



GLMix: Generalized Linear Mixed Models For Large-Scale Response Prediction



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- Jobs homepage

+20-30% lift in job application rate

Ramped to serve **100%** traffic (400 million members)

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- Jobs homepage
 - **+20-30%** lift in job application rate
 - Ramped to serve **100%** traffic
- Article recommendation
 - **+10-20%** lift in CTR
- Sponsored update (Ads)
 - Reduces model training time by **10x**
- People viewed this also viewed
 - **+10-20%** lift in offline experiments

GLMix: a **production-ready** model that **works**

Why GLMix



Desired model properties

- **Interpretable** with features

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Desired model properties

- **Interpretable** with features
- **Scalable** with the economic graph
- **Deployable** with existing (e.g., open-sourced) infras
- **Fine-grained** with users or items with more data

Generalized Linear Model (GLM)

- Predicting the response of ***user i*** on ***item j***:

$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}_{ij}' \mathbf{w}$$

- \mathbf{x}_{ij} : Feature vector
- \mathbf{w} : Coefficient vector
- $\mathbb{E}[y_{ij}]$: Expectation of response
- $g(\cdot)$: Link function

Generalized Linear Model (GLM)

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- Interpretable ✓
- Scalable ✓
- Deployable ✓

Generalized Linear Model (GLM)









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- Fine-grained ?









An example in job recommendation

$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}'_{ij} \mathbf{w}$$

User	Feature	Job	Company	Response
Alice	$\mathbf{x}_{\text{alice}}$	Data Scientist	 Microsoft	
Alice	$\mathbf{x}_{\text{alice}}$	Data Scientist	 airbnb	
Annie	$\mathbf{x}_{\text{annie}}$	Data Scientist	 Microsoft	
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An example in job recommendation

$$\mathbf{x}_{\text{alice}} \approx \mathbf{x}_{\text{annie}} \Rightarrow \mathbf{w} \approx \mathbf{0}$$

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$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}'_{ij} \mathbf{w}$$

Matrix Factorization (MF)

- Predicting the response of ***user i*** on ***item j***:

$$g(\mathbb{E}[y_{ij}]) = \mathbf{u}_i' \mathbf{v}_j$$

- \mathbf{u}_i : User latent factor
- \mathbf{v}_j : Item latent factor
- $\mathbb{E}[y_{ij}]$: Expectation of response
- $g(\cdot)$: Link function

Matrix Factorization (MF)

- Predicting the response of ***user i*** on ***item j***:

$$g(\mathbb{E}[y_{ij}]) = \mathbf{u}_i' \mathbf{v}_j$$

- Interpretable ? (Does not use features)
- Scalable ✓
- Deployable ✓
- Fine-grained ✓

GLMix: Generalized Linear Mixed Model

- Predicting the response of ***user i*** on ***item j***

$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}'_{ij} \mathbf{w} + \mathbf{x}'_j \boldsymbol{\alpha}_i + \mathbf{x}'_i \boldsymbol{\beta}_j$$

- Model coefficients with different **granularities / dimensions**
 - **Per-user** coefficients $\boldsymbol{\alpha}_i$
 - **Per-item** coefficients $\boldsymbol{\beta}_j$

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- GLMix = GLM + per-user model + per-item model

GLMix for Job Recommendation

$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}_{ij}' \mathbf{w} + \mathbf{x}_j' \boldsymbol{\alpha}_i + \mathbf{x}_i' \boldsymbol{\beta}_j$$

- Global model
 - Similarity between member profile and jobs profile, e.g. do the member skills and job skills look similar?

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 - E.g. If a member has applied to a job with title = “software engineer”, we will boost “software engineer” jobs more in her results.









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- Global model
 - Similarity between member profile and jobs profile, e.g. do the member skills and job skills look similar?
- Per-member model
 - E.g. If a member has applied to a job with title = “software engineer”, we will boost “software engineer” jobs more in her results.
- Per-job model
 - E.g. If a job gets an apply with a member titled “software engineer”, we will boost this job more for members with this title.









Alice and Annie's problem revisited

$$g(\mathbb{E}[y_{ij}]) = \mathbf{x}_{ij}'\mathbf{w} + \mathbf{x}_j'\alpha_i + \mathbf{x}_i'\beta_j$$

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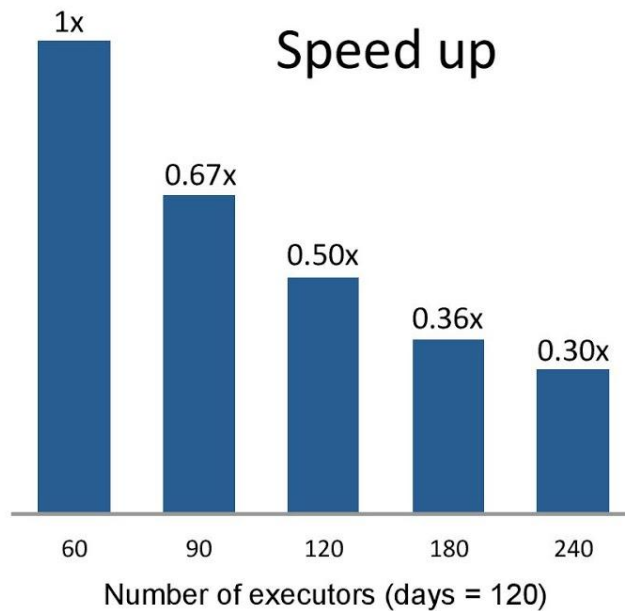
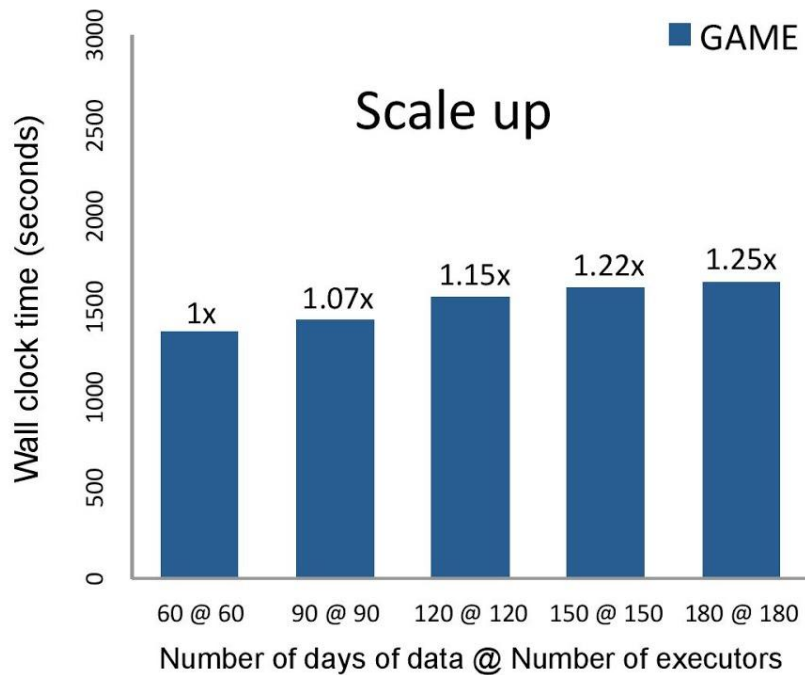
GLMix model properties

- Interpretable ✓ (GLMix = GLM + per-user + per-item + ...)
- Scalable
- Deployable
- Fine-grained ✓

- Scalability challenges
 - 10 million users, 1000 features -> 10B coefficients
 - More users, more features?

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 - Locality aware data pre-partitioning
 - Sharding data by both **rows** (data samples) and **columns** (features)

- Scalability challenges
 - 10 million users, 1000 features -> 10B coefficients
 - More users, more features?
- Solutions (sketch)
 - Locality aware data pre-partitioning
 - Sharding data by both **rows** (data samples) and **columns** (features)
 - Minimize communication cost
 - Coordinate descent, only residuals are shuffled



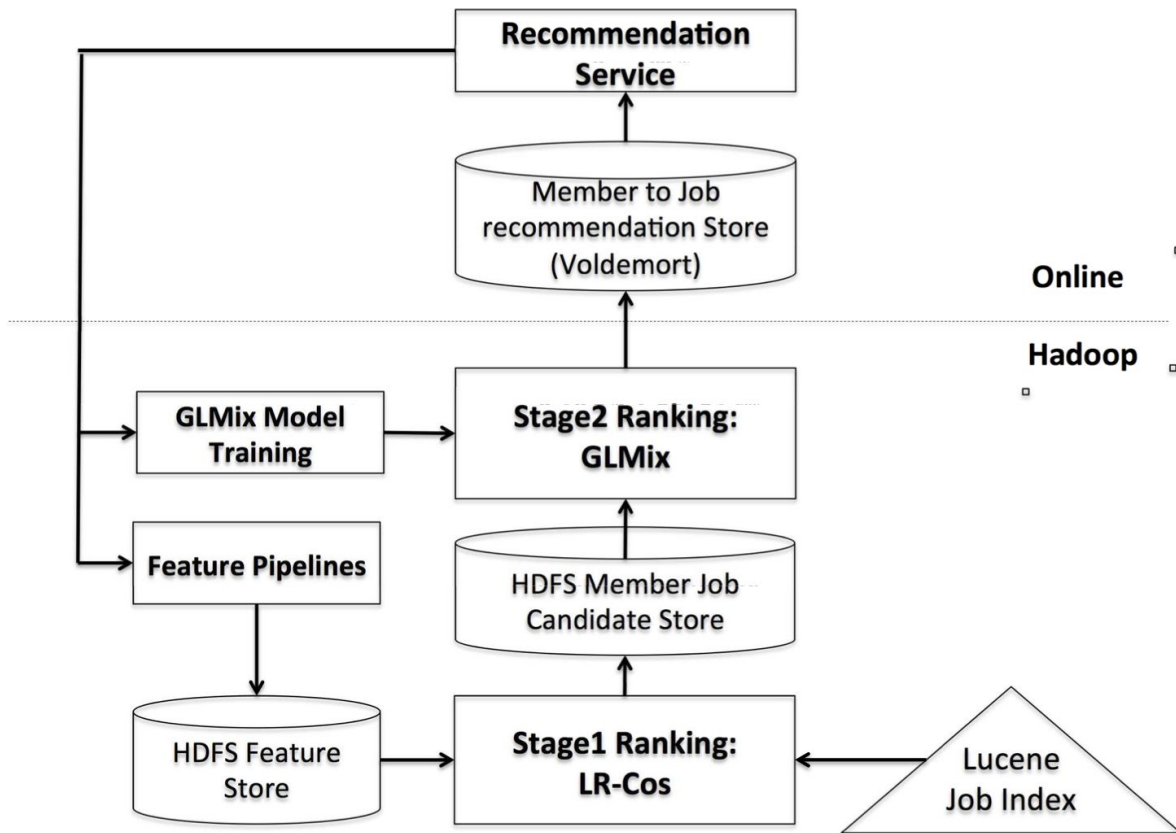
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- Interpretable ✓
- Scalable ✓
- Deployable
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How to **deploy** GLMix with existing
(open-sourced) infra?

- Offline scoring
 - Prepare and score the user-item candidate set offline
 - Push scores to online K-V store
 - Key: ***throughput***
- Online scoring
 - Store model coefficients online
 - Generate and score item candidate set for users in real time
 - Key: ***Latency***

Offline Scoring



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- Jobs homepage

- Ramped to serve 100% traffic
 - With offline scoring, GLMix is ramped to 8% traffic
- +20-30% lift in job application rate

Online Scoring for GLMix

Checkout our hands-on tutorial “Building End-to-End Recommender System with Photon-ML”

- Keyword for Google search: “***Photon-ML***”
- <https://github.com/linkedin/photon-ml/wiki/Photon-ML-Tutorial>



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 - With offline scoring, GLMix is ramped to **8%** traffic
 - Ramped to serve **100%** traffic **with online scoring**
- +20-30% lift in job application rate

GLMix model properties

- Interpretable ✓
- Scalable ✓
- Deployable ✓
- Fine-grained ✓

Takeaways

- **GLMix** is ...
 - Interpretable
 - GLM + per-dimension models
 - Scalable
 - Sharded by samples and features + Coordinate descent
 - Deployable
 - With existing (open source) infra
 - Fine-grained
 - Per-dimension models

Takeaways

- **GLMix** is...
 - Interpretable
 - Scalable
 - Deployable
 - Fine-grained
 - **An open-source library**
 - Search for Photon-ML
 - <https://github.com/linkedin/photon-ml>
 - Implemented in the GAME module

