



14. Exercise: The posterior of a coin's bias

Exercises due Apr 8, 2020 05:29 IST Completed

Exercise: The posterior of a coin's bias

3/3 points (graded)

Let Θ be a continuous random variable that represents the unknown bias (i.e., the probability of Heads) of a coin.

a) The prior PDF f_{Θ} for the bias of a coin is of the form

$$f_{\Theta}(\theta) = a\theta^9(1 - \theta), \quad \text{for } \theta \in [0, 1],$$

where a is a normalizing constant. This indicates a prior belief that the bias Θ of the coin is

High

✓ Answer: High

b) We flip the coin 10 times independently and observe 1 Heads and 9 Tails. The posterior PDF of Θ will be of the form $c\theta^m(1 - \theta)^n$, where c is a normalizing constant and where

$m =$

10

✓ Answer: 10

$n =$

10

✓ Answer: 10

Solution:

a) Because of the high exponent, the term θ^9 is very small when θ is small. This prior, as can also be seen by plotting it, is concentrated on high values of θ and indicates a prior belief in favor of large values.



b) As we saw in the last video, the power to which θ (respectively, $1 - \theta$) is raised needs to be incremented by the number of Heads (respectively, Tails) observed, leading to $m = 9 + 1 = 10$ and $n = 1 + 9 = 10$. Notice that the resulting posterior is symmetric around 0.5.

This exercise indicates that the strength of the "evidence" incorporated in a prior with $\alpha = 9$ and $\beta = 1$ is exactly counterbalanced by observing 1 Heads and 9 Tails. Differently said, a prior with $\alpha = 9$ and $\beta = 1$ can be thought of as equivalent to prior "evidence" based on 9 Heads and 1 Tails.

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8

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3

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