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## 13. Exercise: Nonmonotonic functions

Exercises due Mar 25, 2020 05:29 IST Completed

### Exercise: Nonmonotonic functions

4/4 points (graded)

Suppose that  $X$  is a continuous random variable and that  $Y = X^4$ . Then, for  $y \geq 0$ , we have

$$f_Y(y) = ay^b f_X(-cy^d) + ay^b f_X(cy^d),$$

for some  $a, b, d$ , and some  $c > 0$ . Find  $a, b, c$ , and  $d$ .

$a =$   ✓ Answer: 0.25

$b =$   ✓ Answer: -0.75

$c =$   ✓ Answer: 1

$d =$   ✓ Answer: 0.25

#### Solution:

We have, for  $y \geq 0$ ,

$$F_Y(y) = \mathbf{P}(Y \leq y) = \mathbf{P}(X^4 \leq y) = \mathbf{P}(-y^{1/4} \leq X \leq y^{1/4}) = F_X(y^{1/4}) - F_X(-y^{1/4}).$$

By differentiating, and using also the chain rule, we obtain


$$f_Y(y) = f_X(y^{1/4}) \cdot \frac{1}{4} \cdot y^{-3/4} + f_X(-y^{1/4}) \cdot \frac{1}{4} \cdot y^{-3/4}.$$



Therefore,  $a = 1/4$ ,  $b = -3/4$ ,  $c = 1$ , and  $d = 1/4$ .

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You have used 2 of 3 attempts

 Answers are displayed within the problem


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 Multiple possible answers?

When I solved this exercise, I saw that  $c$  can have two possible values. Namely, the only thing that matters he...

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