# **Computer Vision**

# **Jacobs University Bremen**

## Fall 2022

## **Homework 4**

This notebook includes both coding and written questions. Please hand in this notebook file with all the outputs and your answers to the written questions.

This assignment covers Canny edge detector and Hough transform.

In [20]:

```
# Setup
import numpy as np
import matplotlib.pyplot as plt
import matplotlib.image as mpimg
from time import time
from skimage import io

from __future__ import print_function

%matplotlib inline
plt.rcParams['figure.figsize'] = (15.0, 12.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading extenrnal modules
%load_ext autoreload
%autoreload 2
```

The autoreload extension is already loaded. To reload it, use:  $\mbox{\ensuremath{\$}}\mbox{reload}\mbox{\ensuremath{$}}\mbox{\ensuremath{}}\mbox{\ensuremath{$}}\mbox{\ensuremath{$}}\mbox{\ensuremath{$}}\mbox{\ensuremath{}}\mbox{\$ 

# Part 1: Canny Edge Detector (75 points)

In this part, you are going to implement a Canny edge detector. The Canny edge detection algorithm can be broken down in to five steps, as outlined:

- 1. Smoothing
- 2. Finding gradients
- 3. Non-maximum suppression
- 4. Double thresholding
- 5. Edge tracking by hysterisis

### 1.1 Smoothing (10 points)

### **Implementation (5 points)**

We first smooth the input image by convolving it with a Gaussian kernel. The equation for a Gaussian kernel of size (2k+1) is given by:

$$imes (2k+1)$$

$$h_{ij} = \frac{1}{2\pi\sigma^2} \exp\left[(i-k)^2\right]$$

```
\Big(-rac{+(j-k)^2}{2\sigma^2}\Big), \ 0 \leq i,j < 2k+1
```

Implement gaussian kernel in edge.py and run the code below.

```
In [22]:
```

```
from edge import conv, gaussian_kernel

# Define 3x3 Gaussian kernel with std = 1
kernel = gaussian_kernel(3, 1)
kernel_test = np.array(
    [[ 0.05854983,  0.09653235,  0.05854983],
    [ 0.09653235,  0.15915494,  0.09653235],
    [ 0.05854983,  0.09653235,  0.05854983]]
)

# Test Gaussian kernel
if not np.allclose(kernel, kernel_test):
    print('Incorrect values! Please check your implementation.')
```

#### In [12]:

```
# Test with different kernel size and sigma
kernel size = 5
sigma = 1.4
# Load image
img = io.imread('iguana.png', as gray=True)
# Define 5x5 Gaussian kernel with std = sigma
kernel = gaussian kernel(kernel size, sigma)
# Convolve image with kernel to achieve smoothed effect
smoothed = conv(img, kernel)
plt.subplot(1,2,1)
plt.imshow(img)
plt.title('Original image')
plt.axis('off')
plt.subplot(1,2,2)
plt.imshow(smoothed)
plt.title('Smoothed image')
plt.axis('off')
plt.show()
```

Original image



Smoothed image



#### **Question (5 points)**

What is the effect of changing kernel size and sigma?

Your Answer: Write your solution in this markdown cell.

Increasing sigma will affect the image by making it not as clear as the original image, also increasing the kernel size will make the image more blurry compared to a smaller kernel and it will lose its original shape. We can see that above.

### 1.2 Finding gradients (15 points)

The gradient of a 2D scalar function  $I:\mathbb{R}^2 \to \mathbb{R}$  in Cartesian coordinate is defined by:

$$abla I(x,y) = \left[ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right],$$

where

$$egin{aligned} rac{\partial I(x,y)}{\partial x} = \ & I(x+\Delta x,y) & I(x,y+\Delta y) \ & \lim_{\Delta x o 0} rac{-I(x,y)}{\Delta x} rac{\partial I(x,y)}{\partial y} = \lim_{\Delta y o 0} rac{-I(x,y)}{\Delta y}. \end{aligned}$$

In case of images, we can approximate the partial derivatives by taking differences at one pixel intervals:

$$egin{aligned} rac{\partial I(x,y)}{\partial x} \ & I(x+1,y) \ pprox rac{-I(x-1,y)}{2} \ & rac{\partial I(x,y)}{\partial y} \ & I(x,y+1) \ pprox rac{-I(x,y-1)}{2} \end{aligned}$$

Note that the partial derivatives can be computed by convolving the image  $\ I$  with some appropriate kernels  $D_x$  and  $D_v$ :

$$egin{aligned} rac{\partial I}{\partial x} &pprox I*D_x \ &= G_x \ rac{\partial I}{\partial y} &pprox I*D_y \ &= G_y \end{aligned}$$

### **Implementation (5 points)**

Find the kernels  $D_x$  and  $D_y$  and implement <code>partial\_x</code> and <code>partial\_y</code> using <code>conv</code> defined in <code>edge.py</code> .

-Hint: Remeber that convolution flips the kernel.

```
In [23]:
```

```
from edge import partial_x, partial_y

# Test input
I = np.array(
    [[0, 0, 0],
        [0, 1, 0],
        [0, 0, 0]]
)
```

```
# Expected outputs
I x test = np.array(
    [[ 0, 0, 0],
     [0.5, 0, -0.5],
     [ 0, 0, 0]]
I_y_{test} = np.array(
    [[ 0, 0.5, 0],
    [ 0, 0, 0],
     [0, -0.5, 0]
# Compute partial derivatives
I x = partial x(I)
I_y = partial_y(I)
# Test correctness of partial x and partial y
if not np.all(I_x == I_x_test):
   print('partial_x incorrect')
if not np.all(I_y == I_y_test):
   print('partial y incorrect')
```

partial\_y incorrect

#### In [24]:

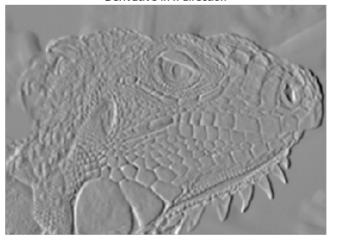
```
# Compute partial derivatives of smoothed image
Gx = partial_x(smoothed)
Gy = partial_y(smoothed)

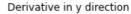
plt.subplot(1,2,1)
plt.imshow(Gx)
plt.title('Derivative in x direction')
plt.axis('off')

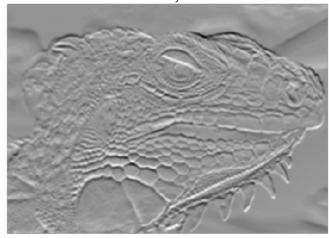
plt.subplot(1,2,2)
plt.imshow(Gy)
plt.title('Derivative in y direction')
plt.axis('off')

plt.axis('off')
```









### **Question (5 points)**

What is the reason for performing smoothing prior to computing the gradients?

Your Answer: Write your solution in this markdown cell.

We perform smoothing prior to computing the gradients to remove first the noise from the image and then we compute the gradients

### **Implementation (5 points)**

Now, we can compute the magnitude and direction of gradient with the two partial derivatives:

$$G = \sqrt{G_x^2 + G_y^2} \ = Arctan \ \left(rac{G_y}{G_x}
ight)$$

Implement gradient in edge.py which takes in an image and outputs G and  $\Theta$ .

```
In [25]:
```

```
from edge import gradient

G, theta = gradient(smoothed)

if not np.all(G >= 0):
    print('Magnitude of gradients should be non-negative.')

if not np.all((theta >= 0) * (theta < 360)):
    print('Direction of gradients should be in range 0 <= theta < 360')

plt.imshow(G)
plt.title('Gradient magnitude')
plt.axis('off')
plt.show()</pre>
```

Gradient magnitude



### 1.3 Non-maximum suppression (15 points)

You should be able to see that the edges extracted from the gradient of the smoothed image are quite thick and blurry. The purpose of this step is to convert the "blurred" edges into "sharp" edges. Basically, this is done by preserving all local maxima in the gradient image and discarding everything else. The algorithm is for each pixel (x,y) in the gradient image:

- 1. Round the gradient direction  $\Theta[y,x]$  to the nearest 45 degrees, corresponding to the use of an 8-connected neighbourhood.
- 2. Compare the edge strength of the current pixel with the edge strength of the pixel in the positive and negative gradient directions. For example, if the gradient direction is south (theta=90), compare with the pixels to the north and south.
- 3. If the edge strength of the current pixel is the largest; preserve the value of the edge strength. If not, suppress (i.e. remove) the value.

Implement non maximum suppression in edge.py.

We provide the correct output and the difference between it and your result for debugging purposes. If you see white spots in the Difference image, you should check your implementation.

```
In [39]:
```

```
from edge import non_maximum_suppression

# Test input
g = np.array(
    [[0.4, 0.5, 0.6],
    [0.3, 0.5, 0.7],
    [0.4, 0.5, 0.6]]
)

# Print out non-maximum suppressed output
# varying theta
for angle in range(0, 180, 45):
    print('Thetas:', angle)
    t = np.ones((3, 3)) * angle # Initialize theta
    print(non_maximum_suppression(g, t))
Thetas: 0
```

```
[[0. 0. 0.]
[[0. 0. 0.]
[[0. 0. 0.]]
[[0. 0. 0.]]
Thetas: 45
[[0. 0. 0.]
[[0. 0. 0.]]
Thetas: 90
[[0. 0. 0.]
[[0. 0. 5 0.]
[[0. 0. 0.]]
Thetas: 135
[[0. 0. 0.]
[[0. 0. 0.]]
```

#### In [40]:

```
nms = non_maximum_suppression(G, theta)
plt.imshow(nms)
plt.title('Non-maximum suppressed')
plt.axis('off')
plt.show()

plt.subplot(1, 3, 1)
plt.imshow(nms)
plt.axis('off')
plt.title('Your result')

plt.subplot(1, 3, 2)
reference = np.load('references/iguana_non_max_suppressed.npy')
```

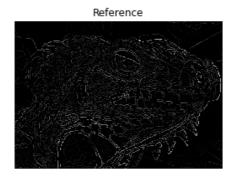
```
plt.imshow(reference)
plt.axis('off')
plt.title('Reference')

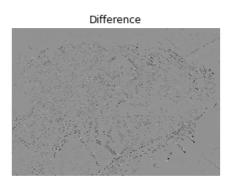
plt.subplot(1, 3, 3)
plt.imshow(nms - reference)
plt.title('Difference')
plt.axis('off')
plt.show()
```

Non-maximum suppressed









## 1.4 Double Thresholding (20 points)

The edge-pixels remaining after the non-maximum suppression step are (still) marked with their strength pixel-by-pixel. Many of these will probably be true edges in the image, but some may be caused by noise or color variations, for instance, due to rough surfaces. The simplest way to discern between these would be to use a threshold, so that only edges stronger that a certain value would be preserved. The Canny edge detection algorithm uses double thresholding. Edge pixels stronger than the high threshold are marked as strong; edge pixels weaker than the low threshold are suppressed and edge pixels between the two thresholds are marked as weak.

```
In [41]:
```

```
from edge import double_thresholding

low_threshold = 0.02
high_threshold = 0.03

strong_edges, weak_edges = double_thresholding(nms, high_threshold, low_threshold)

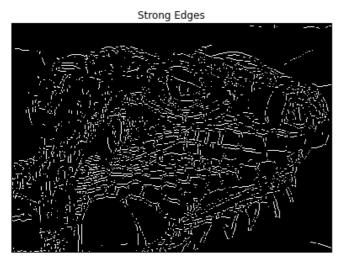
assert(np.sum(strong_edges & weak_edges) == 0)

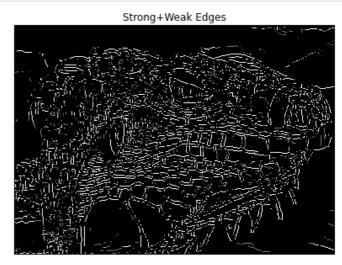
edges=strong_edges * 1.0 + weak_edges * 0.5

plt.subplot(1,2,1)
plt.imshow(strong_edges)
plt.title('Strong Edges')
plt.axis('off')

plt.subplot(1,2,2)
plt.imshow(edges)
plt.title('Strong+Weak Edges')
plt.title('Strong+Weak Edges')
plt.axis('off')

plt.show()
```





### 1.5 Edge tracking (15 points)

Strong edges are interpreted as "certain edges", and can immediately be included in the final edge image. Weak edges are included if and only if they are connected to strong edges. The logic is of course that noise and other small variations are unlikely to result in a strong edge (with proper adjustment of the threshold levels). Thus strong edges will (almost) only be due to true edges in the original image. The weak edges can either be due to true edges or noise/color variations. The latter type will probably be distributed independently of edges on the entire image, and thus only a small amount will be located adjacent to strong edges. Weak edges due to true edges are much more likely to be connected directly to strong edges.

```
Implement link edges in edge.py.
```

We provide the correct output and the difference between it and your result for debugging purposes. If you see white spots in the Difference image, you should check your implementation.

#### In [42]:

```
from edge import get_neighbors, link_edges

test_strong = np.array(
    [[1, 0, 0, 0],
    [0, 0, 0, 0],
    [0, 0, 0, 0],
    [0, 0, 0, 1]],
    dtype=np.bool
)

test_weak = np.array(
```

```
[[0, 0, 0, 1],
     [0, 1, 0, 0],
     [1, 0, 0, 0],
     [0, 0, 1, 0]],
    dtype=np.bool
test linked = link edges(test strong, test weak)
plt.subplot(1, 3, 1)
plt.imshow(test strong)
plt.title('Strong edges')
plt.subplot(1, 3, 2)
plt.imshow(test weak)
plt.title('Weak edges')
plt.subplot(1, 3, 3)
plt.imshow(test linked)
plt.title('Linked edges')
plt.show()
```

<ipython-input-42-13e23629ec71>:8: DeprecationWarning: `np.bool` is a deprecated alias fo
r the builtin `bool`. To silence this warning, use `bool` by itself. Doing this will not
modify any behavior and is safe. If you specifically wanted the numpy scalar type, use `n
p.bool\_` here.

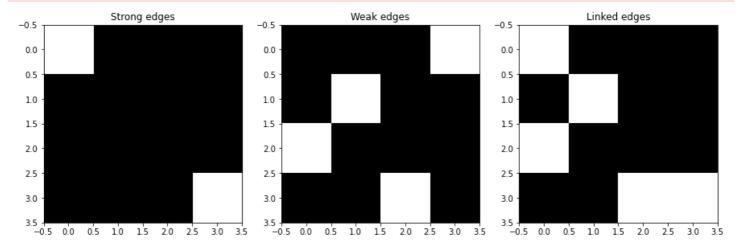
Deprecated in NumPy 1.20; for more details and guidance: https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations

dtype=np.bool

<ipython-input-42-13e23629ec71>:16: DeprecationWarning: `np.bool` is a deprecated alias f
or the builtin `bool`. To silence this warning, use `bool` by itself. Doing this will not
modify any behavior and is safe. If you specifically wanted the numpy scalar type, use `n
p.bool` here.

Deprecated in NumPy 1.20; for more details and guidance: https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations

dtype=np.bool



#### In [43]:

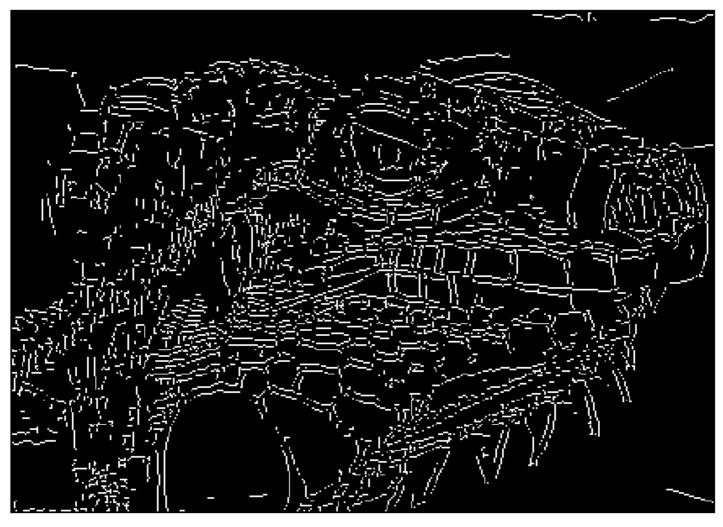
```
edges = link_edges(strong_edges, weak_edges)

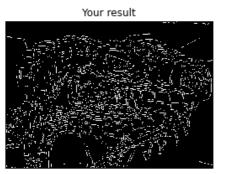
plt.imshow(edges)
plt.axis('off')
plt.show()

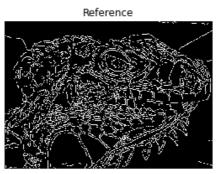
plt.subplot(1, 3, 1)
plt.imshow(edges)
plt.axis('off')
plt.title('Your result')

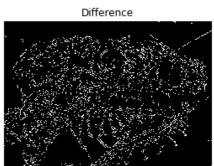
plt.subplot(1, 3, 2)
reference = np.load('references/iguana_edge_tracking.npy')
plt.imshow(reference)
plt.axis('off')
plt.title('Reference')
```

```
plt.subplot(1, 3, 3)
plt.imshow(edges ^ reference)
plt.title('Difference')
plt.axis('off')
plt.show()
```









### 1.6 Canny edge detector

Implement canny in edge.py using the functions you have implemented so far. Test edge detector with different parameters.

Here is an example of the output:

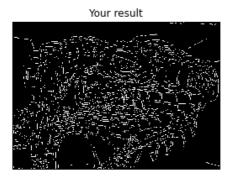
We provide the correct output and the difference between it and your result for debugging purposes. If you see white spots in the Difference image, you should check your implementation.

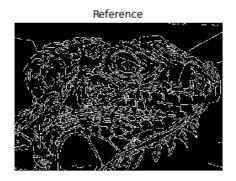
```
In [44]:
```

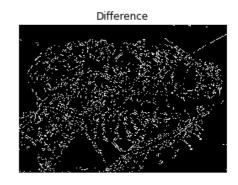
```
from edge import canny
# Load image
img = io.imread('iguana.png', as_gray=True)
```

```
# Run Canny edge detector
edges = canny(img, kernel size=5, sigma=1.4, high=0.03, low=0.02)
print (edges.shape)
plt.subplot(1, 3, 1)
plt.imshow(edges)
plt.axis('off')
plt.title('Your result')
plt.subplot(1, 3, 2)
reference = np.load('references/iguana canny.npy')
plt.imshow(reference)
plt.axis('off')
plt.title('Reference')
plt.subplot(1, 3, 3)
plt.imshow(edges ^ reference)
plt.title('Difference')
plt.axis('off')
plt.show()
```

(310, 433)







# **Part2: Lane Detection (15 points)**

In this section we will implement a simple lane detection application using Canny edge detector and Hough transform. Here are some example images of how your final lane detector will look like.

The algorithm can broken down into the following steps:

- 1. Detect edges using the Canny edge detector.
- 2. Extract the edges in the region of interest (a triangle covering the bottom corners and the center of the image).
- 3. Run Hough transform to detect lanes.

## 2.1 Edge detection

Lanes on the roads are usually thin and long lines with bright colors. Our edge detection algorithm by itself should be able to find the lanes pretty well. Run the code cell below to load the example image and detect edges from the image.

```
In [45]:
```

```
from edge import canny

# Load image
img = io.imread('road.jpg', as_gray=True)

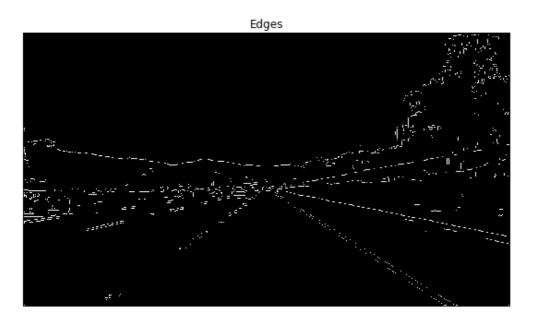
# Run Canny edge detector
edges = canny(img, kernel_size=5, sigma=1.4, high=0.03, low=0.02)

plt.subplot(211)
plt.imshow(img)
```

```
plt.axis('off')
plt.title('Input Image')
plt.subplot(212)
plt.imshow(edges)
plt.axis('off')
plt.title('Edges')
plt.show()
```







# 2.2 Extracting region of interest (ROI)

We can see that the Canny edge detector could find the edges of the lanes. However, we can also see that there are edges of other objects that we are not interested in. Given the position and orientation of the camera, we know that the lanes will be located in the lower half of the image. The code below defines a binary mask for the ROI and extract the edges within the region.

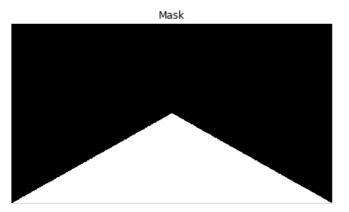
```
In [46]:
```

```
H, W = img.shape
# Generate mask for ROI (Region of Interest)
mask = np.zeros((H, W))
for i in range(H):
    for j in range(W):
        if i > (H / W) * j and i > -(H / W) * j + H:
            mask[i, j] = 1
# Extract edges in ROI
```

```
roi = edges * mask

plt.subplot(1,2,1)
plt.imshow(mask)
plt.title('Mask')
plt.axis('off')

plt.subplot(1,2,2)
plt.imshow(roi)
plt.title('Edges in ROI')
plt.axis('off')
plt.axis('off')
```





### 2.3 Fitting lines using Hough transform (15 points)

The output from the edge detector is still a collection of connected points. However, it would be more natural to represent a lane as a line parameterized as y=ax+b, with a slope a and y-intercept b. We will use Hough transform to find parameterized lines that represent the detected edges.

In general, a straight line y=ax+b can be represented as a point (a,b) in the parameter space. However, this cannot represent vertical lines as the slope parameter will be unbounded. Alternatively, we parameterize a line using  $\theta\in [-\pi,\pi]$  and  $\rho\in\mathbb{R}$  as follows:

$$ho = x \cdot cos\theta + y \ \cdot sin heta$$

Using this parameterization, we can map every point in xy-space to a sine-like line in  $\theta\rho$ -space (or Hough space). We then accumulate the parameterized points in the Hough space and choose points (in Hough space) with highest accumulated values. A point in Hough space then can be transformed back into a line in xy-space.

See notes on Hough transform.

Implement hough transform in edge.py.

#### In [51]:

```
from edge import hough_transform

# Perform Hough transform on the ROI
acc, rhos, thetas = hough_transform(roi)

# Coordinates for right lane
xs_right = []
ys_right = []

# Coordinates for left lane
xs_left = []
ys_left = []

for i in range(20):
   idx = np.argmax(acc)
   r_idx = idx // acc.shape[1]
   t_idx = idx % acc.shape[1]
   acc[r_idx, t_idx] = 0 # Zero out the max value in accumulator
```

```
rho = rhos[r_idx]
    theta = thetas[t_idx]
    # Transform a point in Hough space to a line in xy-space.
    a = - (np.cos(theta)/np.sin(theta)) # slope of the line
   b = (rho/np.sin(theta)) # y-intersect of the line
    # Break if both right and left lanes are detected
    if xs right and xs left:
       break
    if a < 0: # Left lane</pre>
        if xs left:
            continue
        xs = xs left
        ys = ys_left
    else: # Right Lane
        if xs right:
           continue
        xs = xs_right
        ys = ys_right
    for x in range(img.shape[1]):
        y = a * x + b
        if y > img.shape[0] * 0.6 and y < img.shape[0]:</pre>
            xs.append(x)
            ys.append(int(round(y)))
plt.imshow(img)
plt.plot(xs_left, ys_left, linewidth=5.0)
plt.plot(xs_right, ys_right, linewidth=5.0)
plt.axis('off')
plt.show()
```

