

# Testing the unguarded X hypothesis

April 13, 2018

## 1 Introduction

The unguarded X (UX) hypothesis states that one reason for females to live longer than males is that they are usually the homogametic sex. This implies that either somatic or inherited (partially) recessive deleterious mutations in the X chromosome are always exposed in males, but concealed in heterozygous females. This hypothesis requires recessive mutations, maintained by mutation-selection balance, that negatively affect longevity both in males and in females. This scenario is hardly controversial. The main uncertainty is whether this kind of mutations can fully explain the difference in longevity between sexes.

The alternative hypothesis is that a different kind of mutations is required to account for the difference in longevity between males and females. Namely, sexually antagonistic mutations, which are maintained at intermediate frequencies in the population by a selection balance. Sexually antagonistic mutations could happen in any chromosome. However, there are theoretical reasons and evidence to believe that they are especially frequent in the X chromosome [Gibson et al., 2002].

Kelly [1999] suggested an experiment to determine if low-frequency, deleterious mutations can explain the observed genetic variance in a character that is correlated with fitness. The alternative is that high-frequency mutations maintained by a selection balance are required to explain the observed variance. It is a qualitative test, rather than a quantitative measure of the contribution of each frequency class. The experiment is relatively easy and it involves a short selection experiment and two short inbreeding experiments. Needless to say that the conclusion would only apply to the population used in the experiment. The test was originally thought for traits affected mostly by autosomic variation. In section 2 I explain the theoretical bases of Kelly's test. And in section ?? I extend its application to traits mostly affected by X-linked variation.

## 2 John K. Kelly's test of the frequency class of deleterious variants

The method is based on a simple model. In every locus (assumed to be autosomic) affecting a trait correlated with fitness, there are a high allele ( $A_{1i}$ ), and a low allele ( $A_{0i}$ ). The three genotypes in one locus, from low to high, have genotypic values  $-a_i$ ,  $d_i$ , and  $a_i$ , where  $-a_i \leq d_i \leq a_i$ . The frequency of  $A_{1i}$  is  $p_i$ , and that of  $A_{0i}$ ,  $q_i$ . For simplicity, I drop the  $i$  subscript. Under this parameterization, the additive genetic variance contributed by one locus in a population in Hardy-Weinberg equilibrium is  $V_a = 2pq[a + d(q - p)]^2$  [Falconer \[1989, p. 126\]](#).

The other magnitude of interest is the covariance of additive effects with the homozygous dominance effects,  $C_{ad}$ . The additive effects are what [Falconer \[1989, p. 112\]](#) calls average effects, say  $a_j$  and  $a_k$  of alleles  $j$  and  $k$ . The breeding value of an autosomal genotype can be expressed as the sum of the average effects of the two alleles [[Falconer, 1989, p.115](#)]. And the difference between the breeding value and the genotypic value is the dominance deviation, say  $d_{jk}^j$  for genotype  $jk$ . The homozygous dominance effect of allele  $j$  is  $d_j^j$ , the difference between genotypic and breeding values of genotype  $jj$ , due to dominance. Thus, the covariance between average effects and homozygous dominance effects,  $C_{ad}$  is highest when low alleles ( $A_0$ ) are recessive and high alleles ( $A_1$ ), dominant. [Cockerham and Weir \[1984\]](#) defines this covariance for one locus,  $i$ , as  $d_{1i} = \sum_j p_{ji} a_{ji} d_{ji}^j$ . This stems from the definition of covariance ( $\text{Cov}[a, d] = E[ad] - E[a]E[d]$ ), and from the fact that the expected average effect among the alleles in one locus ( $E[a]$ ) is zero. If there are two alleles in the locus,  $p_{ji}$  in that formula are  $p$  and  $q = 1 - p$ . If  $q$  is the frequency of the low allele,  $A_0$ , then  $a_{0i} = -p(a + d(q - p))$ , and  $a_{1i} = q(a + d(q - p))$ . The homozygous dominant effects in this model are  $d_{0i}^0 = -2p^2d$ , and  $d_{1i}^1 = -2q^2d$  [[Falconer, 1989, p. 118](#)]. Substituting these values in the formula above, we obtain the expression for  $C_{ad}$  given by [Kelly \[1999\]](#):  $C_{ad} = 2pq(p - q)d[a + d(q - p)]$ .

When several loci are involved, the additive variance is the sum of  $V_a$  across loci [[Falconer, 1989, p. 129](#)], and the covariance between average effects and homozygous dominance effects,  $C_{ad}$ , is also the sum of the covariances across all loci [[Cockerham and Weir, 1984](#)]. In principle, there are ways to estimate and  $C_{ad}$  and  $V_a$ . These quantities are interesting because their ratio,  $C_{ad}/V_a$ , is sensitive to the allele frequencies. When the low alleles have intermediate frequencies,  $C_{ad}/V_a$  drops to values close to or lower than zero. [Kelly \[1999\]](#) proposes a new and efficient way to estimate directly the ratio  $C_{ad}/V_a$ . [Figure 1](#) shows that a threshold can be chosen on  $C_{ad}/V_a$  below which loci with intermediate allele frequencies are likely to contribute to the phenotype.

In Kelly's terms,  $M$  is the mean phenotype in the population. The directional dominance,  $B$ , is the difference in mean phenotype between an outbred population and a completely inbred population with the same allele frequencies.  $V_a$  is the additive genetic variance, and  $V_p$ , the total phenotypic variance.  $C_{ad}$  is the covariance between the ad-

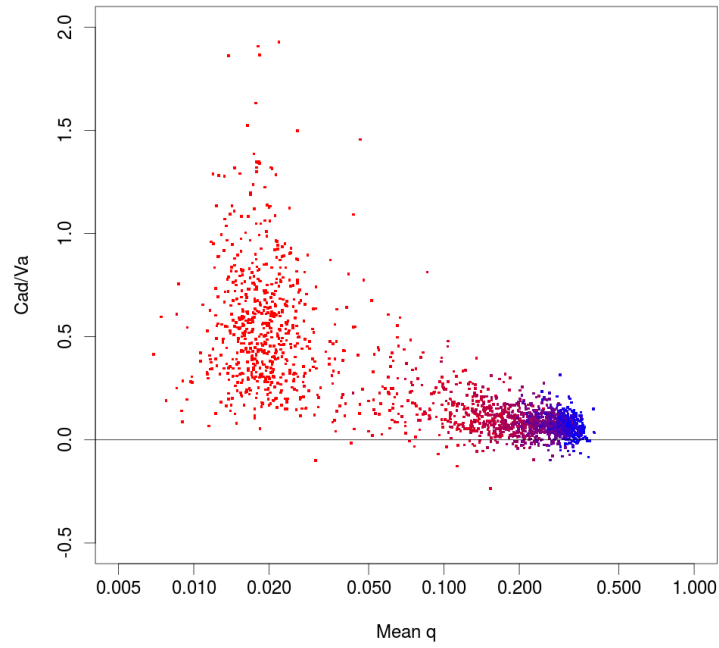


Figure 1: Two thousand simulated  $C_{ad}/V_a$  ratios under variable number of loci contributing to the phenotype (between 50 and 200), and a variable proportion of them with intermediate allele frequencies. The colour indicates, from red to blue, the proportion of loci (up to 70%) the low allele's frequency of which was taken from a Beta distribution with a 0.4 mean

ditive effects and the homozygous dominant effects. "The 'homozygous dominant effect' is the dominance deviation associated with a particular allele when that allele is in homozygous form." Note that Cockerham and Weir [1984] uses the symbol  $d_{1i}$  for what Kelly calls  $C_{ad}$ .

Citing Kelly [1999], who refers to a character (mostly) affected by autosomal loci: "In the short term, the expected change in the mean phenotype ( $M$ ) equals the product of the cumulative selection differential and the narrow sense heritability [Falconer, 1989]. The latter is  $V_a$  divided by  $V_p$ , the phenotypic variance. The expected change in the directional dominance ( $B$ ) is the product of the cumulative selection differential and  $C_{ad}/V_p$  [...]. Thus, the ratio of the cumulative change in  $B$  to the cumulative change in  $M$  provides an estimate of the ratio of  $C_{ad}$  to  $V_a$ ." And the estimate of  $C_{ad}/V_a$  is known to be sensitive to the frequency of partially recessive alleles.

### 3 Sex-linked genes

Dosage compensation in *D. melanogaster* works by doubling the expression of X-linked genes in males, not by inactivating an X chromosome in females. Thus, the genotypic value of a male carrying the  $A_1$  allele in its X chromosome can be reasonably assumed to be equal to the genotypic value of the homozygous  $A_1A_1$  female. Although James [1973] did not know this, he deduced that if that was the case, then the additive genetic variance in males due to a single X-linked locus would be exactly twice the additive genetic variance in females. Actually, his deduction is only correct under his assumption of no dominance. It depends on the heterozygous female having an intermediate genotypic value.

### 4 The experiment

A sex-linked trait has different genetic variances in males and females. If the trait is defined as sex-specific, and therefore selected only in one sex, the expected change in mean (sex-specific) phenotype would still be the product of the cumulative selection differential and the narrow sense (sex-specific) heritability (I think, because this expectation stems only from the definition of heritability [Falconer, 1989, page XX]). This may be the only way to target female longevity, irrespectively of its correlation with male longevity. However, in a population of flies, it is unfeasible to manually select individuals according to the longevity of their mother. Even if individual flies could be marked with their mother's code, marking and reading the codes would not be easier than having the population separated in sex- and family-specific bottles, which is undesirable. A more efficient solution is required. Actually, the literature suggests some options.

Lund-Hansen [2017, p. 19] claims to be the first case of sex-limited evolution in *Drosophila* that targets females, instead of males. Furthermore, she limits evolution to the X chromosome. That’s exactly what we need. Her purpose is just to eliminate male selection on the X chromosome. The female-limited X-chromosome evolution experiment releases sexually antagonistic standing genetic variation from the selection balance, and allows the fixation of alleles beneficial to females in the X chromosome. She accomplishes this by using an X-chromosome balancer and a smart design of crosses. For details, see chapter 2 of Lund-Hansen [2017], which is available online [here](#). First, she introgresses an X-chromosome balancer (FM) into the source population (12 generations of back-crossing). The introgressed population provides a source of males with an FM X-chromosome (FM/Y). In her experiment, a population is a set of 14 vials, with 16 males and 16 females each. In the experimental evolution group, females in a vial are heterozygous FM/X, and the males are FM/Y, so that all the daughters inherit an evolving X chromosome from their mother and an FM balancer from their father. Females must be collected as virgins every generation. In order to allow recombination among evolving X chromosomes, every generation a subset of 16 FM/X females were mated not with FM/Y males, but with X/Y males from the same population. The two evolving X chromosomes in any of their daughters would recombine. When mated with FM/Y males, they would produce FM/X daughters that would go back to the selective regime, one to each of the 14 vials. On the side, Lund-Hansen raised two types of control populations. Each of the three types of populations was replicated four times. That makes  $3 \times 4 \times 14 = 168$  vials. The experiment went on over 40 generations.

For our purpose, in the populations undergoing female-limited X-chromosome evolution we would have to select for longevity. I think that 20 generations should be enough.

To summarize, we would need to: 1) run an inbreeding experiment from the source population to estimate  $B$  before the selection experiment; 2) measure the average female longevity in the source population; 3) run a female-limited X-chromosome evolution experiment selecting for female longevity; 4) measure the average female longevity after the selection experiment; and 5) run a second inbreeding experiment from the evolved population. Actually, the ‘inbreeding experiments’ would be as short as two or three generations, because they need to affect only the X chromosome. An FM/X female, carrying the X chromosome targeted from homozygosity, would be crossed with an unrelated FM/Y male. Among the progeny, an X/Y male would be crossed with an FM/X sister. The X/X progeny would be homozygous for the whole X chromosome. However, the parents being siblings, the other chromosomes would also be partially inbred. To minimize the contribution from autosomes, half-siblings could be used.

Table 1: Model of genetic values. The genic effects ( $\alpha$  terms below) are defined as the average deviation from the sex-specific population's mean produced by each allele. They are:  $\alpha'_{M1} = qb$ ,  $\alpha'_{M2} = -pb$ ,  $\alpha'_{F1} = pqa - qd(p - q)$ , and  $\alpha'_{F2} = -p^2a + pd(p - q)$ . It can be noticed that dominance deviations (in females) vanish in the absence of dominance ( $d = a/2$ ). The prime symbol is used to denote X-linked genes, as in [?, chapter 24]

	Females			males	
Genotypes	$A_1A_1$	$A_1A_2$	$A_2A_2$	$A_1$	$A_2$
Frequencies	$p^2$	$2pq$	$q^2$	$p$	$q$
Genotypic values	$a$	$d$	$0$	$b$	$0$
Average values	$\mu_F = p^2 + 2pqd$			$\mu_M = pb$	
Estimated values	$\mu_F + 2\alpha'_{F1}$	$\mu_F + \alpha'_{F1} + \alpha'_{F2}$	$\mu_F + 2\alpha'_{F2}$	$\mu_M + \alpha'_{M1}$	$\mu_M + \alpha'_{M2}$
Dominance deviations	$q^2(2d - a)$	$-pq(2d - a)$	$p^2(2d - a)$	$0$	$0$

## 5 Apendix

### 5.1 X-linked single locus

## References

- B. Charlesworth and K. A. Hughes. Age-specific inbreeding depression and components of genetic variance in relation to the evolution of senescence. *PNAS*, 93(12):6140–6145, 1996.
- C. C. Cockerham and B. S. Weir. Covariances of Relatives Stemming from a Population Undergoing Mixed Self and Random Mating. *Biometrics*, 40(1):157–164, 1984.
- T. Connallon and L. L. Knowles. Evidence for Overdominant Selection Maintaining X-Linked Fitness Variation in *Drosophila melanogaster*. *Evolution*, 60(7):1445–1453, 2006.
- D. E. Cowley, W. R. Atchley, and J. J. Rutledge. Quantitative Genetics of *Drosophila Melanogaster*. I. Sexual Dimorphism in Genetic Parameters for Wing Traits. *Genetics*, 114(2):549–566, 1986.
- D. S. Falconer. *Introduction to quantitative genetics*. Longman, Scientific & Technical ; Wiley, Burnt Mill, Harlow, Essex, England; New York, 1989. ISBN 978-0-470-21162-5 978-0-582-44195-8 978-0-582-01642-2.

- J. R. Gibson, A. K. Chippindale, and W. R. Rice. The X chromosome is a hot spot for sexually antagonistic fitness variation. *Proceedings of the Royal Society of London B: Biological Sciences*, 269(1490):499–505, 2002.
- J. W. James. 353. Note: Covariances Between Relatives due to Sex-Linked Genes. *Biometrics*, 29(3):584–588, 1973.
- J. K. Kelly. An experimental method for evaluating the contribution of deleterious mutations to quantitative trait variation. *Genetics Research*, 73(3):263–273, 1999.
- K. K. Lund-Hansen. *Experimental manipulation of sexual antagonism in Drosophila melanogaster*. PhD, University of Sussex, Sussex, UK, Jan. 2017. URL <http://sro.sussex.ac.uk/70184/1/Lund-Hansen%2C%20Katrine%20Koch.pdf>.
- T. Mukai, R. A. Cardellino, T. K. Watanabe, and J. F. Crow. The Genetic Variance for Viability and Its Components in a Local Population of *Drosophila melanogaster*. *Genetics*, 78(4):1195–1208, 1974.