CSE 309 (Compilers) Basic Concepts of Parsing in Compiler

Dr. Muhammad Masroor Ali

Professor
Department of Computer Science and Engineering
Bangladesh University of Engineering and Technology
Dhaka-1205, Bangladesh

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Top-Down Parsing

We introduce top-down parsing by considering a grammar that is well-suited for this class of methods.

```
stmt \rightarrow expr;
| if (expr) stmt
| for (optexpr; optexpr; optexpr) stmt
| other

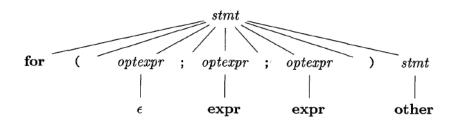
exptexpr \rightarrow \epsilon
| expr
```

- The grammar generates a subset of the statements of C or Java.
- We use the boldface terminals if and for for the keywords "if" and "for", respectively, to emphasize that these character sequences are treated as units, i.e., as single terminal symbols.

```
stmt \rightarrow expr;
| if (expr) stmt
| for (optexpr; optexpr; optexpr) stmt
| other

optexpr \rightarrow \epsilon
| expr
```

- Further, the terminal **expr** represents expressions.
- A more complete grammar would use a nonterminal expr and have productions for nonterminal expr.
- Similarly, other is a terminal representing other statement constructs.



A parse tree according to the grammar

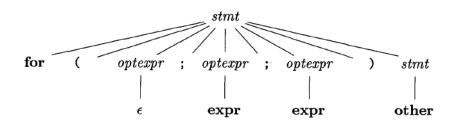
■ The top-down construction of a parse tree is done by starting with the root, labeled with the starting nonterminal *stmt*, and repeatedly performing the following two steps.

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stmt \rightarrow expr;
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A grammar for some statements in C and Java

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A parse tree according to the grammar

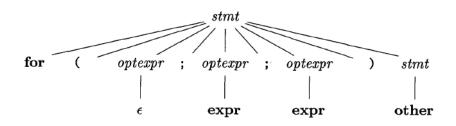
1. At node *N*, labeled with nonterminal *A*, select one of the productions for *A* and construct children at *N* for the symbols in the production body.

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A grammar for some statements in C and Java

1. At node *N*, labeled with nonterminal *A*, select one of the productions for *A* and construct children at *N* for the symbols in the production body.



A parse tree according to the grammar

2. Find the next node at which a subtree is to be constructed, typically the leftmost unexpanded nonterminal of the tree.

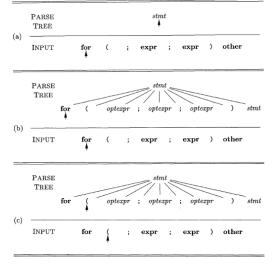
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```

A grammar for some statements in C and Java

2. Find the next node at which a subtree is to be constructed, typically the leftmost unexpanded nonterminal of the tree.

- For some grammars, the above steps can be implemented during a single left-to-right scan of the input string.
- The current terminal being scanned in the input is frequently referred to as the lookahead symbol.
- Initially, the lookahead symbol is the first, *i.e.*, leftmost terminal of the input string.

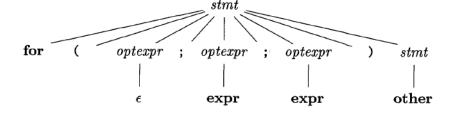


Top-down parsing while scanning the input from left to right

 Figure illustrates the construction of the parse tree in for the input string

for (; expr; expr) other





A parse tree according to the grammar

■ Figure illustrates the construction of the parse tree in for the input string

```
for (; expr; expr) other
```



```
PARSE TREE

(a)

INPUT for ( ; expr ; expr ) other

stmt

st
```

```
stmt → expr;

| if (expr) stmt

| for (optexpr; optexpr; optexpr) stmt

| other

optexpr → ε

| expr
```

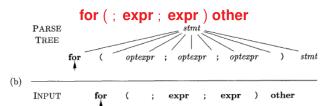
- Initially, the terminal for is the lookahead symbol, and the known part of the parse tree consists of the root, labeled with the starting nonterminal stmt.
- The objective is to construct the remainder of the parse tree in such a way that the string generated by the parse tree matches the input string.

```
PARSE TREE

(a) INPUT for ( ; expr ; expr ) other
```

- For a match to occur, the nonterminal stmt in must derive a string that starts with the lookahead symbol for.
- In the grammar, there is just one production for stmt that can derive such a string, so we select it, and construct the children of the root labeled with the symbols in the production body.
- This expansion of the parse tree is shown in (b).



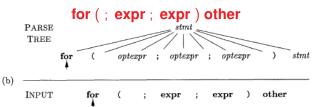


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| if (expr) stmt

| for (optexpr; optexpr; optexpr) stmt

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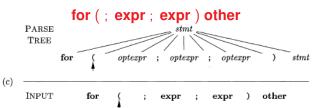
expr

- Each of the three snapshots has arrows marking the lookahead symbol in the input and the node in the parse tree that is being considered.
- Once children are constructed at a node, we next consider the leftmost child.
- In (b), children have just been constructed at the root, and the leftmost child labeled with for is being considered.

for (; expr; expr) other

```
stmt \rightarrow \exp r;
| if (expr) stmt
| for (optexpr; optexpr; optexpr) stmt
| other
```

- When the node being considered in the parse tree is for a terminal, and the terminal matches the lookahead symbol, then we advance in both the parse tree and the input.
- The next terminal in the input becomes the new lookahead symbol, and the next child in the parse tree is considered.



```
stmt → expr;

| if (expr) stmt

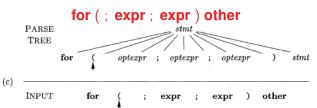
| for (optexpr; optexpr; optexpr) stmt

| other

optexpr → ε

| expr
```

- In (c), the arrow in the parse tree has advanced to the next child of the root, and the arrow in the input has advanced to the next terminal, which is (.
- A further advance will take the arrow in the parse tree to the child labeled with nonterminal optexpr and take the arrow in the input to the terminal;



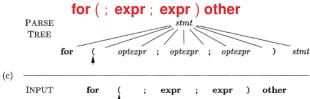
```
stmt \rightarrow \exp r;

| if (expr) stmt

| for (optexpr; optexpr; optexpr) stmt

| other
```

- At the nonterminal node labeled optexpr, we repeat the process of selecting a production for a nonterminal.
- Productions with ϵ as the body (" ϵ -productions") require special treatment.
- For the moment, we use them as a default when no other production can be used.



expr

■ With nonterminal *optexpr* and lookahead;, the ε-production is used, since; does not match the only other production for *optexpr*, which has terminal **expr** as its body.

- In general, the selection of a production for a nonterminal may involve trial- and-error.
- That is, we may have to try a production and backtrack to try another production if the first is found to be unsuitable.
- A production is unsuitable if, after using the production, we cannot complete the tree to match the input string.
- Backtracking is not needed, however, in an important special case called predictive parsing.

Predictive Parsing

- Recursive-descent parsing is a top-down method of syntax analysis in which a set of recursive procedures is used to process the input.
- One procedure is associated with each nonterminal of a grammar.
- Here, we consider a simple form of recursive-descent parsing, called predictive parsing, in which the lookahead symbol unambiguously determines the flow of control through the procedure body for each nonterminal.
- The sequence of procedure calls during the analysis of an input string implicitly defines a parse tree for the input, and can be used to build an explicit parse tree, if desired.

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```
void stmt() {
      switch ( lookahead ) {
      case expr:
             match(expr); match(';'); break;
      case if:
             match(if); match('('); match(expr); match(')'); stmt();
             break:
      case for:
             match(for); match('(');
             optexpr(); match(';'); optexpr(); match(';'); optexpr();
             match(')'); stmt(); break;
      case other;
             match(other); break;
      default:
             report("syntax error");
void optexpr()
      if ( lookahead == expr ) match(expr):
void match(terminal t) {
      if ( lookahead == t ) lookahead = nextTerminal;
      else report("syntax error");
```

Pseudocode for a predictive parser

The predictive parser consists of procedures for the nonterminals stmt and optexpr of the grammar and an additional procedure match, used to simplify the code for stmt and optexpr.

40) 40) 45) 45)

```
stmt \rightarrow expr;
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```
void match(terminal t) {
    if ( lookahead == t ) lookahead = nextTerminal;
    else report("syntax error");
}
```

- Procedure match(t) compares its argument t with the lookahead symbol and advances to the next input terminal if they match.
- Thus match changes the value of variable lookahead, a global variable that holds the currently scanned input terminal.

```
void stmt()  {
      switch ( lookahead ) {
      case expr:
             match(expr); match(';'); break;
      case if:
             match(if); match('('); match(expr); match(')'); stmt();
             break;
      case for:
             match(for); match('(');
             optexpr(); match(';'); optexpr(); match(';'); optexpr();
             match(')'; stmt(); break;
      case other;
             match(other); break;
      default:
             report("syntax error");
```

Parsing begins with a call of the procedure for the starting nonterminal stmt.

```
void stmt()  {
      switch ( lookahead ) {
      case expr:
             match(expr); match(';'); break;
      case if:
             match(if); match('('); match(expr); match(')'); stmt();
             break;
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             match(')'; stmt(); break;
      case other;
             match(other); break;
      default:
             report("syntax error");
```

■ With the input **for** (; **expr**; **expr**) **other**, lookahead is initially the first terminal **for**.

```
void stmt()  {
      switch ( lookahead ) {
      case expr:
             match(expr); match(';'); break;
      case if:
             match(if); match('('); match(expr); match(')'); stmt();
             break;
      case for:
             match(for); match('(');
             optexpr(); match(';'); optexpr(); match(';'); optexpr();
             match(')'; stmt(); break;
      case other;
             match(other); break;
      default:
             report("syntax error");
```

Procedure stmt executes code corresponding to the production

```
stmt \rightarrow for (optexpr; optexpr; optexpr) stmt
```

```
void stmt()  {
      switch ( lookahead ) {
      case expr:
              match(expr); match(';'); break;
      case if:
              match(\mathbf{if}); match('('); match(\mathbf{expr}); match(')'); stmt();
              break:
       case for:
              match(for); match('(');
              optexpr(); match(';'); optexpr(); match(';'); optexpr();
              match(')'; stmt(); break;
       case other;
              match(other); break;
       default:
              report("syntax error");
```

In the code for the production body — that is, the for case of procedure stmt— each terminal is matched with the lookahead symbol.

```
void stmt()  {
      switch ( lookahead ) {
      case expr:
              match(expr); match(';'); break;
       case if:
              match(\mathbf{if}); match('('); match(\mathbf{expr}); match(')'); stmt();
              break:
       case for:
              match(for); match('(');
              optexpr(); match(';'); optexpr(); match(';'); optexpr();
              match(')'); stmt(); break:
       case other;
              match(other); break;
       default:
              report("syntax error");
```

Each nonterminal leads to a call of its procedure, in the following sequence of calls:
match(for); match('(');
 optexpr(); match(';'); optexpr(); match(';'); optexpr();
 match(')'); stmt();

- Predictive parsing relies on information about the first symbols that can be generated by a production body.
- More precisely, let α be a string of grammar symbols (terminals and/or nonterminals).
- We define FIRST(α) to be the set of terminals that appear as the first symbols of one or more strings of terminals generated from α .
- If α is ϵ or can generate ϵ , then ϵ is also in FIRST(α).

- Here, we shall just use ad hoc reasoning to deduce the symbols in FIRST(α).
- Typically, α will either begin with a terminal, which is therefore the only symbol in FIRST(α).
- Or α will begin with a nonterminal whose production bodies begin with terminals, in which case these terminals are the only members of FIRST(α).

```
stmt \rightarrow expr;
| if (expr) stmt
| for (optexpr; optexpr; optexpr) stmt
| other

optexpr \rightarrow \epsilon
| expr
```

- With respect to the grammar, the following are correct calculations of FIRST.
 - FIRST(*stmt*) = {expr, if, for, other}
 - FIRST(expr;) = {expr}

Predictive Parsing — continued

- The FIRST sets must be considered if there are two productions $A \rightarrow \alpha$, and $A \rightarrow \beta$.
- Ignoring *ϵ*-productions for the moment, predictive parsing requires FIRST(*α*) and FIRST(*β*) to be disjoint.
- The lookahead symbol can then be used to decide which production to use.
- If the lookahead symbol is in FIRST(α), then α is used.
- Otherwise, if the lookahead symbol is in FIRST(β), then β is used.

```
void optexpr() {
     if ( lookahead == expr ) match(expr);
}
```

- Our predictive parser uses an ϵ -production as a default when no other production can be used.
- With the input for (; expr; expr) other, after the terminals for and (are matched, the lookahead symbol is;.

```
void optexpr() {
    if ( lookahead == expr ) match(expr);
}
```

At this point procedure optexpr is called, and the code if (lookahead == expr) match(expr); in its body is executed.

```
void optexpr() {
    if ( lookahead == expr ) match(expr);
}
```

- Nonterminal *optexpr* has two productions, with bodies **expr** and ϵ .
- The lookahead symbol ";" does not match the terminal expr, so the production with body expr cannot apply.

```
void optexpr() {
     if ( lookahead == expr ) match(expr);
}
```

- In fact, the procedure returns without changing the lookahead symbol or doing anything else.
- Doing nothing corresponds to applying an ϵ -production.

When to Use ϵ -Productions — *continued*

More generally, consider a variant of the productions where *optexpr* generates an expression nonterminal instead of the terminal **expr**:

$$\begin{array}{ccc} \textit{optexpr} & \rightarrow & \textit{expr} \\ & | & \epsilon \end{array}$$

- Thus, *optexpr* either generates an expression using nonterminal *expr* or it generates ϵ .
- While parsing *optexpr*, if the lookahead symbol is not in FIRST(*expr*) then the ϵ -production is used.

Designing a Predictive Parser

- A predictive parser is a program consisting of a procedure for every nonterminal.
- The procedure for nonterminal *A* does two things.
- 1. It decides which *A*-production to use by examining the lookahead symbol.

The production with body α (where α is not ϵ , the empty string) is used if the lookahead symbol is in FIRST(α).

If there is a conflict between two nonempty bodies for any lookahead symbol, then we cannot use this parsing method on this grammar.

In addition, the ϵ -production for A, if it exists, is used if the lookahead symbol is not in the FIRST set for any other production body for A.

Designing a Predictive Parser

- A predictive parser is a program consisting of a procedure for every nonterminal.
- The procedure for nonterminal *A* does two things.
- 2. The procedure then mimics the body of the chosen production.

That is, the symbols of the body are "executed" in turn, from the left.

A nonterrninal is "executed" by a call to the procedure for that nonterminal, and a terminal matching the lookahead symbol is "executed" by reading the next input symbol.

If at some point the terminal in the body does not match the lookahead symbol, a syntax error is reported.

```
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A grammar for some statements in C and Java

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Pseudocode for a predictive parser

Designing a Predictive Parser — continued

- Just as a translation scheme is formed by extending a grammar, a syntax-directed translator can be formed by extending a predictive parser.
- The following limited construction suffices for the present:
 - Construct a predictive parser, ignoring the actions in productions.
 - Copy the actions from the translation scheme into the parser.
 - If an action appears after grammar symbol X in production p, then it is copied after the implementation of X in the code for p.
 - Otherwise, if it appears at the beginning of the production, then it is copied just before the code for the production body.

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Left Recursion

- It is possible for a recursive-descent parser to loop forever.
- A problem arises with "left-recursive" productions like

$$expr \rightarrow expr + term$$

where the leftmost symbol of the body is the same as the nonterminal at the head of the production.

- Suppose the procedure for expr decides to apply this production.
- The body begins with *expr* so the procedure for *expr* is called recursively.
- Since the lookahead symbol changes only when a terminal in the body is matched, no change to the input took place between recursive calls of expr.
- As a result, the second call to *expr* does exactly what the first call did, which means a third call to *expr*, and so on, forever.

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- A left-recursive production can be eliminated by rewriting the offending production.
- Consider a nonterminal A with two productions

$$A \rightarrow A\alpha \mid \beta$$

where α and β are sequences of terminals and nonterminals that do not start with A.

For example, in

$$\textit{expr} \rightarrow \textit{expr} + \textit{term} \mid \textit{term}$$

nonterminal A = expr, string $\alpha = +term$, and string $\beta = term$.

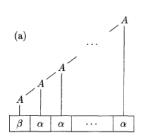


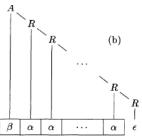
$$A \rightarrow A\alpha \mid \beta$$

■ The nonterminal A and its production are said to be left recursive, because the production $A \to A\alpha$ has A itself as the leftmost symbol on the right side.

$$A \rightarrow A\alpha \mid \beta$$

■ Repeated application of this production builds up a sequence of α 's to the right of A.





Left- and right-recursive ways of generating a string

■ When A is finally replaced by β , we have β followed by a sequence of zero or more α 's.

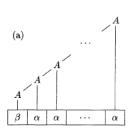
$$A \rightarrow A\alpha \mid \beta$$

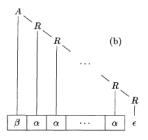
■ The same effect can be achieved, by rewriting the productions for *A* in the following manner, using a new nonterminal *R*:

$$A \rightarrow \beta R$$
 $R \rightarrow \alpha R \mid \epsilon$

$$A \rightarrow \beta R$$
 $R \rightarrow \alpha R \mid \epsilon$

Right-recursive productions lead to trees that grow down towards the right.





Left- and right-recursive ways of generating a string

End of Slides

