

## Recursion

---

### Question No. 1

e.g. in Python:

```
def BinarySearch(Low, High):                                [1]
    global Found
    if Low>High:                                           )
        return                                           ) [1]
    Middle=int((High+Low)/2)
    if SearchData[Middle] == SearchItem:                   )
        Found = Middle                                   ) [1]
    elif SearchData[Middle] < SearchItem:                   )
        BinarySearch(Middle + 1, High)                     ) [1]
    elif SearchData[Middle] > SearchItem:                   )
        BinarySearch(Low, Middle - 1)                       ) [1]
    return
```

```
BinarySearch(1,63)                                         [1]
```

## Recursion

### Question No. 2

3	<pre>FUNCTION Find(BYVAL Name : STRING,               BYVAL Start : INTEGER,               BYVAL Finish : INTEGER) RETURNS INTEGER // base case IF <b>Finish &lt; Start</b> THEN     RETURN -1 ELSE     Middle ← (Start + Finish) DIV 2     IF <b>NameList[Middle] = Name</b>     THEN         RETURN <b>Middle</b>     ELSE // general case         IF SearchItem &gt; <b>NameList[Middle]</b>         THEN             <b>Find(Name, Middle + 1, Finish)</b>         ELSE             <b>Find(Name, Start, Middle - 1)</b>         ENDIF     ENDIF ENDIF ENDFUNCTION</pre>	7
---	--	---

## Recursion

---

### Question No. 3

3(a)	1 mark per bullet point to max 2 <ul style="list-style-type: none"><li>• It is defined in terms of itself // it calls itself</li><li>• It has a stopping condition // base case</li><li>• It is a self-contained subroutine</li><li>• It can return data to its previous call</li></ul>	2
3(b)	1 mark per bullet point to max 3 <ul style="list-style-type: none"><li>• (When the recursive call is made) all values/data are put on ...</li><li>• ... the stack</li><li>• When the stopping condition/base case is met</li><li>• ...the algorithm unwinds</li><li>• ...the last set of values are taken off the stack (in reverse order)</li></ul>	3

### Question No. 4

10(a)	<b>One mark for each correct marking point (Max 3)</b> <ul style="list-style-type: none"><li>• Must have a base case/stopping condition</li><li>• Must have a general case</li><li>• ... which calls itself (recursively) // Defined in terms of itself</li><li>• ... which changes its state and moves towards the base case</li></ul> Unwinding can occur once the base case is reached.	3
10(b)	<b>One mark for each correct marking point (Max 3)</b> <ul style="list-style-type: none"><li>• A stack is a LIFO data structure</li><li>• Each recursive call is pushed onto the stack</li><li>• .... and is then popped as the function ends</li><li>• Enables backtracking/unwinding</li></ul> ... to maintain the required order.	3

## Recursion

### Question No. 5

(a) A procedure that calls itself // is defined in terms of itself [1]

(b) Before procedure call is executed current state of the registers/local variables is saved onto the stack  
When returning from a procedure call the registers/local variables are re-instated [2]

(c)

Call number	n	(n=0) OR (n=1)	n DIV 2	n MOD 2
1	40	FALSE	20	0
2	20	FALSE	10	0
3	10	FALSE	5	0
4	5	FALSE	2	1
5	2	FALSE	1	0
6	1	TRUE		

1 mark

1 mark

1 mark

OUTPUT 101000 – 1 mark for each pair of bits. [6]

(d) Conversion of denary number into binary [1]

(e)

Example Python

```
def X(n):
    if (n == 0) or (n == 1):
        print(n, end="")
    else:
        X(n // 2)
        print(n % 2, end="")
```

Mark as follows:

Procedure heading & ending

Boolean expression

correctly grouped statements within ELSE

recursive call

Using DIV and MOD correctly

[5]

## Recursion

### Question No. 6

2	(a) (i)	A procedure which is defined in terms of itself // A procedure which makes a call to itself // A procedure that calls itself	1																																																																																																																																
	(ii)	08 // 8	1																																																																																																																																
	(b) (i)	<div><table><thead><tr><th>Index</th><th>Item</th></tr></thead><tbody><tr><td>1</td><td>9</td></tr><tr><td>2</td><td></td></tr><tr><td>3</td><td></td></tr><tr><td>4</td><td></td></tr><tr><td>5</td><td></td></tr><tr><td>6</td><td></td></tr><tr><td>7</td><td></td></tr><tr><td>8</td><td></td></tr></tbody></table><table><thead><tr><th colspan="10">MyList</th></tr><tr><th>1</th><th>2</th><th>3</th><th>4</th><th>5</th><th>6</th><th>7</th><th>8</th><th>9</th><th>10</th></tr></thead><tbody><tr><td>3</td><td>5</td><td>8</td><td>9</td><td>13</td><td>16</td><td>27</td><td>0</td><td>0</td><td>0</td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>13</td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>16</td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td>27</td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td>0</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr></tbody></table><p>Note: Final mark only if no additional entries in table Accept last row to show all final values</p></div>	Index	Item	1	9	2		3		4		5		6		7		8		MyList										1	2	3	4	5	6	7	8	9	10	3	5	8	9	13	16	27	0	0	0																								13											16											27											0																								4
Index	Item																																																																																																																																		
1	9																																																																																																																																		
2																																																																																																																																			
3																																																																																																																																			
4																																																																																																																																			
5																																																																																																																																			
6																																																																																																																																			
7																																																																																																																																			
8																																																																																																																																			
MyList																																																																																																																																			
1	2	3	4	5	6	7	8	9	10																																																																																																																										
3	5	8	9	13	16	27	0	0	0																																																																																																																										
			13																																																																																																																																
				16																																																																																																																															
					27																																																																																																																														
						0																																																																																																																													
	(ii)	Any one from: Deletes/removes parameter value/ Item (from the array <code>MyList</code> ) // Deletes the first entry (in <code>MyList</code> ) that equals or is bigger than <code>Item</code>  Overwrites <code>Item</code> by moving subsequent items up/down/across/left R right	1																																																																																																																																

## Recursion

### Question No. 7

4(a)(i)	A function/subroutine defined in terms of itself // a function/subroutine that calls itself	1																								
4(a)(ii)	06	1																								
4(b)	<p>1 mark for each bullet point:</p> <ul style="list-style-type: none"><li>• -60 as final return value</li><li>• 3*2*1*-10</li></ul> <p>1 mark for each row in table</p> <table><thead><tr><th>Call Number</th><th>Function call</th><th>Number = 0 ?</th><th>Return value</th></tr></thead><tbody><tr><td>1</td><td>Calculate(3)</td><td>False</td><td>3*Calculate(2)</td></tr><tr><td>2</td><td>Calculate(2)</td><td>False</td><td>2*Calculate(1)</td></tr><tr><td>3</td><td>Calculate(1)</td><td>False</td><td>1*Calculate(0)</td></tr><tr><td>4</td><td>Calculate(0)</td><td>TRUE</td><td>-10</td></tr><tr><td></td><td></td><td></td><td></td></tr></tbody></table>	Call Number	Function call	Number = 0 ?	Return value	1	Calculate(3)	False	3*Calculate(2)	2	Calculate(2)	False	2*Calculate(1)	3	Calculate(1)	False	1*Calculate(0)	4	Calculate(0)	TRUE	-10					6
Call Number	Function call	Number = 0 ?	Return value																							
1	Calculate(3)	False	3*Calculate(2)																							
2	Calculate(2)	False	2*Calculate(1)																							
3	Calculate(1)	False	1*Calculate(0)																							
4	Calculate(0)	TRUE	-10																							
4(c)(i)	<p>1 mark per bullet point:</p> <ul style="list-style-type: none"><li>• Each time it calls itself the variables are put onto the stack // The function call itself too many times</li><li>• ... it runs out of stack space // stack overflow</li></ul>	2																								
4(c)(ii)	<p>1 mark per bullet point to max 5:</p> <ul style="list-style-type: none"><li>• Function header with parameter <b>and</b> Returning calculated value</li><li>• Loop <b>parameter</b> times (up to number, or down from number)...</li><li>• ...Multiplying by loop counter</li><li>• Multiplying by -10</li><li>• Dealing with starting value correctly</li></ul> <p>For example:</p> <pre>FUNCTION Calculate(Number : INTEGER) RETURNS INTEGER   DECLARE Count : INTEGER   DECLARE Value : INTEGER   Value ← -10   FOR Count ← 1 to Number     Value ← Value * Count   ENDFOR    RETURN Value ENDFUNCTION</pre>	5																								

## Recursion

### Question No. 8

8(a)	<ul style="list-style-type: none"><li>• 8 ...</li><li>• ...it calls itself</li></ul>	2																																										
8(b)	<p>1 mark each:</p> <ul style="list-style-type: none"><li>• Final return value = 5</li><li>• Output column</li><li>• Return value column</li><li>• Value 1 and Value 2 columns</li><li>• Temp column</li></ul> <table><tr><th>Value1</th><th>Value2</th><th>Temp</th><th>EndValue</th><th>OUTPUT</th><th>Return Value</th></tr><tr><td>1</td><td>1</td><td>1</td><td>12</td><td>1</td><td>5</td></tr><tr><td>2</td><td></td><td></td><td></td><td>2</td><td>4</td></tr><tr><td>3</td><td>2</td><td>2</td><td></td><td>3</td><td>3</td></tr><tr><td>5</td><td>3</td><td>3</td><td></td><td>5</td><td>2</td></tr><tr><td>8</td><td>5</td><td>5</td><td></td><td>8</td><td>1</td></tr><tr><td>13</td><td>8</td><td></td><td></td><td>13</td><td>0</td></tr></table>	Value1	Value2	Temp	EndValue	OUTPUT	Return Value	1	1	1	12	1	5	2				2	4	3	2	2		3	3	5	3	3		5	2	8	5	5		8	1	13	8			13	0	5
Value1	Value2	Temp	EndValue	OUTPUT	Return Value																																							
1	1	1	12	1	5																																							
2				2	4																																							
3	2	2		3	3																																							
5	3	3		5	2																																							
8	5	5		8	1																																							
13	8			13	0																																							
8(c)	To output/find a value that is the addition of the two previous values // (output) Fibonacci sequence	1																																										