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Exam Project

Red Wine Quality Data Analysis



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Table of Contents

1.	. Introduction	2
2.		
	2.1 Data quality and data preprocessing	
	2.2 Statistical summary of the data	3
	2.3 Initial assumptions and hypotheses	5
3.	. Exploratory Data analysis (EDA)	6
	3.1 Different Features/Variables Distribution	6
	3.2 Quality and Different variables	14
	3.3 Relationship among the variables	20
	3.4 Correlation matrix	30
	3.5 Regression	31
4.	Trends, Patterns and Anomalies	45
5.	. Discussion	50
6.	. Conclusion	53
7.	. References	54

1. Introduction

Red wine is an expensive beverage. It is essential to know the quality of the wine before ordering it, especially before ordering a large quantity of red wine. Otherwise, it can cause a considerable loss of money and customers. A business will be far more likely to purchase high-quality wine and continue operating successfully if it can develop a scientific approach for assessing the quality of red wine based on its physicochemical features. The certification procedure frequently includes quality evaluation, which can be used to stratify wines like premium brands (helpful for pricing) and enhance winemaking by identifying the most important features.

We need to do a data analysis to know the effect of different features (physicochemical properties) on red wine quality, for example, which features are more important than others for sensual quality rating, exploring different trends, patterns, and correlations in the wine's physicochemical characteristics, and finding the perfect proportion of the materials to maximize the quality.

2. Initial assumptions and hypotheses

The dataset includes a variety of data about red wine. The following table (Table 2.1) shows a list of variables and their description used in the dataset and for the analysis.

All the twelve variables/features are presented in numeric variables.

Features	Role	Description of the features. (units)
	Feature	Mainly tartaric, citric, malic and succinic. They do not evaporate immediately.
Fixed acidity		(g/dm^3)
	Feature	The wine's acetic acid amount which high amount produces an unpleasant
Volatile acidity		vinegar flavor. (g/dm ³)
Citric acid	Feature	Which gives flavor and freshness in modest amounts. (g/dm ³)
Residual sugar	Feature	The quantity of sugar that is left over once fermentation has ended. (g/dm ³)
Chlorides	Feature	how much salt (sodium chloride) is in the wine. (g/dm ³)
Free sulfur dioxide	Feature	It prevents oxidation of wine and microbial growth. (mg/dm ³)
	Feature	The total amount of free + bound forms of SO2. In low dilutions, it is generally
Total sulfur		unnoticeable in wine. However, at free SO2 absorptions over 50 ppm, SO2
dioxide		becomes apparent in the nose and in taste. (mg/dm ³)
	Feature	varying on the proportion of alcohol and sugar substance. sweeter wines are
Density		generally higher in density. (g/cm ³)
рН	Feature	measure of how acidic wine is (pH scale value)

	Feature	
Sulphates		(g/dm^3)
Alcohol	Feature	percentage of alcohol substance. (% vol.)
Quality	Target	A score between 0 and 10 which was assessed on human sensory data.

Table 2.1: List of all the variables and their description

2.1 Data quality and data preprocessing

Missing Values: No missing values found.

Duplicate values: 240 duplicate values/observation (rows) have been detected and removed. After that 1359 values are remaining.

Outliers: Outlying observation has been removed by both Z-score methods (for features' citric acid, density, and pH since their distribution was approximately normally distributed). The rest of the features outliers have been removed by the IQR method since the rest of the features' values are skewed either more than +0.5 or less than -0.5 of skewness value. If the skewness value is between -0.5 and 0.5, then the feature distribution is approximately symmetrical. One thousand thirty-one observations (rows) are remaining after removing the outliers.

Feature scaling: I have done feature scaling before the regression. Still, in the regression with or without feature scaling, the performance is almost the same as the MS Excel Data Analysis Tools Regression.

2.2 Statistical summary of the data

						free	total					
With	fixed	volatile	citric	residual	chlorid	sulfur	sulfur	dens		sulpha	alco	qual
Outliers	acidity	acidity	acid	sugar	es	dioxide	dioxide	ity	pН	tes	hol	ity
									13			135
Count	1359	1359	1359	1359	1359	1359	1359	1359	59	1359	1359	9
									2.7			
Min	4.6	0.12	0	0.9	0.012	1	6	0.99	4	0.33	8.4	3
								1.00	4.0			
Max	15.9	1.58	1	15.5	0.611	72	289	4	1	2	14.9	8
								0.01	1.2			
Range	11.3	1.46	1	14.6	0.599	71	283	4	7	1.67	6.5	5
Mean	8.3	0.5	0.3	2.5	0.1	15.9	46.8	1.0	3.3	0.7	10.4	5.6
								0.99	3.3			
Median	7.9	0.52	0.26	2.2	0.079	14	38	7	1	0.62	10.2	6
								0.99				
Mode	7.2	0.5	0	2	0.08	6	28	7	3.3	0.54	9.5	5
stdev (o)	1.7	0.2	0.2	1.4	0.0	10.4	33.4	0.0	0.2	0.2	1.1	0.8

								0.99	3.2			
Q1	7.1	0.39	0.09	1.9	0.07	7	22	6	1	0.55	9.5	5
								0.99				
Q3	9.2	0.64	0.43	2.6	0.091	21	63	8	3.4	0.73	11.1	6

Table 2.2.1: presents a statistical summary of the data before removing the outliers.

After						free	total					
removing	fixed	volatile	citric	residual	chlo	sulfur	sulfur			sulp	alco	quali
Outliers	acidity	acidity	acid	sugar	rides	dioxide	dioxide	density	pН	hates	hol	ty
Count	1031	1031	1031	1031	1031	1031	1031	1031	1031	1031	1031	1031
					0.03							
Min	5.1	0.12	0	1.2	9	1	6	0.9915	2.88	0.33	8.7	3
					0.12							
Max	12.3	1.01	0.73	3.65	2	42	124	1.001	3.72	0.98	13.5	8
					0.08							
Range	7.2	0.89	0.73	2.45	3	41	118	0.0095	0.84	0.65	4.8	5
	8.1589		0.24	2.1948	0.07	14.9146	42.2075	0.9965	3.32	0.63	10.3	5.63
Mean	72	0.52274	9534	11	8395	5	7	28	3453	0902	9796	7245
					0.07			0.9965				
Median	7.8	0.52	0.24	2.1	8	13	36	5	3.32	0.61	10.1	6
Mode	7.2	0.58	0	2	0.08	6	28	0.998	3.36	0.58	9.5	5
	1.4883		0.18	0.4537	0.01	8.83508		0.0016	0.13	0.11	1.00	0.77
stdev (σ)	17	0.16676	263	32	4991	2	26.5743	41	6563	4906	3188	6928
					0.06							
Q1	7.1	0.39	0.08	1.9	9	8	22	0.9955	3.23	0.55	9.5	5
					0.08						11.0	
Q3	9	0.63	0.4	2.5	7	20	56	0.9976	3.41	0.7	8333	6
								-				
	0.6866	0.31185	0.30	0.5992	0.22	0.84234	0.98761	0.0078	0.07	0.62	0.76	0.30
Skew	52	8	39	49	6293	8	1	4	7565	8241	0384	7078

Table 2.2.2: Statistical summary of the data after removing the outliers.

Statistical summary of the best quality wine (7 & 8):

Let's extract only the wine observations, rated as 7 and 8, and see their statistical summary.

Best												
Quality	fixed	volatile	citric	residual	chlor	free sulfur	total sulfur	dens	p	sulph	alco	qua
Wine	acidity	acidity	acid	sugar	ides	dioxide	dioxide	ity	Н	ates	hol	lity
No. of												
observatio									12			
ns	128	128	128	128	128	128	128	128	8	128	128	128

					0.04			0.99	2.			
Min	5.1	0.12	0	1.2	1	3	7	235	92	0.47	9.5	7
					0.12			1.00	3.		13.	
Max	12	0.85	0.66	3.65	1	42	106	02	71	0.94	4	8
								0.00	0.			
Range	6.9	0.73	0.66	2.45	0.08	39	99	785	79	0.47	3.9	1
									3.		11.	7.0
Mean	8.61	0.41	0.35	2.22	0.07	13.27	30.55	1.00	29	0.73	49	9
								0.99	3.		11.	
Median	8.5	0.375	0.38	2.2	0.07	12	25.5	535	3	0.73	5	7
					0.06			0.99	3.		11.	
Mode	9.1	0.31	0.39	2.4	6	6	10	68	23	0.76	7	7
									0.		0.9	0.2
stdev (σ)	1.66	0.14	0.18	0.50	0.02	8.43	20.45	0.00	14	0.10	1	8
									3.		10.	
Q1	7.38	0.31	0.30	1.80	0.06	6.00	16.00	0.99	20	0.65	90	7.0
									3.		12.	7.0
Q3	9.90	0.51	0.47	2.50	0.08	16.25	37.25	1.00	37	0.80	13	0

Table 2.2.3: Statistical summary of the best quality wine (which were rated as 7 and 8)

2.3 Initial assumptions and hypotheses

Based on the initial insights from the study by (Cortez et al., 2009) in the Red Wine Quality dataset, I have the following assumptions and hypotheses:

- 1. Since the amount of fixed acidity is the highest among all other types of acid (volatile acidity and citric acid (Table 2.2.2)) and since it does not evaporate readily (non-volatile). It will dominate the pH level. An increase in fixed acidity will make the wine sourer. Also, it could decrease the wine quality.
- 2. Since the high amount of volatile acidity in wine (acetic acid) produces an unpleasant vinegar flavor. The increase of this will decrease the wine quality.
- 3. A modest amount of citric acid in wine gives flavor and freshness. Less or too high will decrease the wine quality. Citric acid presence in wine is minimal (Table 2.2.2: Statistical summary). An increase of citric acid will increase the wine quality.
- 4. pH value of any acidic solutions is less than 7. The more it is acidic, the lesser the pH score. An increase in fixed acidity, volatile acidity, and citric acid will decrease the pH score/value. A low score of pH value is very acidic and sour, thus poor in quality.
- 5. Residual sugar is the amount of remaining sugar after the fermentation has stopped. Alcohol is less dense than water. An increase in residual sugar will increase the density of the wine. The more residual sugar

- will be more watery wine with a lesser alcohol percentage. An increase in the amount of residual sugar will decrease the wine quality.
- 6. Chlorides is the amount of salt in the wine. An increase in chlorides means saltier. So, an increase in chloride could be a decrease in quality.
- 7. The density of alcohol is less than water. So, an increase in density means more watery wine. The increase in density will decrease the quality. At room temperature, the alcohol density is around 0.79 g/cm3, and water density is around 0.99 g/cm3.
- 8. Alcohol is the main ingredient of wine. So, an increase in alcohol percentage will increase the quality. Customers also do not expect a very high percentage of alcohol in the red wine. We should look forward to determining which alcohol percentage yields the best result.

3. Exploratory Data analysis (EDA)

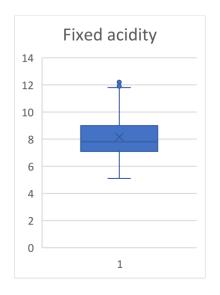
This section presents a detailed analysis of the exploratory data. Here, I show all the different analyses of the variables, their correlations, and finally, the regression analysis to predict the quality.

3.1 Different Features/Variables Distribution

Fixed acidity:

Mean	Median	Mode	Standard Deviation	Kurtosis	Skewness	Range	Minimum	Maximum
8.16	7.80	7.20	1.49	-0.04	0.69	7.20	5.10	12.30

Table 3.1.1: Statistical summary of fixed acidity variable.



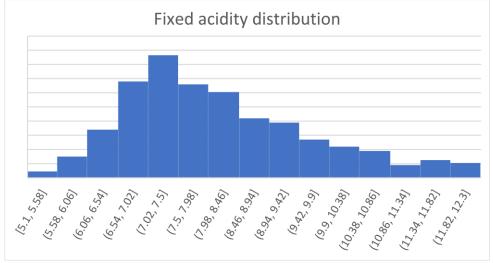


Figure 3.1.1: Fixed acidity distribution

- The fixed acidity distribution is slightly right-skewed and centered around 8 (g/dm3).
- In a fixed acidity variable, the mean is greater than the median.

Volatile acidity:

Mean	Median	Mode	SD (o)	Kurtosis	Skewness	Range	Minimum	Maximum
0.52	0.52	0.58	0.17	-0.27	0.31	0.89	0.12	1.01

Table 3.1.2: Statistical summary of volatile acidity.

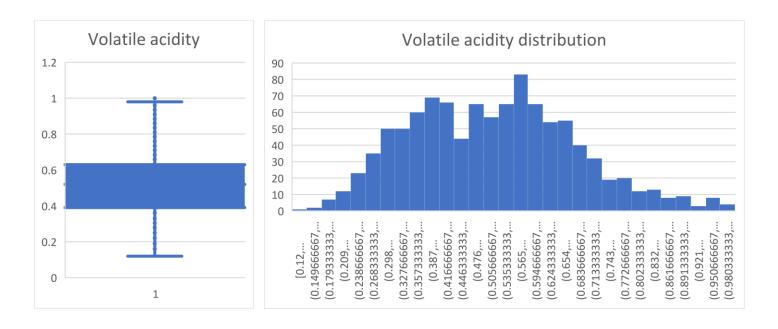


Figure 3.1.2: Volatile acidity distribution

- volatile acidity exists in red wines with an amount mean of 0.52 (g/dm³).
- The distribution looks bimodal at (around 0.39 and 0.57).

Citric acid:

Mean	Median	Mode	SD (o)	Kurtosis	Skewness	Range	Minimum	Maximum
0.25	0.24	0	0.18	-0.95	0.30	0.73	0	0.73

Table 3.1.3: Statistical summary of citric acid

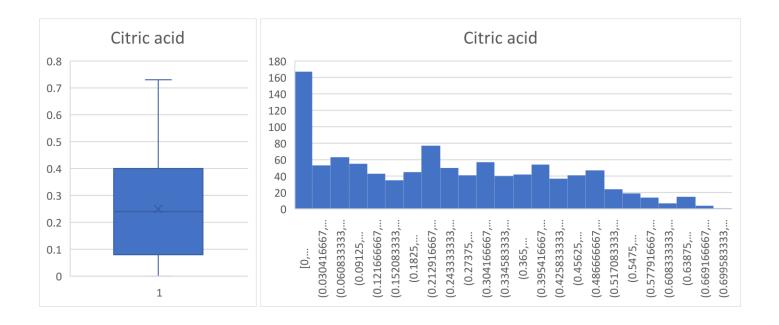


Figure 3.1.3: Citric acid distribution.

- The mode value of the citric acid distribution is 0.
- In red wine, citric acid is present in a very small amount.
- Around 9% of red wine has no citric acid in it.

Residual sugar:

Mean	Median	Mode	SD(o)	Kurtosis	Skewness	Range	Minimum	Maximum
2.19	2.1	2	0.45	0.30	0.60	2.45	1.2	3.65

Table 3.1.4: Statistical summary of residual sugar.

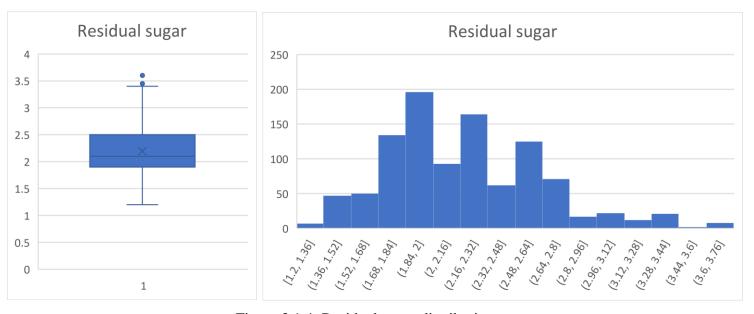


Figure 3.1.4: Residual sugar distribution.

• Residual sugar's Mean 2.2, Medium 2.1, Mode 2 and 75% data is within the range of 2.5 (g/dm3).

Chlorides:

Mean	Median	Mode	SD(o)	Kurtosis	Skewness	Range	Minimum	Maximum
0.078	0.078	0.080	0.015	0.263	0.227	0.083	0.039	0.122

Table 3.1.5: Statistical summary of chlorides.

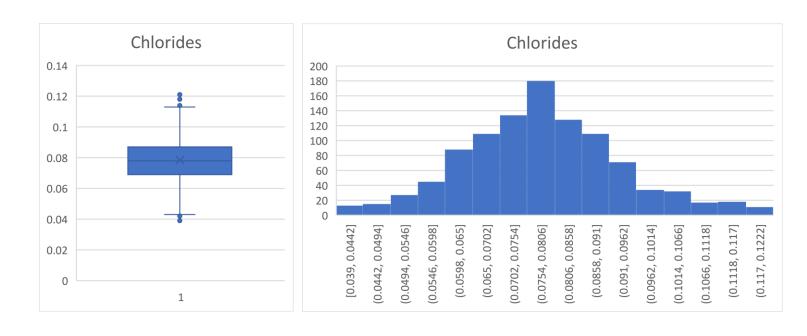


Figure 3.1.5: Chlorides distribution

- Chlorids distribution is normally distributed.
- Around 75% of wine has salt (sodium chloride) less than 0.09 (g/dm3).

Free sulfur dioxide:

Mean	Median	Mode	SD (o)	Kurtosis	Skewness	Range	Minimum	Maximum
14.91	13	6	8.84	0.05	0.84	41	1	42

Table 3.1.6: Statistical summary of free sulfur dioxide

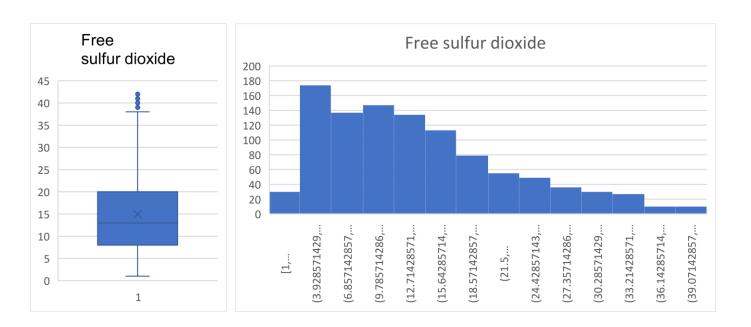


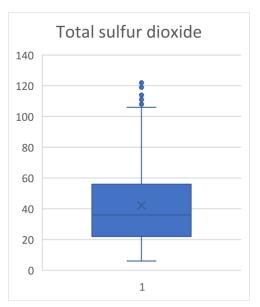
Figure 3.1.6: Free sulfur dioxide distribution

- The distribution of free sulfur dioxide is moderately right skewed.
- 75% of data is within the range of 20 (mg/dm³).

Total sulfur dioxide:

Mean	Median	Mode	SD(σ)	Kurtosis	Skewness	Range	Minimum	Maximum
42.21	36	28	26.59	0.33	0.99	118	6	124

Table 3.1.7: Statistical summary of total sulfur dioxide.



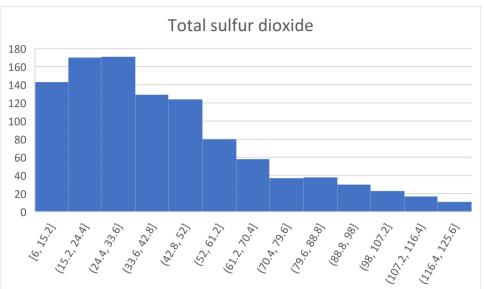


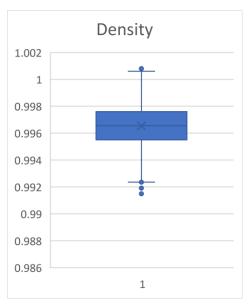
Figure 3.1.7: Total sulfur dioxide distribution

- Total sulfur dioxide's distribution is right skewed.
- 75% of data is within the range of 56 (mg/dm³).

Density:

Mean	Median	Mode	SD (o)	Kurtosis	Skewness	Range	Minimum	Maximum
0.997	0.997	0.998	0.002	0.076	-0.008	0.009	0.992	1.001

Table 3.1.8: Statistical summary of density.



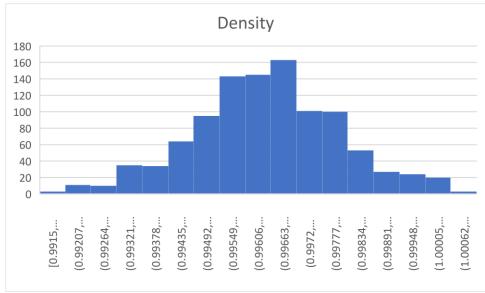


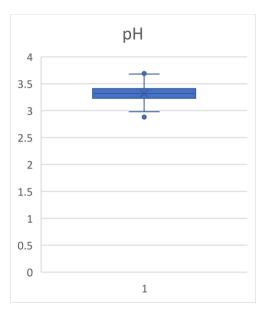
Figure 3.1.8: Density distribution.

Density feature is normally distributed.

pH:

Mean	Median	Mode	SD(σ)	Kurtosis	Skewness	Range	Minimum	Maximum
3.32	3.32	3.36	0.137	0.020	0.078	0.84	2.88	3.72

Table 3.1.9: Statistical summary of pH.



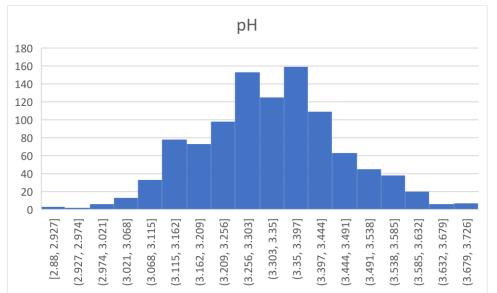


Figure 3.1.9: pH distribution

• pH feature is normally distributed.

Sulphate:

Mean	Median	Mode	SD (o)	Kurtosis	Skewness	Range	Minimum	Maximum
0.631	0.610	0.580	0.115	0.074	0.629	0.650	0.330	0.980

Table 3.1.10: Statistical summary of sulphates.

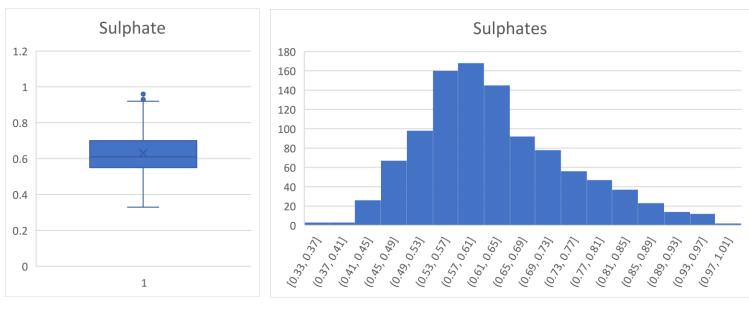


Figure 3.1.10: Sulphate distribution.

- Sulphate is slightly right skewed.
- The mean, median and mode is around 0.6. and 75% of data is within the value of 7 (g/dm³).

Alcohol:

Mean	Median	Mode	SD	Kurtosis	Skewness	Range	Minimum	Maximum
10.40	10.1	9.5	1.00	-0.26	0.76	4.8	8.7	13.5

Table 3.1.11: Statistical summary of alcohol

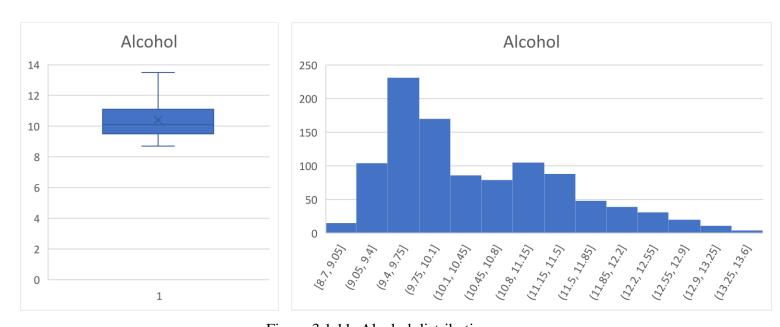


Figure 3.1.11: Alcohol distribution.

• Alcohol features distribution is slightly right skewed.

Quality:

Mean	Median	Mode	SD	Kurtosis	Skewness	Range	Minimum	Maximum
5.64	6	5	0.78	0.22	0.31	5	3	8

Table 3.1.12: Statistical summary of quality.



Figure 3.1.12: Quality distribution

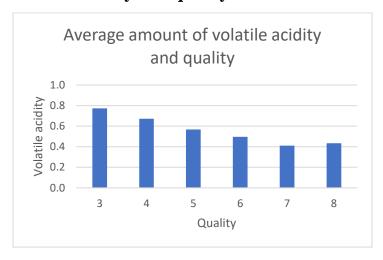
• Most of the wine quality scored either 5 or 6.

3.2 Quality and Different variables

Observa	tions after removing outliers
Quality	Number of Observations
3	3
4	33
5	438
6	429
7	117
8	11

Table 3.2.1: Number of Observations of different quality's of wine.

Volatile acidity and quality:



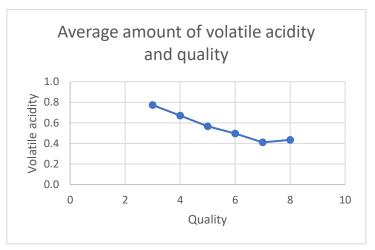
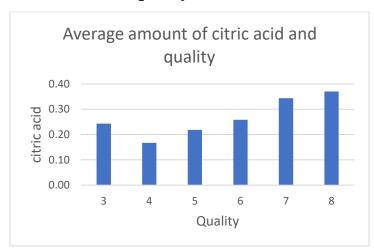


Figure 3.2.1: Average amount of volatile acidity in different quality's of wine

• The lesser the amount of volatile acidity greater the quality.

Citric acid and quality:



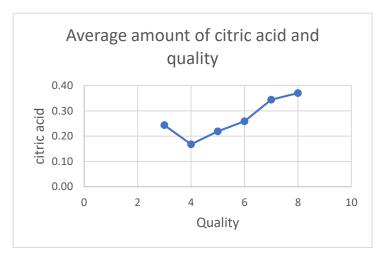
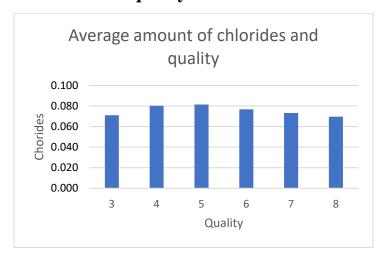


Figure 3.2.2: Average amount of citric acid in different qualities of wine

- After removing the outliers, there are only 03 observations of wine quality of level 3. This is not enough observation to come to any conclusion for level 3. But from the rest of the data, we can see that the greater the amount of citric acid, the greater the quality.
- Citric acid is present in small amounts in the wine. The highest amount of citric acid is 0.73, which was found in a level 6-rated wine.

Chlorides and quality:



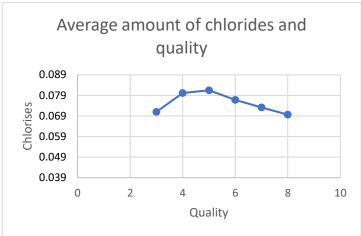
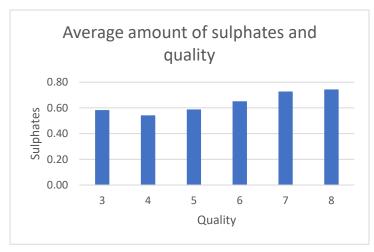


Figure 3.2.3: Average amount of chlorides in different wine qualities.

Note: The minimum value chlorides/salt is 0.039 (g/dm³) and maximum value is 0.122 (g/dm³) (Table 2.2.2). So, I have also started the y-axis from 0.039 in figure 3.2.3.

- More salt is lesser in the test (quality).
- From the observation, we can say that we should look for a wine where the chloride value is lesser than 0.07 (if we ignore the observation of level 3 wine since there are only 03 observations of wine quality of level 3)

Sulphates and quality:



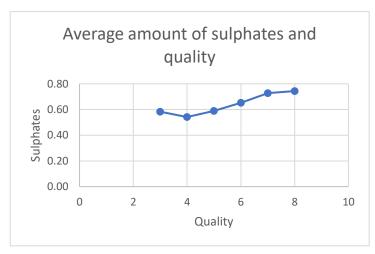
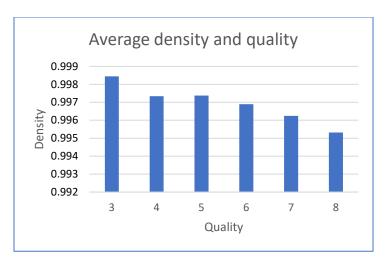


Figure 3.2.4: Average amount of sulphates in different qualities

Increase in sulphates additive increases the quality.

Density and quality:



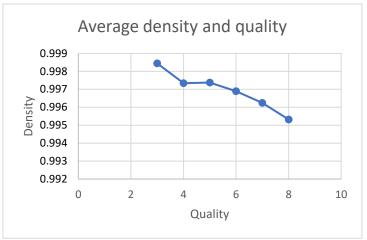


Figure 3.2.5: Average density in different qualities

Note: No liquid is 0 in (g/cm³) density. In our data set the lowest value of density is 0.9915. So, we also start the y-axis from 0.9915 (Table 2.2.2).

- Increase in density decreases the quality.
- The density of water is higher than the density of alcohol. More dense wine means more watery wine.

pH scale and quality:





Figure 3.2.6: Average pH scale value in different qualities

Note: In red wine, pH scale value varies in decimal point (Table 2.2.2). So, I have also started the y-axis from 3.24 in figure 3.2.6.

- In the best quality wines rated as 7 or 8, the average pH value is between 3.2 and 3.3.
- In wine quality, the pH value varies in decimal points/fractions. The decimal fraction variation should not be that noticeable in the tongue.

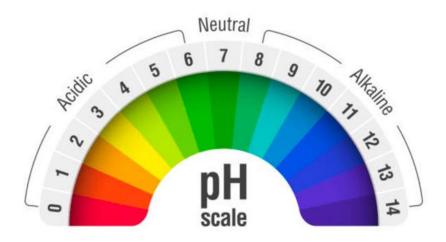


Figure 3.2.7: pH scale

- Red wine is acidic in mild test.
- Decrease in pH value makes little increase in the wine quality.

The pH is a scale measuring how acidic or basic the solution is, which varies from 0 to 14, and where seven is considered neutral. A pH scale value less than seven is considered acidic, and a value greater than seven is considered base.

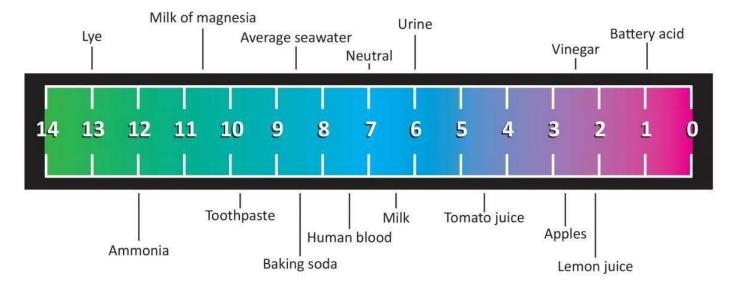
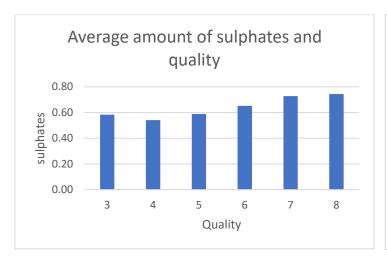


Figure 3.2.8: pH scale value in different item.

Sulphates and wine quality:



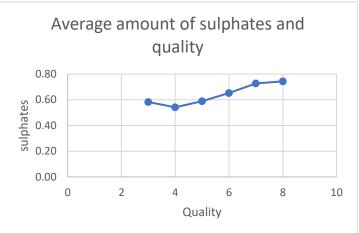
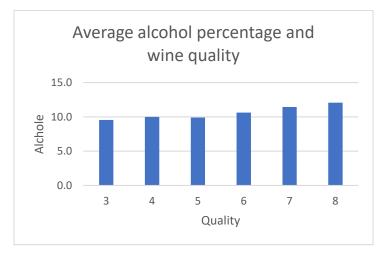


Figure 3.2.9: Average sulphates in different wine quality

• From the cart we can see that increase in sulphates is increase in quality.

Alcohol and wine quality:



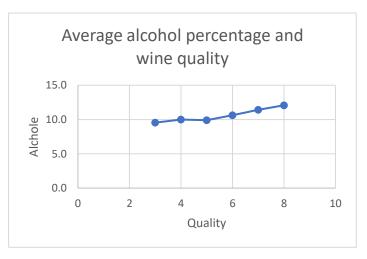


Figure 3.2.10: Average alcohol percentage in different wine quality

- From the cart, we can see an increase in alcohol is an increase in quality.
- In best-quality wines rated as 7 or 8, the average alcohol percentage is between 11 to 13. We should order a wine where the alcohol percentage is within this range. The best choice could be around 12% alcohol.

3.3 Relationship among the variables

Fixed acidity:

Correlation of					lfur	lfur					
different features	ile y	acid	ıal	ides	sulfi de	su. de	ty		ates	ol	ty
with fixed acidity	volatil acidity	citric	residual sugar	chlori	free dioxi	total dioxio	densi	Hd	ydlns	alcoh	qualit
fixed acidity	-0.28	0.66	0.24	0.21	-0.13	-0.08	0.61	-0.70	0.18	-0.05	0.11

Table 3.3.1: Correlation of different features with fixed acidity.

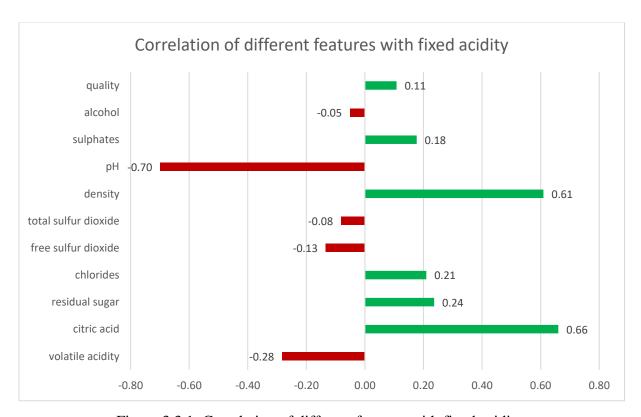


Figure 3.3.1: Correlation of different features with fixed acidity.

- Fixed acidity has a very significant positive correlation with citric acid (with a value of 0.66) and density (with a value of 0.61).
- There is a very significant negative correlation with pH level, with a value of -0.70. It makes sense because the pH value of any acidic solution is less than 7. The more it is acidic, the lesser the pH level.

- Fixed acidity negatively correlates with volatile acidity, with a value of -0.28.
- Fixed acidity hardly correlates negatively with residual sugar, with a value of -0.24.

Volatile acidity:

Correlation of	1			lfur	lfur					
different features	acic	ıal	ides	su	su	ty		ates	ol	Ş.
with volatile acidity	citric	residu sugar	chlori	free dioxic	total dioxic	density	Hd	qd[ns	alcoh	qualit
volatile acidity	-0.62	0.01	0.12	-0.02	0.10	0.04	0.24	-0.31	-0.22	-0.35

Table 3.3.2: Correlation of different features with volatile acidity

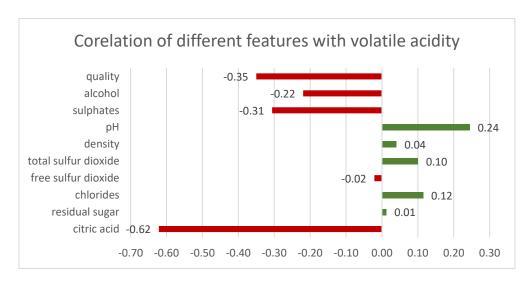


Figure 3.3.2: Correlation of different features with volatile acidity

- There is a very strong negative correlation between volatile acidity and citric acid, with a value of -0.62. Citric acid is able to add freshness and flavor to red wine, where a very high amount of volatile acidity can start a vinegar taste, which is unpleasant. It has a *strong* negative correlation with quality -0.35, which seems very logical.
- Volatile acidity has a strong negative correlation with sulphate -0.31.
- It has a mild positive correlation with pH 0.24. it's unusual.

Citric acid:

Correlation of different features with citric acid	residual	chlorides	free sulfur dioxide	total sulfur dioxide	density	Hd	sulphates	alcohol	quality
citric acid	0.16	0.07	-0.06	0.01	0.29	-0.49	0.27	0.14	0.22

Table 3.3.3: Correlation of different features with citric acid

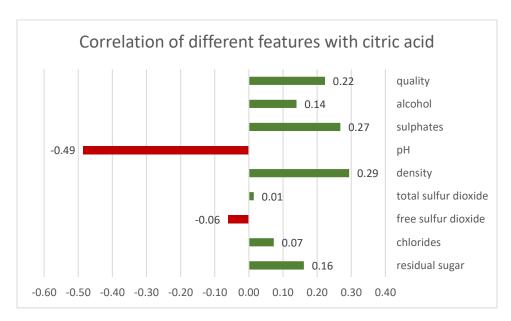


Figure 3.3.3: Correlation of different features with citric acid

- Citric acid has a very strong negative correlation with pH -0.49. The more it increases the more the wine will become acidic. Which makes sense.
- Citric acid has a positive correlation with density 0.29 and with sulphates 0.27.

Residual sugar:

Correlation of	es	ur	fur e	1		Se	1	1
different features	oride	sulfu	sulf xide	nsity	Hd	hate	ohol	ality
with residual sugar	chle	free	total dic	der	1	hdlus	alc	nb
residual sugar	0.27	0.08	0.18	0.40	-0.07	0.07	0.08	0.02

Table 3.3.4: Correlation of different features with residual sugar.

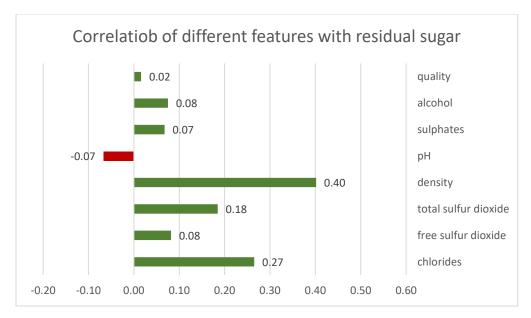


Figure 3.3.4: Correlation of different features with residual sugar.

- Residual sugar has a very strong positive correlation with density 0.40. That makes sense because residual sugar is the amount of remaining sugar after the fermentation has stopped. Alcohol is less dense than water. More residual sugar is more watery wine.
- Residual sugar has a strong positive correlation with chlorides/salt.

Chlorides:

Correlation of							
different features							
with chlorides	free sulfur dioxide	total sulfur dioxide	density	pН	sulphates	alcohol	quality
chlorides	0.03	0.18	0.43	-0.19	-0.07	-0.30	-0.18

Table 3.3.5: Correlation of different features with chlorides

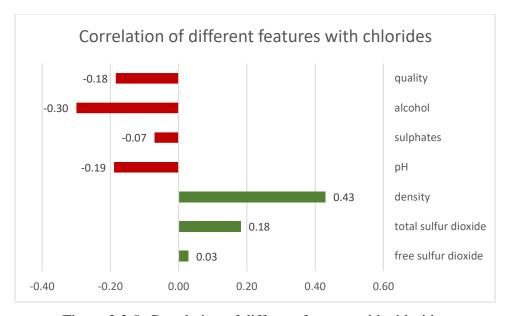


Figure 3.3.5: Correlation of different features with chlorides

- Chlorides has a strong positive correlation with density 0.43. So, more salt means higher density.
- It has a strong negative correlation with alcohol with value -0.30.
- More salty wine means higher in density and lower in alcohol percentage.

Free sulfur dioxide:

Correlation of						
different features						
with free sulfur	total sulfur					
dioxide	dioxide	density	pН	sulphates	alcohol	quality
free sulfur dioxide	0.62	-0.01	0.10	0.08	-0.05	-0.01

Table 3.3.6: Correlation of different features with free sulfur dioxide.

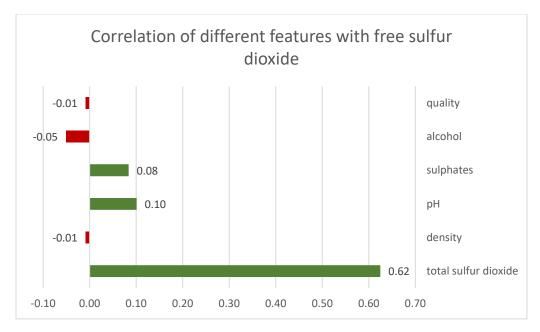


Figure 3.3.6: Correlation of different features with free sulfur dioxide.

• Free sulfur dioxide has a very strong positive correlation with total sulfur dioxide of 0.62. Total Sulfur Dioxide = amount of Free sulfur dioxide + bound forms of sulfur dioxide, which was expected.

Total sulfur dioxide:

Correlation of					
different features with					
total sulfur dioxide	density	рН	sulphates	Alcohol	quality
total sulfur dioxide	0.16	-0.01	-0.06	-0.27	-0.20

Table 3.3.7: Correlation of different features with total sulfur dioxide.

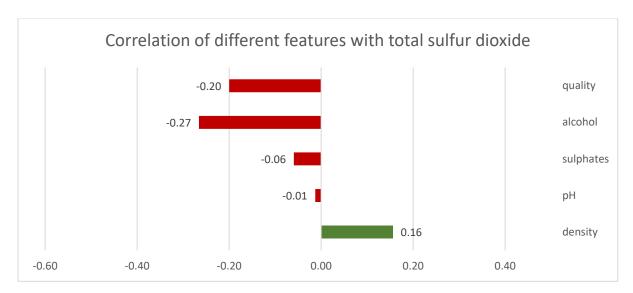


Figure 3.3.7: Correlation of different features with total sulfur dioxide.

- Total sulfur dioxide has a strong negative correlation with an alcohol percentage of -0.27.
- Total sulfur dioxide has a negative correlation with quality-0.20. "at free SO2 concentrations over 50 ppm, SO2 becomes evident in the nose and taste of wine" [from the description]

Density:

Correlation of different				
features with density	pН	sulphates	alcohol	quality
density	-0.24	0.09	-0.56	-0.24

Table 3.3.8: Correlation of different features with density.

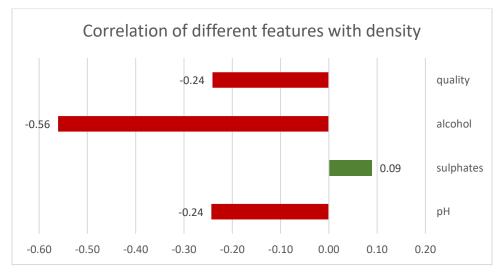


Figure 3.3.8: Correlation of different features with density.

- Density has a very strong negative correlation with alcohol percentage of -0.56. High density wine is more watery wine.
- Density has a mild negative correlation with pH and quality (with a value of -0.24).

pH:

Correlation of different			
features with pH	sulphates	alcohol	quality
рН	0.01	0.13	-0.07

Table 3.3.9: Correlation of different features with pH.

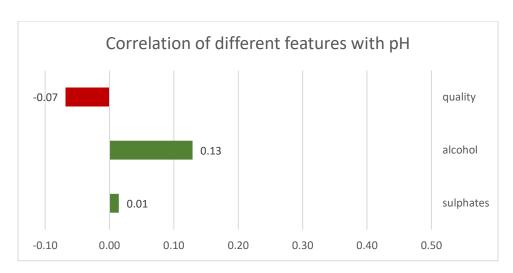


Figure 3.3.9: Correlation of different features with pH.

Before we saw that pH has a very strong negative correlations with fixed acidity -0.70 and with citric acid -0.49. But pH has a mild positive correlation with volatile acidity with value 0.24 (which seems unusual).

Sulphates:

Correlation sulphates with			
different variables	alcohol	quality	volatile acidity
sulphates	0.27	0.42	-0.31

Table 3.3.10: Correlation of different features with sulphates.

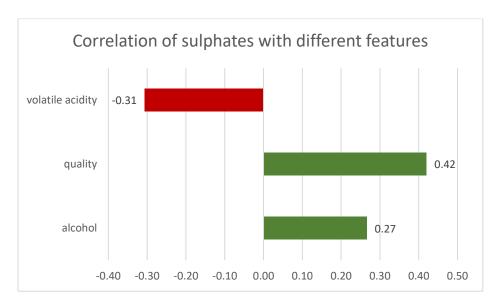


Figure 3.3.10: Correlation of different features with sulphates.

- Sulphate has a very strong positive correlation with quality 0.42. "Sulphites in wine are used to stop fermentation at a specific point in the winemaking process." [1]
- Sulphate has a mild positive correlation with an alcohol percentage of 0.27.
- Sulphate has a high negative correlation with volatile acidity -0.31 (Table 3.3.1) (Figure 3.3.2).

Quality:

Correlation		>										
of different	lity	acidity	_	sugar		ı	Ħ					
features with	acidity	ile a	acid		ides	sulfur ide	sulfur	ty		ıates	lol	ty
quality	fixed	volatile	citric	residual	chlorides	free sulf dioxide	total su	density	hф	sulphates	alcoh	quality
		ŕ				.,,	,	-	-			
Quality	0.11	-0.35	0.22	0.02	-0.18	-0.01	-0.20	0.24	0.07	0.42	0.51	1

Table 3.3.11: Correlation of different features with quality.

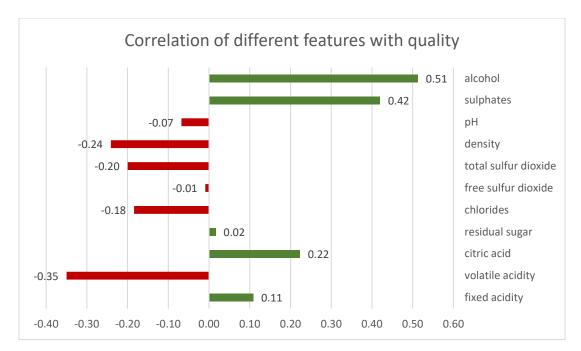


Figure 3.3.11: Correlation of different features with quality.

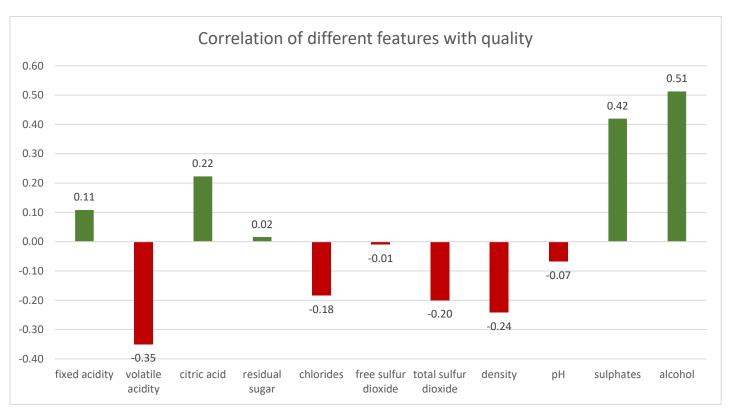


Figure 3.3.12: Correlation of different features with quality.

We can see that wine quality has a very significant positive correlation with alcohol. In fact, alcohol is the most correlated feature with quality in our data set, with a value of 0.51.

The alcohol feature is the amount of alcohol percent content in the wine. A higher percentage of alcohol content would yield better satisfaction for a customer purchasing red wine; it seems like the most important ingredient in wine.

Next, we can see the second strongest positive correlation, 0.41, between sulphates & our quality predictor. It seems that people rate the quality higher when an additive is contributed to the drink. Sulphate acts as an antimicrobial. "Sulphites in wine are used to stop fermentation at a specific point in the winemaking process. Besides, they function as preservatives to prevent spoiling and oxidation and as protection from bacteria. All in all, sulphites help to maintain the freshness and flavour of wine and prolong its shelf life." [1] Wine quality has the strongest negative correlation with volatile acidity, with a correlation of -0.35. This is expected because too high acetic acid levels can lead to an unpleasant vinegar taste.

Wine quality has a mild positive correlation with citric acid 0.2, even though it adds freshness and flavor to wines. It seems to be present in a very small quantity in the wine, and around 9% of red wine does not have any citric acid (Mode =0) (Table 3.1.3).

Wine quality has a mild negative correlation with density with a value of -0.24.

3.4 Correlation matrix

Correlation matrix	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur	density	Hd	sulphates	alcohol	quality
fixed acidity	1											
volatile acidity	-0.28	1										
citric acid	0.66	-0.62	1									
residual sugar	0.24	0.01	0.16	1								
Chlorides	0.21	0.12	0.07	0.27	1							
free sulfur dioxide	-0.13	-0.02	-0.06	0.08	0.03	1						
total sulfur dioxide	-0.08	0.10	0.01	0.18	0.18	0.62	1					
Density	0.61	0.04	0.29	0.40	0.43	-0.01	0.16	1				
pН	-0.70	0.24	-0.49	-0.07	-0.19	0.10	-0.01	-0.24	1			
Sulphates	0.18	-0.31	0.27	0.07	-0.07	0.08	-0.06	0.09	0.01	1		
Alcohol	-0.05	-0.22	0.14	0.08	-0.30	-0.05	-0.27	-0.56	0.13	0.27	1	
Quality	0.11	-0.35	0.22	0.02	-0.18	-0.01	-0.20	-0.24	-0.07	0.42	0.51	1

Table 3.4.1: Correlation matrix of the variables.

3.5 Regression

The target /dependent variable (Y) is wine quality, which is determined by the rest of the 11 features/independent variables (X).

Simple Linear Regression

Fixed acidity and wine quality:

Simple regression between the independent variable/feature fixed acidity and the dependent variable quality:

SUMMARY								
OUTPUT								
Regression Stat	tistics							
Multiple R	0.108253376							
R Square	0.108233370							
Adjusted R	0.011/18/94							
Square	0.010758365							
Standard								
Error	0.773112814							
Observations	1031							
ANOVA								
					Signifi			
					cance			
	df	SS	MS	F	F			
		7.292						
		95415	7.292954	12.2016268	0.0004			
Regression	1	7	157	8	9778			
		615.0						
		36822	0.597703					
Residual	1029	8	423					
		622.3						
		29776						
Total	1030	9						
		Stand						
		ard				Upper	Lower	Upper
	Coefficients	Error	t Stat	P-value	95%	95%	95.0%	95.0%
		0.134						
		17190	38.57871	4.1169E-	4.9128	5.439461	4.912898	5.439461
Intercept	5.17618006	6	757	202	98278	843	278	843

		0.016						
		17775	3.493082		0.0247	0.088255	0.024765	0.088255
fixed acidity	0.056510225	2	718	0.00049778	65074	375	074	375

Table 3.5.1: a simple regression model with fixed acidity and wine quality.

P-value of the fixed acidity variable is 0.00049778, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the fixed acidity variable is 0.024765074, and the upper bound (Upper 95%) is 0.088255375. Zero does not fall within this confidence interval. So, the fixed acidity variable is statistically significant.

By the R-squared value, this simple regression model with a fixed acidity variable explains about 1% of the data..

Volatile acidity and Quality:

Simple regression between the independent variable/feature volatile acidity and the dependent variable quality:

1 0		1			•	1	1 2
SUMMARY							
OUTPUT							
Regression Stat	tistics						
	0.349875						
Multiple R	121						
	0.122412						
R Square	6						
Adjusted R	0.121559						
Square	745						
Standard	0.728530						
Error	592						
Observations	1031						
ANOVA							
					Significa		
	df	SS	MS	F	nce F		
		76.181006	76.18100	143.5327	4.6951E-		
Regression	1	1	61	872	31		
		546.14877	0.530756				
Residual	1029	08	823				
		622.32977					
Total	1030	69					

	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	6.489340	0.0746548	86.92462		6.342847	6.635833	6.342847	6.635833
Intercept	773	02	672	0	741	805	741	805
	-		-		-	-	-	-
volatile	1.630055	0.1360588	11.98051	4.6951E-	1.897040	1.363071	1.897040	1.363071
acidity	64	73	7	31	17	11	17	11

Table 3.5.2: a simple regression model with volatile acidity and wine quality.

The p-value of the volatile acidity variable is 4.6951E-31, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the volatile acidity variable is -1.897040167 and the upper bound (Upper 95%) is -1.363071114. Zero does not fall within this confidence interval. So, the volatile acidity variable is statistically significant.

By the R-squared value, this simple regression model with volatile acidity variable explains about 12% of the data.

Citric acid and Quality:

Simple regression between the independent variable/feature citric acid and the dependent variable quality:

SUMMARY							
OUTPUT							
Regression Stat	tistics						
	0.222887						
Multiple R	042						
	0.049678						
R Square	634						
Adjusted R	0.048755						
Square	095						
Standard	0.758119						
Error	819						
Observations	1031						
ANOVA							
					Significa		
	df	SS	MS	F	nce F		
		30.916492	30.91649	53.79160	4.5102E-		
Regression	1	92	292	746	13		

		591.41328	0.574745					
Residual	1029	4	66					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	5.400639	0.0399773	135.0925		5.322193	5.479086	5.322193	5.479086
Intercept	908	33	525	0	505	311	505	311
	0.948187	0.1292817	7.334276	4.5102E-	0.694501	1.201873	0.694501	1.201873
citric acid	72	03	205	13	845	595	845	595

Table 3.5.3: a simple regression model with citric acid and wine quality.

The p-value of the citric acid variable is 4.5102E-13, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the citric acid variable is 0.694501845, and the upper bound (Upper 95%) is 1.201873595. Zero does not fall within this confidence interval.

So, the citric acid variable is statistically significant.

By the R-squared value, this simple regression model with citric acid variable explains about 5% of the data.

Residual sugar and Wine quality:

Regression between the independent variable residual sugar and the dependent variable quality:

SUMMARY					
OUTPUT					
Regression Stat	istics				
	0.015983				
Multiple R	874				
	0.000255				
R Square	484				
	-				
Adjusted R	0.000716				
Square	08				
Standard	0.777583				
Error	647				
Observations	1031				
ANOVA				 	

					Significa			
	df	SS	MS	F	nce F			
		0.1589954	0.158995	0.262960	0.608203			
Regression	1	37	437	444	607			
		622.17078	0.604636					
Residual	1029	15	328					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	5.577174	0.1196197	46.62419	5.9036E-	5.342448	5.811901	5.342448	5.811901
Intercept	964	6	475	256	451	476	451	476
					-		-	
	0.027369	0.0533726	0.512796	0.608203	0.077362	0.132100	0.077362	0.132100
residual sugar	296	08	689	607	28	874	28	874

Table 3.5.4: a simple regression model with residual sugar and wine quality.

The p-value of the residual sugar variable is 0.608203607, which is greater than the threshold value. So, it is not statistically significant.

The confidence interval's lower bound (Lower 95%) for the residual sugar is -0.077362281 and the upper bound (Upper 95%) is 0.132100874. Zero falls within this confidence interval. So, the residual sugar variable is not statistically significant.

Chlorides and Wine quality:

Regression between the independent variable chlorides and the dependent variable quality:

SUMMARY OUTPUT					
Regression Stat	istics				
	0.184235				
Multiple R	985				
	0.033942				
R Square	898				
Adjusted R	0.033004				
Square	067				

Standard	0.764370							
Error	649							
Observations	1031							
ANOVA								
					Significa			
	Df	SS	MS	F	nce F			
		21.123676	21.12367	36.15442	2.52891E			
Regression	1	28	628	836	-09			
		601.20610	0.584262					
Residual	1029	06	488					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	6.385761	0.1267416	50.38408	4.5947E-	6.137059	6.634462	6.137059	6.634462
Intercept	197	22	946	280	653	741	653	741
	-		-		-	-	-	-
	9.548033	1.5879366	6.012855	2.52891	12.66399	6.432069	12.66399	6.432069
chlorides	33	66	26	E-09	71	57	71	57

Table 3.5.5: a simple regression model with chlorides and wine quality.

The p-value of the chloride variable is 2.52891E-09, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the chloride's variable is -12.6639971 and the upper bound (Upper 95%) is -6.43206957. Zero does not fall within this confidence interval. So, the chlorides variable is statistically significant.

By the R-squared value, this simple regression model with chlorides variable explains about 3% of the data.

Free sulfur dioxide and Wine quality:

Regression between the independent variable free sulfur dioxide and the dependent variable quality:

SUMMARY OUTPUT					
Regression Stat	Regression Statistics				
	0.009032				
Multiple R	395				

	8.15842							
R Square	E-05							
	-							
Adjusted R	0.000890							
Square	15							
Standard	0.777651							
Error	272							
Observations	1031							
ANOVA								
					Significa			
	Df	SS	MS	F	nce F			
		0.0507722	0.050772	0.083956	0.772063			
Regression	1	5	25	946	389			
		622.27900	0.604741					
Residual	1029	47	501					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	5.649091	0.0475194	118.8796		5.555845	5.742337	5.555845	5.742337
Intercept	789	14	61	0	771	807	771	807
	-		-		-		-	
free sulfur	0.000794	0.0027412	0.289753	0.772063	0.006173	0.004584	0.006173	0.004584
dioxide	28	27	25	389	31	754	31	754

Table 3.5.6: a simple regression model with free sulfur dioxide and wine quality.

The p-value of the free sulfur dioxide variable is 0.772063389, which is greater than the threshold value. So, it is not statistically significant.

The confidence interval's lower bound (Lower 95%) for the free sulfur dioxide is -0.00617331 and the upper bound (Upper 95%) is 0.004584754. Zero falls within this confidence interval. So, the free sulfur dioxide variable is not statistically significant.

Total sulfur dioxide and Wine quality:

Regression between the independent variable total sulfur dioxide and the dependent variable quality:

SUMMARY OUTPUT					
Regression Statistics					

	0.199957							
Multiple R	602							
	0.039983							
R Square	043							
Adjusted R	0.039050							
Square	082							
Standard	0.761977							
Error	339							
Observations	1031							
ANOVA								
71110171					Significa			
	df	SS	MS	F	nce F			
		24.882638	24.88263	42.85606	9.28112E			
Regression	1	01	801	683	-11			
		597.44713	0.580609					
Residual	1029	89	464					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	5.883989	0.0445397	132.1065		5.796590	5.971388	5.796590	5.971388
Intercept	789	13	944	0	755	824	755	824
	-		-		-	-	-	-
total sulfur	0.005845	0.0008929	6.546454	9.28112	0.007598	0.004093	0.007598	0.004093
dioxide	98	99	52	E-11	28	67	28	67

Table 3.5.7: a simple regression model with total sulfur dioxide and wine quality.

The p-value of the total sulfur dioxide variable is 9.28112E-11, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the total sulfur dioxide variable is -0.00759828 and the upper bound (Upper 95%) is -0.00409367. Zero does not fall within this confidence interval.

So, the total sulfur dioxide variable is statistically significant.

By the R-squared value, this simple regression model with total sulfur dioxide variable explains about 4% of the data.

Density and Wine quality:

Regression between the independent variable Density and the dependent variable quality:

SUMMARY OUTPUT								
Regression Stat	tistics							
	0.241047							
Multiple R	313							
	0.058103							
R Square	807							
Adjusted R	0.057188							
Square	456							
Standard	0.754751							
Error	742							
Observations	1031							
ANOVA								
					Significa			
	df	SS	MS	F	nce F			
		36.159729	36.15972	63.47707	4.28065E			
Regression	1	29	929	733	-15			
		586.17004	0.569650					
Residual	1029	76	192					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	119.3615	14.273993	8.362170	1.98273	91.35210	147.3710	91.35210	147.3710
Intercept	666	05	709	E-16	877	245	877	245
1	-		-		-	-	-	-
	114.1205	14.323703	7.967250	4.28065	142.2275	86.01352	142.2275	86.01352
density	29	21	3	E-15	31	6	31	6

Table 3.5.8: a simple regression model with density and wine quality.

The p-value of the density variable is 4.28065E-15 which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the density variable is -142.227531 and the upper bound (Upper 95%) is -86.013526. Zero does not fall within this confidence interval.

So, the density variable is statistically significant.

By the R-squared value, this simple regression model with density variable explains about 6% of the data.

pH and Wine quality:

Regression between the independent variable pH and the dependent variable quality:

SUMMARY								
OUTPUT								
Regression Stat	tistics							
	0.067635							
Multiple R	918							
	0.004574							
R Square	617							
Adjusted R	0.003607							
Square	246							
Standard	0.775902							
Error	156							
Observations	1031							
ANOVA								
					Significa			
	df	SS	MS	F	nce F			
		2.8469206	2.846920	4.728914	0.029886			
Regression	1	07	607	247	828			
		619.48285	0.602024					
Residual	1029	63	156					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	6.916083	0.5885743	11.75056	5.2633E-	5.761140	8.071026	5.761140	8.071026
Intercept	943	49	976	30	939	947	939	947
	-		-		-	-	-	-
	0.384792	0.1769479	2.174606	0.029886	0.732012	0.037572	0.732012	0.037572
pН	13	21	69	828	09	17	09	17

Table 3.5.9: a simple regression model with pH and wine quality.

The p-value of the pH variable is 0.029886828 which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the pH variable is -0.73201209 and the upper bound (Upper 95%) is -0.03757217. Zero does not fall within this confidence interval.

So, the pH variable is statistically significant.

By the R-squared value, this simple regression model with pH variable explains about 0.5% of the data.

Sulphates and Wine quality:

Regression between the independent variable sulphates and the dependent variable quality:

SUMMARY								
OUTPUT								
Regression Statis	tics							
	0.41967							
Multiple R	5136							
	0.17612							
R Square	722							
Adjusted R	0.17532							
Square	6566							
	0.70588							
Standard Error	2931							
Observations	1031							
ANOVA								
					Significa			
	df	SS	MS	F	nce F			
	-5	109.60921	109.609	219.979	3.02562E			
Regression	1	36	2136	2418	-45			
8		512.72056	0.49827					
Residual	1029	33	0713					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
	3.84699	0.1226900	31.3553	5.0576E	3.606243	4.08774	3.60624	4.08774
Intercept	4314	18	9786	-152	12	5508	312	5508
	2.83760	0.1913203	14.8316	3.02562	2.462182	3.21302	2.46218	3.21302
sulphates	5482	49	972	E-45	906	8059	2906	8059

Table 3.5.10: a simple regression model with sulphates and wine quality.

The p-value of the sulphate variable is 3.02562E-45, which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the sulphate variable is 2.462182906 and the upper bound (Upper 95%) is 3.213028059. Zero does not fall within this confidence interval.

So, the sulphates variable is statistically significant.

By the R-squared value, this simple regression model with sulphates variable explains about 18% of the data.

Alcohol and Wine quality:

Regression between the independent variable alcohol and the dependent variable quality:

SUMMARY								
OUTPUT								
Regression Stat	tistics							
-	0.512761							
Multiple R	543							
	0.262924							
R Square	4							
Adjusted R	0.262208							
Square	097							
Standard	0.667665							
Error	016							
Observations	1031							
ANOVA								
					Significa			
	df	SS	MS	F	nce F			
		163.62568	163.6256	367.0576	3.30735E			
Regression	1	32	832	092	-70			
		458.70409	0.445776					
Residual	1029	38	573					
		622.32977						
Total	1030	69						
	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%

	1.508080	0.2165245	6.964940	5.8515E-	1.083200	1.932960	1.083200	1.932960
Intercept	283	01	582	12	303	263	303	263
	0.397112	0.0207274	19.15874	3.30735	0.356439	0.437785	0.356439	0.437785
alcohol	882	97	759	E-70	894	87	894	87

Table 3.5.11: a simple regression model with alcohol and wine quality.

The p-value of the alcohol variable is 3.30735E-70 which is smaller than the threshold value (0.05). So, it is statistically significant.

The confidence interval's lower bound (Lower 95%) for the alcohol variable is 0.356439894 and the upper bound (Upper 95%) is 0.43778587. Zero does not fall within this confidence interval.

So, the alcohol variable is statistically significant.

By the R-squared value, this simple regression model with alcohol variable explains about 26% of the data.

Multiple Linear Regression:

SUMMARY							
OUTPUT							
Regression Stat	tistics						
	0.629295						
Multiple R	839						
	0.396013						
R Square	253						
Adjusted R	0.389493						
Square	278						
Standard	0.607347						
Error	018						
Observations	1031						
ANOVA							
					Significa		
	df	SS	MS	F	nce F		
		246.45083	22.40462	60.73846	1.2671E-		
Regression	11	94	176	469	103		
		375.87893	0.368870				
Residual	1019	75	4				
		622.32977					
Total	1030	69					

	Coefficie	Standard			Lower	Upper	Lower	Upper
	nts	Error	t Stat	P-value	95%	95%	95.0%	95.0%
					-		-	
	42.69182	29.650961	1.439812	0.150227	15.49209	100.8757	15.49209	100.8757
Intercept	993	43	67	539	58	557	58	557
					-		-	
	0.026885	0.0338119	0.795152	0.426709	0.039463	0.093234	0.039463	0.093234
fixed acidity	679	58	965	695	35	707	35	707
			-		-	-	-	-
volatile	-	0.1592015	5.077914	4.53547	1.120812	0.496011	1.120812	0.496011
acidity	0.808412	63	95	E-07	38	61	38	61
	-		-		-		-	
	0.266643	0.1812625	1.471033	0.141590	0.622333	0.089047	0.622333	0.089047
citric acid	15	16	01	915	63	338	63	338
					-		-	
	0.023640	0.0541305	0.436728	0.662401	0.082579	0.129860	0.082579	0.129860
residual sugar	343	86	012	135	82	508	82	508
	-		-		-		-	
	0.934910	1.4569212	0.641702	0.521210	3.793819	1.923998	3.793819	1.923998
chlorides	33	57	72	539	26	591	26	591
					-		-	
free sulfur	0.004017	0.0028814	1.394176	0.163568	0.001636	0.009671	0.001636	0.009671
dioxide	187	05	266	292	98	353	98	353
	-		-		-	-	-	-
total sulfur	0.002445	0.0010290	2.376239	0.017674	0.004464	0.000425	0.004464	0.000425
dioxide	19	16	62	104	42	96	42	96
	-		-		-		-	
	39.03836	30.251392	1.290464	0.197182	98.40051	20.32378	98.40051	20.32378
density	18	42	96	003	02	65	02	65
	-		-		-	-	-	-
	0.553697	0.2480871	2.231867	0.025840	1.040517	0.066877	1.040517	0.066877
pН	58	34	39	501	66	51	66	51
	1.882830	0.1894104	9.940480	2.75978	1.511151	2.254509	1.511151	2.254509
sulphates	432	07	392	E-22	387	477	387	477
	0.272650	0.0361605	7.539999	1.03717	0.201692	0.343608	0.201692	0.343608
alcohol	702	74	277	E-13	998	406	998	406

Table 3.5.12: Multiple linear Regression to wine quality based on the different explanatory variables of the wine.

Interpret R-squared/adjusted R-squared:

Let's see how well our model fits the data. For this reason, we need to interpret R-squared and adjusted R-squared. Generally, in Multiple Linear Regression, when we have more than one explanatory/Independent variable, it is preferable to use the adjusted R-square than the R-squared. Adjusted R-square considers the number of independent variables in the regression model. It can deliver a more accurate view of the correlation. By the adjusted R-square, that means controlling the number of independent variables in the regression model, the variability of the features of the Red wine explains almost 0.389 (39%) of the variability of the wine quality.

By the R-squared value, our regression model explains about 0.396 (40%) of the data. Alcohol, sulphate, and volatile acidity have a high influence on the model.

In the simple regression models, the highest R-squared value was 26% with the alcohol. However, in the Multiple Linear Regression Model, the R-squared value is around almost 39%. This means the multiple regression model adds about 13% points of explanatory power compared to the simple regression model. Multiple Linear regression has more/better explanatory power.

4. Trends, Patterns and Anomalies

This section presents the patterns and trends that I have identified from the EDA presented in Section 3. Below, I summarize the identified patterns and trends.

Patterns in fixed acidity:

The fixed acidity distribution is slightly right-skewed and centered around 8 g/dm3 (Figure 3.1.1). Fixed acidity has a very significant positive correlation with citric acid (with a value of 0.66) and with density (with a value of 0.61) (Figure 3.3.1). It has a very significant negative correlation with pH level, with a value of -0.70 (the highest negative correlation among the features). It makes sense because the pH value of any acidic solution is less than 7. The more it is acidic, the lesser the pH level. Fixed acidity negatively correlates with volatile acidity, with a value of -0.28. Fixed acidity hardly correlates negatively with residual sugar, with a value of -0.24 (Figure 3.3.1). Fixed acidity has very weak positive correlation with the wine quality, with a value of 0.11 (Figure 3.3.1).

Patterns in volatile acidity:

Volatile acidity exists in small amounts in wines with a mean of 0.52 (g/dm³). The distribution looks bimodal (at around 0.39 and 0.57) (Figure 3.1.2). There is a very strong negative correlation between volatile acidity and

citric acid, with value of -0.62 (Figure 3.3.2). Citric acid is able to add freshness and flavor to the red wine. Where a very high amount of volatile acidity can start a vinegar taste that is unpleasant, it has a strong negative correlation with quality -0.35 (Figure 3.3.2), which seems very logical. Volatile acidity has a strong negative correlation with sulphate -0.31. It has a mild positive correlation with pH 0.24, which is unusual. The smaller the amount of volatile acidity, the greater the quality (Figure 3.2.1).

Patterns in citric acid:

The mode value of citric acid distribution is 0 (Table 3.1.3). In red wine, citric acid is present in a very small amount. Around 9% of red wine has no citric acid in them. The highest amount of citric acid is 0.73 (g/dm³), which was found in a level 6-rated wine. It seems like there is a very little possibility that a higher value can reduce the wine quality (because it is present in wine in a very small quantity). Citric acid has a strong negative correlation with pH score, with a value of -0.49 (Figure 3.3.3). The more it increases, the more the wine will become acidic, which makes sense. Citric acid has a positive correlation with a density of 0.29 and with sulphates of 0.27 (Figure 3.3.3). Citric acid has a mild positive correlation with the wine quality, with a value of 0.22 (Figure 3.3.3). Citric acid adds freshness and flavor to the wine. The greater the amount of citric acid, the greater the wine quality (Figure 3.2.2).

Patterns in residual sugar:

Residual sugar's Mean 2.2, Medium 2.1, Mode 2, and 75% of data is within the range of 2.5 (g/dm3) (Table 3.1.4). Residual sugar has a strong positive correlation with density with a value of 0.40 (Figure 3.3.4). That makes sense because residual sugar is the amount of remaining sugar after the fermentation has stopped. Alcohol is less dense than water. More residual sugar is more watery wine. Residual sugar significantly correlates with chlorides/salt (with a value of 0.27) (Table 3.4.1). Residual sugar has a negligible positive correlation with wine quality, with a value of 0.02 (Table 3.3.11).

Patterns in Chlorides:

Chloride distribution is normally distributed (Figure 3.1.5). Around 75% of wine has a salt of less than 0.09 g/dm³ (Figure 3.1.5). Chloride has a strong positive correlation with density, with a value of 0.43 (Figure 3.3.5). So, more salt means higher density. It has a strong negative correlation with alcohol -0.30 (Figure 3.3.5). More salty wine means higher in density and lower in alcohol percentage. Chloride has a mild positive correlation with residual sugar, with a value of 0.27 (Table 3.4.1). Chlorides have a very weak negative correlation with wine quality, with a value of -0.18 (Table 3.3.11).

Patterns in free sulfur dioxide:

The distribution of free sulfur dioxide is moderately right-skewed (Figure 3.1.6). 75% of the data is within the range of 20 mg/dm3 (Figure 3.1.6). Free sulfur dioxide has a very strong positive correlation with total sulfur dioxide 0.62 (Figure 3.3.6). Which was expected. Since, Total Sulfur Dioxide = amount of Free sulfur dioxide + bound forms of sulfur dioxide. Free sulfur dioxide has a very weak negative correlation with wine quality, with a value of -0.01, which is negligible.

Patterns in total sulfur dioxide:

The total sulfur dioxide distribution is right-skewed (Figure 3.1.7). 75% of the data is within the range of 56 mg/dm3 (Figure 3.1.7). Total sulfur dioxide has a very strong positive correlation with total sulfur dioxide 0.62 (Figure 3.3.6), which was anticipated. Because the amount of total sulfur dioxide = amount of Free sulfur dioxide + bound forms of sulfur dioxide. Total sulfur dioxide has a negative correlation with an alcohol percentage of -0.27 (Figure 3.3.7). So, an increase in total sulfur dioxide means a mild decrease in alcohol (% vol.). Total sulfur dioxide has a negative correlation with quality, with a value of -0.20.

Patterns in density:

The density feature is normally distributed (Figure 3.1.8). Density has a very strong positive correlation with fixed acidity with a value of 0.61, with residual sugar 0.40, with chlorides 0.43 (Table 3.4.1). Residual sugar is the amount of remaining sugar after fermentation has been stopped. More dense wine seems sweeter, more salty, and more acidic wine. Density has a very strong negative correlation with alcohol (% vol.) -0.56 (Figure 3.3.8). High-density wine is more watery wine and has less alcohol. The density of water is higher than the density of alcohol. Density has a negative correlation with pH and quality, with a value of -0.24 (Figure 3.3.8). An increase in density mildly decreases the quality (Figure 3.2.5). More dense wine means more watery wine.

Patterns in pH:

The pH feature is normally distributed (Figure 3.1.9). In the best quality wines rated as 7 or 8, the average pH value is between 3.2 and 3.3 (Figure 3.2.6 and Table 2.2.3). In wine quality, the pH value varies in decimal points. This decimal place variation should not be that much fillable in the tongue. pH has a very strong negative correlation with fixed acidity -0.70 and with citric acid -0.49. This is obvious because a low pH value is more acidic. pH has a mild positive correlation with volatile acidity 0.24 (which is odd) and a mild negative correlation

with density -0.24 (Table 3.4.1). pH has a very weak negative correlation with wine quality, with a value of -0.07 (Table 3.4.1), which is negligible.

Patterns in Sulphates:

Sulphites in wine are used to stop fermentation at a specific point in the winemaking process [1]. It works as an antioxidant and antimicrobial in the wine. Sulphates distribution is slightly right skewed (Figure 3.1.10). The mean, median, and mode are around 0.6 g/dm³. and 75% of the data is within the value of 7 g/dm³ (Figure 3.1.10). Sulphate has a strong negative correlation with volatile acidity -0.31 (Table 3.4.1). Sulphate has a very strong positive correlation with wine quality, with a value of 0.42 (Table 3.4.1). We can say that the higher the amount of sulphate, the higher the wine quality. Which is also supported by other studies in [2][3].

Patterns in alcohol:

Alcohol features distribution is slightly right-skewed (Figure 3.1.11). Alcohol has a very strong negative correlation with density -0.56 (Figure 3.3.8) (Table 3.4.1). Water density is higher than the density of alcohol. An increase in alcohol (% vol.) is a decrease in wine density. So, we can say that high-density wine is more watery wine with less alcohol. Alcohol has a strong negative correlation with chlorides -0.30 (Figure 3.3.5). So, wine with a high percentage of alcohol is less salty and also less in density. As we also observed before in the chart, that increase in alcohol percentage is an increase in the wine quality (Figure 3.2.10). There is a strong positive correlation between alcohol percentage and wine quality, with a value of 0.51 (Table 3.4.1), which is the highest positive correlation of wine quality with other wine features, which is also supported by another analysis [2][3]. In best quality wine, which was rated as 7 or 8, the average alcohol percentage is between 11% and 13% (Figure 3.2.9). We should order a wine where the alcohol percentage is within this range. The best choice could be around 12 (% vol.) alcohol. Alcohol also has a mild positive correlation with sulphates, with a value of 0.27 (Table 3.4.1), and a mild negative correlation with total sulfur dioxide, with a value of -0.27 (Table 3.4.1). It also has a small negative correlation with volatile acidity with a value of -0.22 (Table 3.4.1).

Summary of the patterns and impact on quality:

Most of the wine's quality is either 5 (with 438 observations) or 6 (with 429 observations) (Table 3.2.1). There are only 03 observations of wine quality of level 3, which is not enough to come up with any decision for this type (level 3) of wine. We have 117 observations of level-7 wine and 11 observations of level-8-rated wine (Table 3.2.1).

Red wine quality has the strongest positive correlation with alcohol (% vol.), with a value of 0.51 (Figure 3.3.11). It makes sense that a higher amount of alcohol (% vol.) would bring better customer satisfaction. That is also supported by other analyses [2][3]. Additionally, a simple regression model with alcohol (independent variable) and wine quality (dependent variable) showed that the alcohol variable is statistically significant (Table 3.5.11), and by the R-squared value, this simple regression model with alcohol variable explains about 26% of the data (which is the highest compared to the other independent wine features). So, alcohol (% vol.) is the most important physicochemical characteristic of red wine quality.

Subsequently, the second strongest correlation of wine quality is with the sulphates additive, with a positive value of 0.41. It seems like people rate the wine higher quality when more sulphate additives are added to the wine-making process. Moreover, a simple regression model with sulphates (independent variable) and wine quality (dependent variable) exhibited that the sulphates variable is statistically significant (Table 3.5.10), and by the R-squared value, this simple regression model with sulphates variable explains about 18% of the data (which is the second highest value among the independent features). Therefore, sulphate is the second most important physicochemical characteristic of red wine.

Next, wine quality has the third strongest correlation with the volatile acidity with a negative value of -0.35. This was expected because too high acetic acid (g/dm3) can lead to an unpleasant vinegar taste. The lesser the amount of volatile acidity, the greater the wine quality. which is also supported by other studies [2][3]. Additionally, a simple regression model with volatile acidity (independent variable) and wine quality (dependent variable) showed that the volatile acidity variable is statistically significant (Table 3.5.2), and by the R-squared value, this simple regression model with volatile acidity variable explains about 12% of the data (which is the third highest value among the independent features). Therefore, volatile acidity negatively plays the third most important role in wine quality.

The fourth highest correlated value with quality is with the density, which is a mild negative correlation, with a value of -0.24. Moreover, a simple regression model with density (independent variable) and quality (dependent variable) showed that the density variable is statistically significant (Table 3.5.8), and by the R-squared value, the regression model with density variable explains only 6% of the data (which is the fourth highest value among the independent features). Therefore, Wine density is the fourth most important factor for the red wine quality.

After that, wine quality has a mild positive correlation with citric acid 0.22. Even though it adds freshness and flavor to wines, in a simple regression model with quality (dependent variable) and citric acid (independent

variable), by the R-squared value, the citric acid variable explains only 5% of the data, which is the fifth-highest value among the independent variables. The possible reason is that it exists in a very small amount in the wine (Table 3.1.3).

Wine quality also has a very weak negative correlation with the pH score with a value of -0.07, and in the simple regression model with quality (dependent variable) and pH (independent variable), by the R-squared value, the pH variable explains about only 0.5% of the data, which is very small.

5. Discussion

Assumption 01:

As presented in Section 2.3, I initially assumed that since the amount of fixed acidity is the highest quantity among all other types of acid (volatile acidity and citric acid (Table 2.2.2)) and since it does not evaporate readily (non-volatile). It will dominate the pH level. An increase in fixed acidity will make the wine sourer. Also, it could decrease the wine quality. After analyzing the data, I have found that fixed acidity dominates the pH level significantly. Fixed acidity has a very strong negative correlation value with a pH score of -0.70. In fact, it is the highest correlated feature among the features. This means that I was also correct that an increase in fixed acidity will make the wine sourer. However, I was wrong about an increase in fixed acidity, which will decrease the wine quality. However, fixed acidity has a very little positive correlation with the wine quality, with a value of 0.11 (Figure 3.3.1), which means the increase of fixed acidity will increase the wine quality slightly. The correlation is very weak even though the assumption was quite the opposite.

Moreover, as presented in Table 3.5.1, a simple regression model with fixed acidity (independent variable) and wine quality (dependent variable) showed that the fixed acidity variable is statistically significant. By the R-squared value, the regression model with fixed acidity variable explains about 01% of the data. So, I was partly right about my 1st assumption.

Assumption 02:

My second assumption was that since the high amount of volatile acidity in wine (acetic acid) produces an unpleasant vinegar flavor (Cortez et al. (2009).) so, the increase of volatile acidity will decrease the wine quality. After analyzing the data, I have found that there is a strong negative correlation between volatile acidity and wine quality, with a value of -0.35 (Table 3.3.2). As presented in Table 3.5.2, a simple regression model with volatile acidity (independent variable) and wine quality (dependent variable) showed that the volatile acidity variable is statistically significant. By the R-squared value, this simple regression model with volatile acidity variable explains about 12% of the data. Thus, it proves my assumption to be true.

Assumption 03:

My third assumption was also proved true: increased citric acid will increase the wine quality.

In red wine, citric acid is present in a very small amount in the wine (Table 2.2.2). Around 9% of red wine has no citric acid in it. After removing the outliers, there are only 03 observations of wine quality of level 3. This is not enough observation to come to any conclusion for level 3 wine. In level 3 wine, we saw that an increase in it decreased the quality. But from the rest of the data, we can see that the greater the amount of citric acid, the greater the quality (Figure 3.2.3). Also, the highest amount of citric acid is 0.73, which was found in a level 6-rated wine. There is very little chance that a higher value can reduce the wine quality heavily. Since, it is generally present in wine with a very small amount. As per the analysis, there is a mild positive correlation between citric acid and wine quality, with a value of 0.22 (Table 3.4.1). Moreover, as presented in Table 3.5.3, a simple regression model with citric acid (independent variable) and wine quality (dependent variable) showed that the citric acid variable is statistically significant. By the R-squared value, this simple regression model with citric acid variable explains about 5% of the data.

Assumption 04:

My fourth assumption was proved as partly true that an increase of different acid substances (fixed acidity, volatile acidity, and citric acid) will decrease the wine's pH score/level, and since a low score of pH value is very acidic and very sour thus poor in wine quality. pH has a very strong negative correlation with fixed acidity with a value of -0.70 and with citric acid -0.49 (Table 3.4.1). But pH has a mild positive correlation with volatile acidity with a value of 0.24 (Table 3.4.1), which seems odd. In wine quality, the pH value varies in decimal point (Figure 3.2.6) (Table 2.2.2). The decimal fraction variation should not be that noticeable in the tongue. Red wine is mild in the sour/acidic test (Figure 3.2.8). An increase by decimal point, the pH value will cause very little decrease in the wine quality (Figure 3.2.6).

The pH has a minimal negative correlation with the wine quality, with a value of -0.07 (Table 3.4.1), which is a very weak correlation. Additionally, as presented in Table 3.5.9, a simple regression model with pH (independent variable) and wine quality (dependent variable) showed that the pH variable is statistically significant. By the R-squared value, this simple regression model with pH variable explains only about 0.5% of the data.

Assumption 05:

My fifth assumption was proven partly true. I assumed that an increase in residual sugar would increase the wine density. More residual sugar will be more watery wine with a lesser alcohol percentage. An increase in the amount of residual sugar will decrease the wine quality. Residual sugar has a very strong positive correlation with density with a value of 0.40 (Figure 3.3.4). So, I was right. Alcohol is less dense than water. So, more residual sugar is more watery wine. Residual sugar has a very weak positive correlation with alcohol, with a value of 0.08 (Table 3.4.1). This is the opposite of my initial assumption that more residual sugar will be with a lesser alcohol percentage. Residual sugar has a negligible positive correlation with the wine quality, with value of 0.02 (Table 3.3.11). This is a very weak correlation. Additionally, as presented in Table 3.5.4, a simple regression model with residual sugar (independent variable) and wine quality (dependent variable) showed that the residual sugar variable is not statistically significant.

Assumption 06:

My sixth assumption was true. An increase in chlorides can lead to a decrease in quality. More chlorides mean more saltier wine. Chlorides have a strong positive correlation with density, with a value of 0.43 (Figure 3.3.5). It has a strong negative correlation with alcohol -0.30 (Figure 3.3.5). More salty wine means higher in density and lower in alcohol percentage. Chloride has a small negative correlation with wine quality, with a value of -0.18 (Table 3.3.11). Furthermore, as presented in Table 3.5.5, a simple regression model with chlorides (independent variable) and wine quality (dependent variable) showed that the chlorides variable is statistically significant. By the R-squared value, this simple regression model with chloride variable explains about 3% of the data.

Assumption 07:

My seventh assumption was true. An increase in density will decrease the wine quality. At room temperature, the alcohol density is around 0.79 g/cm3, and water density is around 0.99 g/cm3. An increase in density means more watery wine. Density has a very high positive correlation with fixed acidity with a value of 0.61, residual sugar 0.40, and chlorides 0.43 (Table 3.4.1). Density also has a negative correlation with pH, with a value of -0.24 (Figure 3.4.1). More dense wine seems sweeter, saltier, more watery, and more acidic/sour wine. Density strongly correlates negatively with an alcohol percentage of -0.56 (Figure 3.3.8). High-density wine is more watery wine and has less alcohol. In Figure 3.2.5, the increase in density decreases in quality. Density negatively correlates with wine quality, with a value of -0.24 (Figure 3.3.8). In addition, as presented in Table 3.5.8, a simple regression model with density (independent variable) and wine quality (dependent variable) showed that the density variable

is statistically significant. By the R-squared value, this simple regression model with density variable explains about 6% of the data.

Assumption 08:

Finally, my eighth assumption was true that an increase in alcohol percentage would increase the wine quality. Alcohol has a very strong negative correlation with density -0.56 (Figure 3.3.8) (Table 3.4.1). An increase in alcohol percentage is a decrease in wine density. High-density wine is more watery wine. Alcohol has a strong negative correlation with chlorides -0.30 (Figure 3.3.5). A high percentage of alcohol in wine is less salty. According to Figure 3.2.10, an increase in average alcohol percentage is an increase in the wine quality. There is a very high positive correlation between alcohol percentage and wine quality, with a value of 0.51 (Table 3.4.1), which is the highest positive correlation of wine quality among all the wine features. Besides, as presented in Table 3.5.11, a simple regression model with alcohol (independent variable) and wine quality (dependent variable) showed that the alcohol variable is statistically significant. By the R-squared value, this simple regression model with the alcohol variable explains about 26% of the data.

6. Conclusion

In 2023, the wine market revenue amounted to USD 333.00 billion. The wine market is expected to grow annually by 5.52% (CAGR 2023-2027) [4]. As a result, companies are trying to acquire new technologies to progress wine production, quality, and sales. Quality certification is a vital phase in all the processes, which now relies heavily on experienced human wine tasting. I looked for a method that would allow me to evaluate red wines scientifically using their physicochemical properties. A sizable dataset (1599 red observations) was considered, including Vinho Verde samples from Portugal's northwest through Kaggle [1]. Firstly, data quality has been checked, and some data preprocessed. After that, I have made some assumptions and hypotheses. To check assumptions and hypotheses, I have done Exploratory Data analysis (EDA) on the data and look for different Trends, Patterns, and Anomalies in the data. I have also done different Simple and Multiple Linear Regressions where quality was always the dependent variable. The multiple linear regression model explains almost 0.389 (39%) of the variability of the wine quality.

Businesses can use this analysis report before ordering red wine in large quantities as this analysis will help to evaluate the red wine quality based on its physicochemical properties and could be a great help for the businesses to ensure choosing red wine of good quality and thus could maintain a good business. For instance, as identified in this analysis, alcohol quantity is the most important substance for red wine quality. The business should give more emphasis on the alcohol quantity. For the best rating, they should collect wine, where the

alcohol percentage is around 12%. Sulphate additives play the second most important role in wine quality. Both in the production level and collection phase, this should be the second most considerable factor. Since volatile acidity negatively plays the third most important role in wine quality, it could lead to an unpleasant vinegar taste. Businesses keep an eye on it's (acetic acid)/dm3) quantity in the wine. Wine density is the fourth most important factor for red wine quality.

Wine manufacturers can also use the results of this analysis to enhance the wine's quality because some production-related elements are controllable. For instance, by keeping an eye on the sugar content of the grapes before harvest, the alcohol percentage can be raised or lowered. Additionally, the residual sugar in wine may be controlled by stopping the yeast's process of fermenting sugar by sulphates.

7. References

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