

# Tit For Tat

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# 1 Base

## 1.1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 using i64 = long long;
5 using u64 = unsigned long long;
6 using i128 = __int128_t;
7 using u128 = __uint128_t;
8 using ld = long double;
9
10 constexpr int INF32 = 0x3f3f3f3f; // ~1e9
11 constexpr i64 INF64 = (i64)4e18;
12 constexpr ld EPS = 1e-12L;
13 constexpr ld PI = 3.14159265358979323846264338327950288L;
14 constexpr int MOD = 1e9 + 7;
15
16 #define fastio \
17     ios::sync_with_stdio(false); \
18     cin.tie(nullptr); \
19     cout.tie(nullptr);
20
21 // ----- optional -----
22 template <class T> using V = vector<T>;
23 template <class K, class Val> using umap = unordered_map<K, Val>;
24 template <class K> using uset = unordered_set<K>;
25
26 #define rep(i, n) for (int i = 0; i < n; ++i)
27 #define per(i, n) for (int i = n - 1; i >= 0; --i)
28 #define reps(i, a, b) for (int i = a; i < b; ++i)
29 #define pers(i, a, b) for (int i = b - 1; i >= a; --i)
30 #define all(x) begin(x), end(x)
31 #define rall(x) rbegin(x), rend(x)
32 #define len(x) (x.size())
33
34 template <class T> using MinHeap = priority_queue<T, vector<T>, greater<T>>;
35 template <class T> using MaxHeap = priority_queue<T>;
36 // ----- optional -----
37
38 void solve() {}
39
40 int main() {
41     fastio;
42     int T = 1;
43     // cin >> T;
44     while (T--) solve();
45     return 0;
46 }
```

Listing 1: template.cpp

## 1.2 Tester

```
1#!/bin/bash
2# Uso: ./tester A.cpp -> buscará in/A.in, in/A1.in, etc.
3
4SRC=$1
5BIN="\${SRC%.*}"
6
7BASENAME=\$(basename "\$BIN")
8mkdir -p out
9g++ -std=c++17 -O2 -Wall -DLOCAL -fsanitize=address,undefined "\$SRC" -o "\$BIN" || exit 1
10shopt -s nullglob
11for IN in in/"\${BASENAME}*.in"; do
12    TEST_FILE=\$(basename "\$IN")
13    TEST_NAME="\${TEST_FILE%.in}"
14    echo -e "\nTesting \$IN..."
15    /usr/bin/time -v "./\$BIN" < "\$IN" > "out/\$TEST_NAME.out" 2>&1 || {
```

```

16     time "./$BIN" < "$IN" > "out/$TEST_NAME.out"
17 }
18 echo "--- INPUT ($IN) ---"
19 head -n 5 "$IN"
20 echo -e "\n--- OUTPUT (out/$TEST_NAME.out) ---"
21 head -n 10 "out/$TEST_NAME.out"
22 echo "====="
23 done

```

Listing 2: tester.sh

## 2 Data Structures

### 2.1 DSU

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct DSU {
5     vector<int> parent, size;
6     DSU(int n) {
7         parent.resize(n);
8         size.resize(n);
9     }
10    void make_set(int v) {
11        parent[v] = v;
12        size[v] = 1;
13    }
14    int find_set(int v) {
15        if(v == parent[v]) return v;
16        return parent[v] = find_set(parent[v]);
17    }
18    void union_sets(int a, int b) {
19        a = find_set(a);
20        b = find_set(b);
21        if(a == b) return;
22        if(size[a] < size[b]) swap(a, b);
23        parent[b] = a;
24        size[a] += size[b];
25    }
26};

```

Listing 3: DSU.cpp

### 2.2 MergeSortTree

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct MergeSortTree {
5     vector<vector<int>> heap;
6     // s.build(array, 1, 0, n-1);
7     void build(vector<int> &array, int v, int tl, int tr) {
8         if(heap.size() <= v) heap.resize(v+1);
9         if(tl == tr) heap[v] = vector<int> (1, array[tl]);
10        else {
11            int tm = (tl + tr) / 2;
12            build(array, 2*v, tl, tm);
13            build(array, 2*v+1, tm+1, tr);
14            merge(heap[2*v].begin(), heap[2*v].end(), heap[2*v+1].begin(),
15                  heap[2*v+1].end(), back_inserter(heap[v]));
16        }
17    }
18    // s.get(1, 0, n-1, l, r);
19    vector<int> get(int v, int tl, int tr, int l, int r) {
20        if(l > r) return vector<int> ();
21        if(l == tl and r == tr) return heap[v];
22        int tm = (tl + tr) / 2;

```

```

23     vector<int> v1 = get(v*2, tl, tm, l, min(r, tm)), v2 = get(v*2+1, tm+1, tr, max(l, tm
24     +1), r), result;
25     merge(v1.begin(), v1.end(), v2.begin(), v2.end(), back_inserter(result));
26     return result;
27 }
28 // s.update(1, 0, n-1, pos, x);
29 void update(int v, int tl, int tr, int pos, int x) {
30     if(tl == tr) {
31         heap[v] = vector<int> (1, x);
32     } else {
33         int tm = (tl + tr) / 2;
34         if(pos <= tm) update(2*v, tl, tm, pos, x);
35         else update(2*v+1, tm+1, tr, pos, x);
36         heap[v] = vector<int> ();
37         merge(heap[2*v].begin(), heap[2*v].end(), heap[2*v+1].begin(),
38               heap[2*v+1].end(), back_inserter(heap[v]));
39     }
40 }

```

Listing 4: MergeSortTree.cpp

## 2.3 SegmentTree

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct SegmentTree {
5     vector<int> heap;
6     vector<long long> lazy;
7
8     // s.init(n);
9     void init(int n) {
10         int size = 4 * n + 1;
11         heap.assign(size, 0);
12         lazy.assign(size, 0);
13     }
14
15     // s.build(array, 1, 0, n-1);
16     void build(vector<int> &array, int v, int tl, int tr) {
17         if(tl == tr) heap[v] = array[tl];
18         else {
19             int tm = (tl + tr) / 2;
20             build(array, 2*v, tl, tm);
21             build(array, 2*v+1, tm+1, tr);
22             heap[v] = heap[2*v] + heap[2*v+1];
23         }
24     }
25
26     // s.sum(1, 0, n-1, l, r);
27     int sum(int v, int tl, int tr, int l, int r) {
28         if(l > r) return 0;
29         if(l == tl and r == tr) return heap[v];
30         int tm = (tl + tr) / 2;
31         return sum(v*2, tl, tm, l, min(r, tm)) + sum(v*2+1, tm+1, tr, max(l, tm+1), r);
32     }
33
34     // s.update(1, 0, n-1, pos, x); in position pos set value x
35     void update(int v, int tl, int tr, int pos, int x) {
36         if(tl == tr) heap[v] = x;
37         else {
38             int tm = (tl + tr) / 2;
39             if(pos <= tm) update(2*v, tl, tm, pos, x);
40             else update(2*v+1, tm+1, tr, pos, x);
41             heap[v] = heap[2*v] + heap[2*v+1];
42         }
43     }
44
45     // push for lazy propagation
46     void push(int v, int tl, int tr) {
47         if (lazy[v] != 0 && tl != tr) {

```

```

48     int tm = (tl + tr) / 2;
49     long long addval = lazy[v];
50     heap[2*v] += addval * (tm - tl + 1);
51     heap[2*v+1] += addval * (tr - tm);
52     lazy[2*v] += addval;
53     lazy[2*v+1] += addval;
54   }
55   lazy[v] = 0;
56 }
57
58 // s.lazyupdate(1, 0, n-1, l, r, addend); // add 'addval' to range [l, r]
59 void lazyupdate(int v, int tl, int tr, int l, int r, int addval) {
60   push(v, tl, tr); // Propagate any pending updates
61   if (l > r) return;
62   if (l > tr || r < tl) return;
63   if (l <= tl && tr <= r) {
64     // Apply update to the current heap value
65     heap[v] += (long long)addval * (tr - tl + 1);
66     // Mark the lazy tag for future children updates
67     lazy[v] += addval;
68     return;
69   }
70
71   int tm = (tl + tr) / 2;
72   lazyupdate(2*v, tl, tm, l, r, addval);
73   lazyupdate(2*v+1, tm+1, tr, l, r, addval);
74   heap[v] = heap[2*v] + heap[2*v+1];
75 }
76 };

```

Listing 5: SegmentTree.cpp

## 2.4 SparseTable

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct SparseTable {
5   int N, K;
6   vector<vector<int>> table;
7   vector<int> logs;
8
9   // Constructor to build the table
10  SparseTable(const vector<int>& arr) {
11    N = arr.size();
12    K = floor(log2(N)) + 1; // Max power of 2
13    table.assign(N, vector<int>(K));
14    logs.resize(N + 1);
15
16    logs[1] = 0;
17    for (int i = 2; i <= N; i++) {
18      logs[i] = logs[i / 2] + 1;
19    }
20
21    for (int i = 0; i < N; i++) {
22      table[i][0] = arr[i];
23    }
24
25    for (int j = 1; j < K; j++) {
26      for (int i = 0; i + (1 << j) <= N; i++) {
27        table[i][j] = min(table[i][j - 1],
28                           table[i + (1 << (j - 1))][j - 1]);
29      }
30    }
31  }
32
33  // Query the range [L, R] (inclusive) in O(1)
34  int query(int L, int R) {
35    // Find largest k such that 2^k <= (R - L + 1)
36    int k = logs[R - L + 1];
37

```

```

38     // Return min of the two overlapping ranges
39     return min(table[L][k], table[R - (1 << k) + 1][k]);
40 }
41 };

```

Listing 6: SparseTable.cpp

## 2.5 Fenwick (BIT)

```

1 #include <bits/stdc++.h>
2 #define ll long long
3 using namespace std;
4
5 struct FenwickTree {
6     vector<int> bit; // binary indexed tree
7     int n;
8
9     FenwickTree(int n) {
10         this->n = n;
11         bit.assign(n, 0);
12     }
13
14     FenwickTree(vector<int> const &a) : FenwickTree(a.size()) {
15         for (size_t i = 0; i < a.size(); i++)
16             add(i, a[i]);
17     }
18
19     ll sum(int r) {
20         ll ret = 0;
21         for (; r >= 0; r = (r & (r + 1)) - 1)
22             ret += bit[r];
23         return ret;
24     }
25
26     ll sum(int l, int r) {
27         return sum(r) - (l == 0 ? 0LL : sum(l - 1));
28     }
29
30     ll add(int idx, int delta) {
31         for (; idx < n; idx = idx | (idx + 1))
32             bit[idx] += delta;
33     }
34 };
35
36 // Gemini implementation
37 struct RangeFenwickTree {
38     FenwickTree B1;
39     FenwickTree B2;
40     int n;
41
42     RangeFenwickTree(int size) : n(size), B1(size), B2(size) {}
43
44     ll prefix_sum(int idx) {
45         return B1.sum(idx) * (idx + 1) - B2.sum(idx);
46     }
47
48     ll range_sum(int l, int r) {
49         ll sum_r = prefix_sum(r);
50         ll sum_l_minus_1 = (l == 0) ? 0LL : prefix_sum(l - 1);
51         return sum_r - sum_l_minus_1;
52     }
53
54     void range_add(int l, int r, ll x) {
55         B1.add(l, x);
56         if (r + 1 < n) {
57             B1.add(r + 1, -x);
58         }
59
60         B2.add(l, x * l);
61         if (r + 1 < n) {
62             B2.add(r + 1, -x * (r + 1));

```

```

63     }
64 }
65 }
```

Listing 7: Fenwick.cpp

### 3 Trees

#### 3.1 Heavy-Light Decomposition (HLD)

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 vector<int> parent, depth, heavy, head, pos;
5 int cur_pos;
6
7 int dfs(int v, vector<vector<int>> const& adj) {
8     int size = 1;
9     int max_c_size = 0;
10    for (int c : adj[v]) {
11        if (c != parent[v]) {
12            parent[c] = v, depth[c] = depth[v] + 1;
13            int c_size = dfs(c, adj);
14            size += c_size;
15            if (c_size > max_c_size)
16                max_c_size = c_size, heavy[v] = c;
17        }
18    }
19    return size;
20 }
21
22 void decompose(int v, int h, vector<vector<int>> const& adj) {
23     head[v] = h, pos[v] = cur_pos++;
24     if (heavy[v] != -1)
25         decompose(heavy[v], h, adj);
26     for (int c : adj[v]) {
27         if (c != parent[v] && c != heavy[v])
28             decompose(c, c, adj);
29     }
30 }
31
32 void init(vector<vector<int>> const& adj) {
33     int n = adj.size();
34     parent = vector<int>(n);
35     depth = vector<int>(n);
36     heavy = vector<int>(n, -1);
37     head = vector<int>(n);
38     pos = vector<int>(n);
39     cur_pos = 0;
40
41     dfs(0, adj);
42     decompose(0, 0, adj);
43 }
44
// how queries should be implemented
45 int segment_tree_query(int a, int b);
46 int query(int a, int b) {
47     int res = 0;
48     for (; head[a] != head[b]; b = parent[head[b]]) {
49         if (depth[head[a]] > depth[head[b]])
50             swap(a, b);
51         int cur_heavy_path_max = segment_tree_query(pos[head[b]], pos[b]);
52         res = max(res, cur_heavy_path_max);
53     }
54     if (depth[a] > depth[b])
55         swap(a, b);
56     int last_heavy_path_max = segment_tree_query(pos[a], pos[b]);
57     res = max(res, last_heavy_path_max);
58     return res;
59 }
```

---

Listing 8: HLD.cpp

### 3.2 Centroid Decomposition

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 // A centroid of a tree is defined as a node such that when the tree is rooted at it, no other
4 // nodes have a subtree of size greater than  $\frac{N}{2}$ 
5 const int maxn = 200010;
6
7 int n;
8 vector<int> adj[maxn];
9 int subtree_size[maxn];
10
11 // must be called first at 0 to fill subtree_size
12 int get_subtree_size(int node, int parent = -1) {
13     int &res = subtree_size[node];
14     res = 1;
15     for (int i : adj[node]) {
16         if (i == parent) { continue; }
17         res += get_subtree_size(i, node);
18     }
19     return res;
20 }
21
22 int get_centroid(int node, int parent = -1) {
23     for (int i : adj[node]) {
24         if (i == parent) { continue; }
25
26         if (subtree_size[i] * 2 > n) { return get_centroid(i, node); }
27     }
28     return node;
29 }
```

Listing 9: CentroidDecomposition.cpp

### 3.3 Lowest Common Ancestor (LCA) - Binary Lifting

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 int n, l;
4 vector<vector<int>> adj;
5
6 int timer;
7 vector<int> tin, tout;
8 vector<vector<int>> up;
9
10 void dfs(int v, int p) {
11     tin[v] = ++timer;
12     up[v][0] = p;
13     for (int i = 1; i <= l; ++i)
14         up[v][i] = up[up[v][i-1]][i-1];
15
16     for (int u : adj[v]) {
17         if (u != p)
18             dfs(u, v);
19     }
20
21     tout[v] = ++timer;
22 }
23
24 bool is_ancestor(int u, int v) {
25     return tin[u] <= tin[v] && tout[u] >= tout[v];
26 }
27
28 int lca(int u, int v) {
```

```

29     if (is_ancestor(u, v))
30         return u;
31     if (is_ancestor(v, u))
32         return v;
33     for (int i = 1; i >= 0; --i) {
34         if (!is_ancestor(up[u][i], v))
35             u = up[u][i];
36     }
37     return up[u][0];
38 }
39
40 void preprocess(int root) {
41     tin.resize(n);
42     tout.resize(n);
43     timer = 0;
44     l = ceil(log2(n));
45     up.assign(n, vector<int>(l + 1));
46     dfs(root, root);
47 }

```

Listing 10: LCA.cpp

### 3.4 Rerooting

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 vector<vector<int>> graph(200001);
5 vector<int> fir(200001), sec(200001), ans(200001);
6
7 void dfs1(int node = 1, int parent = 0) {
8     for (int i : graph[node])
9         if (i != parent) {
10             dfs1(i, node);
11             if (fir[i] + 1 > fir[node]) {
12                 sec[node] = fir[node];
13                 fir[node] = fir[i] + 1;
14             } else if (fir[i] + 1 > sec[node]) {
15                 sec[node] = fir[i] + 1;
16             }
17         }
18 }
19
20 void dfs2(int node = 1, int parent = 0, int to_p = 0) {
21     ans[node] = max(to_p, fir[node]);
22     for (int i : graph[node])
23         if (i != parent) {
24             if (fir[i] + 1 == fir[node]) dfs2(i, node, max(to_p, sec[node]) + 1);
25             else dfs2(i, node, ans[node] + 1);
26         }
27 }
28
29 int main() {
30     ios_base::sync_with_stdio(0);
31     cin.tie(0);
32     int n;
33     cin >> n;
34     for (int i = 1; i < n; i++) {
35         int u, v;
36         cin >> u >> v;
37         graph[u].push_back(v);
38         graph[v].push_back(u);
39     }
40     dfs1();
41     dfs2();
42     for (int i = 1; i <= n; i++) cout << ans[i] << ' ';
43     return 0;
44 }

```

Listing 11: Rerooting.cpp

## 4 Graphs

### 4.1 Dijkstra

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int INF = 1000000000;
5 vector<vector<pair<int, int>>> adj;
6 int n_vertices;
7
8 void dijkstra(int source, vector<int> &distances, int current_time) {
9     distances.assign(n_vertices, INF);
10    priority_queue<pair<int, int>, vector<pair<int, int>>, greater<pair<int, int>>> tour;
11
12    distances[source] = current_time;
13    tour.push({distances[source], source});
14
15    while(!tour.empty()) {
16        auto u = tour.top();
17        tour.pop();
18
19        if (distances[u.second] != u.first) continue;
20        for (pair<int, int> &v: adj[u.second]) {
21            int d = u.first + v.second;
22            if (d < distances[v.first]) {
23                distances[v.first] = d;
24                tour.push({d, v.first});
25            }
26        }
27    }
28}
```

Listing 12: Dijkstra.cpp

### 4.2 Bellman-Ford

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 struct Edge {
4     int a, b, cost;
5 };
6
7 int n, m, v;
8 vector<Edge> edges;
9 const int INF = 1e9;
10
11 // negatives cycles reachable from v
12 void solve()
13 {
14     vector<int> d(n, INF);
15     d[v] = 0;
16     vector<int> p(n, -1);
17     int x;
18     for (int i = 0; i < n; ++i) {
19         x = -1;
20         for (Edge e : edges)
21             if (d[e.a] < INF)
22                 if (d[e.b] > d[e.a] + e.cost) {
23                     d[e.b] = max(-INF, d[e.a] + e.cost);
24                     p[e.b] = e.a;
25                     x = e.b;
26                 }
27     }
28
29     if (x == -1)
30         cout << "No negative cycle from " << v;
31     else {
32         int y = x;
33         for (int i = 0; i < n; ++i)
```

```

34     y = p[y];
35
36     vector<int> path;
37     for (int cur = y;; cur = p[cur]) {
38         path.push_back(cur);
39         if (cur == y && path.size() > 1)
40             break;
41     }
42     reverse(path.begin(), path.end());
43
44     cout << "Negative cycle: ";
45     for (int u : path)
46         cout << u << ' ';
47 }
48
49 // spfa
50 vector<vector<pair<int, int>>> adj;
51
52 bool spfa(int s, vector<int>& d) {
53     int n = adj.size();
54     d.assign(n, INF);
55     vector<int> cnt(n, 0);
56     vector<bool> inqueue(n, false);
57     queue<int> q;
58
59     d[s] = 0;
60     q.push(s);
61     inqueue[s] = true;
62     while (!q.empty()) {
63         int v = q.front();
64         q.pop();
65         inqueue[v] = false;
66
67         for (auto edge : adj[v]) {
68             int to = edge.first;
69             int len = edge.second;
70
71             if (d[v] + len < d[to]) {
72                 d[to] = d[v] + len;
73                 if (!inqueue[to]) {
74                     q.push(to);
75                     inqueue[to] = true;
76                     cnt[to]++;
77                     if (cnt[to] > n)
78                         return false; // negative cycle
79                 }
80             }
81         }
82     }
83     return true;
84 }

```

Listing 13: BellmanFord.cpp

### 4.3 Floyd-Warshall

```

1 #include <bits/stdc++.h>
2 using i64 = long long;
3 using namespace std;
4 const i64 INF = 1e18;
5
6 void floydWarshall(vector<vector<i64>>& d, int N) {
7     d.resize(N, vector<i64>(N, INF)); // all paths inf by default
8     for (int k = 0; k < N; ++k) {
9         for (int i = 0; i < N; ++i) {
10            for (int j = 0; j < N; ++j) {
11                if (d[i][k] < INF && d[k][j] < INF)
12                    d[i][j] = min(d[i][j], d[i][k] + d[k][j]);
13            }
14        }

```

```
15 }
16 }
```

Listing 14: FloydWarshall.cpp

## 4.4 Kruskal

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct Edge {
5     int u, v, weight;
6     bool operator<(Edge const& other) {
7         return weight < other.weight;
8     }
9 };
10 int n;
11 vector<Edge> edges;
12
13 vector<Edge> kruskal() {
14     int cost = 0;
15     vector<int> tree_id(n);
16     vector<Edge> result;
17
18     for (int i = 0; i < n; i++)
19         tree_id[i] = i;
20
21     sort(edges.begin(), edges.end());
22
23     for (Edge e : edges) {
24         if (tree_id[e.u] != tree_id[e.v]) {
25             cost += e.weight;
26             result.push_back(e);
27
28             int old_id = tree_id[e.u], new_id = tree_id[e.v];
29             for (int i = 0; i < n; i++) {
30                 if (tree_id[i] == old_id)
31                     tree_id[i] = new_id;
32             }
33         }
34     }
35     return result;
36 }
```

Listing 15: Kruskal.cpp

## 4.5 Max Flow (Dinic)

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct FlowEdge {
5     int v, u;
6     long long cap, flow = 0;
7     FlowEdge(int v, int u, long long cap) : v(v), u(u), cap(cap) {}
8 };
9
10 struct Dinic {
11     const long long flow_inf = 1e18;
12     vector<FlowEdge> edges;
13     vector<vector<int>> adj;
14     int n, m = 0;
15     int s, t;
16     vector<int> level, ptr;
17     queue<int> q;
18
19     Dinic(int n, int s, int t) : n(n), s(s), t(t) {
20         adj.resize(n);
21         level.resize(n);
```

```

22     ptr.resize(n);
23 }
24
25 void add_edge(int v, int u, long long cap) {
26     edges.emplace_back(v, u, cap);
27     edges.emplace_back(u, v, 0);
28     adj[v].push_back(m);
29     adj[u].push_back(m + 1);
30     m += 2;
31 }
32
33 bool bfs() {
34     while (!q.empty()) {
35         int v = q.front();
36         q.pop();
37         for (int id : adj[v]) {
38             if (edges[id].cap == edges[id].flow)
39                 continue;
40             if (level[edges[id].u] != -1)
41                 continue;
42             level[edges[id].u] = level[v] + 1;
43             q.push(edges[id].u);
44         }
45     }
46     return level[t] != -1;
47 }
48
49 long long dfs(int v, long long pushed) {
50     if (pushed == 0)
51         return 0;
52     if (v == t)
53         return pushed;
54     for (int& cid = ptr[v]; cid < (int)adj[v].size(); cid++) {
55         int id = adj[v][cid];
56         int u = edges[id].u;
57         if (level[v] + 1 != level[u])
58             continue;
59         long long tr = dfs(u, min(pushed, edges[id].cap - edges[id].flow));
60         if (tr == 0)
61             continue;
62         edges[id].flow += tr;
63         edges[id ^ 1].flow -= tr;
64         return tr;
65     }
66     return 0;
67 }
68
69 long long flow() {
70     long long f = 0;
71     while (true) {
72         fill(level.begin(), level.end(), -1);
73         level[s] = 0;
74         q.push(s);
75         if (!bfs())
76             break;
77         fill(ptr.begin(), ptr.end(), 0);
78         while (long long pushed = dfs(s, flow_inf)) {
79             f += pushed;
80         }
81     }
82     return f;
83 }
84 };

```

Listing 16: Dinic.cpp

## 4.6 Topological Sort (Kahn's Algorithm)

```

1 #include <bits/stdc++.h>
2 using namespace std;
3

```

```

4 int n; // number of vertices
5 vector<vector<int>> adj; // adjacency list of graph
6 vector<bool> visited;
7 vector<int> ans;
8
9 void dfs(int v) {
10     visited[v] = true;
11     for (int u : adj[v]) {
12         if (!visited[u]) {
13             dfs(u);
14         }
15     }
16     ans.push_back(v);
17 }
18
19 void topological_sort() {
20     visited.assign(n, false);
21     ans.clear();
22     for (int i = 0; i < n; ++i) {
23         if (!visited[i]) {
24             dfs(i);
25         }
26     }
27     reverse(ans.begin(), ans.end());
28 }
```

Listing 17: TopoSort.cpp

## 5 Mathematics and Number Theory

### 5.1 Sieve

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int N = 10000000;
5 vector<int> lp(N+1);
6 vector<int> pr;
7
8 void sieve_init() {
9     for (int i=2; i <= N; ++i) {
10         if (lp[i] == 0) {
11             lp[i] = i;
12             pr.push_back(i);
13         }
14         for (int j = 0; i * pr[j] <= N; ++j) {
15             lp[i * pr[j]] = pr[j];
16             if (pr[j] == lp[i]) {
17                 break;
18             }
19         }
20     }
21 }
22
23 // Get all primes in range [L, R] with R up to 10e12 and R-L up to 10e7
24 vector<char> segmentedSieve(long long L, long long R) {
25     // generate all primes up to sqrt(R)
26     long long lim = sqrt(R);
27     vector<char> mark(lim + 1, false);
28     vector<long long> primes;
29     for (long long i = 2; i <= lim; ++i) {
30         if (!mark[i]) {
31             primes.emplace_back(i);
32             for (long long j = i * i; j <= lim; j += i)
33                 mark[j] = true;
34         }
35     }
36
37     vector<char> isPrime(R - L + 1, true);
38     for (long long i : primes)
```

```

39     for (long long j = max(i * i, (L + i - 1) / i * i); j <= R; j += i)
40         isPrime[j - L] = false;
41     if (L == 1)
42         isPrime[0] = false;
43     return isPrime;
44 }

```

Listing 18: Sieve.cpp

## 5.2 Extended Euclidean Algorithm

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int gcd(int a, int b, int& x, int& y) {
5     if (b == 0) {
6         x = 1;
7         y = 0;
8         return a;
9     }
10    int x1, y1;
11    int d = gcd(b, a % b, x1, y1);
12    x = y1;
13    y = x1 - y1 * (a / b);
14    return d;
15 }
16
17 bool find_any_solution(int a, int b, int c, int &x0, int &y0, int &g) {
18     g = gcd(abs(a), abs(b), x0, y0);
19     if (c % g) {
20         return false;
21     }
22
23     x0 *= c / g;
24     y0 *= c / g;
25     if (a < 0) x0 = -x0;
26     if (b < 0) y0 = -y0;
27     return true;
28 }
29
30 void shift_solution(int &x, int &y, int a, int b, int cnt) {
31     x += cnt * b;
32     y -= cnt * a;
33 }
34
35 int find_all_solutions(int a, int b, int c, int minx, int maxx, int miny, int maxy) {
36     int x, y, g;
37     if (!find_any_solution(a, b, c, x, y, g))
38         return 0;
39     a /= g;
40     b /= g;
41
42     int sign_a = a > 0 ? +1 : -1;
43     int sign_b = b > 0 ? +1 : -1;
44
45     shift_solution(x, y, a, b, (minx - x) / b);
46     if (x < minx)
47         shift_solution(x, y, a, b, sign_b);
48     if (x > maxx)
49         return 0;
50     int lx1 = x;
51
52     shift_solution(x, y, a, b, (maxx - x) / b);
53     if (x > maxx)
54         shift_solution(x, y, a, b, -sign_b);
55     int rx1 = x;
56
57     shift_solution(x, y, a, b, -(miny - y) / a);
58     if (y < miny)
59         shift_solution(x, y, a, b, -sign_a);
60     if (y > maxy)

```

```

61     return 0;
62     int lx2 = x;
63
64     shift_solution(x, y, a, b, -(maxy - y) / a);
65     if (y > maxy)
66         shift_solution(x, y, a, b, sign_a);
67     int rx2 = x;
68
69     if (lx2 > rx2)
70         swap(lx2, rx2);
71     int lx = max(lx1, lx2);
72     int rx = min(rx1, rx2);
73
74     if (lx > rx)
75         return 0;
76     return (rx - lx) / abs(b) + 1;
77 }
```

Listing 19: ExtendedEuclid.cpp

### 5.3 Binomial Coefficients ( $nCr$ ) and Modular Arithmetic

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 using i64 = long long;
5 using u64 = unsigned long long;
6 using i128 = __int128_t;
7 using u128 = __uint128_t;
8 using ld = long double;
9
10 constexpr int MOD = 1e9 + 7;
11
12 inline i64 addmod(i64 a, i64 b, i64 mod = MOD) {
13     a %= mod;
14     b %= mod;
15     a += b;
16     if (a >= mod)
17         a -= mod;
18     return a;
19 }
20
21 inline i64 submod(i64 a, i64 b, i64 mod = MOD) {
22     a %= mod;
23     b %= mod;
24     a -= b;
25     if (a < 0)
26         a += mod;
27     return a;
28 }
29
30 inline i64 mulmod(i64 a, i64 b, i64 mod = MOD) {
31     return (i64)((i128)a * b % mod);
32 }
33
34 i64 binpow(i64 a, i64 e, i64 mod = MOD) {
35     i64 r = 1 % mod;
36     a %= mod;
37     while (e) {
38         if (e & 1)
39             r = mulmod(r, a, mod);
40         a = mulmod(a, a, mod);
41         e >>= 1;
42     }
43     return r;
44 }
45
46 inline i64 lcm_ll(i64 a, i64 b) {
47     if (a == 0 || b == 0)
48         return 0;
49     return a / std::gcd(a, b) * b;
```

```

50 }
51 // Devuelve el GCD de a y b, y x, y tales que ax + by = GCD(a, b)
52 i64 egcd(i64 a, i64 b, i64 &x, i64 &y) {
53     if (!b) {
54         x = 1;
55         y = 0;
56         return a;
57     }
58     i64 x1, y1;
59     i64 g = egcd(b, a % b, x1, y1);
60     x = y1;
61     y = x1 - (a / b) * y1;
62     return g;
63 }
64 }

65 // Inverso modular: usar Fermat si mod es primo, si no, usar egcd
66 inline i64 invmod(i64 a, i64 mod = MOD) {
67     if (std::gcd(a, mod) != 1) {
68         return -1; // no existe
69     }
70     // Fermat si MOD es primo
71     // return binpow((a % mod + mod) % mod, mod - 2, mod);
72     i64 x, y;
73     egcd(a, mod, x, y);
74     x %= mod;
75     if (x < 0)
76         x += mod;
77     return x;
78 }
79 }

80 inline i64 moddiv(i64 a, i64 b, i64 mod = MOD) {
81     i64 inv = invmod(b, mod);
82     return inv == -1 ? -1 : mulmod((a % mod + mod) % mod, inv, mod);
83 }
84 }

85 // ----- Binomial coefficients -----
86 // Exact binomial coefficient (integer). For large n this may overflow i64.
87 inline i64 binom_exact(i64 n, i64 k) {
88     if (k < 0 || k > n)
89         return 0;
90     k = min(k, n - k);
91     i64 res = 1;
92     // Compute iteratively: res = C(n, i) for i from 1..k
93     for (i64 i = 1; i <= k; ++i) {
94         // Multiply then divide; this stays integral at every step because
95         // res = C(n, i-1) and res * (n - i + 1) / i = C(n, i).
96         res = res * (n - i + 1) / i;
97     }
98     return res;
99 }
100 }

101 // Modular binomial coefficients using precomputed factorials.
102 // Usage: call init_fact(MAX_N) once (MAX_N >= maximum n you'll query).
103 static vector<i64> fact_mod, invfact_mod;
104

105 inline void init_fact(int N, i64 mod = MOD) {
106     fact_mod.assign(N + 1, 1);
107     invfact_mod.assign(N + 1, 1);
108     for (int i = 1; i <= N; ++i)
109         fact_mod[i] = mulmod(fact_mod[i - 1], i, mod);
110     // invfact[N] = inverse of fact[N]
111     invfact_mod[N] = invmod(fact_mod[N], mod);
112     // compute invfact downwards
113     for (int i = N; i > 0; --i)
114         invfact_mod[i - 1] = mulmod(invfact_mod[i], i, mod);
115 }
116 }

117 inline i64 nCr_mod(int n, int r, i64 mod = MOD) {
118     if (r < 0 || r > n)
119         return 0;
120     if ((int)fact_mod.size() <= n) {
121

```

```

122 // Not initialized for this n; fallback to multiplicative method modulo (works if mod is
123 // prime)
124 // This multiplicative method requires mod to be prime for modular division.
125 i64 num = 1, den = 1;
126 r = min(r, n - r);
127 for (int i = 1; i <= r; ++i) {
128     num = mulmod(num, n - r + i, mod);
129     den = mulmod(den, i, mod);
130 }
131 i64 inv = invmod(den, mod);
132 return mulmod(num, inv, mod);
133 }
134 return mulmod(fact_mod[n], mulmod(invfact_mod[r], invfact_mod[n - r], mod), mod);
135 }
136 // -----
137 // Exact Catalan number: C_n = binom(2n, n) / (n+1). May overflow for large n.
138 inline i64 catalan_exact(i64 n) {
139     if (n < 0)
140         return 0;
141     return binom_exact(2 * n, n) / (n + 1);
142 }
143
144 // Catalan modulo MOD (MOD should be prime for invmod to work reliably)
145 inline i64 catalan_mod(int n, i64 mod = MOD) {
146     if (n < 0)
147         return 0;
148     i64 c = nCr_mod(2 * n, n, mod);
149     i64 inv = invmod(n + 1, mod);
150     if (inv == -1) // no inverse
151         return -1;
152     return mulmod(c, inv, mod);
153 }
```

Listing 20: BinomialCoefficients.cpp

## 6 Strings

### 6.1 Hashing

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 using i64 = long long;
5 using u64 = unsigned long long;
6 constexpr int MOD = 1e9 + 7;
7
8 struct StringHash {
9     vector<u64> hashed, pwrs;
10    u64 MOD_VAL;
11    u64 BASE;
12
13    StringHash(const string &s, u64 base = 257, u64 mod = MOD)
14        : MOD_VAL(mod), BASE(base) {
15        int n = s.length();
16        hashed.resize(n + 1, 0);
17        pwrs.resize(n + 1, 0);
18
19        pwrs[0] = 1;
20        for (int i = 1; i <= n; i++) {
21            pwrs[i] = (pwrs[i - 1] * BASE) % MOD_VAL;
22        }
23
24        for (int i = 0; i < n; i++) {
25            hashed[i + 1] = (hashed[i] * BASE + s[i]) % MOD_VAL;
26        }
27    }
28
29    u64 getHash(int l, int r) {
30        u64 hash = (hashed[r + 1] - (hashed[l] * pwrs[r - l + 1] % MOD_VAL) + MOD_VAL) %
31        MOD_VAL;
```

```

31         return hash;
32     }
33 };
34
35 struct DoubleHash {
36     StringHash hash1, hash2;
37
38     DoubleHash(const string &s)
39         : hash1(s, 257, 1e9 + 7), hash2(s, 353, 1e9 + 9) {}
40
41     bool areEqual(int l1, int r1, int l2, int r2) {
42         if (r1 - l1 != r2 - l2) return false;
43         return hash1.getHash(l1, r1) == hash2.getHash(l2, r2) && hash1.getHash(l1, r1) ==
44             hash2.getHash(l2, r2);
45     }
46
47     bool areEqualStrict(int l1, int r1, int l2, int r2) {
48         if (r1 - l1 != r2 - l2) return false;
49         return hash1.getHash(l1, r1) == hash1.getHash(l2, r2) && hash2.getHash(l1, r1) ==
50             hash2.getHash(l2, r2);
51     }
52 };

```

Listing 21: Hashing.cpp

## 6.2 KMP

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 vector<int> prefix_function(string s) {
5     int n = (int)s.length();
6     vector<int> pi(n);
7     for (int i = 1; i < n; i++) {
8         int j = pi[i-1];
9         while (j > 0 && s[i] != s[j])
10            j = pi[j-1];
11         if (s[i] == s[j])
12             j++;
13         pi[i] = j;
14     }
15     return pi;
16 }
17
18 // Busqueda de patron P en texto T
19 vector<int> kmp_search(const string &P, const string &T) {
20     string s = P + "#" + T;
21     vector<int> pi = prefix_function(s);
22     vector<int> matches;
23     int m = P.length();
24     for (int i = m + 1; i < s.length(); i++) {
25         if (pi[i] == m) {
26             matches.push_back(i - 2 * m); // posicion en T
27         }
28     }
29     return matches;
30 }

```

Listing 22: KMP.cpp

## 6.3 Manacher

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 // manachers finds all palindromic substrings in O(n) time
5 vector<int> manacher_odd(string s) {
6     int n = s.size();
7     s = "$" + s + "^";

```

```

8     vector<int> p(n + 2);
9     int l = 0, r = 1;
10    for(int i = 1; i <= n; i++) {
11        p[i] = min(r - i, p[l + (r - i)]);
12        while(s[i - p[i]] == s[i + p[i]]) {
13            p[i]++;
14        }
15        if(i + p[i] > r) {
16            l = i - p[i], r = i + p[i];
17        }
18    }
19    return vector<int>(begin(p) + 1, end(p) - 1);
20}
21
22vector<int> manacher(string s) {
23    string t;
24    for(auto c: s) {
25        t += string("#") + c;
26    }
27    auto res = manacher_odd(t + "#");
28    return vector<int>(begin(res) + 1, end(res) - 1);
29}

```

Listing 23: Manacher.cpp

## 6.4 Aho-Corasick - Trie

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int K = 26;
5
6 struct Vertex {
7     int next[K];
8     bool output = false;
9     int p = -1;
10    char pch;
11    int link = -1;
12    int go[K];
13
14    Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
15        fill(begin(next), end(next), -1);
16        fill(begin(go), end(go), -1);
17    }
18};
19
20vector<Vertex> t(1);
21
22void add_string(string const& s) {
23    int v = 0;
24    for (char ch : s) {
25        int c = ch - 'a';
26        if (t[v].next[c] == -1) {
27            t[v].next[c] = t.size();
28            t.emplace_back(v, ch);
29        }
30        v = t[v].next[c];
31    }
32    t[v].output = true;
33}
34
35int go(int v, char ch);
36
37int get_link(int v) {
38    if (t[v].link == -1) {
39        if (v == 0 || t[v].p == 0)
40            t[v].link = 0;
41        else
42            t[v].link = go(get_link(t[v].p), t[v].pch);
43    }
44    return t[v].link;

```

```

45 }
46
47 int go(int v, char ch) {
48     int c = ch - 'a';
49     if (t[v].go[c] == -1) {
50         if (t[v].next[c] != -1)
51             t[v].go[c] = t[v].next[c];
52         else
53             t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
54     }
55     return t[v].go[c];
56 }
```

Listing 24: AhoCorasick.cpp

## 6.5 Suffix Array + LCP Array

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 vector<int> sort_cyclic_shifts(string const& s) {
5     int n = s.size();
6     const int alphabet = 256;
7
8     vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
9     for (int i = 0; i < n; i++)
10        cnt[s[i]]++;
11    for (int i = 1; i < alphabet; i++)
12        cnt[i] += cnt[i-1];
13    for (int i = 0; i < n; i++)
14        p[~cnt[s[i]]] = i;
15    c[p[0]] = 0;
16    int classes = 1;
17    for (int i = 1; i < n; i++) {
18        if (s[p[i]] != s[p[i-1]])
19            classes++;
20        c[p[i]] = classes - 1;
21    }
22
23    vector<int> pn(n), cn(n);
24    for (int h = 0; (1 << h) < n; ++h) {
25        for (int i = 0; i < n; i++) {
26            pn[i] = p[i] - (1 << h);
27            if (pn[i] < 0)
28                pn[i] += n;
29        }
30        fill(cnt.begin(), cnt.begin() + classes, 0);
31        for (int i = 0; i < n; i++)
32            cnt[c[pn[i]]]++;
33        for (int i = 1; i < classes; i++)
34            cnt[i] += cnt[i-1];
35        for (int i = n-1; i >= 0; i--)
36            p[~cnt[c[pn[i]]]] = pn[i];
37        cn[p[0]] = 0;
38        classes = 1;
39        for (int i = 1; i < n; i++) {
40            pair<int, int> cur = {c[p[i]], c[(p[i] + (1 << h)) % n]};
41            pair<int, int> prev = {c[p[i-1]], c[(p[i-1] + (1 << h)) % n]};
42            if (cur != prev)
43                ++classes;
44            cn[p[i]] = classes - 1;
45        }
46        c.swap(cn);
47    }
48    return p;
49 }
50
51 vector<int> suffix_array_construction(string s) {
52     s += "$";
53     vector<int> sorted_shifts = sort_cyclic_shifts(s);
54     sorted_shifts.erase(sorted_shifts.begin());
```

```

55     return sorted_shifts;
56 }
57
58 vector<int> lcp_construction(string const& s, vector<int> const& p) {
59     int n = s.size();
60     vector<int> rank(n, 0);
61     for (int i = 0; i < n; i++)
62         rank[p[i]] = i;
63
64     int k = 0;
65     vector<int> lcp(n-1, 0);
66     for (int i = 0; i < n; i++) {
67         if (rank[i] == n - 1) {
68             k = 0;
69             continue;
70         }
71         int j = p[rank[i] + 1];
72         while (i + k < n && j + k < n && s[i+k] == s[j+k])
73             k++;
74         lcp[rank[i]] = k;
75         if (k)
76             k--;
77     }
78     return lcp;
79 }
```

Listing 25: SuffixArray.cpp

## 7 Geometry

### 7.1 Convex Hull

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct pt {
5
6     double x, y;
7     bool operator == (pt const& t) const {
8         return x == t.x && y == t.y;
9     }
10 };
11
12 int orientation(pt a, pt b, pt c) {
13     double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);
14     if (v < 0) return -1; // clockwise
15     if (v > 0) return +1; // counter-clockwise
16     return 0;
17 }
18
19 bool cw(pt a, pt b, pt c, bool include_collinear) {
20     int o = orientation(a, b, c);
21     return o < 0 || (include_collinear && o == 0);
22 }
23
24 bool collinear(pt a, pt b, pt c) { return orientation(a, b, c) == 0; }
25
26 void convex_hull(vector<pt>& a, bool include_collinear = false) {
27     pt p0 = *min_element(a.begin(), a.end(), [] (pt a, pt b) {
28         return make_pair(a.y, a.x) < make_pair(b.y, b.x);
29     });
30     sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
31         int o = orientation(p0, a, b);
32         if (o == 0)
33             return (p0.x-a.x)*(p0.x-a.x) + (p0.y-a.y)*(p0.y-a.y)
34             < (p0.x-b.x)*(p0.x-b.x) + (p0.y-b.y)*(p0.y-b.y);
35         return o < 0;
36     });
37     if (include_collinear) {
38         int i = (int)a.size()-1;
39         while (i >= 0 && collinear(p0, a[i], a.back())) i--;
40     }
41 }
```

```

39     reverse(a.begin() + i + 1, a.end());
40 }
41
42 vector<pt> st;
43 for (int i = 0; i < (int)a.size(); i++) {
44     while (st.size() > 1 && !cw(st[st.size() - 2], st.back(), a[i], include_collinear))
45         st.pop_back();
46     st.push_back(a[i]);
47 }
48
49 if (include_collinear == false && st.size() == 2 && st[0] == st[1])
50     st.pop_back();
51
52 a = st;
53 }
```

Listing 26: ConvexHull.cpp

## 7.2 Closest Pair

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 using i64 = long long;
5 using ld = long double;
6
7
8 struct pt {
9     i64 x, y;
10    pt() {}
11    pt(i64 x_, i64 y_) : x(x_), y(y_) {}
12    void read() {
13        cin >> x >> y;
14    }
15};
16
17 bool operator==(const pt& a, const pt& b) {
18     return a.x == b.x and a.y == b.y;
19 }
20
21
22 struct CustomHashPoint {
23     size_t operator()(const pt& p) const {
24         static const uint64_t C = chrono::steady_clock::now().time_since_epoch().count();
25         return C ^ ((p.x << 32) ^ p.y);
26     }
27 };
28
29
30 i64 dist2(pt a, pt b) {
31     i64 dx = a.x - b.x;
32     i64 dy = a.y - b.y;
33     return dx*dx + dy*dy;
34 }
35
36
37 pair<int,int> closest_pair_of_points(vector<pt> P) {
38     int n = int(P.size());
39     assert(n >= 2);
40
41     // if there is a duplicated point, we have the solution
42     unordered_map<pt,int,CustomHashPoint> previous;
43     for (int i = 0; i < int(P.size()); ++i) {
44         auto it = previous.find(P[i]);
45         if (it != previous.end()) {
46             return {it->second, i};
47         }
48         previous[P[i]] = i;
49     }
50
51     unordered_map<pt,vector<int>,CustomHashPoint> grid;
```

```

52     grid.reserve(n);
53
54     mt19937 rd(chrono::system_clock::now().time_since_epoch().count());
55     uniform_int_distribution<int> dis(0, n-1);
56
57     i64 d2 = dist2(P[0], P[1]);
58     pair<int,int> closest = {0, 1};
59
60     auto candidate_closest = [&](int i, int j) -> void {
61         i64 ab2 = dist2(P[i], P[j]);
62         if (ab2 < d2) {
63             d2 = ab2;
64             closest = {i, j};
65         }
66     };
67
68     for (int i = 0; i < n; ++i) {
69         int j = dis(rd);
70         int k = dis(rd);
71         while (j == k) k = dis(rd);
72         candidate_closest(j, k);
73     }
74
75     i64 d = i64( sqrt(1d(d2)) + 1 );
76
77     for (int i = 0; i < n; ++i) {
78         grid[{P[i].x/d, P[i].y/d}].push_back(i);
79     }
80
81     // same block
82     for (const auto& it : grid) {
83         int k = int(it.second.size());
84         for (int i = 0; i < k; ++i) {
85             for (int j = i+1; j < k; ++j) {
86                 candidate_closest(it.second[i], it.second[j]);
87             }
88         }
89     }
90
91     // adjacent blocks
92     for (const auto& it : grid) {
93         auto coord = it.first;
94         for (int dx = 0; dx <= 1; ++dx) {
95             for (int dy = -1; dy <= 1; ++dy) {
96                 if (dx == 0 and dy == 0) continue;
97                 pt neighbour = pt(
98                     coord.x + dx,
99                     coord.y + dy
100                );
101                for (int i : it.second) {
102                    if (not grid.count(neighbour)) continue;
103                    for (int j : grid.at(neighbour)) {
104                        candidate_closest(i, j);
105                    }
106                }
107            }
108        }
109    }
110
111    return closest;
112}

```

Listing 27: ClosestPair.cpp

## 8 DP

### 8.1 LIS - Longest Increasing Subsequence

```

1 #include <bits/stdc++.h>
2 using namespace std;

```

```

3 // longest increasing subsequence in O(n log n)
4 int lis(vector<int> const& a) {
5     int n = a.size();
6     const int INF = 1e9;
7     vector<int> d(n+1, INF);
8     d[0] = -INF;
9
10    for (int i = 0; i < n; i++) {
11        int l = upper_bound(d.begin(), d.end(), a[i]) - d.begin();
12        if (d[l-1] < a[i] && a[i] < d[l])
13            d[l] = a[i];
14    }
15
16    int ans = 0;
17    for (int l = 0; l <= n; l++) {
18        if (d[l] < INF)
19            ans = l;
20    }
21    return ans;
22}

```

Listing 28: LIS.cpp

## 8.2 DP Divide and Conquer

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int m, n;
5 vector<long long> dp_before, dp_cur;
6
7 long long C(int i, int j);
8
9 // compute dp_cur[l], ... dp_cur[r] (inclusive)
10 void compute(int l, int r, int optl, int optr) {
11     if (l > r)
12         return;
13
14     int mid = (l + r) >> 1;
15     pair<long long, int> best = {LLONG_MAX, -1};
16
17     for (int k = optl; k <= min(mid, optr); k++) {
18         best = min(best, {(k ? dp_before[k - 1] : 0) + C(k, mid), k});
19     }
20
21     dp_cur[mid] = best.first;
22     int opt = best.second;
23
24     compute(l, mid - 1, optl, opt);
25     compute(mid + 1, r, opt, optr);
26 }
27
28 long long solve() {
29     dp_before.assign(n, 0);
30     dp_cur.assign(n, 0);
31
32     for (int i = 0; i < n; i++)
33         dp_before[i] = C(0, i);
34
35     for (int i = 1; i < m; i++) {
36         compute(0, n - 1, 0, n - 1);
37         dp_before = dp_cur;
38     }
39
40     return dp_before[n - 1];
41 }

```

Listing 29: DPDivideAndConquer.cpp

## 9 Bitmasking

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 bool is_set(unsigned int number, int x) {
5     return (number >> x) & 1;
6 }
7
8 int set_bit(int number, int x) {
9     return number | (1 << x);
10}
11
12 int clear_bit(int number, int x) {
13     return number & ~(1 << x);
14 }
15
16 int toggle_bit(int number, int x) {
17     return number ^ (1 << x);
18 }
19
20 int modify_bit(int number, int x, bool val) {
21     return (number & ~(1 << x)) | (val << x);
22 }
23
24 bool isDivisibleByPowerOf2(int n, int k) {
25     int powerOf2 = 1 << k;
26     return (n & (powerOf2 - 1)) == 0;
27 }
28
29 bool isPowerOfTwo(unsigned int n) {
30     return n && !(n & (n - 1));
31 }
32
33 int nextPowerOfTwo(int n) {
34     n--;
35     n |= n >> 1;
36     n |= n >> 2;
37     n |= n >> 4;
38     n |= n >> 8;
39     n |= n >> 16;
40     return n + 1;
41 }
42
43 // Contar bits (g++ >= 20)
44 long long countSetBits(unsigned int n) {
45     long long count = 0;
46     while (n > 0) {
47         int x = std::bit_width(n) - 1;
48         if (x > 0) {
49             count += (long long)x * (1LL << (x - 1));
50         }
51         n -= (1U << x);
52         count += n + 1;
53     }
54     return count;
55 }
56
57 // Contar bits (g++ < 20)
58 long long countSetBits(unsigned int n) {
59     long long count = 0;
60     while (n > 0) {
61         int x = static_cast<int>(std::log2(n));
62         if (x > 0) {
63             count += (long long)x * (1LL << (x - 1));
64         }
65         n -= (1U << x);
66         count += n + 1;
67     }
68     return count;
69 }
70
71 int countSetBitsBuiltIn(int n) {
```

```

72     return __builtin_popcount(n);
73 }
74
75 int countSetBitsLong(long long n) {
76     return __builtin_popcountll(n);
77 }
78
79 // Posición de bits
80 int lowestSetBit(int n) {
81     return __builtin_ffs(n) - 1; // First set bit (0-indexed)
82 }
83
84 int highestSetBit(int n) {
85     return 31 - __builtin_clz(n); // Count leading zeros
86 }
87
88 int trailingZeros(int n) {
89     return __builtin_ctz(n);
90 }
91
92 int leadingZeros(int n) {
93     return __builtin_clz(n);
94 }
95
96 // Operaciones con máscaras de bits
97 int getAllSetBits(int n) {
98     return (1 << n) - 1; // Máscara con los primeros n bits en 1
99 }
100
101 int getRangeMask(int l, int r) {
102     // Máscara con bits de l a r en 1 (0-indexed)
103     return ((1 << (r - l + 1)) - 1) << l;
104 }
105
106 int clearRightmostSetBit(int n) {
107     return n & (n - 1);
108 }
109
110 int isolateRightmostSetBit(int n) {
111     return n & (-n);
112 }
113
114 int isolateRightmostZeroBit(int n) {
115     return ~n & (n + 1);
116 }
117
118 int setRightmostZeroBit(int n) {
119     return n | (n + 1);
120 }
121
122 // Iterar sobre subconjuntos
123 void iterateSubsets(int mask) {
124     // Iterar sobre todos los subconjuntos de mask
125     for (int s = mask; s > 0; s = (s - 1) & mask) {
126         // Procesar subconjunto s
127     }
128 }
129
130 void iterateAllMasks(int n) {
131     // Iterar sobre todas las máscaras de n bits
132     for (int mask = 0; mask < (1 << n); mask++) {
133         // Procesar mask
134     }
135 }
136
137 void iterateSetBits(int mask) {
138     // Iterar sobre las posiciones de los bits en 1
139     while (mask) {
140         int pos = __builtin_ctz(mask);
141         // Procesar posición pos
142         mask &= mask - 1; // Eliminar el bit más bajo
143     }
144 }

```

```

145 // Operaciones avanzadas
146 int reverseBits(unsigned int n) {
147     n = ((n >> 1) & 0x55555555) | ((n & 0x55555555) << 1);
148     n = ((n >> 2) & 0x33333333) | ((n & 0x33333333) << 2);
149     n = ((n >> 4) & 0x0F0F0F0F) | ((n & 0x0F0F0F0F) << 4);
150     n = ((n >> 8) & 0x00FF00FF) | ((n & 0x00FF00FF) << 8);
151     n = (n >> 16) | (n << 16);
152     return n;
153 }
154
155 int swapBits(int n, int i, int j) {
156     // Intercambiar bits en posiciones i y j
157     if (((n >> i) & 1) != ((n >> j) & 1)) {
158         n ^= (1 << i) | (1 << j);
159     }
160     return n;
161 }
162
163 bool parityBit(unsigned int n) {
164     // true si número impar de bits en 1
165     return __builtin parity(n);
166 }
167
168 // Operaciones con máscaras de bits para DP y combinatoria
169 int addElement(int mask, int pos) {
170     return mask | (1 << pos);
171 }
172
173 int removeElement(int mask, int pos) {
174     return mask & ~(1 << pos);
175 }
176
177 bool hasElement(int mask, int pos) {
178     return (mask >> pos) & 1;
179 }
180
181 int maskSize(int mask) {
182     return __builtin_popcount(mask);
183 }
184
185
186 int complementMask(int mask, int n) {
187     // Complemento de mask con respecto a n bits
188     return ((1 << n) - 1) ^ mask;
189 }
190
191 int unionMask(int a, int b) {
192     return a | b;
193 }
194
195 int intersectionMask(int a, int b) {
196     return a & b;
197 }
198
199 int differenceMask(int a, int b) {
200     return a & ~b;
201 }
202
203 bool isSubset(int subset, int mask) {
204     return (subset & mask) == subset;
205 }
206
207 // XOR útil
208 int xorRange(int l, int r) {
209     // XOR de todos los números de l a r
210     auto xor_till = [] (int n) {
211         int mod = n % 4;
212         if (mod == 0) return n;
213         if (mod == 1) return 1;
214         if (mod == 2) return n + 1;
215         return 0;
216     };
217     return xor_till(r) ^ xor_till(l - 1);

```

```
218 }
219
220 int findXorPair(int arr[], int n) {
221     // XOR de todos los elementos
222     int xor_all = 0;
223     for (int i = 0; i < n; i++) {
224         xor_all ^= arr[i];
225     }
226     return xor_all;
227 }
228
229 // Máximo XOR de dos números en un rango
230 int maxXOR(int l, int r) {
231     int xor_val = l ^ r;
232     int msb = highestSetBit(xor_val);
233     return (1 << (msb + 1)) - 1;
234 }
```

Listing 30: Bitwise.cpp