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18. Exercise: Second generation offspring

Exercises due Mar 25, 2020 05:29 IST Completed

Exercise: Second generation offspring

2/2 points (graded)

Every person has a random number of children, drawn from a common distribution with mean 3 and variance 2. The numbers of children of each person are independent. Let M be the number of grandchildren of a certain person. Then:

$$\mathbf{E}\left[M
ight]= \boxed{9}$$
 Answer: 9

Solution:

Let N be the number of children and let X_i be the number of children of the ith child. Then, $M=X_1+\cdots+X_N$. It follows that $\mathbf{E}[M]=\mathbf{E}[N]\cdot\mathbf{E}[X]=3\cdot 3=9$. Furthermore,

$$\mathsf{Var}\left(M
ight) = \mathbf{E}\left[N
ight]\mathsf{Var}\left(X
ight) + \left(\mathbf{E}\left[X
ight]
ight)^{2}\mathsf{Var}\left(N
ight) = 3\cdot 2 + 9\cdot 2 = 24.$$

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You have used 2 of 3 attempts

1 Answers are displayed within the problem

Topic: Unit 6: Further topics on random variables:Lec. 13: Conditional expectation and variance revisited; Sum of a random number of independent r.v.'s / 18. Exercise: Second generation offspring

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2		w to solve this sucker Write it out. Part (a): What is a grandchild? What is the grandchild's relationship to the infor	6
?	Is this statis		1
?	Hint Any hint whic	ch formula to use or how to proceed?	9
2	Solution I tried to solve	e this problem but my answers were wrong. Seeing the solution, I understand the calculatio	1 new_
2	_	eat-grandchildren ve the mean and variance of number of grandchildren, you can use the same approach for t	. 1
2	•	on stumped me for a while odor to be a standard on stumped me for a while odor on stumped me formulas. Ended up overthinking things a bit (I guess). Was thrown	. 1
2	_	eater than Expectation. dard Deviation of a random variable be greater than the Expected value of that random vari	1 new_
?	Question at	bout an alternative solution	2

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