

Binary Tree (ADT)

Question No. 1

1(a)	Horse	1
1(b)	Cat // Elephant // Kangaroo	1
1(c)	<p>1 mark for Iguana and Jaguar in the correct place 1 mark for Rabbit and Fish in the correct place</p> <pre> graph TD Horse[Horse] --> Donkey[Donkey] Horse --> Kangaroo[Kangaroo] Donkey --> Cat[Cat] Donkey --> Elephant[Elephant] Elephant --> Fish[Fish] Elephant --> Iguana[Iguana] Iguana --> Jaguar[Jaguar] Kangaroo --> Rabbit[Rabbit] </pre>	2
1(d)	<p>1 mark per bullet point. Mark in pairs.</p> <ul style="list-style-type: none"> • (Compare Elephant to horse) Elephant/E is less than Horse/H so check/go left ... • ... (Compare to Elephant to Donkey) Elephant/E is greater than Donkey/D so check/go right (Elephant found) <p>or</p> <ul style="list-style-type: none"> • Check if Elephant/E is less than or greater than root node ... • ... check subtree/follow pointer to next node to left/right recursively until found or leaf 	2

Binary Tree (ADT)

Question No. 2

4(a)	<div>1 mark for adding D and H below G 1 mark for adding J and P below L</div> <div><pre>graph TD; M[M] --- C[C]; M --- R[R]; C --- A[A]; C --- G[G]; R --- L[L]; R --- W[W]; G --- D[D]; G --- H[H]; L --- J[J]; L --- P[P];</pre></div>	2																																																								
4(b)(i)	<div>1 mark for rootPointer pointing to 0 1 mark for freePointer pointing to 11 1 mark for left and right correctly linked nodes 0 TO 5 1 mark for -1 added as pointer for all remaining null pointers</div> <table><tr><td>rootPointer</td><td>0</td></tr><tr><td>freePointer</td><td>11</td></tr></table> <table><tr><th>Index</th><th>leftPointer</th><th>data</th><th>rightPointer</th></tr><tr><td>0</td><td>1</td><td>M</td><td>5</td></tr><tr><td>1</td><td>2</td><td>C</td><td>4</td></tr><tr><td>2</td><td>-1</td><td>A</td><td>-1</td></tr><tr><td>3</td><td>7</td><td>L</td><td>9</td></tr><tr><td>4</td><td>8</td><td>G</td><td>10</td></tr><tr><td>5</td><td>3</td><td>R</td><td>6</td></tr><tr><td>6</td><td>-1</td><td>W</td><td>-1</td></tr><tr><td>7</td><td>-1</td><td>J</td><td>-1</td></tr><tr><td>8</td><td>-1</td><td>D</td><td>-1</td></tr><tr><td>9</td><td>-1</td><td>P</td><td>-1</td></tr><tr><td>10</td><td>-1</td><td>H</td><td>-1</td></tr><tr><td>11</td><td>(-1)</td><td></td><td>(-1)</td></tr></table>	rootPointer	0	freePointer	11	Index	leftPointer	data	rightPointer	0	1	M	5	1	2	C	4	2	-1	A	-1	3	7	L	9	4	8	G	10	5	3	R	6	6	-1	W	-1	7	-1	J	-1	8	-1	D	-1	9	-1	P	-1	10	-1	H	-1	11	(-1)		(-1)	4
rootPointer	0																																																									
freePointer	11																																																									
Index	leftPointer	data	rightPointer																																																							
0	1	M	5																																																							
1	2	C	4																																																							
2	-1	A	-1																																																							
3	7	L	9																																																							
4	8	G	10																																																							
5	3	R	6																																																							
6	-1	W	-1																																																							
7	-1	J	-1																																																							
8	-1	D	-1																																																							
9	-1	P	-1																																																							
10	-1	H	-1																																																							
11	(-1)		(-1)																																																							
4(b)(ii)	<div>1 mark per bullet point</div> <ul style="list-style-type: none">Defining 1D array with 100 elementsof type node, with identifier binaryTree <div>Example: DECLARE binaryTree : ARRAY[0:99] OF node</div>	2																																																								

(ii) Write **pseudocode** to declare the array `binaryTree` to store up to 100 objects of type `node`.

.....

.....

.....

..... [2]

Binary Tree (ADT)

Question No. 3

1(a)(i)	<div>1 mark per bullet point</div> <div><ul style="list-style-type: none">13 to left of 2134 to right of 2154 to left of 6553 to left of 54Null and other pointers on all boxes written and no other pointers filled in</div> <div></div>	5																																																
1(a)(ii)	<div>1 mark per bullet point</div> <div><ul style="list-style-type: none">FreePointer364521 and 6566 and 1354, 53 and 34</div> <div><table><tr><td>RootPointer</td></tr><tr><td>0</td></tr></table><table><tr><td>FreePointer</td></tr><tr><td>9</td></tr></table></div> <div><table><tr><th>Index</th><th>LeftPointer</th><th>Data</th><th>RightPointer</th></tr><tr><td>[0]</td><td>2</td><td>36</td><td>1</td></tr><tr><td>[1]</td><td>null</td><td>45</td><td>3</td></tr><tr><td>[2]</td><td>5</td><td>21</td><td>8</td></tr><tr><td>[3]</td><td>6</td><td>65</td><td>4</td></tr><tr><td>[4]</td><td>null</td><td>66</td><td>null</td></tr><tr><td>[5]</td><td>null</td><td>13</td><td>null</td></tr><tr><td>[6]</td><td>7</td><td>54</td><td>null</td></tr><tr><td>[7]</td><td>null</td><td>53</td><td>null</td></tr><tr><td>[8]</td><td>null</td><td>34</td><td>null</td></tr><tr><td>[9]</td><td></td><td></td><td></td></tr></table></div>	RootPointer	0	FreePointer	9	Index	LeftPointer	Data	RightPointer	[0]	2	36	1	[1]	null	45	3	[2]	5	21	8	[3]	6	65	4	[4]	null	66	null	[5]	null	13	null	[6]	7	54	null	[7]	null	53	null	[8]	null	34	null	[9]				6
RootPointer																																																		
0																																																		
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Index	LeftPointer	Data	RightPointer																																															
[0]	2	36	1																																															
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[3]	6	65	4																																															
[4]	null	66	null																																															
[5]	null	13	null																																															
[6]	7	54	null																																															
[7]	null	53	null																																															
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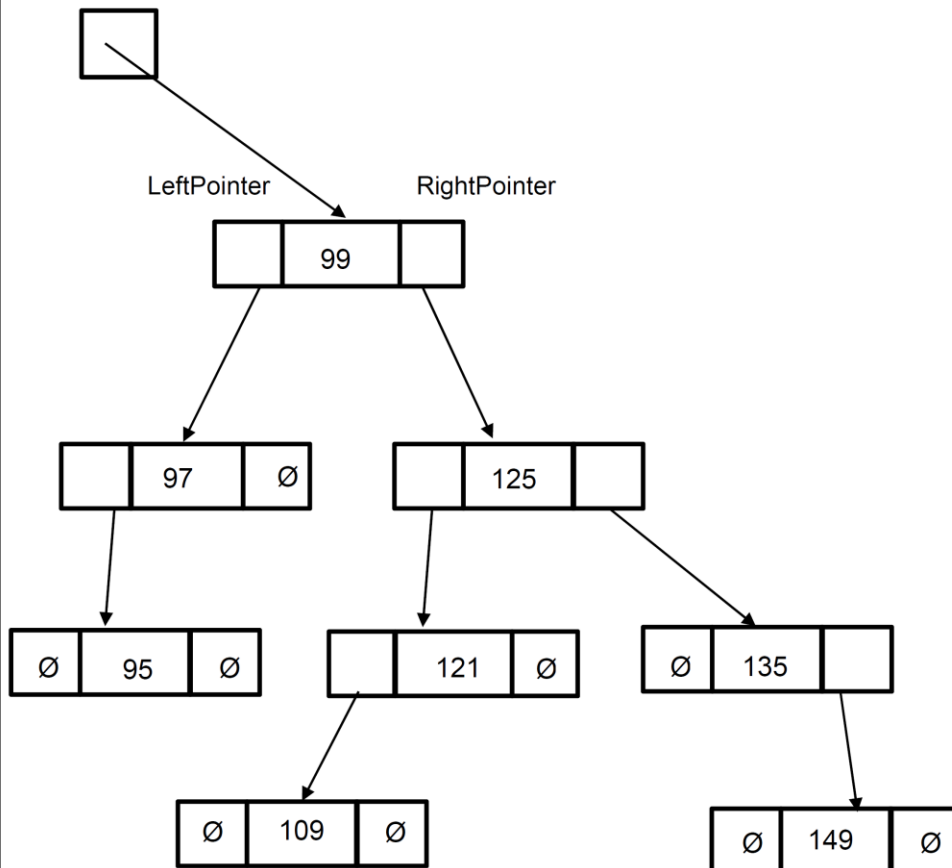
Question No. 4

2(a)(i)

1 mark per bullet point

- 95 to left of 97
- 109 to left of 121
- 135 to right of 125
- 149 to right of 135
- Null points in all places and no inappropriate pointers

RootPointer



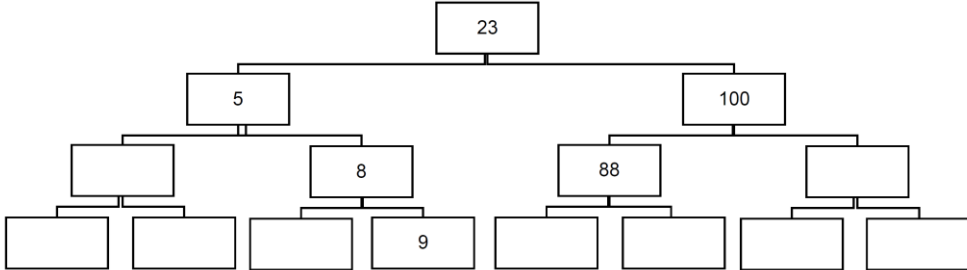
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Binary Tree (ADT)

2(a)(ii)	<div>1 mark per bullet point</div> <div><ul style="list-style-type: none">FreePointer as 899125121 and 97109 and 95135 and 149</div> <div><table><tr><td>RootPointer</td></tr><tr><td>0</td></tr></table><table><tr><td>FreePointer</td></tr><tr><td>8</td></tr></table><table><tr><th>Index</th><th>LeftPointer</th><th>Data</th><th>RightPointer</th></tr><tr><td>[0]</td><td>3</td><td>99</td><td>1</td></tr><tr><td>[1]</td><td>2</td><td>125</td><td>6</td></tr><tr><td>[2]</td><td>4</td><td>121</td><td>null</td></tr><tr><td>[3]</td><td>5</td><td>97</td><td>null</td></tr><tr><td>[4]</td><td>null</td><td>109</td><td>null</td></tr><tr><td>[5]</td><td>null</td><td>95</td><td>null</td></tr><tr><td>[6]</td><td>null</td><td>135</td><td>7</td></tr><tr><td>[7]</td><td>null</td><td>149</td><td>null</td></tr><tr><td>[8]</td><td></td><td></td><td></td></tr></table></div>	RootPointer	0	FreePointer	8	Index	LeftPointer	Data	RightPointer	[0]	3	99	1	[1]	2	125	6	[2]	4	121	null	[3]	5	97	null	[4]	null	109	null	[5]	null	95	null	[6]	null	135	7	[7]	null	149	null	[8]				6
RootPointer																																														
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Index	LeftPointer	Data	RightPointer																																											
[0]	3	99	1																																											
[1]	2	125	6																																											
[2]	4	121	null																																											
[3]	5	97	null																																											
[4]	null	109	null																																											
[5]	null	95	null																																											
[6]	null	135	7																																											
[7]	null	149	null																																											
[8]																																														
2(b)	<div>1 mark for each completed section</div> <div><pre>FUNCTION FindElement(Item : INTEGER) RETURNS INTEGER CurrentPointer ← RootPointer WHILE CurrentPointer <> NullPointer IF List[CurrentPointer].Data <> Item THEN CurrentPointer ← List[CurrentPointer].Pointer ELSE RETURN CurrentPointer ENDIF ENDWHILE CurrentPointer ← NullPointer RETURN CurrentPointer ENDFUNCTION</pre></div>	6																																												

Binary Tree (ADT)

Question No. 5

4(c)(i)	To point to the start/first of the empty node/nodes	1
4(c)(ii)	-1 or below // 101 or above	1
4(c)(iii)	<p>1 mark for 23 at top, with 5 below left, 100 below right 1 mark for remaining in correct places below 5 and 100</p> 	2
4(c)(iv)	<p>1 mark for each completed statement</p> <pre> PROCEDURE AddData (NewNode) BinaryTree[FreePointer] ← NewNode BinaryTree[FreePointer].LeftPointer ← -1 BinaryTree[FreePointer].RightPointer ← -1 DECLARE PositionFound : BOOLEAN DECLARE PointerCounter : INTEGER PositionFound ← FALSE PointerCounter ← RootNode WHILE NOT PositionFound IF NewNode.Data < BinaryTree[PointerCounter].Data THEN IF BinaryTree[PointerCounter].LeftPointer = -1 THEN BinaryTree[PointerCounter].LeftPointer ← FreePointer PositionFound ← TRUE ELSE PointerCounter ← BinaryTree[PointerCounter].LeftPointer ENDIF ELSE IF BinaryTree[PointerCounter].RightPointer = -1 THEN BinaryTree[PointerCounter].RightPointer ← FreePointer PositionFound ← True ELSE PointerCounter ← BinaryTree[PointerCounter].RightPointer ENDIF ENDIF ENDWHILE FreePointer ← FreePointer + 1 ENDPROCEDURE </pre>	5

Binary Tree (ADT)

Question No. 6

2(a)	<ul style="list-style-type: none">A pointer that doesn't point to another node/other data/address // indicates the end of the branch	1																																												
2(b)	one mark per bullet <ul style="list-style-type: none">node with 'Athens' linked to left pointer of Berlin (ignore null pointer)null pointers in left and right pointers of Athens	2																																												
2(c)(i)	<div><div><div>RootPointer</div><div>0</div></div><div><div>FreePointer</div><div>7</div><div>1 mark</div></div><table><thead><tr><th></th><th>LeftPointer</th><th>Tree Data</th><th>RightPointer</th></tr></thead><tbody><tr><td>[0]</td><td>2</td><td>Dublin</td><td>1</td></tr><tr><td>[1]</td><td>-1/∅</td><td>London</td><td>3</td></tr><tr><td>[2]</td><td>6</td><td>Berlin</td><td>5</td></tr><tr><td>[3]</td><td>4</td><td>Paris</td><td>-1/∅</td></tr><tr><td>[4]</td><td>-1/∅</td><td>Madrid</td><td>-1/∅</td></tr><tr><td>[5]</td><td>-1/∅</td><td>Copenhagen</td><td>-1/∅</td></tr><tr><td>[6]</td><td>-1/∅</td><td>Athens</td><td>-1/∅</td></tr><tr><td>[7]</td><td>8</td><td></td><td>-1/∅</td></tr><tr><td>[8]</td><td>9</td><td></td><td>-1/∅</td></tr><tr><td>[9]</td><td>-1/∅</td><td></td><td>-1/∅</td></tr></tbody></table></div>		LeftPointer	Tree Data	RightPointer	[0]	2	Dublin	1	[1]	-1/∅	London	3	[2]	6	Berlin	5	[3]	4	Paris	-1/∅	[4]	-1/∅	Madrid	-1/∅	[5]	-1/∅	Copenhagen	-1/∅	[6]	-1/∅	Athens	-1/∅	[7]	8		-1/∅	[8]	9		-1/∅	[9]	-1/∅		-1/∅	5
	LeftPointer	Tree Data	RightPointer																																											
[0]	2	Dublin	1																																											
[1]	-1/∅	London	3																																											
[2]	6	Berlin	5																																											
[3]	4	Paris	-1/∅																																											
[4]	-1/∅	Madrid	-1/∅																																											
[5]	-1/∅	Copenhagen	-1/∅																																											
[6]	-1/∅	Athens	-1/∅																																											
[7]	8		-1/∅																																											
[8]	9		-1/∅																																											
[9]	-1/∅		-1/∅																																											
2(c)(ii)	<ul style="list-style-type: none">-1It is not the number for any node.	2																																												

Binary Tree (ADT)

2(d)(i)	<pre> TYPE Node LeftPointer : INTEGER RightPointer : INTEGER Data : STRING ENDTYPE DECLARE Tree : ARRAY[0 : 9] OF Node DECLARE FreePointer : INTEGER DECLARE RootPointer : INTEGER PROCEDURE CreateTree() DECLARE Index : INTEGER RootPointer ← -1 FreePointer ← 0 FOR Index ← 0 TO 9 // link nodes Tree[Index].LeftPointer ← Index + 1 Tree[Index].RightPointer ← -1 ENDFOR Tree[9].LeftPointer ← -1 ENDPROCEDURE </pre>	7
2(d)(ii)	<pre> PROCEDURE AddToTree(ByVal NewDataItem : STRING) // if no free node report an error IF FreePointer = -1 THEN ERROR("No free space left") ELSE // add new data item to first node in the free list NewNodePointer ← FreePointer Tree[NewNodePointer].Data ← NewDataItem // adjust free pointer FreePointer ← Tree[FreePointer].LeftPointer // clear left pointer Tree[NewNodePointer].LeftPointer ← -1 // is tree currently empty ? IF RootPointer = -1 THEN // make new node the root node RootPointer ← NewNodePointer ELSE // find position where new node is to be added Index ← RootPointer CALL FindInsertionPoint(NewDataItem, Index, Direction) </pre>	8
	<pre> IF Direction = "Left" THEN // add new node on left Tree[Index].LeftPointer ← NewNodePointer ELSE // add new node on right Tree[Index].RightPointer ← NewNodePointer ENDIF ENDFOR ENDFOR ENDFOR ENDPROCEDURE </pre>	

Binary Tree (ADT)

2(e)	<p>1 mark per bullet</p> <ul style="list-style-type: none">• test for base case (null/-1)• recursive call for left pointer• output data• recursive call for right pointer• order, visit left, output, visit right <pre>IF Pointer <> NULL THEN TraverseTree(Tree[Pointer].LeftPointer) OUTPUT Tree[Pointer].Data TraverseTree(Tree[Pointer].RightPointer) ENDIF ENDPROCEDURE</pre>	5
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Binary Tree (ADT)

Question No. 7

4(a)	<p>1 mark per bullet point</p> <ul style="list-style-type: none">• Record declaration with identifier Node ...• ... all three fields declared with type integer <p>Example:</p> <pre>TYPE Node DECLARE LeftPointer : INTEGER DECLARE Data : INTEGER DECLARE RightPointer : INTEGER ENDTYPE</pre>	2
4(b)	<p>1 mark per bullet point:</p> <ul style="list-style-type: none">• Declaration with correct identifier (Node100) of type Node• Assigning LeftPointer to 1 and RightPointer to 4• Assigning 100 to the Data <p>Example pseudocode</p> <pre>DECLARE Node100 : Node Node100.LeftPointer ← 1 Node100.Data ← 100 Node100.RightPointer ← 4</pre>	3