

May 22, 2018

$$\begin{aligned}
C_k &= \frac{k^k}{(k+1)^{k+1}} = \frac{1}{k} \left( \frac{k}{k+1} \right)^{k+1} \rightarrow 0, \quad k \rightarrow \infty \\
, \quad &: \\
\|x_{k+1} - x_*\| &\leq C_k \|x_k - x_*\|, \quad C_k \rightarrow 0 \quad k \rightarrow \infty \\
x_* &= \lim_{k \rightarrow \infty} \frac{1}{k^k} = 0 \\
\Rightarrow \frac{1}{(k+1)^{k+1}} &\leq C_k \frac{1}{k^k} = \frac{k^k}{(k+1)^{k+1}} \frac{1}{k^k} = \frac{1}{(k+1)^{k+1}} \\
: \quad &\frac{1}{(k+1)^{k+1}} \leq \frac{1}{(k+1)^{k+1}}
\end{aligned}$$