

CSE 103
DISCRETE MATHEMATICS

Chapter : 1 , Section : 1

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Question :

33. Construct a truth table for each of these compound propositions.

a) $(p \vee q) \rightarrow (p \oplus q)$ **b)** $(p \oplus q) \rightarrow (p \wedge q)$

c) $(p \vee q) \oplus (p \wedge q)$ **d)** $(p \leftrightarrow q) \oplus (\neg p \leftrightarrow q)$

e) $(p \leftrightarrow q) \oplus (\neg p \leftrightarrow \neg r)$

f) $(p \oplus q) \rightarrow (p \oplus \neg q)$

Answer:

To construct the truth table for a compound proposition, we work from the inside out. In each case, we will

show the intermediate steps. In part (a), for example, we first construct the truth table for $p \vee q$, then the

truth table for $p \oplus q$, and finally combine them to get the truth table for $(p \vee q) \rightarrow (p \oplus q)$. For parts (a),

(b), and (c) we have the following table (column five for part (a), column seven for part (b), column eight

for part (c)).

$p \quad q \quad p \vee q \quad p \oplus q \quad (p \vee q) \rightarrow (p \oplus q) \quad p \wedge q \quad (p \oplus q) \rightarrow (p \wedge q) \quad (p \vee q) \oplus (p \wedge q)$

T T T F F T T F

T F T T T F F T

F T T T T F F T

F F F F T F T F

For part (d) we have the following table.

$p \quad q \quad \neg p \quad \neg q \quad p \leftrightarrow q \quad \neg p \leftrightarrow \neg q \quad (p \leftrightarrow q) \oplus (\neg p \leftrightarrow \neg q)$

T T F T F T

T F F F T T

F T T F T T

F F T T F T

For part (e) we need eight rows in our truth table, because we have three variables.

$p \quad q \quad r \quad \neg p \quad \neg q \quad \neg r \quad (p \leftrightarrow q) \oplus (\neg p \leftrightarrow \neg r)$

T T T F F T T F

T T F F T T F T

T F T F F F T T

T F F F T F F F

F T T T F F F F

F T F T T F T T

F F T T F T F T

F F F T T T T F

For part (f) we have the following table.

$p \quad q \quad \bullet q \quad p \text{ EB } q \quad p \text{ EB } \bullet q \quad (p \text{ EB } q) \rightarrow (p \text{ EB } \bullet q)$

T T F F T T

T F T T F F

F T F T F F

F F T F T T