

Hw 2 / 1a

$$\int_{-1}^1 f(x) = [1]_{-1}^1 \rightarrow 1$$

$$b) \int_{-\pi}^{\pi} f(x) = [-\cos(x)]_{-\pi}^{\pi} \rightarrow 0$$

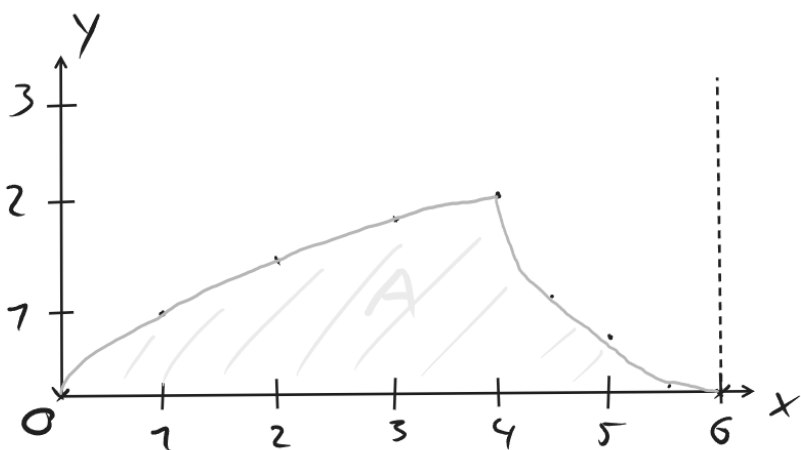
$$c) \int_0^{\pi} f(x) = [4\sin(x)]_0^{\pi} \rightarrow 0$$

$$d) \int_0^{\pi} f(x) = [-3\cos(x) + 5\sin(x)]_0^{\pi} = [-3\cos(x)]_0^{\pi} \rightarrow 6$$

$$e) \int_1^2 f(x) = [e^x]_1^2 = e^2 - e^1 \rightarrow 4.67$$

$$f) \int_0^1 f(x) = [e^x + 2]_0^1 \rightarrow 1.72$$

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$$A = A_1 + A_2$$

$$A_1 = \left[\frac{2}{3} x^{1.5} \right]_0^4$$

$$= 5 \frac{1}{3}$$

$$A_2 = \left[\frac{1}{6} x^3 - 3x^2 + 18x \right]_4^6$$

$$= 7 \frac{1}{3}$$

$$A = 6 \frac{2}{3}$$

13a $F(x) = 1e^y - 1y^3$

$$\int f(x) = [e^y - y^3]_b^a = e^a - a^3 - e^b + b^3$$

$$b) f(x) = x^2 \cdot \sqrt{x} \cdot \frac{1}{\sqrt[3]{x^5}} = x^2 \cdot \sqrt{x} \cdot x^{-\frac{5}{3}} \quad | \quad (\sqrt[3]{x^5})^{-1} = (x^5)^{-\frac{1}{3}} = x^{-\frac{5}{3}}$$

$$= x^2 \cdot x^{\frac{1}{2}} \cdot x^{-\frac{5}{3}} = x^{\frac{5}{6}}$$

$$\int f(x) = \left[\frac{6}{11} \cdot x^{\frac{11}{6}} \right]_b^a = \frac{6}{11} \cdot a^{\frac{11}{6}} - \frac{6}{11} \cdot b^{\frac{11}{6}}$$

$$c) \lim_{x \rightarrow \infty} \int_{-1}^{\infty} |x|^{-2} dx = \infty$$