Deriving Via

or, How to Turn Hand-Written Instances into an Anti-Pattern

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Abstract

Haskell's `deriving` construct is a cheap and cheerful way to quickly generate instances of type classes that follow common patterns. But at present, there are only a subset of such type class patterns that `deriving` supports, and if a particular class lies outside of this subset, then one cannot derive it at all, with no alternative than to laboriously declare the instances by hand.

To overcome this deficit, we introduce Deriving Via, an extension to `deriving` that enables programmers to compose instances from named programming patterns, thereby turning `deriving` into a high-level domain-specific language for defining instances. Deriving Via leverages newtypes—an already familiar tool of the Haskell trade—to give names to recurring patterns in a way that both feels natural and allows a high degree of abstraction.

1 Introduction

In Haskell, type classes capture common interfaces. When defining class instances we often happen upon repeated patterns where different instances have the same definition.

```haskell
instance Monoid a => Monoid (IO a) where
  mempty  = pure mempty
  mappend = liftA2 mappend

instance Monoid a => Monoid (ST s a) where
  mempty  = pure mempty
  mappend = liftA2 mappend
```

These instance declarations appear in the GHC base package and have identical instance bodies. This rule is not limited to `IO` and `(ST s)` but will work for any applicative functor `f`.

It is tempting to avoid this obvious repetition by defining an instance for all such types in one fell swoop.

```haskell
instance (Applicative f, Monoid a)
  => Monoid (f a) where
  mempty  = pure mempty
  mappend = liftA2 mappend
```

Unfortunately, this general instance is undesirable as it overlaps with all other `(f a)`-instances. Instance resolution will match the instance head first before considering the context, whether `f` is applicative or not. Once it has commited to an instance it will never backtrack. Consider:

```haskell
newtype Endo a = MkEndo (a -> a)   -- Data.Monoid
```

`Endo` is not even a `Functor`, yet it admits a perfectly valid monoid instance that overlaps with the lifted instance above.

```haskell
instance Monoid (Endo a) where
  mempty = MkEndo id
  mappend (MkEndo f) (MkEndo g) = MkEndo (f . g)
```

Even if we have an `Applicative` functor `f` on our hands there is no guarantee that this is the definition we want. Lists are notably the *free monoid* (the most 'fundamental' monoid) but that instance does not coincide with the rule above and in particular, imposes no `(Monoid a)` constraint.

```haskell
instance Monoid [a] where
  mempty  = []
  mappend = (++)
```

In fact, the monoid instance for lists is captured by a *different* rule based on `Alternative`:

```haskell
instance Alternative f => Monoid (f a) where
  mempty  = empty
  mappend = (<|>)
```

Because instance resolution never backtracks we can't define these two distinct rules for `Monoid (f a)`, even with overlapping instances.

The only viable workaround using the Haskell type class system is to write ▬▬ instances for each data type by hand, each one with an identical definition (like the instances for `(IO a)` and `(ST s a)`) which is extremely unsatisfactory:

- It is not obvious that we are instantiating a general principle.
- Because the general principle is not written down in code with a name and documentation it has to be communicated by folklore or in comments and is difficult

to discover and search for. Our code has lost a connection to its origin.

- There are many such rules, some quite obvious, but some more surprising and easy to miss.
- While for `Monoid`—which only has two methods—the work required to define the instance manually is perhaps acceptable, it quickly becomes extremely tedious and error-prone for classes with many methods.

As an illustration of the final point, consider `Num`. There is a way to lift a `Num` instance through any `Applicative` functor:[1]

```haskell
instance (Applicative f, Num a) => Num (f a) where
  (+) = liftA2 (+)
  (-) = liftA2 (-)
  (*) = liftA2 (*)
  negate = liftA negate
  abs    = liftA abs
  signum = liftA signum
  fromInteger = pure . fromInteger
```

Defining such a boilerplate instance manually for a concrete type constructor is so annoying that Conal Elliott has introduced a preprocessor for this particular use case several years ago. [7]

1.1 Deriving

Those familiar with Haskell's deriving mechanism may wonder why this cannot simply be derived but in reality our options are very limited.

`Monoid` is not one of the few blessed type classes that GHC has built-in support to derive. It so happens that (`IO` a), (`ST` s a) and (`Endo` a) are all newtypes so they are eligible for *generalized newtype deriving* (GND) where they would derive their instance via the instance of their underlying type [1] but this gives us the wrong definition in all three cases (even if it worked for the first two, which it doesn't).

Our last hope is that the the `Monoid` type class has the right generic implementation [10]. If that were the case we could use a deriving clause, and with nearly no work, we get the compiler to generate the an instance of that rule for us.

However, that is not the case. There is no generic implementation for `Monoid`, a class from base that we have no control over. But a generic instance, if it exists, captures a single rule over all others, so we couldn't use it to derive a monoid instance for lists as well as (`ST` s a). We have no other choice but to write some instances by hand. This means that we have to provide explicit implementations of at least a minimal subset of the class methods.

There is no middle ground and the difference can be drastic—especially if the class has many methods—so the option of **deriving** remains tantalizing.

In this paper, we introduce Deriving Via, a new language extension that bridges this gap. With Deriving Via, we can vastly increase the number of type class instances that we can derive. As a result, we no longer have to rely on a few (if any at all) essentially pre-defined ways to define a particular class instance. Instead, we can teach the compiler new rules for deriving classes, and select the one we want using a high-level description.

Our extension is light-weight in the sense that it is easy to implement and builds on concepts that are already in the language such as deriving strategies, newtypes, and safe coercions. Furthermore, it naturally generalizes a number of language extensions such as generalized newtype deriving and default signatures.

1.2 Introducing Deriving Via

Our approach to deal with this unfortunate lack of abstraction has two parts:

1. We capture general rules for defining new instances using newtypes.
2. We use such newtypes in a new Deriving Via language construct to explain to the compiler how to construct the instance without having to write it manually.

For the *first part*, let us revisit the rule that explains how to lift a monoid instance through an `Applicative` functor. We can turn the problematic generic and overlapping instance for `Monoid` (f a) into an entirely unproblematic instance by defining a suitable *adapter* newtype [8] and wrapping the instance head in it:

```haskell
newtype App f a = App (f a)
instance (Applicative f, Monoid a)
  => Monoid (App f a) where
  mempty = App (pure mempty)
  mappend (App f) (App g) = App (liftA2 mappend f g)
```

Since GHC 8.4, we also need a `Semigroup` instance, because it just became a superclass of `Monoid`[2]:

```haskell
instance (Applicative f, Semigroup a)
  => Semigroup (App f a) where
  App f <> App g = App (liftA2 (<>) f g)
```

The *second part* is to now use such a rule in our new form of **deriving** statement. We can do this when defining a new data type, such as in

```haskell
data Maybe a = Nothing | Just a
  deriving Monoid via (App Maybe a)
```

This requires that we independently have an `Applicative` instance for `Maybe`, but then we obtain the desired `Monoid` instance nearly for free.

In the deriving clause, **via** is a new language construct that explains *how* GHC should derive the instance, namely by reusing the instance already available for the given type.

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[1]There are similar ways to lift `Floating` and `Fractional`.

[2]See Section 4.4 for a more detailed discussion of this aspect.

It should be easy to see why this works: due to the use of a newtype, `App Maybe` a has the same internal representation as `Maybe` a, and any instance available on one type can be made to work on a representationally equal type as well.

The `Data.Monoid` module defines many further adapters that can readily be used with Deriving Via. For example, the rule that obtains a `Monoid` instance from an `Alternative` instance is already implemented in terms of `Alt`:

```
newtype Alt f a = Alt (f a)

instance Alternative f => Monoid (Alt f a) where
  mempty              = Alt empty
  mappend (Alt f) (Alt g) = Alt (f <|> g)

instance Alternative f => Semigroup (Alt f a) where
  (<>) = mappend
```

Using adapters such as `App` and `Alt`, a vast amount of `Monoid` instances that currently have to be defined by hand can instead be derived using the **via** construct.

1.3 Contributions and structure of the paper

The paper is structured as follows:

In Section 2, we use the QuickCheck library as a case study to explain in more detail how Deriving Via can be used, and how it works. In Section 3, we explain in detail how to typecheck and translate Deriving Via clauses. In Section 4, we discuss several additional applications of Deriving Via. We discuss related ideas in Section 5 and conclude in Section 6.

Our extension is fully implemented in a GHC branch[3], and we are working on a proposal to include it into GHC, so it will hopefully be available in one of the next releases of GHC.

The idea of Deriving Via is surprisingly simple, yet it has a number of powerful and perhaps surprising properties:

- It generalizes the *generalized newtype deriving* extension. (Section 3.2.1).
- It generalizes the concept of *default signatures.* (Section 4.2).
- It provides a possible solution to the problem of introducing additional boilerplate code when introducing new superclasses (such as `Applicative` for `Monad`, Section 4.4).
- It allows to reuse instances not just from representationtally equal, but also from isomorphic or similarly related types 4.3).

2 Case study: QuickCheck

QuickCheck [3] is a well-known Haskell library for randomized property-based testing. At the core of QuickCheck's test case generation functionality is the `Arbitrary` class. Its primary method `arbitrary` describes how to generate suitable random values of a given size and type. It also has a

method `shrink` that is used to try to shrink failing counterexamples of test properties.

Many standard Haskell types such as `Int` or lists are already an instance of `Arbitrary`. This can be very convenient, because many properties involving these types can be quickchecked without any extra work.

On the other hand, there are often additional constraints imposed on the actual values of a type that are not sufficiently expressed in their types. Depending on the context and the situation, we might want to guarantee the generation of positive integers, or non-empty lists, or even sorted lists.

The QuickCheck library provides a number of newtype-based adapters (called *modifiers* in the library) for this purpose. As an example, QuickCheck defines

```
newtype NonNegative a =
  NonNegative {getNonNegative :: a}
```

which comes with a predefined instance of the form

```
instance (Num a, Ord a, Arbitrary a)
  => Arbitrary (NonNegative a)
```

that explains how to generate and shrink non-negative numbers. A user who wants a non-negative integer can now use `NonNegative Int` rather than `Int` to make this obvious.

This approach, however, has a drastic disadvantage: we have to wrap each value in an extra constructor, and the newtype and constructor are QuickCheck-specific. An implementation detail (the choice of testing library) leaks into the data model of an application. While we might be willing to use domain-specific newtypes for added type safety, such as `Age` or `Duration`, we might not be eager to add QuickCheck modifiers everywhere. And what if we need more than one modifier? And what if other libraries export their own set of modifiers as well? We certainly do not want to change the actual definition of our data types (and corresponding code) whenever we start using a new library.

With Deriving Via, we have the option to reuse the existing infrastructure of modifiers without paying the price of cluttering up our data type definitions. We can choose an actual domain-specific newtype such as

```
newtype Duration = Duration Int   -- in seconds
```

and now specify exactly how the `Arbitrary` should be derived for this:

```
  deriving Arbitrary via (NonNegative Int)
```

and now we get the `Arbitrary` instance for non-negative integers. Only the deriving clause changes, not the data type itself. If we later decide we want only positive integers as durations, we replace `NonNegative` with `Positive` in the deriving clause. Again, the data type itself is unaffected. In particular, we do not have to change any constructor names anywhere in our code.

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[3]https://github.com/RyanGlScott/ghc/tree/deriving-via

2.1 Composition

Multiple modifiers can be combined. For example, there is another modifier called `Large` that will scale up integral values being produced by a generator in size. It is defined as

```haskell
newtype Large a = Large {getLarge :: a}
```

with an instance

```haskell
instance (Integral a, Bounded a) => Arbitrary (Large a)
```

For our `Duration` type, we can easily write

```haskell
  deriving Arbitrary via (NonNegative (Large Int))
```

The types `NonNegative (Large Int)` and `Duration` still share the same run-time representation (namely that of `Int`), so the instance can be reused.

2.2 Adding new modifiers

Of course, we can add add our own modifiers if the set of predefined modifiers is not sufficient. For example, it is difficult to provide a completely generic `Arbitrary` instance that works for all data types, simply because there are too many assumptions about what makes good test data that need to be taken into account.

But for certain subclasses of data types, there are quite reasonable strategies of coming up with a generic instance. For example, for enumeration type, one reasonable strategy is to simply desire a uniform distribution of the finite set of values.

QuickCheck even offers such a generator, but it does not expose it as a newtype modifier:

```haskell
arbitraryBoundedEnum :: (Bounded a, Enum a) => Gen a
```

But from this, we can easily define our own:

```haskell
newtype BoundedEnum a = BoundedEnum a

instance (Bounded a, Enum a)
    => Arbitrary (BoundedEnum a) where
  arbitrary = BoundedEnum <$> arbitraryBoundedEnum
```

We can then use this functionality to derive `Arbitrary` for a new enumeration type:

```haskell
data Weekday = Mo | Tu | We | Th | Fr | Sa | Su
  deriving (Enum, Bounded)
  deriving Arbitrary via (BoundedEnum Weekday)
```

2.3 Parameterized modifiers

Sometimes, we might want to parameterize a generator with extra data. We can do so by using a modifier that has extra arguments, and using the extra arguments in the associated `Arbitrary` instance.

An extreme case that also makes use from type-level programming features in GHC is a modifier that allows us to specify a lower and an upper bound of a generated natural number.

```haskell
newtype Between (l :: Nat) (u :: Nat) = Between Int
```

```haskell
instance (KnownNat l, KnownNat u)
  => Arbitrary (Between l u) where
  arbitrary = Between <$> choose
              ( fromIntegral (natVal (Proxy @l))
              , fromIntegral (natVal (Proxy @u)))
```

(Note that this instance makes use of visible type application in `Proxy @l` and `Proxy @u` [6].)

We can then equip an application-specific type for years with a generator implementing respecting a plausible range:

```haskell
newtype Year = Year Int
  deriving Show
  deriving Arbitrary via (Between 1900 2100)
```

3 Typechecking

Seeing enough examples of Deriving Via can give the impression that it is a somewhat magical feature. In this section, we aim to explain the magic underlying Deriving Via by giving a more precise description of:

- How Deriving Via clauses are typechecked.
- What code Deriving Via generates behind the scenes.
- How to determine the scoping of type variables in Deriving Via clauses.

To avoid clutter, we assume that all types have monomorphic kinds. However, it is easy to incorporate kind polymorphism [12], and our implementation of these ideas in GHC does so.

3.1 Well-typed uses of Deriving Via

Deriving Via grants the programmer the ability to put extra types in her programs, but the flip side to this is that it's possible for her to accidentally put total nonsense into a Deriving Via clause, such as:

```haskell
newtype S = S Char
  deriving Eq via Maybe
```

In this section, we describe a general algorithm for when a Deriving Via clause should typecheck, which will allow us to reject ill-formed examples like the one above.

3.1.1 Aligning kinds

Suppose we are deriving the following instance:

```haskell
data D d_1 ... d_m
  deriving (C c_1 ... c_n) via (V v_1 ... v_p)
```

In order for this declaration to typecheck, we must check the *kinds* of each type. In particular, the following conditions must hold:

1. The type $C\ c_1\ \dots\ c_n$ must be of kind $(k_1 \to \dots \to k_r \to *) \to$ `Constraint` for some kinds $k_1, \dots, k_r$. The reason is that the instance we must generate,

   ```haskell
   instance C c_1 ... c_n (D d_1 ... d_i) where ...
   ```

requires that we can apply `C` $c_1 \ldots c_n$ to another type `D` $d_1 \ldots d_i$ (where $i \leqslant m$, see Section 3.1.2). Therefore, it would be nonsense to try to derive an instance of `C` $c_1 \ldots c_n$ if it had kind, say, `Constraint`.

2. The kinds `V` $v_1 \ldots v_p$ and `D` $d_1 \ldots d_i$, and the kind of the argument of `C` $c_1 \ldots c_n$ must all unify. This check rules out the above example of **deriving** `Eq` **via** `Maybe`, as it does not even make sense to talk about reusing the `Eq` instance for `Maybe`—which is of kind $(* \to *)$— as `Eq` instances can only exist for types of kind $*$.

3.1.2 Eta-reducing the data type

Note that the conditions above, `D` $d_1 \ldots d_i$ (for some i), instead of `D` $d_1 \ldots d_m$. That is because in general, the kind of `C` $c_1 \ldots c_n$ is allowed to be different from the kind of `D` $d_1 \ldots d_m$! For instance, the following example is perfectly legitimate:

```
class Functor (f :: * -> *) where …
data Foo a = Foo a a
  deriving Functor
```

despite the fact that `Foo` a has kind $*$ and the argument to `Functor` has kind $(* \to *)$. This is because the code that actually gets generated has the following shape:

```
instance Functor Foo where …
```

To put it differently, we have *eta-reduced* away the a in `Foo` a before applying `Functor` to it. The power to eta-reduce variables from the data types is part of what makes deriving clauses so flexible.

To determine how many variables to eta-reduce, we must examine the kind of `C` $c_1 \ldots c_n$, which by condition (1) is of the form $((k_1 \to \ldots \to k_r \to *) \to$ `Constraint`$)$ for some kinds $k_1, \ldots, k_r$. Then the number of variables to eta-reduce is simply r, so to compute the i in `D` $d_1 \ldots d_i$, we take $i = m - r$.

This is better explained by example, so consider the following two scenarios, both of which typecheck:

```
newtype A a = A a deriving Eq      via (Identity a)
newtype B b = B b deriving Functor via Identity
```

In the first example, we have the class `Eq`, which is of kind $* \to$ `Constraint`. The argument to `Eq`, which is of kind $*$, does not require that we eta-reduce any variables. As a result, we check that `A` a is of kind $*$, which is the case.

In the second example, we have the class `Functor`, which is of kind $(* \to *) \to$ `Constraint`. The argument to `Functor` is of kind $(* \to *)$, which requires that we eta-reduce one variable from `B` b to obtain `B`. We then check that `B` is kind of $(* \to *)$, which is true.

3.2 Code generation

Once the typechecker has ascertained that a **via** type is fully compatible with the data type and the class for which an instance is being derived, GHC proceeds with generating the

code for the instance itself. This generated code is then fed *back* into the typechecker, which acts as a final sanity check that GHC is doing the right thing under the hood.

3.2.1 Generalized newtype deriving (GND)

The process by which Deriving Via generates code is heavily based off of the approach that the GND takes, so it is informative to first explain how GND works. From there, Deriving Via is a straightforward generalization—so much so that Deriving Via could be thought of as "generalized GND ".

Our running example in this section will be the newtype `Age`, which is a simple wrapper around `Int` (which we will call the *representation type*):

```
newtype Age = MkAge Int deriving Enum
```

A naïve way to generate code would be to manually wrap and unwrap the `MkAge` constructor wherever necessary, such as in the code below:

```
instance Enum Age where
  toEnum i = MkAge (toEnum i)
  fromEnum (MkAge x) = fromEnum x
  enumFrom (MkAge x) = map MkAge (enumFrom x)
```

This works, but is somewhat unsatisfying. After all, a newtype is intended to be a zero-cost abstraction that acts identically to its representation type at runtime. Accordingly, any function that mentions a newtype in its type signature should be able to be converted to a new function with all occurrences of the newtype in the type signature replaced with the representation type, and moreover, that new function should behave identically to the old one at runtime.

Unfortunately, the implementation of `enumFrom` may not uphold this guarantee. While wrapping and unwrapping the `MkAge` constructor is certain to be a no-op, the `map` function is definitely *not* a no-op, as it must walk the length of a list. But the fact that we need to call `map` in the first place feels rather silly, as all we are doing is wrapping a newtype at each element.

Luckily, there is a convenient solution to this problem: the safe `coerce` function [1]:

```
coerce :: Coercible a b => a -> b
```

Operationally, `coerce` can be thought of as behaving like its wily cousin, `unsafeCoerce`, which takes a value of one type as casts it to a value at a another type. Unlike `unsafeCoerce`, which can break programs if used carelessly, `coerce` is completely type-safe due to its use of the `Coercible` constraint. We will explain `Coercible` in more detail later, but for now, it suffices to say that a `Coercible` a b constraint witnesses the fact that two types a and b have the same representation at runtime, and thus any value of type a can be casted to type b.

Armed with `coerce`, we can show what code GND would actually generate for the `Enum Age` instance above:

```
instance Enum Age where
  toEnum =
    coerce @(Int -> Int) @(Int -> Age) toEnum
  fromEnum =
    coerce @(Int -> Int) @(Age -> Int) fromEnum
  enumFrom =
    coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Now we have a strong guarantee that the `Enum` instance for `Age` has exactly the same runtime characteristics as the instance for `Int`. As an added benefit, the code ends up being simpler, as every method can be implemented as a straightforward application of `coerce`. The only interesting part is generating the two explicit type arguments [6] that are being used to specify the source type (using the representation type) and the target type (using the newtype) of `coerce`.

3.2.2 The `Coercible` constraint

A `Coercible` constraint can be thought of as evidence that GHC can use to cast between two types. `Coercible` is not a type class, so it is impossible to write a `Coercible` instance by hand. Instead, GHC can generate and solve `Coercible` constraints automatically as part of its built-in constraint solver, much like it can solve equality constraints. (Indeed, `Coercible` can be thought of as a broader notion of equality among types.)

As mentioned in the previous section, a newtype can be safely cast to and from its representation type, so GHC treats them as inter-`Coercible`. Continuing our earlier example, this would mean that GHC would be able to conclude that:

```
instance Coercible Age Int
instance Coercible Int Age
```

But this is not all that `Coercible` is capable of. A key property is that GHC's constraint solver can look inside of other type constructors when determining if two types are inter-`Coercible`. For instance, both of these statements hold:

```
instance Coercible (Age -> [Age]) (Int -> [Int])
instance Coercible (Int -> [Int]) (Age -> [Age])
```

This demonstrates the ability to cast through the function and list type constructors. This ability is important, as our derived `enumFrom` instance would not typecheck otherwise!

Another crucial fact about `Coercible` that we rely on is that it is transitive: if `Coercible` a b and `Coercible` b c hold, then `Coercible` a c also holds. This is perhaps unsurprising if one views `Coercible` as an equivalence relation, but it a fact that is worth highlighting, as the transitivity of `Coercible` is what allows us to `coerce` *between newtypes*. For instance, if we have these two newtypes:

```
newtype A a = A [a]
newtype B   = B [Int]
```

then GHC is able to conclude that `Coercible (A Int) B` holds, because we have the following `Coercible` rules

```
instance Coercible (A Int) [Int]
instance Coercible [Int] B
```

as well as transitivity. As we will discuss momentarily, Deriving Via in particular makes heavy use of the transitivity of `Coercible`.

3.2.3 From GND to Deriving Via

As we saw in Section 3.2.1, the code which GND generates relies on `coerce` to do the heavy lifting. In this section, we will generalize this technique slightly to give us a way to generate code for Deriving Via.

Recall the following GND-derived instance:

```
newtype Age = MkAge Int deriving Enum
```

As stated above, it generates the following code for `enumFrom`:

```
instance Enum Age where
  …
  enumFrom =
    coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Here, there are two crucially important types: the representation type, `Int`, and the original newtype itself, `Age`. The implementation of `enumFrom` simply sets up an invocation of `coerce enumFrom`, with explicit type arguments to indicate that we should reuse the existing `enumFrom` implementation for `Int` and reappropriate it for `Age`.

The only difference in the code that GND and Deriving Via generate is that in the former strategy, GHC always picks the representation type for you, but in Deriving Via, the *user* has the power to choose this type. For example, if a programmer had written this instead:

```
newtype T = T Int
instance Enum T where …
newtype Age = MkAge Int deriving Enum via T
```

then the following code would be generated:

```
  enumFrom =
    coerce @(T -> [T]) @(Age -> [Age]) enumFrom
```

This time, GHC coerces from an `enumFrom` implementation for `T` (the **via** type) to an implementation for `Age`. (Recall from Section 3.2.2 that this is possible since we can `coerce` transitively from `T` to `Int` to `Age`).

Now we can see why the instances that Deriving Via can generate are a strict superset of those that GND can generate. For instance, our earlier GND example

```
newtype Age = MkAge Int deriving Enum
```

could equivalently have been written using Deriving Via like so:

```
newtype Age = MkAge Int deriving Enum via Int
```

3.3 Type variable scoping

In the remainder of this section, we will present an overview of how type variables are bound in Deriving Via clauses, and over what types they scope. Deriving Via introduces a new place where types can go, and more importantly, it introduces a new place where type variables can be *quantified*, so it takes some amount of care to devise a consistent treatment for it.

3.3.1 Binding sites

Consider the following example:

```
data Foo a = …
  deriving (Baz a b c) via (Bar a b)
```

Where is each type variable quantified?

- a is bound by `Foo` itself in the declaration **data** `Foo` a. Such a variable scopes over both the derived class, `Baz` a b c, as well as the **via** type, `Bar` a b.
- b is bound by the **via** type, `Bar` a b. Note that b is bound here but a is not, as it was bound earlier by the **data** declaration. b scopes over the derived class type, `Baz` a b c, as well.
- c is bound by the derived class, `Baz` a b c, as it was not bound elsewhere. (a and b were bound earlier.)

In other words, the order of scoping starts at the **data** declaration, then the **via** type, and then the derived classes associated with that **via** type.

3.3.2 Establishing order

This scoping order may seem somewhat surprising, as one might expect the type variables bound by the derived classes to scope over the **via** type instead. However, this choice introduces additional complications that are tricky to resolve. For instance, consider a scenario where one attempts to derive multiple classes at once with a single **via** type:

```
data D
  deriving (C1 a, C2 a) via (T a)
```

Suppose we first quantified the variables in the derived classes and *then* the variables in the **via** type. Because each derived class has its own type variable scope, the a in `C1` a is bound independently from the a in `C2` a. In other words, we have something like this (using a hypothetical **forall** syntax):

```
  deriving (forall a . C1 a, forall a . C2 a) via (T a)
```

Now we are faced with a thorny question: which a is used in the **via** type, `T` a? There are multiple choices here, since the a variables in `C1` a and `C2` a are distinct! This is an important choice, since the kinds of `C1` and `C2` might differ, so the choice of a could affect whether `T` a kind-checks or not.

On the other hand, if one binds the a in `T` a first, then this becomes a non-issue. We would instead have this:

```
  deriving (C1 a, C2 a) via (forall a . T a)
```

Now, there is no ambiguity regarding a, as both a variables in the list of derived classes were bound in the same place.

It might feel strange visually to see a variable being used *before* of its binding site (assuming one reads code from left to right). However, this is not unprecedented within Haskell, as this is also legal:

```
f = g + h where g = 1; h = 2
```

In this example, we have another scenario where things are bound (g and h) after their use sites. In this sense, the **via** keyword is continuing a rich tradition pioneered by **where** clauses.

One alternative idea (which was briefly considered) was to put the **via** type *before* the derived classes so as to avoid this "zigzagging" scoping. However, this would introduce additional ambiguities. Imagine one were to take this example:

```
  deriving Z via X Y
```

And convert it to a form in which the **via** type came first:

```
  deriving via X Y Z
```

Should this be parsed as (X Y) Z, or X (Y Z)? It's not clear visually, so this choice would force programmers to write additional parentheses.

4 More use cases

We have already seen in Section 2 how Deriving Via facilitates greater code reuse in the context of QuickCheck. This far from the only domain where Deriving Via proves to be a natural fit, however. In fact, there are so many of these domains, there would be enough to fill pages upon pages!

Unfortunately, we do not have enough space to document all of these use cases, so in this section, we present a cross-section of scenarios in which Deriving Via can capture interesting patterns and allow programmers to abstract over them in a convenient way.

4.1 Asymptotic improvements with ease

A widely used feature of type classes is their ability to give default implementations for their methods if a programmer leaves them off. One example of this can be found in the `Applicative` class. The main workhorse of `Applicative` is the (<*>) method, but on occasion, it is more convenient to use the (<*) or (*>) methods, which sequence their actions but discard the result of one of their arguments:

```
class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
  (<*) :: f a -> f b -> f a
  (<*) = liftA2 (\ a _ -> a)
  (*>) :: f a -> f b -> f b
  (*>) = liftA2 (\ _ b -> b)
```

As shown here, (<*>) and (*>) have default implementations in terms of `liftA2`. This works for any `Applicative`, but is not as efficient as it could be in some cases. For some instances of `Applicative`, we can actually implement these methods in $O(1)$ time instead of using `liftA2`, which can often run in superlinear time. One such `Applicative` is the function type (->):

```
instance Applicative ((->) r) where
  pure = const
  (<*>) f g x = f x (g x)
  f <* _ = f
  _ *> g = g
```

Note that we had to explicitly define (<*>) and (*>), as the default implementations would not have been as efficient. But (->) is not the only type for which this trick works—it also works for any data type that is isomorphic to (->) r (for some r)!. These function-like types are characterized by the `Representable` type class:

```
class Functor f => Representable f where
  type Rep f
  index :: f a -> (Rep f -> a)
  tabulate :: (Rep f -> a) -> f a
```

This is a good deal more abstract than (->) r, so it can be helpful to see how `Representable` works for (->) r itself:

```
instance Representable ((->) r) where
  type Rep ((->) r) = r
  index f = f
  tabulate f = f
```

With `Representable`, we can codify the `Applicative` shortcut for (<*>) and (*>) with a suitable newtype:

```
newtype WrapRep f a = WrapRep (f a)
  deriving (Functor, Representable)

instance Representable f
  => Applicative (WrapRep f) where
  pure = tabulate . pure
  f <*> g = tabulate (index f <*> index g)
  f <* _ = f
  _ *> g = g
```

Now, instead of having to manually override (<*>) and (*>) to get the desired performance, one can accomplish this in a more straightforward fashion by using Deriving Via:

```
newtype IntConsumer a = IntConsumer (Int -> a)
  deriving (Functor, Representable)
  deriving Applicative via (WrapRep IntConsumer)
```

Not only does this save code in the long run, but it also gives a name to the optimization being used, which allows it to be documented, exported from a library, and thereby easier to spot "in the wild" for other programmers.

4.2 Making defaults more flexible

In the previous section, we saw an example of how relying too much on a type class's default implementations can backfire. This is an unfortunately common trend with type classes in general: Many classes try to pick one-size-fits-all defaults that don't work well in certain scenarios, but because Haskell allows specifying only one default per method, if the provided default doesn't work for a programmer's use case, then she is forced to implement her own implementations by hand.

In this section, we continue the trend of generalizing defaults by looking at another language extension that Deriving Via can substitute for: *default signatures*. Default signatures (a slight generalization of default implementations) can eliminate large classes of boilerplate, but they too are limited by the one-default-per-method restriction. Here, we demonstrate how one can scrap uses of default signatures in favor of Deriving Via, and show how Deriving Via can overcome the limitations of default signatures.

The typical use case for default signatures is when one has a type class method that has a frequently used default implementation at a constrained type. For instance, consider a `Pretty` class with a method `pPrint` for pretty-printing data:

```
class Pretty a where
  pPrint :: a -> Doc
```

Coming up with `Pretty` instances for the vast majority of data types is repetitive and tedious, so a common pattern is to abstract away this tedium using generic programming libraries, such as those found in `GHC.Generics` [10] or generics-sop [4]. For example, using `GHC.Generics`, we can define

```
genericPPrint ::
  (Generic a, GPretty (Rep a)) => a -> Doc
```

The details of how `Generic`, `GPretty`, and `Rep` work are not important to understanding the example. What is important is to note that we cannot just add

```
  pPrint = genericPPrint
```

as a conventional default implementation to the `Pretty` class, because it does not typecheck due to the extra constraints.

Before the advent of default signatures, one had to work around this by defining `pPrint` to be `genericPPrint` in every `Pretty` instance, as in the examples below:

```
instance Pretty Bool where
  pPrint = genericPPrint
instance Pretty a => Pretty (Maybe a) where
  pPrint = genericPPrint
```

To avoid this repetition, default signatures allow one to provide a default implementation of a type class method using *additional* constraints on the method's type. For example:

```
class Pretty a where
  pPrint :: a -> Doc
```

```
default pPrint ::
  (Generic a, GPretty (Rep a)) => a -> Doc
pPrint = genericPPrint
```

Now, if any instances of `Pretty` are given without an explicit definition of `pPrint`, the default implementation is used. For this to typecheck, the data type a used in the instance must satisfy the constraints (`Generic a`, `GPretty (Rep a)`). Thus, we can reduce the instances above to just

```
instance Pretty Bool
instance Pretty a => Pretty (Maybe a)
```

Although default signatures remove the need for many occurrences of boilerplate code, it also imposes a significant limitation: every type class method can have at most one default implementation. As a result, default signatures effectively endorse one default implementation as the canonical one. But in many scenarios, there is far more than just one way to do something. Our `pPrint` example is no exception. Instead of `genericPPrint`, one might one to:

- leverage a `Show`-based default implementation instead of a `Generic`-based one,
- use a different generic programming library such as generics-sop instead of `GHC.Generics`,
- use a tweaked version of `genericPPrint` which displays extra debugging information.

All of these are perfectly reasonable choices a programmer might want to make, but alas, GHC only lets type classes bless each method with one default.

Fortunately, Deriving Via provides a convenient way of encoding default implementations with the ability to toggle between different choices: newtypes! For instance, we can codify two different approaches to implementing `pPrint` as follows:

```
newtype GenericPPrint a = GenericPPrint a
instance (Generic a, GPretty (Rep a))
  => Pretty (GenericPPrint a) where
  pPrint (GenericPPrint x) = genericPPrint x
newtype ShowPPrint a = ShowPPrint a
instance Show a => Pretty (ShowPPrint a) where
  pPrint (ShowPPrint x) = stringToDoc (show x)
```

With these newtypes in hand, choosing between them is as simple as changing a single type:

```
deriving Pretty via (GenericPPrint DataType1)
deriving Pretty via (ShowPPrint    DataType2)
```

We have seen how Deriving Via makes it quite simple to give names to particular defaults, and how toggling between defaults is a matter of choosing a name. In light of this, we believe that many current uses of default signatures ought to be removed entirely and replaced with the Deriving Via-based idiom presented in this section. This avoids the need to bless one particular default, and forces programmers to

consider which default is best suited to their use case, instead of blindly trusting the type class's blessed default to always do the right thing.

An additional advantage is that it allows to decouple the definition of such defaults from the site of the class definition. Hence, if a package author is hesitant to add a default because that might incur and unwanted additional dependency, nothing is lost, and the default can simply be added in a separate package.

4.3 Deriving via isomorphisms

All of the examples presented thus far in the paper rely on deriving through data types that have the same runtime representation as the original data type. In the following, however, we point out that—perhaps surprisingly—we can also derive through datatypes are are *isomorphic*, not just representationally equal. To accomplish this feat, we rely on techniques from generic programming.

Let us go back to QuickCheck (as in Section 2) once more and consider the data type

```
data Track = Track Title Duration
```

for which we would like to define an `Arbitrary` instance. Let us further assume that we already have `Arbitrary` instances for both `Title` and `Duration`.

The QuickCheck library defines an instance for pairs, so we could generate values of type (`Title`, `Duration`), and in essence, this is exactly what we want. But unfortunately, the two types are not inter-`Coercible`, even though they are isomorphic[4].

However, we can exploit the isomorphism and still get an instance for free, and the technique we apply is quite widely applicable in similar situations. As a first step, we declare a newtype to capture that one type is isomorphic to another:

```
newtype SameRepAs a b = SameRepAs a
```

Note that the idea here is that a and b are isomorphic in some sense, but only a is used as the value of the type. So `SameRepAs a b` is inter-`Coercible` with a.

We choose to witness an isomorphism between the two types via their generic representations: if two types have inter-`Coercible` generic representations, we can transform back and forth using the `from` and `to` methods of the `Generic` class from `GHC.Generics` [10]. We can use this to define a suitable `Arbitrary` instance for `SameRepAs`:

```
instance
  ( Generic a, Generic b, Arbitrary b
  , Coercible (Rep a ()) (Rep b ()), Arbitrary b
  ) => Arbitrary (a `SameRepAs` b) where
  arbitrary = SameRepAs . coerceViaRep <$> arbitrary
```

---

[4]Isomorphic in the sense that we can define a function from `Track` to (`Title`, `Duration`) and vice versa. Depending on the class we want to derive, sometimes an even weaker relationship between the types is sufficient, but we will focus on the case of isomorphism here for reasons of space.

Can you derive Traversable with DerivingVia? I guess not because it relies on Coercible (ie roles). But perhaps you can do it via an isomorphism?

```
      where
        coerceViaRep :: b -> a
        coerceViaRep =
          to . (coerce :: Rep b () -> Rep a ()) . from
```

Here, we first use `arbitrary` to give us a generator of type `Gen b`, then coerce this via the generic representations into an `arbitrary` value of type `Gen a`.

Finally, we can use the following **deriving** declarations for `Track` to obtain the desired `Arbitrary` instance:

```
  deriving Generic
  deriving Arbitrary
    via (Track `SameRepAs` (String, Duration))
```

With this technique, we can significantly expand the "equivalence classes" of data types that can be used when picking suitable types to derive through.

4.4 Retrofitting superclasses

On occasion, the need arises to retrofit an existing type class with a superclass, such as when `Monad` was changed to have `Applicative` as a superclass (which in turn has `Functor` as a superclass).

One disadvantage of such a change is that if the primary goal is to define the `Monad` instance for a type, one now has to write two additional instances, for `Functor` and `Applicative`, even though these instances are actually determined by the `Monad` instance.

With Deriving Via, we can capture this fact as a newtype, thereby making the process of defining such instances much less tedious:

```
newtype FromMonad m a = FromMonad (m a)
  deriving Monad

instance Monad m => Functor (FromMonad m) where
  fmap = liftM

instance Monad m => Applicative (FromMonad m) where
  pure  = return
  (<*>) = ap
```

Now, if we have a data type with a `Monad` instance, we can simply derive the corresponding `Functor` and `Applicative` instances by referring to `FromMonad`:

```
data Stream a b = Done b | Yield a (Stream a b)
  deriving (Functor, Applicative)
    via (FromMonad (Stream a))

instance Monad (Stream a) where
  return = Done

  Yield a k ≫= f = Yield a (k ≫= f)
  Done b ≫= f    = f b
```

One potentially problematic aspect remains. Another proposal [11] has been put forth (but has not been implemented, as of now) to remove the `return` method from the `Monad` class

and make it a synonym for `pure` from `Applicative`. The argument is that `return` is redundant, given that `pure` does the same thing with a more general type signature. All other prior discussion about the proposal aside, it should be noted that removing `return` from the `Monad` class would prevent `FromMonad` from working, as then `Monad` instances would not have any way to define `pure`. [5]

4.5 Avoiding orphan instances

Not only can Deriving Via quickly procure type class instances, in some cases, it can eliminate the need for certain instances altogether. Haskell programmers often want to avoid *orphan instances*: instances defined in a separate module from both the type class and data types being used. Sometimes, however, it's quite tempting to reach for orphan instances, as in the following example adapted from a blog post by Gonzalez [9]:

```
newtype Plugin = Plugin (IO (String -> IO ()))
  deriving Semigroup
```

In order for this derived `Semigroup` instance to typecheck, there must be a `Semigroup` instance for `IO` available. Suppose for a moment that there was no such instance for `IO`. How can one work around this issue?

- One could patch the base library to add the instance for `IO`. But given base's slow release cycle, it would be a while before one could actually use this instance.
- Write an orphan instance for `IO`. This works, but is undesirable, as now anyone who uses `Plugin` must incur a possibly unwanted orphan instance.

Luckily, Deriving Via presents a more convenient third option: re-use a `Semigroup` instance from *another* data type. Recall the `App` data type from Section 1.2 that lets us define a `Semigroup` instance by lifting through an `Applicative` instance. As luck would have it, `IO` already has an `Applicative` instance, so we can derive the desired `Monoid` instance for `Plugin` like so:

```
newtype Plugin = Plugin (IO (String -> IO ()))
  deriving Semigroup
    via (App IO (String -> App IO ()))
```

Note that we have to use `App` twice in the **via** type, corresponding to the two occurences of `IO` in the `Plugin` type. This is ok, because `App IO` has the same representation as `IO`. As desired, we completely bypass the need for a `Semigroup` instance for `IO`.

5 Related Ideas

We have demonstrated in the previous section that Deriving Via is an extremely versatile technique, and can be used to tackle a wide variety of problems. Deriving Via also bears a

---

[5]A similar, yet somewhat weaker, argument applies to suggested changes to relax the constraints of `liftM` and `ap` to merely `Applicative` and to change their definitions to be identical to `fmap` and (`<*>`), respectively.

resemblance to other distinct language features, such as ML functors and explicit dictionary passing, so in this section, we present an overview of their similarities and differences.

Say generative functors to placate certain members of the committee ;)

5.1 ML functors

Languages in the ML family, such as Standard ML or OCaml, provide *functors*, which are a feature of the module system that allows writing functions from modules of one signature to modules of another signature. In terms of functionality, functors somewhat closely resemble Deriving Via, as functors allow "lifting" of code into the module language much like Deriving Via allows lifting of code into GHC's deriving construct.

5.2 Explicit dictionary passing

The power and flexibility of Deriving Via is largely due to GHC's ability to take a class method of a particular type and massage it into a method of a different type. This process is almost completely abstracted away from the user, however. A user only needs to specify the types involved, and GHC will handle the rest behind the scenes.

An alternative approach, which would put more power into the hands of the programmer, is to permit the ability to explicitly construct and pass the normally implicit dictionary arguments corresponding to type class instances [5]. Unlike in Deriving Via, where going between class instances is a process that is carefully guided by the compiler, permitting explicit dictionary arguments would allow users to actually coerce concrete instance values and pass them around as first-class objects. In this sense, explicit dictionary arguments could be thought of as a further generalization of the technique that Deriving Via uses.

However, explicit dictionary arguments are a considerable extension of the language and its type system, and we feel that to be too large a hammer for the nail we are trying to hit. Deriving Via works by means of a simple desugaring of code with some light typechecking on top, which makes it much simpler to describe and implement. Finally, the problem which explicit dictionaries aims to solve—resolving ambiguity in implicit arguments—almost never arises in Deriving Via, as the programmer must specify all the types involved in the process.

6 Current status

We have implemented Deriving Via within GHC. Our implementation also interacts well with other GHC features that were not covered in this paper, such as kind polymorphism [12], `StandaloneDeriving`, and type classes with associated type families [2]. However, there are still challenges remaining, which we will describe in this section.

6.1 Quality of error messages

The nice thing about `deriving` is that when it works, it tends to work extremely well. When it *doesn't* work, however, it can be challenging to formulate an error message that adequately explains what went wrong. The fundamental issue is that error messages resulting from uses of `deriving` are usually rooted in *generated* code, and pointing to code that the user didn't write in error messages can sometimes lead to a confusing debugging experience.

Fortunately, we have found in our experience that the quality of Deriving Via-related error messages is overall on the positive side. GHC has already invested significant effort into making type errors involving `Coercible` to be easily digestible by programmers, so Deriving Via benefits from this work. For instance, if one inadvertently tries to derive through a type that is not inter-`Coercible` with the original data type, such as in the following example:

```
newtype UhOh = UhOh Char deriving Ord via Int
```

Then GHC will tell you exactly that, in plain language:

- Couldn't match representation of type `Char` with that of `Int` arising from the coercion of the method `compare`
  from type '`Int -> Int -> Ordering`'
  to type '`UhOh -> UhOh -> Ordering`'

That is not to say that every error message is this straightforward. There is are some scenarios that produce less-than-ideal errors, such as this:

```
newtype Foo a = Foo (Maybe a) deriving Ord via a
```

- Occurs check: cannot construct the infinite type: `a ~ Maybe a` arising from the coercion of the method '`compare`'
  from type '`a -> a -> Ordering`'
  to type '`Foo a -> Foo a -> Ordering`'

The real problem is that a and `Maybe` a do not have the same representation at runtime, but the error does not make this obvious. It is possible that one could add an *ad hoc* check for this class of programs, but there are likely many more tricky corner cases lurking around the corner, given that one can put anything after `via`.

We do not propose a solution to this problem here, but instead note that issues with Deriving Via error quality are ultimately issues with `coerce` error quality, given that the error messages are a result of `coerce` failing to typecheck. It is likely that investing more effort into making `coerce`'s error messages easier to understand would benefit Deriving Via as well.

6.2 Multi-Parameter Type Classes

GHC extends Haskell by permitting type classes with more than one parameter. Multi-parameter type classes are extremely common in modern Haskell, to the point where we assumed the existence of them in Section 3.1.1 without further mention. However, multi-parameter type classes pose

an intriguing design question when combined with Deriving Via and `StandaloneDeriving`, another GHC feature which allows one to write `deriving` declarations independently of a data type.

For example, one can write the following instance using `StandaloneDeriving`:

```haskell
class Triple a b c where
  triple :: (a, b, c)
instance Triple () () () where
  triple = ((), (), ())
newtype A = A ()
newtype B = B ()
newtype C = C ()

deriving via () instance Triple A B C
```

However, the code it generates is somewhat surprising. Instead of reusing the `Triple () () ()` instance in the derived instance, it will attempt to reuse an instance for `Triple A B ()`. This is because, by convention, `StandaloneDeriving` will only ever coerce through the *last* argument of a class. That is because the standalone instance above would be the same as if a user had written:

```haskell
newtype C = C () deriving (Triple A B) via ()
```

This consistency is perhaps a bit limiting in this context, where we have multiple arguments to `C` that one could "derive through". But it is not clear how GHC would figure out which of these arguments to `C` should be derived through, as there seven different combinations to choose from! It is possible that another syntax would need to be devised to allow users to specify which arguments should be coerced to avoid this ambiguity.

6.3 Conclusions

In this paper, we have introduced the Deriving Via language extension, explained how it is implemented, and shown a wide variety of use cases. We believe that Deriving Via has the potential to dramatically change the way we write instances: We are encouraged to give names to recurring patterns, and to reuse them where needed. It is our feeling that most instance declarations that occur in the wild can actually be derived by using a pattern that deserves to be known and named, and that instances defined manually should become an anti-pattern in all but some rare situations.

Acknowledgements

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