

1.5 MOMENT and MOMENTUM

Moment of a force

Moment of a force This is the Product of force and its Perpendicular distance from the Pivot.

Moment = Force X distance

Moment= $F \times d$

Its units are Nm (Newton meter)

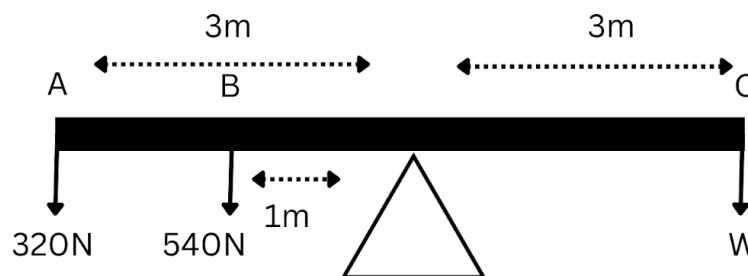
The law of moments (Law of the lever) states that:

When a body is in equilibrium, the sum of the clockwise moments About any point equals the sum of anticlockwise moments about the same point. There is no resultant moment on an object in equilibrium.

Clockwise moment = anticlockwise moment

$$F_1 \times d_1 = F_2 \times d_2$$

Example: The seesaw balances when Shani of weight 320 N is at A. Tom of weight 540N is at B and Harry of weight W is at C. Find W.



Clockwise moment:

Moment= $F \times d$

Moment= $3 \times W = 3W \text{ Nm}$

Anticlockwise moment:

Moment = $(F \times d) + (F \times d) = (540 \times 1) + (320 \times 3) = 540 + 960$

Moment= 1500 Nm

Clockwise moment = Anticlockwise moment

$$3W = 1500$$

$$W = 500 \text{ N}$$

Note: The further the distance, the lesser the force needed to be used. E.g. the distance between the door handle and the hinge is far apart so that it does not require a lot of energy to open the door.

Conditions for equilibrium:

- The sum of forces in one direction equals the forces in the opposite direction.
- The law of the moment must apply. When there is no resultant force and no resultant moment, an object is in equilibrium.

Equilibrium: When there is no resultant force and resultant moment.

Momentum

Momentum is the product of the mass of a body and its velocity.

It is measured in **Kilogram meter Per second (kg m/s)**

Momentum = mass x velocity

$$P = mv$$

$$\Delta P = \Delta(mv)$$

P is rho

Momentum is a *vector quantity* and has both magnitude (size) and direction

The Conservation of Momentum Principle

In a closed system, the total momentum before an event like a Collision is the same as the total momentum after the event

To find the Force used to change the momentum:

$$F = \frac{(mv - mu)}{t}$$

mv is the Final Momentum
mu is the Initial Momentum
t is Time

Example 1:

Ball A has a mass of 4500 kg and its velocity is 12m/s On the other hand ball B has a mass of 1200 kg and its velocity is 20m/s. Calculate their momentum Separately, and their velocity after collision.

Ball A is moving to the right
Ball B is moving to the left.

Ball A:

$$P=mv = 4500 \times 12 = 54,000 \text{ Kg m/s}$$

$$P= + 54,000 \text{ kg m/s}$$

Ball B:

$$P=mv= 1200 \times 20 = 24000 \text{ kgm/s}$$

$$P= - 24,000 \text{ kg m/s}$$

Find their momentum

Ball A + Ball B momentum.

$$54,000 + - 24,000$$

$$P=+30,000 \text{ kg m/s}$$

$$V= p/m$$

Find their total mass:

$$m_1 + m_2 = m_{\text{total}}$$

$$4500 + 1200 = 5700 \text{ kg}$$

$$V= 30,000 \text{ kg m/s} / 5700 \text{ kg}$$

$$V= 5.3 \text{ m/s after collision.}$$

Note: If the object is moving to the right, it has positive momentum and if it is moving to the left, it has negative momentum.

Example 2:

Calculate the force required to accelerate a 750g ball from rest to 18m/s in 0.25s.

$$F = \frac{(mv - mu)}{t}$$

$$V = 18 \text{ m/s}$$

$$m = 750 \text{ g or } 0.75 \text{ kg}$$

$$t = 0.25 \text{ s}$$

$$F = \frac{(0.75 \times 18) - (0.75 \times 0)}{0.25}$$

$$F = \frac{13.5 - 0}{0.25}$$

$$F = 54 \text{ N}$$

Impulse

Impulse is the product of force and time.

$$\text{Impulse} = \text{Force} \times \text{time}$$

$$I = F \times t$$

It is measured in **Newton Seconds (Ns)**

$$\text{Impulse} = \text{Change in Momentum}$$

$$\text{Force} \times \text{Time} = \text{Mass} \times \text{Velocity}$$

A force acting on an object for a given time is equal to the mass times the change in velocity of the Object.

Force is the rate at which the momentum of an object changes.

$$\text{Force} = \frac{\text{Change in Momentum}}{\text{Change in Time}}$$

$$\text{Force} = \frac{\text{Mass} \times \text{Velocity}}{\text{Change in Time}}$$

$$\text{Acceleration} = \frac{\text{Change in Velocity}}{\text{Change in Time}}$$

$$\text{Force} = m \times \frac{\text{Change in Velocity}}{\text{Change in Time}}$$

$$\text{Force} = \text{mass} \times \text{acceleration}$$