

P1 A. The current state {C, F} has an error of 8. The states for the next step are {C}, {F}, {C, D, F}, {C, E, F}, {C, F, G}, {C, F, H} with errors 1, 10, 22, 16, 11, 9. The best neighbor is S = {C}, where the cost is $\text{Error}(S) = \max(18-18, 0) + \max(20-19, 0) = 1$.

As we're using hill-climbing, there is no better error smaller than $\text{Error}(\{C\})$, thus in the next iteration no update will be made and the set {C} is the result.

B. The state space size is 2^N as each object can either be taken or not.

Let the current state have m objects then there are m objects to be deleted and (N-m) objects to be added. The maximum number of neighbors is N where at most (N-m)+m=N objects can be either added or deleted.

P2 1. $A \rightarrow \neg(B \wedge C) = \neg A \vee \neg(B \wedge C) = \neg A \vee \neg B \vee \neg C$
 $\{\neg A \vee \neg B \vee \neg C\}$

2. $C \leftrightarrow \neg(D \vee E) = (C \rightarrow \neg(D \vee E)) \wedge (\neg(D \vee E) \rightarrow C) = (\neg C \vee \neg(D \vee E)) \wedge (C \vee D \vee E)$
 $= (\neg C \vee (\neg D \wedge \neg E)) \wedge (C \vee D \vee E) = (\neg C \vee \neg D) \wedge (\neg C \vee \neg E) \wedge (C \vee D \vee E)$
 $\{\neg C \vee \neg D, \neg C \vee \neg E, C \vee D \vee E\}$

3. $D \rightarrow B = \neg D \vee B$
 $\{\neg D \vee B\}$

4. $(D \wedge E) \rightarrow \neg B \wedge A = \neg(D \wedge E) \vee (\neg B \wedge A) = \neg D \vee \neg E \vee (\neg B \wedge A)$
 $= (\neg D \vee \neg E \vee \neg B) \wedge (\neg D \vee \neg E \vee A)$
 $\{\neg D \vee \neg E \vee \neg B, \neg D \vee \neg E \vee A\}$

5. $D \leftrightarrow E = (\neg D \vee E) \wedge (D \vee \neg E)$
 $\{\neg D \vee E, D \vee \neg E\}$

P3 $S_0 = \{C_1: \neg A \vee \neg B \vee \neg C, C_2: \neg C \vee \neg D, C_3: \neg C \vee \neg E, C_4: C \vee D \vee E, C_5: \neg D \vee B, C_6: \neg D \vee \neg E \vee \neg B, C_7: \neg D \vee \neg E \vee A, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, try A = T;
 $S_1 = \{C_1: \neg B \vee \neg C, C_2: \neg C \vee \neg D, C_3: \neg C \vee \neg E, C_4: C \vee D \vee E, C_5: \neg D \vee B, C_6: \neg D \vee \neg E \vee \neg B, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, try B = T;
 $S_2 = \{C_1: \neg C, C_2: \neg C \vee \neg D, C_3: \neg C \vee \neg E, C_4: C \vee D \vee E, C_6: \neg D \vee \neg E, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, C = F;
 $S_3 = \{C_4: D \vee E, C_6: \neg D \vee \neg E, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, try D = T;
 $S_4 = \{C_6: \neg E, C_8: E\}$, contradicted and get back to S_3 ;
 $S_3 = \{C_4: D \vee E, C_6: \neg D \vee \neg E, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, try D = F;
 $S_4 = \{C_4: E, C_9: \neg E\}$, contradicted and get back to S_3 then to S_2 then to S_1 ;
 $S_1 = \{C_1: \neg B \vee \neg C, C_2: \neg C \vee \neg D, C_3: \neg C \vee \neg E, C_4: C \vee D \vee E, C_5: \neg D \vee B, C_6: \neg D \vee \neg E \vee \neg B, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, try B = F;
 $S_2 = \{C_2: \neg C \vee \neg D, C_3: \neg C \vee \neg E, C_4: C \vee D \vee E, C_5: \neg D, C_8: \neg D \vee E, C_9: D \vee \neg E\}$, D = F;
 $S_3 = \{C_3: \neg C \vee \neg E, C_4: C \vee E, C_9: \neg E\}$, try C = T;
 $S_3 = \{C_3: \neg E, C_9: \neg E\}$, E = F;
Return {A-T, B-F, C-T, D-F, E-F}.