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## 9. Exercise: More on fresh start

Exercises due May 13, 2020 05:29 IST Completed

Exercise: More on fresh start

1/1 point (graded)

Consider a Bernoulli process with parameter p=1/3. Let  $T_1$  be the time of the first success and let  $T_1 + T_2$  be the time of the second success. We are told that the results of the two slots that follow the first success are failures, so that  $X_{T_1+1}=X_{T_1+2}=0$ . What is the conditional expectation of the second interarrival time,  $T_2$ , given this information? (Recall that the expectation of a geometric random variable with parameter p is equal to 1/p.)

5

✓ Answer: 5

## Solution:

After time  $T_1$ , we have two failures, and these are part of the interarrival time  $T_2$ . Given this information, the process starts fresh at time  $T_1+3$  and the number of trials from time  $T_1+3$  onwards until the next success is geometric with parameter 1/3, and has an expected value of 3. Therefore, the conditional expectation of  $T_2$ , given the information we were given, is 2+3=5.

Submit

You have used 1 of 3 attempts

**1** Answers are displayed within the problem

## Discussion

**Hide Discussion** 

Topic: Unit 9: Bernoulli and Poisson processes:Lec. 21: The Bernoulli process / 9. Exercise: More on fresh start





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|----------|--|--------------|------|
| 2        | Even after reading the solution I have no idea why the answer is what it is.  Can someone post a more detailed explanation of the solution after the homework due date? I'm to | tally        | 1    |
| ?        | Does the time count from 0 or 1?  I looked at the answer and now supposing that my answer was wrong due to I didn't get at what time   | <u>e do</u>  | 1    |
| 2        | Well I completely ignored the pt of this excercise  Thinking was right, reading was careless>> interarrival TIME (for those who want to avoid my mista                         | ake)         | 3    |
| 2        | Hint - Another approach from the solution printed  | 2 new_       | 6    |
| ₹        | Unit of time? What is the unit of time that we should consider in this problem? It is **not mentioned** in the problem?  | olem         | 2    |
| <b>∀</b> | Final exam date?  Does anyone know when the final exam will be out? I thought it was supposed to be available on the   | <u>: 30t</u> | 3    |
| Q        | <u>Hint</u>  |              | 4    |
| ?        | Is the answer supposed to be a number or an expression?  Is the answer supposed to be a number or an expression?   |              | 3    |
| Q        | another hint what is the expected value of an event that is certain in a time slot of a Bernoulli process?   |              | 1    |
| 2        | Another Hint Following the two failures, T2 follows a geometric r.v. with the known mean. After you obtain that nu   | <u>ımb</u>   | 1    |
| ?        | About fresh start  I thought the future event is independent of the past, regardless of the results after 1st success. The   | refr         | 2    |

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