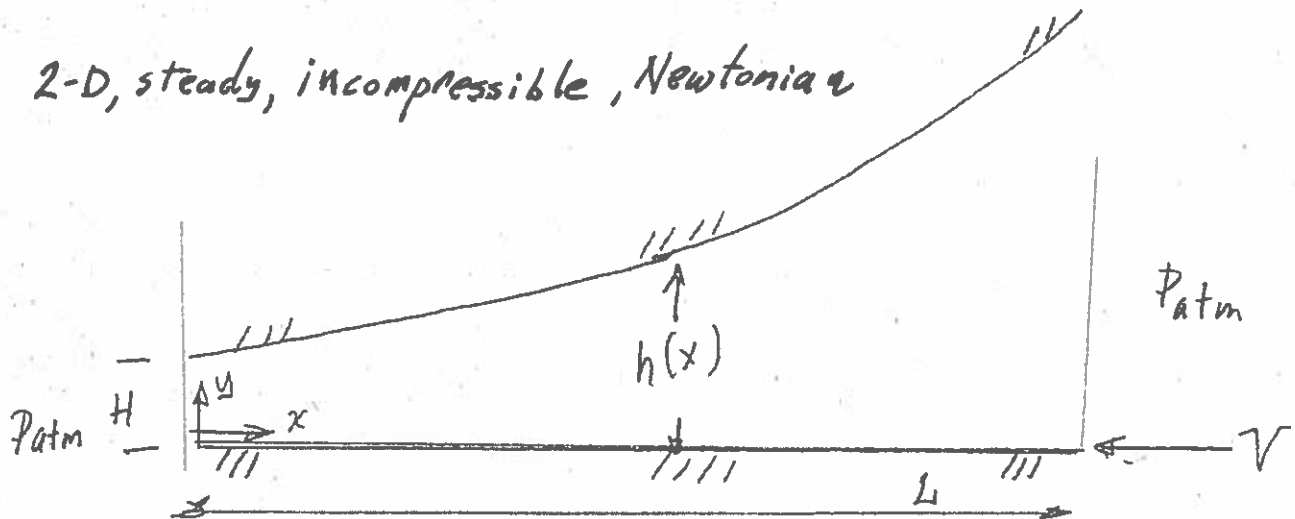


MANE 6520 - Fluid Mechanics

Homework #5 - Thurs 27 October 2022, due Thurs 3 November

2-D, steady, incompressible, Newtonian



Consider an exponential slider bearing, $h = H \exp\left(m \frac{x}{L}\right)$. In this case the sliding of the lower surface is in the negative x -direction. Pressure is atmospheric at both ends $x = 0, L$.

The parameters are $H, L, W, V, \rho, g, \mu, p_{\text{atm}}$.

- Find an expression for the pressure p , in terms of x and the above parameters.
- Find an expression for the velocity profile v_x in terms of x, y , and the above parameters.
- Find an expression for the location x_m , where the viscosity gradient is zero, in terms of the above parameters.
- Find an expression for the force on the lower surface, in terms of the above parameters.

Now, use the following parameter values:

$$H = 1 \text{ mm}, L = 100 \text{ mm}, W = 1 \text{ m}, V = -1 \text{ m/s}, \rho = 850 \text{ kg/m}^3, g = 9.81 \text{ m/s}^2, \\ \mu = 0.020 \text{ Pa-s}, p_{\text{atm}} = 0.1 \text{ MPa}.$$

Plot h/H , $0 \leq x/L \leq 1$ for $m = 0.5$ and $m = 1.5$. Two curves on the same plot.

Plot $p(x)$, $0 \leq x \leq L$ for $m = 0.5$ and $m = 1.5$. Two curves on the same plot.

Plot $v_x(x, y)$, $0 \leq y \leq h$ for $m = 1.5$ and $x = 0$ and $x = L$. Two plots, each with one curve.