

$$\text{I} \quad f_0 + g_0 = 0 \quad \Rightarrow \quad g_0 = -f_0 = 4f_0$$

$$\text{II} \quad f_0 + f_1 + g_0 + g_1 + g_2 + g_3 = 0$$

$$\text{III} \quad g_0 + 2g_1 + 4g_2 + 8g_3 = 0$$

$$\text{IV} \quad 4f_0 + 12f_1 + g_0 + 3g_1 + 3g_2 + 2g_3 = 0$$

$$\text{V} \quad 2f_0 + 8f_1 + g_0 + 4g_1 + 16g_2 + 64g_3 = 0$$

$$\text{II} \quad f_1 + g_1 + g_2 + g_3 = 0$$

$$\text{III} \quad 4f_0 + 2g_1 + 4g_2 + 3g_3 = 0$$

$$\text{IV} \quad 3f_0 + 2f_1 + 3g_1 + 4g_2 + 2g_3 = 0$$

$$\text{V} \quad f_0 + 3f_1 + 4g_1 + g_2 + 4g_3 = 0$$

| f_0 | f_1 | g_1 | g_2 | g_3 |
|-------|-------|-------|-------|-------|
| 0 | 1 | 1 | 1 | 1 |
| 4 | 0 | 2 | 4 | 3 |
| 3 | 2 | 3 | 4 | 2 |
| 1 | 3 | 4 | 1 | 4 |



| | f_1 | f | g_1 | g_2 | g_3 | |
|----------|-------|-----|-------|-------|-------|-------------------------------------------------|
| \times | 1 | 0 | 1 | 1 | 1 | |
| | 0 | 4 | 2 | 4 | 3 | $/ \text{ oh}$ |
| | 2 | 3 | 3 | 4 | 2 | $/ \cdot (-\frac{1}{2}) = \cdot (-3) = \cdot 2$ |
| | 3 | 1 | 4 | 1 | 4 | $/ \cdot (-\frac{1}{3}) = \cdot (-2) = \cdot 3$ |

| | f_1 | f | g_1 | g_2 | g_3 | |
|----------|-------|-----|-------|-------|-------|---------------------------------------------------------|
| | 1 | 0 | 1 | 1 | 1 | |
| \times | 0 | 4 | 2 | 4 | 3 | |
| | 0 | 1 | 2 | 4 | 0 | $/ \cdot (-\frac{1}{4}) = \cdot (-4) = \cdot 1$ |
| | 0 | 3 | 3 | 4 | 3 | $/ \cdot (-\frac{4}{3}) = \cdot (-4 \cdot 2) = \cdot 2$ |

| | f_1 | f | g_1 | g_2 | g_3 | |
|----------|-------|-----|-------|-------|-------|------------------------------------|
| | 1 | 0 | 1 | 1 | 1 | |
| | 0 | 4 | 2 | 4 | 3 | |
| \times | 0 | 0 | 4 | 3 | 3 | |
| | 0 | 0 | 3 | 2 | 4 | $/ \cdot (-\frac{4}{3}) = \cdot 2$ |

| | | | | | |
|--|---|---|---|---|---|
| | 0 | 0 | 0 | 2 | 1 |
|--|---|---|---|---|---|

| | f_1 | f_2 | g_1 | g_2 | g_3 |
|--------------|-------|-------|-------|-------|-------|
| Π | 1 | 0 | 1 | 1 | 1 |
| III | 0 | 4 | 2 | 4 | 3 |
| IV | 0 | 0 | 4 | 3 | 3 |
| V | 0 | 0 | 0 | 2 | 1 |

choose, e.g., $g_2 = 1$:

$$\begin{aligned}
 \text{V} \quad & 2 + g_3 = 0 \Rightarrow g_3 = -2 = 3 \\
 \text{IV} \quad & 4f_1 + 3 + g = 0 \Rightarrow g_1 = -\frac{12}{4} = -3 = 2 \\
 \text{III} \quad & 4f_2 + 4 + 4 + g = 0 \Rightarrow f_2 = -\frac{2}{4} = -1 = 2 \\
 \text{II} \quad & f_1 + 2 + 1 + 3 = 0 \Rightarrow f_1 = -1 = 4
 \end{aligned}$$