

Algebraic Path Problems and GraphBLAS: a Way to High-Performance Network Analysis

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Agenda

- Algebraic Path Problems
- GraphBLAS
- Our team

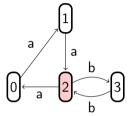
GraphBLAS API^{1,2}

- Graph-matrix duality
- Operations over matrices and vectors
 - Parametrized by semiring-like structures
 - Sparse data
 - Parallel
- High-performance implementations
 - SuiteSparse:GraphBLAS
 - GraphBLAST
 - Huawei

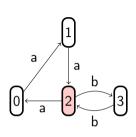
¹https://graphblas.org/

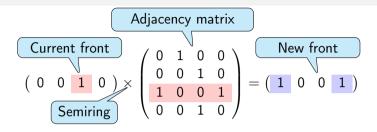
²https://graphblas.org/GraphBLAS-Pointers/

BFS-like Skeleton

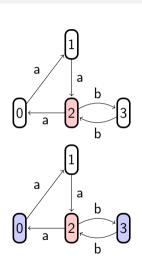


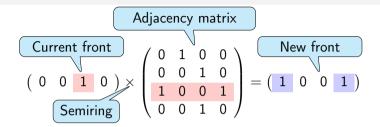
BFS-like Skeleton





BFS-like Skeleton





Research areas

- High-performance graph analysis
- Path problems with constraints
- Graph databases

Team

- Semyon Grigorev (Lead)
 - ▶ PhD (2016)
 - Associate professor (2016, SPbSU)
 - s.v.grigoriev@spbu.ru
- Ekaterina Shemetova
 - ▶ PhD student
 - Path problems with constraints
- Rustam Azimov
 - PhD student
 - Linear algebra based graph analysis

- ▶ High-performance graph analysis
- Graph databases
- dblp: https://dblp.org/pid/181/9903.html

- Fine-grained complexity
- Dynamic graph problems

- GraphBLAS API
- Algebraic path problem

Team: Master Students

- Alexandra Istomina
 - Master student
 - Fine-grained complexity
- Egor Orachev
 - Master student
 - Linear algebra based graph analysis
- Vladimir Kutuev
 - Master student
 - Linear algebra based graph analysis
- Julia Susanina
 - Master student
 - Linear algebra based graph analysis

- ▶ Path problems with constraints
- ► Algebraic path problem

- GraphBLAS API
- ► GPGPU programming

- GraphBLAS API
- Parallel programming

- Probabilistic graph analysis
- ► GPGPU programming

High-Performance Graph Analysis

- Linear algebra based algorithms for graph analysis
 - ▶ Parallel algorithms on CPU and GPGPU
 - ► Sparse linear algebra for graph analysis
 - ▶ GraphBLAS API³

High-Performance Graph Analysis

- Linear algebra based algorithms for graph analysis
 - Parallel algorithms on CPU and GPGPU
 - Sparse linear algebra for graph analysis
 - GraphBLAS API³
- Research directions
 - GraphBLAS-based algorithms design, implementation and evaluation
 - Portable multi-GPGPU implementation of GraphBALS-like API
 - GraphBLAS API analysis

Path Problems With Constraints: Algebraic Path Problems

- Semiring-like structures to specify constraints on paths
 - ► Reachability boolean semiring
 - ▶ Shortest paths tropical semiring
 - **.** . . .

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 - ► Transitive closure using matrix-matrix multiplication
 - ► APSP using matrix-matrix multiplication
 - ▶ BFS-like traversals using matrix-vector multiplication
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- Compositionality
 - Having two semirings one can create a new one
 - Single solution for similar problems
 - ★ Generic solution
 - ★ Configurable solution

- Particular case of algebraic path problem
 - Multiplication is not associative
 - Multiplication is not commutative

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 - Graph database querying

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- Research directions
 - New algorithms development
 - ► Complexity analysis
 - New classes of languages investigation
 - ► High performance algorithms implementation and evaluation

Our Results

- Tools
 - ▶ Spla: sparse linear algebra framework for multi-GPU computations based on OpenCL
 - ► SPbLA: library of GPGPU-powered sparse boolean linear algebra operations

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 - CFPQ_PyAlgo: set of GraphBLAS-based FLPQ algorithms
 - ▶ LDBC Graphalytics extension for evaluation of formal language constrained path querying

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- GLL4Graph: CFPQ for Neo4j
- CFPQ for RedisGraph
- Papers (> 10)
 - SPbLA: The Library of GPGPU-Powered Sparse Boolean Linear Algebra Operations (GrAPL@IPDPS)
 - Evaluation of the context-free path querying algorithm based on matrix multiplication (GRADES-NDA@SIGMOD)
 - ▶ Multiple-Source Context-Free Path Querying in Terms of Linear Algebra (EDBT, Core A)
 - Context-free path querying by matrix multiplication (GRADES-NDA@SIGMOD)

Possible Ways for Collaboration

- Algebraic Path Problem framework applicability for network analysis
 - ▶ Which constraints can be specified in terms of semirings?
 - **★** Length minimality
 - ★ Nodes to visit
 - *
 - ► Is it flexible enough?
- High-performance network analysis
 - GraphBLAS-based solution
 - Algorithms development and analysis
 - Algorithms implementation and evaluation

Possible Ways for Collaboration

- Algebraic Path Problem framework applicability for network analysis
 - Unstructured path problems and the making of semirings (https://link.springer.com/chapter/10.1007/BFb0028261)
 - ► Efficient Algorithms for Path Problems with Gernal Cost Citeria (https://www.semanticscholar.org/paper/Efficient-Algorithms-for-Path-Problems-with-Gernal-Lengauer-Theune/3fd320d97db0a581952d2919587b112f8df57c0b)
 - ► Path Problems in Networks https://www.morganclaypool.com/doi/abs/10.2200/S00245ED1V01Y201001CNT003
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