules

```
instance Coercible (A Int) [Int]
instance Coercible [Int] B
```

as well as transitivity. As we will discuss momentarily, Deriving Via in particular makes heavy use of the transitivity of `Coercible`.

3.2.3 From GND to Deriving Via

As we saw in Section 3.2.1, the code which GND generates relies on `coerce` to do the heavy lifting. In this section, we generalize this technique slightly to give us a way to generate code for Deriving Via.

Recall the following GND-derived instance:

```
newtype Age = MkAge Int deriving Enum
```

As stated above, it generates the following code for `enumFrom`:

```
instance Enum Age where
  ...
  enumFrom =
    coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Here, there are two crucially important types: the representation type, Int, and the original newtype itself, Age. The implementation of enumFrom simply sets up an invocation of coerce enumFrom, with explicit type arguments to indicate that we should reuse the existing enumFrom implementation for Int and reappropriate it for Age.

The only difference in the code that GND and Deriving Via generate is that in the former strategy, GHC always picks the representation type for you, but in Deriving Via, the *user* has the power to choose this type. For example, if a programmer had written this instead:

```
newtype T = T Int
instance Enum T where ...
```

```
newtype Age = MkAge Int deriving Enum via T
```

then the following code would be generated:

```
  enumFrom =
    coerce @(T -> [T]) @(Age -> [Age]) enumFrom
```

This time, GHC coerces from an enumFrom implementation for T (the **via** type) to an implementation for Age. (Recall from Section 3.2.2 that this is possible since we can coerce transitively from T to Int to Age).

Now we can see why the instances that Deriving Via can generate are a strict superset of those that GND can generate. For instance, our earlier GND example

```
newtype Age = MkAge Int deriving Enum
```

could equivalently have been written using Deriving Via like so:

```
newtype Age = MkAge Int deriving Enum via Int
```

Unlike GND, which is only suitable for deriving instances for newtypes, Deriving Via can derive instances for data types and newtypes alike (see Weekday in Section 2.2 for one example of a data type).

3.3 Type Variable Scoping

In the remainder of this section, we present an overview of how type variables are bound in Deriving Via clauses, and over what types they scope. Deriving Via introduces a new place where types can go, and more importantly, it introduces a new place where type variables can be *quantified*, so it takes some amount of care to devise a consistent treatment for it.

3.3.1 Binding Sites

Consider the following example:

```
data Foo a = ...
  deriving (Baz a b c) via (Bar a b)
```

Where is each type variable quantified?

- a is bound by Foo itself in the declaration **data** Foo a. Such a variable scopes over both the derived class, Baz a b c, as well as the **via** type, Bar a b.
- b is bound by the **via** type, Bar a b. Note that b is bound here but a is not, as it was bound earlier by the **data** declaration. b scopes over the derived class type, Baz a b c, as well.
- c is bound by the derived class, Baz a b c, as it was not bound elsewhere. (a and b were bound earlier.)

In other words, the order of scoping starts at the **data** declaration, then the **via** type, and then the derived classes associated with that **via** type.

3.3.2 Establishing Order

This scoping order may seem somewhat surprising, as one might expect the type variables bound by the derived classes to scope over the **via** type instead. However, this choice introduces additional complications that are tricky to resolve. For instance, consider a scenario where one attempts to derive multiple classes at once with a single **via** type:

```
data D
  deriving (C1 a, C2 a) via (T a)
```

Suppose we first quantified the variables in the derived classes and made them scope over the **via** type. Because each derived class has its own type variable scope, the a in C1 a would be bound independently from the a in C2 a. In other words, we would have something like this (using a hypothetical **forall** syntax):

```
  deriving (forall a . C1 a, forall a . C2 a) via (T a)
```

Now we are faced with a thorny question: which a is used in the **via** type, T a? There are multiple choices here, since the a variables in C1 a and C2 a are distinct! This is an important decision, since the kinds of C1 and C2 might differ, so the choice of a could affect whether T a kind-checks or not.

On the other hand, if one binds the a in T a first and has it scope over the derived classes, then this becomes a non-issue. We would instead have this:

```
  deriving (C1 a, C2 a) via (forall a . T a)
```

Now, there is no ambiguity regarding a, as both a variables in the list of derived classes were bound in the same place.

It might feel strange visually to see a variable being used *before* its binding site (assuming one reads code from left to right). However, this is not unprecedented within Haskell, as this is also legal:

```
f = g + h where g = 1; h = 2
```

In this example, we have another scenario where things are bound (g and h) after their use sites. In this sense, the **via** keyword is continuing a rich tradition pioneered by **where** clauses.

One alternative idea (which was briefly considered) was to put the **via** type *before* the derived classes so as to avoid this "zigzagging" scoping. However, this would introduce additional ambiguities. Imagine one were to take the example

```
deriving Z via X Y
```

and convert it to a form in which the `via` type came first:

```
deriving via X Y Z
```

Should this be parsed as `(X Y) Z`, or `X (Y Z)`? It's not clear visually, so this choice would force programmers to write additional parentheses.

4 More Use Cases

We have already seen in Section 2 how Deriving Via facilitates greater code reuse in the context of QuickCheck. This is far from the only domain where Deriving Via proves to be a natural fit, however. In fact, there are so many of these domains, there would be enough to fill pages upon pages!

Unfortunately, we do not have enough space to document all of these use cases, so in this section, we present a cross-section of scenarios in which Deriving Via can capture interesting patterns and allow programmers to abstract over them in a convenient way.

4.1 Asymptotic Improvements with Ease

A widely used feature of type classes is their ability to give default implementations for their methods if a programmer leaves them off. One example of this can be found in the `Applicative` class. The main workhorse of `Applicative` is the `(<*>)` method, but on occasion, it is more convenient to use the `(<*)` or `(*>)` methods, which sequence their actions but discard the result of one of their arguments:

```
class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b

  (<*) :: f a -> f b -> f a
  (<*) = liftA2 (\ a _ -> a)
  (*>) :: f a -> f b -> f b
  (*>) = liftA2 (\ _ b -> b)
```

As shown here, `(<*)` and `(*>)` have default implementations in terms of `liftA2`. This works for any `Applicative`, but is not as efficient as it could be in some cases. For some instances of `Applicative`, we can actually implement these methods in $O(1)$ time instead of using `liftA2`, which can often run in superlinear time. One such `Applicative` is the function type `(->)`:

```
instance Applicative ((->) r) where
  pure = const
  (<*>) f g x = f x (g x)
  f <* _ = f
  _ *> g = g
```

Note that we had to explicitly define `(<*)` and `(*>)`, as the default implementations would not have been as efficient.

But `(->)` is not the only type for which this trick works—it also works for any data type that is isomorphic to `(->) r` (for some `r`). These function-like types are characterized by the `Representable` type class:

```
class Functor f => Representable f where
  type Rep f
  index :: f a -> (Rep f -> a)
  tabulate :: (Rep f -> a) -> f a
```

This is a good deal more abstract than `(->) r`, so it can be helpful to see how `Representable` works for `(->) r` itself:

```
instance Representable ((->) r) where
  type Rep ((->) r) = r
  index f = f
  tabulate f = f
```

With `Representable`, we can codify the `Applicative` shortcut for `(<*)` and `(*>)` with a suitable newtype:

```
newtype WrapRep f a = WrapRep (f a)
  deriving (Functor, Representable)

instance Representable f
   => Applicative (WrapRep f) where
  pure = tabulate . pure
  f <*> g = tabulate (index f <*> index g)

  f <* _ = f
  _ *> g = g
```

Now, instead of having to manually override `(<*)` and `(*>)` to get the desired performance, one can accomplish this in a more straightforward fashion by using Deriving Via:

```
newtype IntConsumer a = IntConsumer (Int -> a)
  deriving (Functor, Representable)
  deriving Applicative via (WrapRep IntConsumer)
```

Not only does this save code in the long run, but it also gives a name to the optimization being used, which allows it to be documented, exported from a library, and thereby easier to spot "in the wild" for other programmers.

4.2 Making Defaults more Flexible

In the previous section, we saw an example of how relying too much on a type class's default implementations can backfire. This is an unfortunately common trend with type classes in general: many classes try to pick one-size-fits-all defaults that do not work well in certain scenarios, but because Haskell allows specifying only one default per method, if the provided default does not work for a programmer's use case, then she is forced to write her own implementations by hand.

In this section, we continue the trend of generalizing defaults by looking at another language extension that Deriving Via can substitute for: *default signatures*. Default signatures (a slight generalization of default implementations) can eliminate large classes of boilerplate, but they too are limited by the one-default-per-method restriction. Here, we demonstrate how one can scrap uses of default signatures in favor of Deriving Via and show how Deriving Via can overcome the limitations of default signatures.

The typical use case for default signatures is when one has a class method that has a frequently used default implementation at a constrained type. For instance, consider a `Pretty` class with a method `pPrint` for pretty-printing data:

```
class Pretty a where
  pPrint :: a -> Doc
```

Coming up with `Pretty` instances for the vast majority of data types is repetitive and tedious, so a common pattern is to abstract away this tedium using generic programming libraries, such as those found in `GHC.Generics` [11] or generics-sop [4]. For example, using `GHC.Generics`, we can define

```
genericPPrint ::
  (Generic a, GPretty (Rep a)) => a -> Doc
```

The details of how `Generic`, `GPretty`, and `Rep` work are not important to understanding the example. What is important is to note that we cannot just add

```
  pPrint = genericPPrint
```

as a conventional default implementation to the `Pretty` class, because it does not typecheck due to the extra constraints.

Before the advent of default signatures, one had to work around this by defining `pPrint` to be `genericPPrint` in every `Pretty` instance, as in the examples below:

```
instance Pretty Bool where
  pPrint = genericPPrint

instance Pretty a => Pretty (Maybe a) where
  pPrint = genericPPrint
```

To avoid this repetition, default signatures allow one to provide a default implementation of a class method using *additional* constraints on the method's type. For example:

```
class Pretty a where
  pPrint :: a -> Doc
  default pPrint ::
    (Generic a, GPretty (Rep a)) => a -> Doc
  pPrint = genericPPrint
```

Now, if any instances of `Pretty` are given without an explicit definition of `pPrint`, the default implementation is used. For this to typecheck, the data type a used in the instance must satisfy the constraints `(Generic a, GPretty (Rep a))`. Thus, we can reduce the instances above to just

```
instance Pretty Bool
instance Pretty a => Pretty (Maybe a)
```

Although default signatures remove the need for many occurrences of boilerplate code, it also retains a significant limitation of Haskell default methods: every class method can have at most one default implementation. As a result, default signatures effectively endorse one default implementation as the canonical one. But in many scenarios, there is far more than just one way to do something. Our `pPrint` example is no exception. Instead of `genericPPrint`, one might want to:

- leverage a `Show`-based default implementation instead of a `Generic`-based one,
- use a different generic programming library, such as generics-sop, instead of `GHC.Generics`, or
- use a tweaked version of `genericPPrint` that displays extra debugging information.

All of these are perfectly reasonable choices a programmer might want to make, but alas, GHC lets type classes bless each method with only one default.

Fortunately, Deriving Via provides a convenient way of encoding default implementations with the ability to toggle between different choices: newtypes! For instance, we can codify two different approaches to implementing `pPrint` as follows:

```
newtype GenericPPrint a = GenericPPrint a

instance (Generic a, GPretty (Rep a))
   => Pretty (GenericPPrint a) where
  pPrint (GenericPPrint x) = genericPPrint x

newtype ShowPPrint a = ShowPPrint a

instance Show a => Pretty (ShowPPrint a) where
  pPrint (ShowPPrint x) = stringToDoc (show x)
```

With these newtypes in hand, choosing between them is as simple as changing a single type:

```
  deriving Pretty via (GenericPPrint DataType1)
  deriving Pretty via (ShowPPrint    DataType2)
```

We have seen how Deriving Via makes it quite simple to give names to particular defaults, and how toggling between defaults is a matter of choosing a name. In light of this, we believe that many current uses of default signatures ought to be removed entirely and replaced with the Deriving Via-based idiom presented in this section. This avoids the need to bless one particular default and forces programmers to consider which default is best suited to their use case, instead of blindly trusting the type class's blessed default to always do the right thing.

An additional advantage is that it allows decoupling the definition of such defaults from the site of the class definition. Hence, if a package author is hesitant to add a default because that might incur an unwanted additional dependency, nothing is lost, and the default can simply be added in a separate package.

4.3 Deriving via Isomorphisms

All of the examples presented thus far in the paper rely on deriving through data types that have the same runtime representation as the original data type. In the following, however, we point out that—perhaps surprisingly—we can also derive through data types that are *isomorphic*, not just representationally equal. To accomplish this feat, we rely on techniques from generic programming.

Let us go back to QuickCheck (as in Section 2) once more and consider the data type

```
data Track = Track Title Duration
```

for which we would like to define an `Arbitrary` instance. Let us further assume that we already have `Arbitrary` instances for both `Title` and `Duration`.

The QuickCheck library defines an instance for pairs, so we could generate values of type `(Title, Duration)`, and in essence, this is exactly what we want. But unfortunately, the two types are not inter-`Coercible`, even though they are isomorphic[5].

However, we can exploit the isomorphism and still get an instance for free, and the technique we apply is quite widely applicable in similar situations. As a first step, we declare a newtype to capture that one type is isomorphic to another:

```
newtype SameRepAs a b = SameRepAs a
```

We call this type `SameRepAs`, because it denotes that `a` and `b` have inter-`Coercible` generic representations, i.e., that

```
Coercible (Rep a ()) (Rep b ())
```

holds. Furthermore, the type `SameRepAs a b` is representationally equal to `a`, which implies that `a` and `SameRepAs a b` are inter-`Coercible`.

We now witness the isomorphism between the two types via their generic representations: if they have inter-`Coercible` generic representations, we can transform back and forth between the two types using the `from` and `to` methods of the `Generic` class from `GHC.Generics` [11]. We can use this to define a suitable `Arbitrary` instance for `SameRepAs`:

```
instance
  ( Generic a, Generic b
  , Coercible (Rep a ()) (Rep b ()), Arbitrary b
  ) => Arbitrary (a ‘SameRepAs‘ b) where
  arbitrary = SameRepAs . coerceViaRep <$> arbitrary
    where
      coerceViaRep :: b -> a
      coerceViaRep =
        to . (coerce :: Rep b () -> Rep a ()) . from
```

Here, we first use `arbitrary` to give us a generator of type `Gen b`, then coerce this via the generic representations into an `arbitrary` value of type `Gen a`.

Finally, we can use the following `deriving` declarations for `Track` to obtain the desired `Arbitrary` instance:

```
  deriving Generic
  deriving Arbitrary
    via (Track ‘SameRepAs‘ (String, Duration))
```

[5]Isomorphic in the sense that we can define a function from `Track` to `(Title, Duration)` and vice versa. Depending on the class we want to derive, sometimes an even weaker relationship between the types is sufficient, but we focus on the case of isomorphism here for reasons of space.

With this technique, we can significantly expand the “equivalence classes” of data types that can be used when picking suitable types to derive through.

4.4 Retrofitting Superclasses

On occasion, the need arises to retrofit an existing type class with a superclass, such as when `Monad` was changed to have `Applicative` as a superclass (which in turn has `Functor` as a superclass).

One disadvantage of such a change is that if the primary goal is to define the `Monad` instance for a type, one now has to write two additional instances, for `Functor` and `Applicative`, even though these instances are actually determined by the `Monad` instance.

With Deriving Via, we can capture this fact as a newtype, thereby making the process of defining such instances much less tedious:

```
newtype FromMonad m a = FromMonad (m a)
  deriving Monad

instance Monad m => Functor (FromMonad m) where
  fmap = liftM

instance Monad m => Applicative (FromMonad m) where
  pure  = return
  (<*>) = ap
```

Now, if we have a data type with a `Monad` instance, we can simply derive the corresponding `Functor` and `Applicative` instances by referring to `FromMonad`:

```
data Stream a b = Done b | Yield a (Stream a b)
  deriving (Functor, Applicative)
    via (FromMonad (Stream a))

instance Monad (Stream a) where
  return = Done

  Yield a k >>= f = Yield a (k >>= f)
  Done b >>= f    = f b
```

One potentially problematic aspect remains. Another proposal [12] has been put forth (but has not been implemented, as of now) to remove the `return` method from the `Monad` class and make it a synonym for `pure` from `Applicative`. The argument is that `return` is redundant, given that `pure` does the same thing with a more general type signature. All other prior discussion about the proposal aside, it should be noted that removing `return` from the `Monad` class would prevent `FromMonad` from working, as then `Monad` instances would not have any way to define `pure`. [6]

4.5 Avoiding Orphan Instances

Not only can Deriving Via quickly procure class instances, in some cases, it can eliminate the need for certain instances

[6]A similar, yet somewhat weaker, argument applies to suggested changes to relax the constraints of `liftM` and `ap` to merely `Applicative` and to change their definitions to be identical to `fmap` and `(<*>)`, respectively.

altogether. Haskell programmers often want to avoid *orphan instances*: instances defined in a separate module from both the type class and data types being used. Sometimes, however, it is quite tempting to reach for orphan instances, as in the following example adapted from a blog post by Gonzalez [10]:

```
newtype Plugin = Plugin (IO (String -> IO ()))
  deriving Semigroup
```

In order for this derived Semigroup instance to typecheck, there must be a Semigroup instance for IO available. Suppose for a moment that there was no such instance for IO. How could one work around this issue?

- One could patch the base library to add the instance for IO. But given base's slow release cycle, it would be a while before one could actually use this instance.
- Write an orphan instance for IO. This works, but is undesirable, as now anyone who uses Plugin must incur a possibly unwanted orphan instance.

Luckily, Deriving Via presents a more convenient third option: re-use a Semigroup instance from *another* data type. Recall the Ap data type from Section 1.2 that lets us define a Semigroup instance by lifting through an Applicative instance. As luck would have it, IO already has an Applicative instance, so we can derive the desired Semigroup instance for Plugin like so:

```
newtype Plugin = Plugin (IO (String -> IO ()))
  deriving Semigroup
    via (Ap IO (String -> Ap IO ()))
```

Note that we have to use Ap twice in the **via** type, corresponding to the two occurences of IO in the Plugin type. This is possible because Ap IO has the same representation as IO, and it is also necessary if we want to completely bypass the need for a Semigroup instance for IO: Via the inner Ap IO () and the existing instance

```
instance Semigroup b => Semigroup (a -> b)
```

we first obtain a Semigroup instance for String -> IO (), which we then, via the outer Ap IO application, lift to IO (String -> IO ()) and therefore the Plugin type.

5 Related Ideas

We have demonstrated in the previous section that Deriving Via is an extremely versatile technique, and can be used to tackle a wide variety of problems. Deriving Via also bears a resemblance to other distinct language features which address similar issues, so in this section, we present an overview of their similarities and differences.

5.1 Code Reuse in Dependent Type Theory

Diehl *et al.* present a dependent type theory which permits zero-cost conversions between indexed and non-indexed variants of data types [5], much in the same vein as Coercible. However, these conversions must be explicitly constructed with combinators, whereas Coercible-based casts are built automatically by GHC's constraint solver. Therefore, while Diehl *et al.* allow conversions between more data types than Deriving Via does, it also introduces some amount of boilerplate than Deriving Via avoids.

5.2 Explicit Dictionary Passing

The power and flexibility of Deriving Via is largely due to GHC's ability to take a class method of a particular type and massage it into a method of a different type. This process is almost completely abstracted away from the user, however. A user only needs to specify the types involved, and GHC will handle the rest behind the scenes.

An alternative approach, which would put more power into the hands of the programmer, is to permit the ability to explicitly construct and pass the normally implicit dictionary arguments corresponding to type class instances [6]. Unlike in Deriving Via, where going between class instances is a process that is carefully guided by the compiler, permitting explicit dictionary arguments would allow users to actually coerce concrete instance values and pass them around as first-class values. In this sense, explicit dictionary arguments could be thought of as a further generalization of the technique that Deriving Via uses.

However, explicit dictionary arguments are a considerable extension of the language and its type system, and we feel that to be too large a hammer for the nail we are trying to hit. Deriving Via works by means of a simple desugaring of code with some light typechecking on top, which makes it much simpler to describe and implement. Finally, the problem that explicit dictionaries aim to solve—resolving ambiguity in implicit arguments—almost never arises in Deriving Via, as the programmer must specify all the types involved in the process.

6 Current Status

We have implemented Deriving Via within GHC. Our implementation also interacts well with other GHC features that were not covered in this paper, such as kind polymorphism [13], StandaloneDeriving, and type classes with associated type families [2]. However, there are still challenges remaining, which we describe in this section.

6.1 Quality of Error Messages

The nice thing about **deriving** is that when it works, it tends to work extremely well. When it *doesn't* work, however, it can be challenging to formulate an error message that adequately explains what went wrong. The fundamental issue is that error messages resulting from uses of **deriving** are usually rooted in *generated* code, and pointing to code that the user did not write in error messages can lead to a confusing debugging experience.

Fortunately, we have found in our experience that the quality of Deriving Via-related error messages is overall on the positive side. GHC has already invested significant effort into making type errors involving `Coercible` to be easily digestible by programmers, so Deriving Via benefits from this work. For instance, if one inadvertently tries to derive through a type that is not inter-`Coercible` with the original data type, such as in the following example:

```
newtype UhOh = UhOh Char deriving Ord via Int
```

Then GHC will tell you exactly that, in plain language:

```
• Couldn't match representation of type Char with that of Int
    arising from the coercion of the method compare
      from type 'Int -> Int -> Ordering'
      to type 'UhOh -> UhOh -> Ordering'
```

That is not to say that every error message is this straightforward. There are some scenarios that produce less-than-ideal errors, such as this:

```
newtype Foo a = Foo (Maybe a) deriving Ord via a
```

```
• Occurs check: cannot construct the infinite type: a ~ Maybe a
    arising from the coercion of the method 'compare'
      from type 'a -> a -> Ordering'
      to type 'Foo a -> Foo a -> Ordering'
```

The real problem is that `a` and `Maybe a` do not have the same representation at runtime, but the error does not make this obvious. It is possible that one could add an *ad hoc* check for this class of programs, but there are likely many more tricky corner cases lurking around the corner given that one can put anything after **via**.

We do not propose a solution to this problem here, but instead note that issues with Deriving Via error quality are ultimately issues with `coerce` error quality, given that the error messages are a result of `coerce` failing to typecheck. It is likely that investing more effort into making `coerce`'s error messages easier to understand would benefit Deriving Via as well.

6.2 Multi-Parameter Type Classes

GHC extends Haskell by permitting type classes with more than one parameter. Multi-parameter type classes are extremely common in modern Haskell, to the point where we assumed the existence of them in Section 3.1.1 without further mention. However, multi-parameter type classes pose an intriguing design question when combined with Deriving Via and `StandaloneDeriving`, another GHC feature that allows one to write **deriving** declarations independently of a data type.

For example, one can write the following instance using `StandaloneDeriving`:

```
class Triple a b c where
  triple :: (a, b, c)
```

```
instance Triple () () () where
  triple = ((), (), ())
newtype A = A ()
newtype B = B ()
newtype C = C ()
deriving via () instance Triple A B C
```

However, the code this generates is somewhat surprising. Instead of reusing the `Triple () () ()` instance in the derived instance, GHC will attempt to reuse an instance for the type `Triple A B ()`. The reason is that, by convention, `StandaloneDeriving` will only ever coerce through the *last* argument of a class. That is because the standalone instance above would be the same as if a user had written:

```
newtype C = C () deriving (Triple A B) via ()
```

This consistency is perhaps a bit limiting in this context, where we have multiple arguments to `C` that one could "derive through". But it is not clear how GHC would figure out which of these arguments to `C` should be derived through, as there seven different combinations to choose from! It is possible that another syntax would need to be devised to allow users to specify which arguments should be coerced to avoid this ambiguity.

7 Conclusions

In this paper, we have introduced the Deriving Via language extension, explained how it is implemented, and shown a wide variety of use cases. We believe that Deriving Via has the potential to dramatically change the way we write instances, as it encourages giving names to recurring patterns and reusing them where needed. It is our feeling that most instance declarations that occur in the wild can actually be derived by using a pattern that deserves to be known and named, and that instances defined manually should become an anti-pattern in all but some rare situations.

Acknowledgements

We would like to thank Richard Eisenberg for his feedback on Section 3.3, as well as the first author's former colleagues at Standard Chartered Bank for their feedback. We also thank the anonymous reviewers and Simon Peyton Jones for their many insightful suggestions.

References

[1] Joachim Breitner, Richard A. Eisenberg, Simon Peyton Jones, and Stephanie Weirich. 2014. Safe Zero-cost Coercions for Haskell. In *Proceedings of the 19th ACM SIGPLAN International Conference on Functional Programming (ICFP '14)*. ACM, New York, NY, USA, 189–202. https://doi.org/10.1145/2628136.2628141

[2] Manuel M. T. Chakravarty, Gabriele Keller, and Simon Peyton Jones. 2005. Associated Type Synonyms. In *Proceedings of the Tenth ACM SIGPLAN International Conference on Functional Programming (ICFP '05)*. ACM, New York, NY, USA, 241–253. https://doi.org/10.1145/1086365.1086397

[3] Koen Claessen and John Hughes. 2000. QuickCheck: A Lightweight Tool for Random Testing of Haskell Programs. In *Proceedings of the Fifth ACM SIGPLAN International Conference on Functional Programming (ICFP '00)*. ACM, New York, NY, USA, 268–279. https://doi.org/10.1145/351240.351266

[4] Edsko de Vries and Andres Löh. 2014. True Sums of Products. In *Proceedings of the 10th ACM SIGPLAN Workshop on Generic Programming (WGP '14)*. ACM, New York, NY, USA, 83–94. https://doi.org/10.1145/2633628.2633634

[5] Larry Diehl, Denis Firsov, and Aaron Stump. 2018. Generic Zero-cost Reuse for Dependent Types. *Proc. ACM Program. Lang.* 2, ICFP, Article 104 (July 2018), 30 pages. https://doi.org/10.1145/3236799

[6] Atze Dijkstra and S. Doaitse Swierstra. 2005. *Making implicit parameters explicit.* Technical Report UU-CS-2005-032. Department of Information and Computing Sciences, Utrecht University. http://www.cs.uu.nl/research/techreps/repo/CS-2005/2005-032.pdf

[7] Richard A. Eisenberg, Stephanie Weirich, and Hamidhasan G. Ahmed. 2016. Visible Type Application. In *Proceedings of the 25th European Symposium on Programming Languages and Systems - Volume 9632*. Springer-Verlag New York, Inc., New York, NY, USA, 229–254. https://doi.org/10.1007/978-3-662-49498-1_10

[8] Conal Elliott. 2009. applicative-numbers: Applicative-based numeric instances. https://hackage.haskell.org/package/applicative-numbers

[9] Jeremy Gibbons and Bruno c. d. s. Oliveira. 2009. The Essence of the Iterator Pattern. *J. Funct. Program.* 19, 3-4 (July 2009), 377–402. https://doi.org/10.1017/S0956796809007291

[10] Gabriel Gonzalez. 2014. Equational reasoning at scale. http://www.haskellforall.com/2014/07/equational-reasoning-at-scale.html

[11] José Pedro Magalhães, Atze Dijkstra, Johan Jeuring, and Andres Löh. 2010. A Generic Deriving Mechanism for Haskell. In *Proceedings of the Third ACM Haskell Symposium on Haskell (Haskell '10)*. ACM, New York, NY, USA, 37–48. https://doi.org/10.1145/1863523.1863529

[12] Herbert V. Riedel and David Luposchainsky. 2015. Monad of no `return` Proposal (MRP): Moving `return` out of `Monad`. https://mail.haskell.org/pipermail/libraries/2015-September/026121.html

[13] Brent A. Yorgey, Stephanie Weirich, Julien Cretin, Simon Peyton Jones, Dimitrios Vytiniotis, and José Pedro Magalhães. 2012. Giving Haskell a Promotion. In *Proceedings of the 8th ACM SIGPLAN Workshop on Types in Language Design and Implementation (TLDI '12)*. ACM, New York, NY, USA, 53–66. https://doi.org/10.1145/2103786.2103795