

Prova 2

Calculo I

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2. Altura = h

largura = l

AI = h.l

→ Area total

$$A_T = (l + 2 + 2,5) \cdot (h + 3,5 + 2) = (l + 4,5) \cdot (h + 5,5)$$

$$A_I = h.l \text{ e } 375 = h.l \Rightarrow h = \frac{375}{l}$$

$$\text{Substituindo } A_T \text{ temos: } A_T = (l + 4,5) \left(\frac{375}{l} + 5,5 \right) = (l + 4,5) \left(\frac{375 + 5,5l}{l} \right)$$

$$A_T = \frac{5,5l^2 + 399,75l + 1687,5}{l}$$

$$A'(l) = \left[\frac{5,5l^2 + 399,75l + 1687,5}{l} \right]'$$

$$A'(l) = \frac{(11l + 399,75)l - (5,5l^2 + 399,75l + 1687,5) \cdot 1}{l^2}$$

$$A'(l) = 0 = \frac{11l^2 - 5,5l^2 + 399,75l - 399,75l - 1687,5}{l^2} = 0$$

$$= \frac{5,5l^2 - 1687,5}{l^2} = 0 \Rightarrow 5,5l^2 = 1687,5$$

$$= l^2 = \frac{1687,5}{5,5} = 306,818$$

$$= l = \pm \sqrt{306,818} \Rightarrow l = 17,51$$

$$\text{Por } h = \frac{375}{l} \Rightarrow h = \frac{375}{17,51}$$

$$\boxed{21,41}$$

$$h = 21,41 \text{ e } l = 17,51$$

$$\text{altura} = 21,41 + 5,5 = 26,91 \text{ cm}$$

$$\text{largura} = 17,51 + 4,5 = 22,01 \text{ cm}$$

$$1. \quad g(x) = x^4 - 2x^2 + 2$$

a) Derivando: $4x^3 - 4x = 0$ / $x^2 - 1 = 0$

$$g'(x) = 4x^3 - 4x$$

$$x = 0$$

$$x^2 = 1$$

$$4x^3 - 4x = 0$$

$$x = 1 \text{ ou } x = -1$$

$$4x(x^2 - 1) = 0$$

-1, 0, 1 são números críticos

b) $g'(x) = 4x^3 - 4x$

$$g'(x) > 0$$

$$g'(x) = 0 \text{ se } x = 1 \text{ ou } x = -1 \text{ ou } x = 0$$

$$g'(x) = 0$$

$$g'(x) > 0 \text{ se } x < -1 \text{ ou } x > 1$$

$$g'(x) < 0 \text{ se } -1 < x < 1$$

$$g = \text{Crescente se } x < -1 \text{ ou } x > 1$$

$$-\infty < x < \infty$$

$$g = \text{Decrescente } -1 < x < 1$$

$$(-\infty, \infty)$$

c) $g''(x) = 12x^2 - 4$

$$\text{Para } x = -1 = g''(-1) = 12(-1)^2 - 4 = 8$$

$$8 > 0 = \text{Mínimo}$$

$$\text{Para } x = 0 = g''(0) = 12(0)^2 - 4 = -4$$

$$-4 < 0 = \text{Máximo}$$

$$\text{Para } x = 1 = g''(1) = 12(1)^2 - 4 = 8$$

$$8 > 0 = \text{Mínimo}$$

$$g''(x) = x^4 - 2x^2 + 2$$

$$g''(-1) = (-1)^4 - 2(-1)^2 + 2 = 1 - 2 + 2 = 1 \quad (-1, 1) = \text{Mínimo}$$

$$g''(0) = 0^4 - 2(0)^2 + 2 = 2 \quad (0, 2) = \text{Máximo}$$

$$g''(1) = 1^4 - 2(1)^2 + 2 = 1 - 2 + 2 = 1 \quad (1, 1) = \text{Mínimo}$$

Ponto mínimo $\rightarrow (-1, 1) \text{ e } (1, 1)$

Ponto máximo $\rightarrow (0, 2)$

$$f.d) \quad g(x) = x^4 - 2x^2 + 2$$

$$g'(x) = \frac{d}{dx} (x^4 - 2x^2 + 2)$$

$$g'(x) = 4x^3 - 2 \cdot 2x + 0$$

$$g'(x) = 4x^3 - 4x$$

$$0 = 4x^3 - 4x$$

$$-4x^2 = -4$$

$$x'' = \frac{1}{3} - x \pm \frac{\sqrt{3}}{3}$$

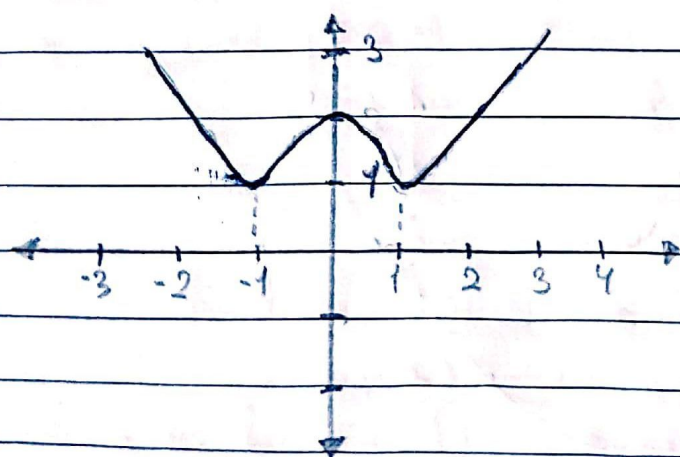
$$g\left(\frac{-\sqrt{3}}{3}\right) = \left(\frac{-\sqrt{3}}{3}\right)^4 - 2\left(\frac{\sqrt{3}}{3}\right)^2 + 2$$

$$g\left(\frac{-\sqrt{3}}{3}\right) = \frac{9}{81} - \frac{2}{9} + 2$$

$$g\left(\frac{-\sqrt{3}}{3}\right) = \frac{13}{9}$$

Mesmo processo para a segunda, só muda o x

$$\left(\frac{-\sqrt{3}}{3}, \frac{13}{9}\right) \text{ e } \left(\frac{\sqrt{3}}{3}, \frac{13}{9}\right)$$



4-i) $\int \sin^4(2x) \cos(2x) dx$

$$\int \sin^4(2x) \cos(2x) \cdot \frac{1}{\cos(2x) \cdot 2} \cdot dx \quad \text{Let } t = 2x$$

$$\int \frac{\sin^4(2x) \cdot 1}{2} dt$$

$$\int \frac{\sin^4(2x)}{2} dt = \int \frac{t^4}{2} dt = \frac{1}{2} \cdot \frac{t^5}{5} = \frac{1}{2} \cdot \frac{\sin(2x)^5}{5}$$

$$\frac{\sin(2x)^5}{10} = \frac{\sin(2x)^5}{10} + C$$

ii) $\int 4x^2 e^x dx$

$$4(x^2 \cdot e^x - \int e^x \cdot 2x dx) =$$

$$4(x^2 e^x - 2 \cdot \int e^x x dx) =$$

$$4(x^2 e^x - 2 \cdot \int x e^x dx) =$$

$$4(x^2 e^x - 2(x e^x - \int e^x dx))$$

$$4(x^2 e^x - 2(x e^x - e^x))$$

$$4(x^2 e^x - 2x e^x + 2 e^x) = (4x^2 e^x - 8x e^x + 8 e^x) =$$

$$4x^2 e^x - 8x e^x + 8 e^x + C$$

5. $y = e^{-x}$, $y = x+1$ $x = -1$

$$\int_{-1}^{x+1} (e^{-x}) dx$$

Substituindo $u = -x$ $\Rightarrow du = -1 dx$ $dx = (-1) du$

$$= \int e^u (-1) du$$

$$= \int -e^u du \quad x = -1 \quad u = 1 \rightarrow u = -x = -(-1) = 1$$

$$\int_1^{-x-1} -e^u du \quad \leftarrow \quad x = x+1 \quad u = -x-1$$

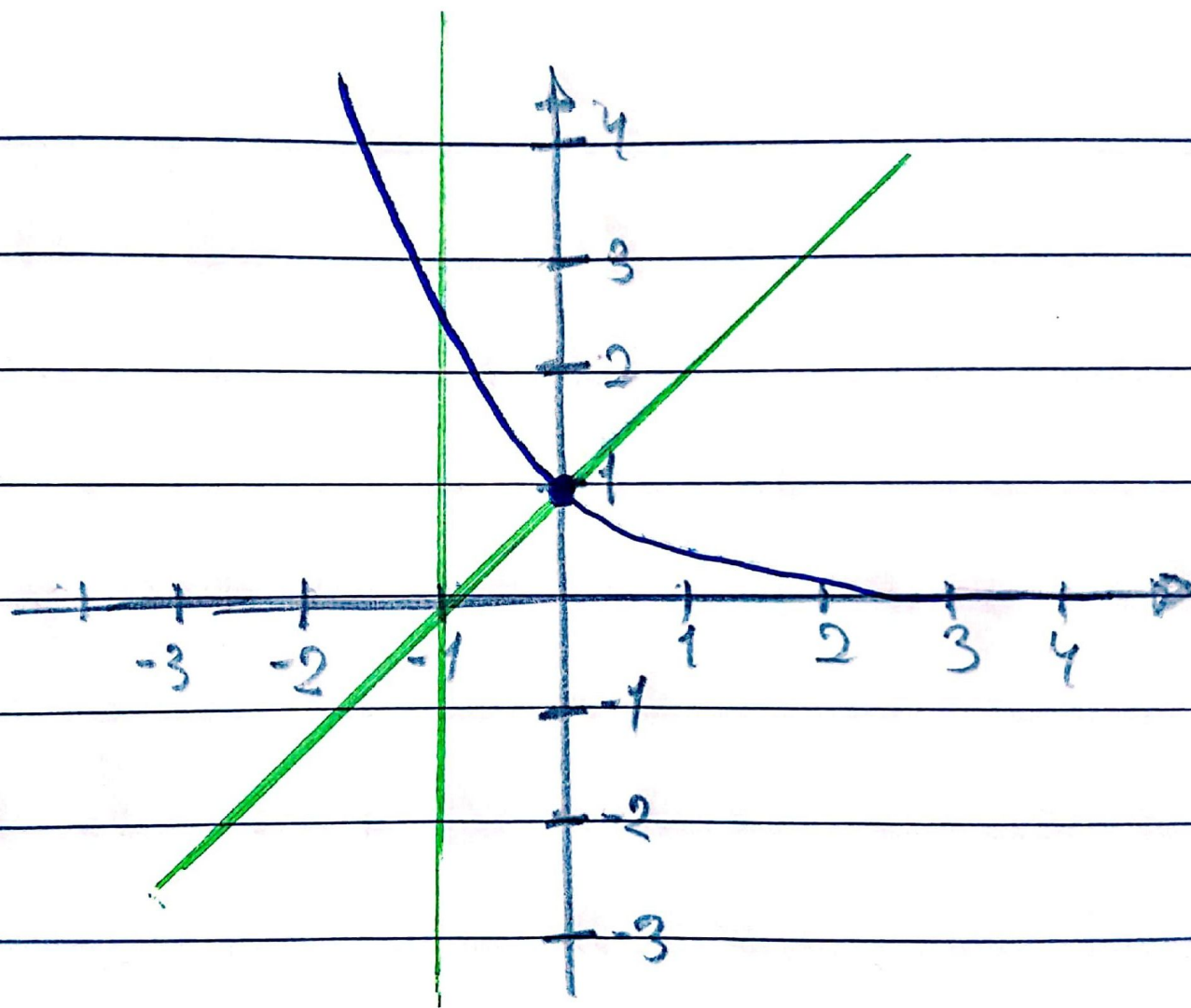
$$= -[e^u]_1^{-x-1} = \int_a^b f(x) dx = F(b) - F(a) = \lim_{x \rightarrow b^-} F(x) - (F(a)) - \lim_{x \rightarrow a^+} F(x) + (F(a))$$

$$\lim_{u \rightarrow 1^+} (e^u) = e$$

$$\lim_{u \rightarrow -x-1} (e^u) = e^{-x-1}$$

$$= e^{-x-1} \rightarrow e^{-x-1} - e \rightarrow (-e^{-x-1} - e) =$$

$$= -e^{-x-1} + e$$



3- $x_1 = 0 + \Delta x = x_1 = 0 + 1 = 1$; $f(x) = -2x$
 $x_2 = 0 + 2 \cdot 1 = x_2 = 2$

$$\Delta x = \frac{b-a}{2} = \quad \quad \quad \Delta m = f(x_1) \Delta x + f(x_2) \Delta x$$

$$\Delta x = \frac{2-0}{2} = 1 \quad \quad \quad -2 \cdot 1 + (-2 \cdot 2) = \frac{-2}{1} + \frac{-2}{2} = \frac{(-4) \cdot (-2)}{2} = \frac{8}{2}$$

$$\Delta x = \frac{-2-0}{4} = 0,5 \quad \quad \quad x_1 = 0 + 0,5 = 0,5$$

$$x_2 = 0 + 2,05 = 1 \quad \quad \quad \frac{1}{2} \text{ u.a}$$

$$x_3 = 0 + 3,05 = 1,5$$

$$x_4 = 0 + 4,05 = 2$$

$$\Delta x = \frac{2-0}{8} = 0,25$$

$$x_1 = 0 + 0,25 = 0,25 \quad \quad \quad x_5 = 0 + 5 \cdot 0,25 = 1,25$$

$$x_2 = 0 + 2 \cdot 0,25 = 0,50 \quad \quad \quad x_6 = 0 + 6 \cdot 0,25 = 1,50 \quad \frac{1}{2} \text{ u.a}$$

$$x_3 = 0 + 3 \cdot 0,25 = 0,75 \quad \quad \quad x_7 = 0 + 7 \cdot 0,25 = 1,75 \quad 2$$

$$x_4 = 0 + 4 \cdot 0,25 = 1 \quad \quad \quad x_8 = 0 + 8 \cdot 0,25 = 2$$