

# A3 Simulative Engineering - Learning paper is NOT allowed in exam

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## 1 Definitions

**Simulation** is the imitation of the operation of a real world process or system over time (e.g. via MATLAB/Simulink)

**Hardware in the loop (HiL)** means testing of software in combination with an existing hardware component OR: HiL is a technique for testing a embedded system by simulating the real environment around the embedded system. (Abb. 1)

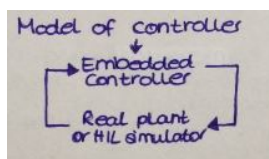


Abbildung 1: Hardware in the loop (HiL)

**Software in the loop (SiL)** is a simulation technique for software models only with a simulated hardware and not with a realworld existing hardware OR SiL is a technique for testing software by simulating the target hardware (Abb. 2).

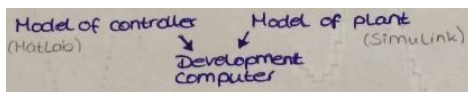


Abbildung 2: Software in the loop (SiL)

**Model** is an abstraction from realworld objects; mostly easier to display.

**Fourier-Transform** transforms time domain based signals into frequendy domain based signals; needed for calculation of signals

**Time discrete** means that a signal is only defined at specifiv time values (Abb. 3).

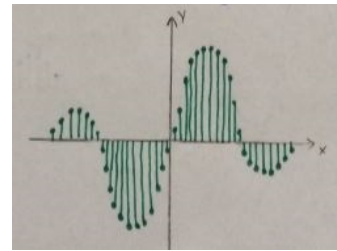


Abbildung 3: Time discrete signal: A y-value exists only for specific x-values.

**Time continuos** means that a signal is defined for the whole time or for an specific interval (Abb. 4).

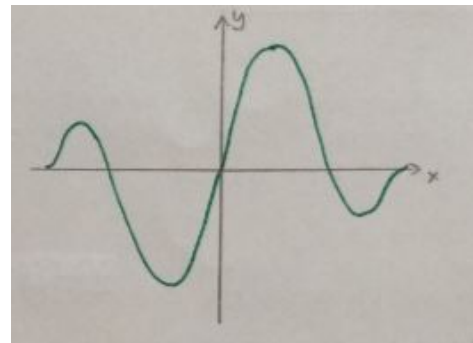


Abbildung 4: Time continuos signal: A y-value exists for every x-value (in the intervall).

**Discrete values** A signal can be measured in time ranges (time continuos) (Abb. 5) or at specific time values (time discrete)(Abb. 6). Each y-value in one time range has got the same value. Discrete values can be counted.

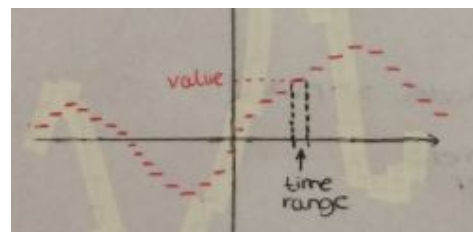


Abbildung 5: Continuos X, discrete Y

**Continuos values** can be measured and can take any value ((Abb. 7) and (Abb. 8))

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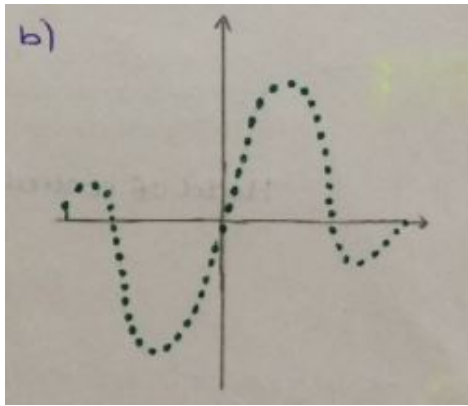


Abbildung 6: Discrete X, discrete Y

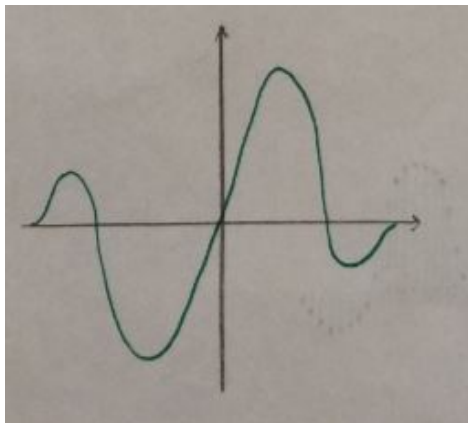


Abbildung 7: Continuous X, discrete Y

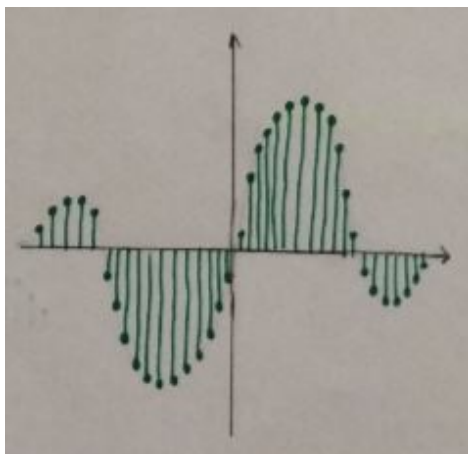


Abbildung 8: Discrete X, continuous Y

**Discrete Fourier Transform (DFT)** is a stand alone definition for time discrete signals of limited duration besides the Fourier Transform (Abb. 9).

**Dirac distribution**  $\delta(t)$  is not function, but a distribution. It cannot be defined directly, but has to

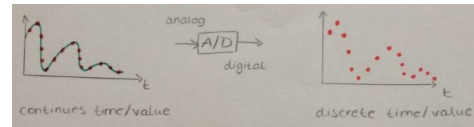


Abbildung 9: images/Discrete Fourier Transform (DFT)

be described indirectly e.g. by integration.

$$1. \delta(t) = 0 \text{ for all } t \neq 0 \text{ and } \int_{-\infty}^{+\infty} \delta(t) dt = 1$$

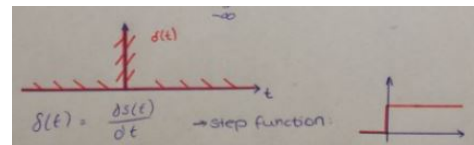


Abbildung 10: Dirac

$$2. \text{Sifting property (similar to window function)} \int_{-\infty}^{+\infty} f(t) \cdot \delta(t) dt = f(0)$$

$$3. \delta(t) = \lim_{\varepsilon \rightarrow 0} \frac{1}{2\varepsilon} [s(t+\varepsilon) - s(t-\varepsilon)]; \varepsilon > 0$$

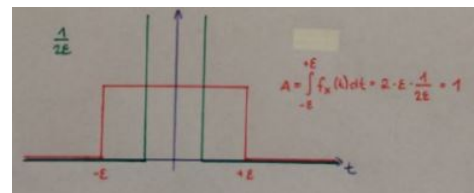


Abbildung 11: Dirac2

**Dirac comb**  $\text{III}_T$  is a periodic function of the Dirac distribution. The ideal sampling can be described by Dirac distributions located with distances  $T_s$  which results in a spectrum of Dirac distributions having the distance  $\frac{1}{T_s}$  (Abb. 12).

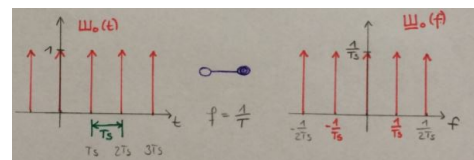


Abbildung 12: Dirac Comb

**Algorithm** is a self-contained step by step set of operations to be performed in order to get a solu-

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tion. Algorithms perform calculations, data processing and/or automated reasoning tasks.

**DFT/FFT** The Fast Fourier Transform (FFT) is a special algorithm for calculating the DFT.

**Sequence** is a ordered collection of objects in which repetitions are allowed. The number of elements is called the length  $n$  of a sequence and can be infinite. The position of the elements is called index. E.g. prim numbers until 41:

prim numbers	2	3	5	7	...	37	41
	↓	↓	↓	↓		↓	↓
index	1	2	3	4	...	12	13

The Length of this sequence is  $n = 13$ .

**Sampling** converts a continuous time signal into a discrete time signal. Sampling is done by a multiplication of the signal  $u(t)$  with the dirac comb. A multiplication in the time domain results in a convolution in frequency domain. It is performed over a limited time.

**Time domain and frequency domain** The function values of a signal in time domain depend on time values. In the frequency domain the function values depend on frequency values.

$$f(t) \xrightarrow{\bullet} F(f) \text{ with } f = \frac{1}{t}$$

**Periodic function** repeats itself after a period of time. Examples:  $\sin(x)$ ,  $\cos(x)$

**Limited function** is only defined for a specific time range. A limited function in time domain contains an unlimited spectrum of frequencies in frequency domain.

**Convolution** is a mathematical operation on two functions, similar to cross-correlation (system theory). The solution is a third function being the first function modified by the second one. Multiplication in time domain  $\rightarrow$  Convolution in frequency domain.

**Frequency spectrum** is a composition of different frequencies.

**Amplitude spectrum** is the absolute value of a frequency spectrum OR is a composition of different amplitudes.

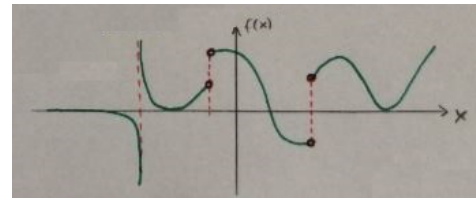


Abbildung 13: Example of a function with discontinuities

different amplitudes.

**Discontinuities** appear where a function is not continuous (Abb. 13).

**Sifting property of Dirac distribution** means that the function value  $f(t = 0)$  can be extracted with the multiplication of the function with the Dirac distribution.

$$\int_{-\infty}^{+\infty} f(t) \cdot \delta(t) dt = f(0) \text{ because of } \delta(t) = \begin{cases} 0, & t \neq 0 \\ \infty, & t = 0 \end{cases} \text{ and } \int_{-\infty}^{+\infty} \delta(t) dt = 1$$

**Window function** is a rectangular function used as a window for calculating a DFT. When a function is multiplied by a window function, the product is zero-valued outside of the window's interval; all that is left is the part where they overlap, the "view through the window" (Abb. 14).

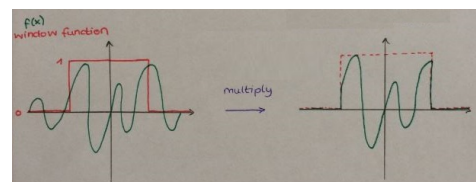


Abbildung 14: Use of a window function

**Zero padding** adds zeros to the end of signals to compress the signal (Abb. 15).

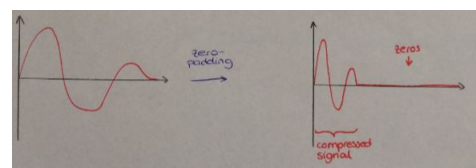


Abbildung 15: Zero padding

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## 2 ODEs

## 3 DFT

### 2.1 How to solve an ODE?

An ODE of n-th order is given. Change it to n ODEs of 1st order via substitution. Now you can use MATLAB to solve it.

Example:

$$y^{(3)} + a_2 y'' + a_1 y' + a_0 y = b$$

Substitution	Derivation
$y_1 = y$	$y'_1 = y' = y_2$
$y_2 = y'$	$y'_2 = y'' = y_3$
$y_3 = y''$	$y'_3 = y^{(3)} = b - a_2 y_3 - a_1 y_2 - a_0 y_1$

### 2.2 How to get $G(s)$ ?

Transform the ODE from the time into the frequency domain.

Derivatives	Integrals
$y(t) \circ \bullet Y(s)$	$\int y(t) dt \circ \bullet \frac{1}{s} Y(s)$
$y'(t) \circ \bullet s Y(s)$	$\int \int y(t) dt \circ \bullet \frac{1}{s^2} Y(s)$
$y''(t) \circ \bullet s^2 Y(s)$	$\int \int \int y(t) dt \circ \bullet \frac{1}{s^3} Y(s)$
and so on...	and so on...

Exclude the output signal and calculate  $G(s) = \frac{\text{output}}{\text{input}}$ .

Example:

$$y^{(3)} + a_2 y'' + a_1 y' + a_0 y = b$$

with  $b$  as input signal and  $y$  as output signal.

Laplace Transform:

$$s^3 Y(s) + s^2 a_2 Y(s) + s a_1 Y(s) + a_0 Y(s) = B(s)$$

$$Y(s)(s^3 + s^2 a_2 + s a_1 + a_0) = B(s)$$

$$G(s) = \frac{Y(s)}{B(s)} = \frac{1}{s^3 + s^2 a_2 + s a_1 + a_0}$$

If the input signal is 0, then integrate and solve the equation for the output variable.