

rewriting b0-b3:

$$b_0 = \frac{1}{a_0}$$

$$b_1 = \frac{\frac{1 - a_0 \cdot \frac{1}{a_0}}{z} - a_1 \cdot \frac{1}{a_0}}{a_0} = \frac{\frac{1 - 1}{z} - \frac{a_1}{a_0}}{a_0} = -\frac{\frac{a_1}{a_0}}{\frac{1}{a_0}} = -\frac{a_1}{a_0^2}$$

$$b_2 = \frac{\frac{1 - (a_0 \cdot (-\frac{a_1}{a_0^2}) + (a_1 \cdot \frac{1}{a_0}))}{z^2} - (a_0 \cdot \frac{1}{a_0}) \cdot z^0 - a_1 \cdot (-\frac{a_1}{a_0^2}) - \frac{a_2}{a_0}}{a_0}$$

$$= \frac{1 - (-\frac{a_1}{a_0} + \frac{a_1}{a_0}) \cdot z^1 - 1}{z^2} + \frac{a_1^2}{a_0^2} - \frac{a_2}{a_0}$$

$$= \frac{0}{z^2} + \frac{a_1^2}{a_0^2} - \frac{a_2}{a_0}$$

$$= \frac{\frac{a_1^2}{a_0^2}}{\frac{a_0}{1}} - \frac{\frac{a_2}{a_0}}{\frac{1}{1}} = \frac{a_1^2}{a_0^3} - \frac{a_2}{a_0^2} = b_2$$

$$b_3 = (((1 - (a_2 \cdot b_0 + a_1 \cdot b_1 + a_0 \cdot b_2) \cdot z^2 - (a_1 \cdot b_0 + a_0 \cdot b_1) \cdot z - (a_0 \cdot b_0) \cdot 1) / z^3) - a_3 \cdot b_0 - a_2 \cdot b_1 - a_1 \cdot b_2) / a_0$$

$$= (((1 - (a_2 \cdot (1/a_0) + a_1 \cdot (-a_1/a_0^2)) + a_0 \cdot ((a_1^2/a_0^3) - (a_2/a_0^2))) \cdot z^2 - (a_1 \cdot (1/a_0) + a_0 \cdot (-a_1/a_0^2))) \cdot z - (a_0 \cdot (1/a_0)) \cdot 1) / z^3) - a_3 \cdot (1/a_0) - a_2 \cdot (-a_1/a_0^2) - a_1 \cdot ((a_1^2/a_0^3) - (a_2/a_0^2)) / a_0$$

$$= (((1 - 0 - 0 - 1) / z^3) - (a_3/a_0) - (a_1^3/a_0^3)) / a_0$$

$$b_3 = \frac{\frac{0}{z^3} - \frac{a_3}{a_0} - \frac{a_1^3}{a_0^3}}{a_0} = -\frac{\frac{a_3}{a_0}}{\frac{1}{a_0}} - \frac{\frac{a_1^3}{a_0^3}}{\frac{1}{a_0}} = -\frac{a_3}{a_0^2} - \frac{a_1^3}{a_0^4}$$