

NCSU ST 503 Discussion 8

Problem 10.6 Faraway, Julian J. Linear Models with R CRC Press.

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10.6 Model Selection with the hipcenter data.

Use the seatpos data with hipcenter as the response.

(a) Fit a model with all eight predictors. Comment on the effect of leg length on the response.

```
##
## Call:
## lm(formula = hipcenter ~ ., data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -73.827 -22.833  -3.678  25.017  62.337
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  436.43213   166.57162    2.620   0.0138 *
## Age           0.77572     0.57033    1.360   0.1843
## Weight        0.02631     0.33097    0.080   0.9372
## HtShoes      -2.69241     9.75304   -0.276   0.7845
## Ht            0.60134    10.12987    0.059   0.9531
## Seated        0.53375     3.76189    0.142   0.8882
## Arm          -1.32807     3.90020   -0.341   0.7359
## Thigh        -1.14312     2.66002   -0.430   0.6706
## Leg          -6.43905     4.71386   -1.366   0.1824
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 37.72 on 29 degrees of freedom
## Multiple R-squared:  0.6866, Adjusted R-squared:  0.6001
## F-statistic:  7.94 on 8 and 29 DF,  p-value: 1.306e-05
```

We note that leg length is significant at a level of $\alpha = 0.018$ and it has a negative association with the response.

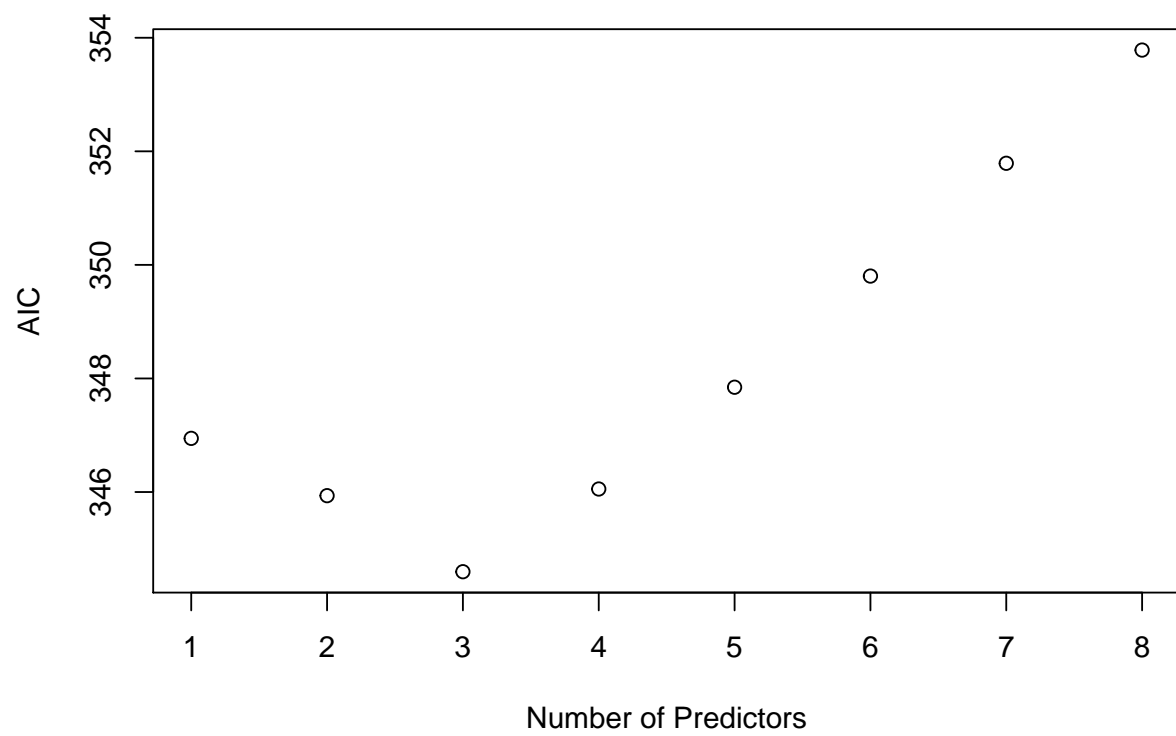
(b) Compute a 95% prediction interval for the mean value of the predictors.

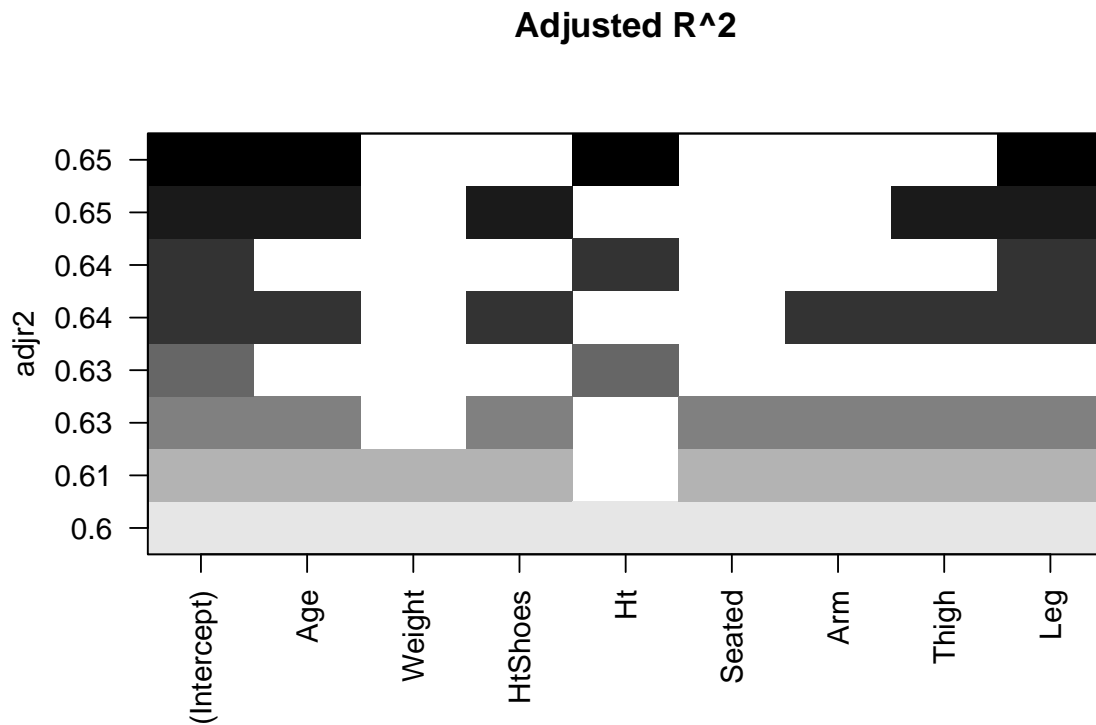
| ## | fit | lwr | upr |
|------|-----------|---------|-----------|
| ## 1 | -164.8849 | -243.04 | -86.72972 |

| pi.width |
|----------|
| 156.3 |

(c) Use AIC to select a model. Now interpret the effect of leg length and compute the prediction interval. Compare the conclusions from the two models.

| ## | (Intercept) | Age | Weight | HtShoes | Ht | Seated | Arm | Thigh | Leg |
|------|-------------|-------|--------|---------|-------|--------|-------|-------|-------|
| ## 1 | TRUE | FALSE | FALSE | FALSE | TRUE | FALSE | FALSE | FALSE | FALSE |
| ## 2 | TRUE | FALSE | FALSE | FALSE | TRUE | FALSE | FALSE | FALSE | TRUE |
| ## 3 | TRUE | TRUE | FALSE | FALSE | TRUE | FALSE | FALSE | FALSE | TRUE |
| ## 4 | TRUE | TRUE | FALSE | TRUE | FALSE | FALSE | FALSE | TRUE | TRUE |
| ## 5 | TRUE | TRUE | FALSE | TRUE | FALSE | FALSE | TRUE | TRUE | TRUE |
| ## 6 | TRUE | TRUE | FALSE | TRUE | FALSE | TRUE | TRUE | TRUE | TRUE |
| ## 7 | TRUE | TRUE | TRUE | TRUE | FALSE | TRUE | TRUE | TRUE | TRUE |
| ## 8 | TRUE | TRUE | TRUE | TRUE | TRUE | TRUE | TRUE | TRUE | TRUE |





We see that $hipcenter \sim +age + ht + Leg$ is the model with the lowest AIC. We also plot the Adjusted R^2 of the models.

```
##
## Call:
## lm(formula = hipcenter ~ Age + Ht + Leg, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -79.715 -22.758  -4.102   21.394   60.576
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  452.1976    100.9482   4.480 8.04e-05 ***
## Age           0.5807     0.3790   1.532  0.1347
## Ht          -2.3254     1.2545  -1.854  0.0725 .
## Leg          -6.7390     4.1050  -1.642  0.1099
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 35.12 on 34 degrees of freedom
```

```
## Multiple R-squared:  0.6814, Adjusted R-squared:  0.6533
## F-statistic: 24.24 on 3 and 34 DF,  p-value: 1.426e-08
```

Leg now has a p-value of 0.1099

```
##          fit          lwr          upr
## 1 -164.8849 -237.192 -92.57771
```

| | |
|--|----------|
| | pi.width |
| | 144.6 |

As expected our prediction interval has decreased in width. Ht is now significant at 0.07 which is a dramatic change. We presume this is due to linear association among the predictors.