

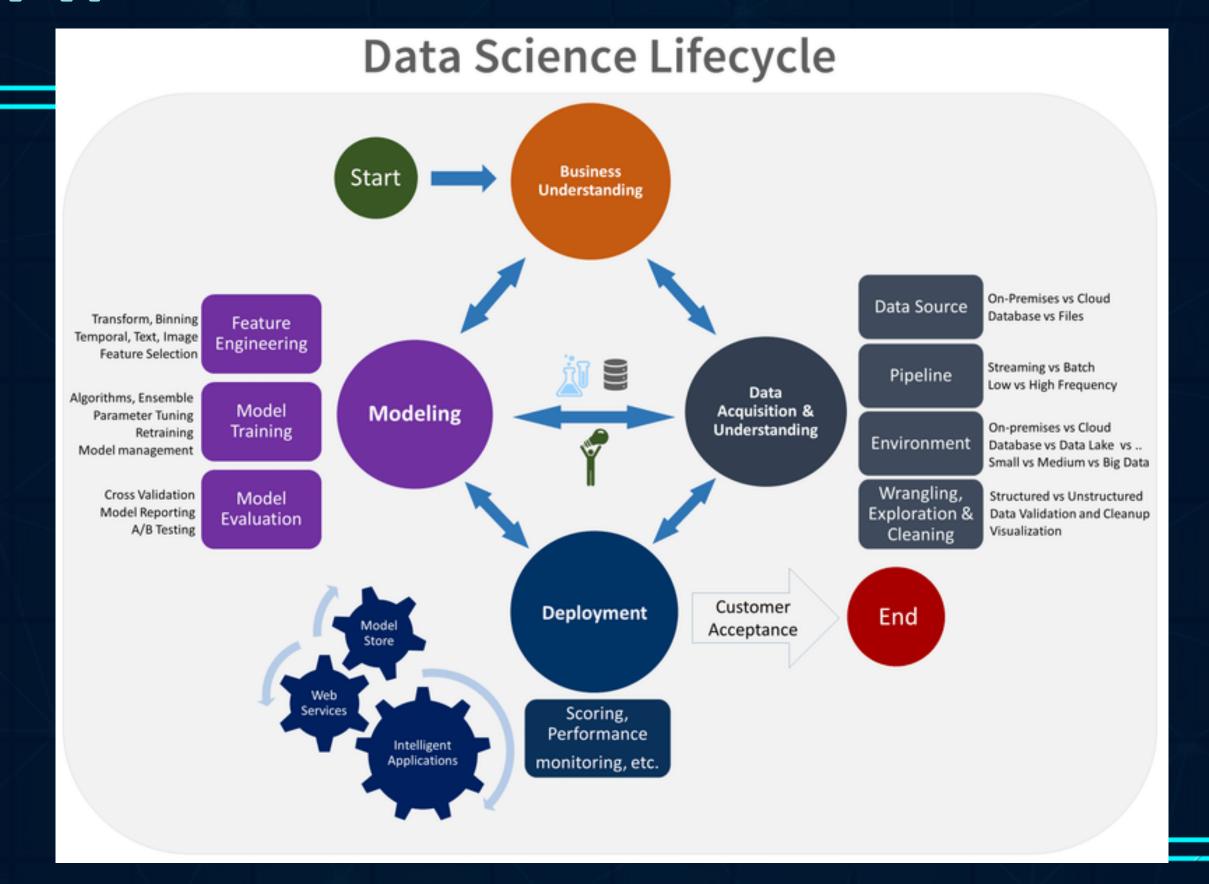


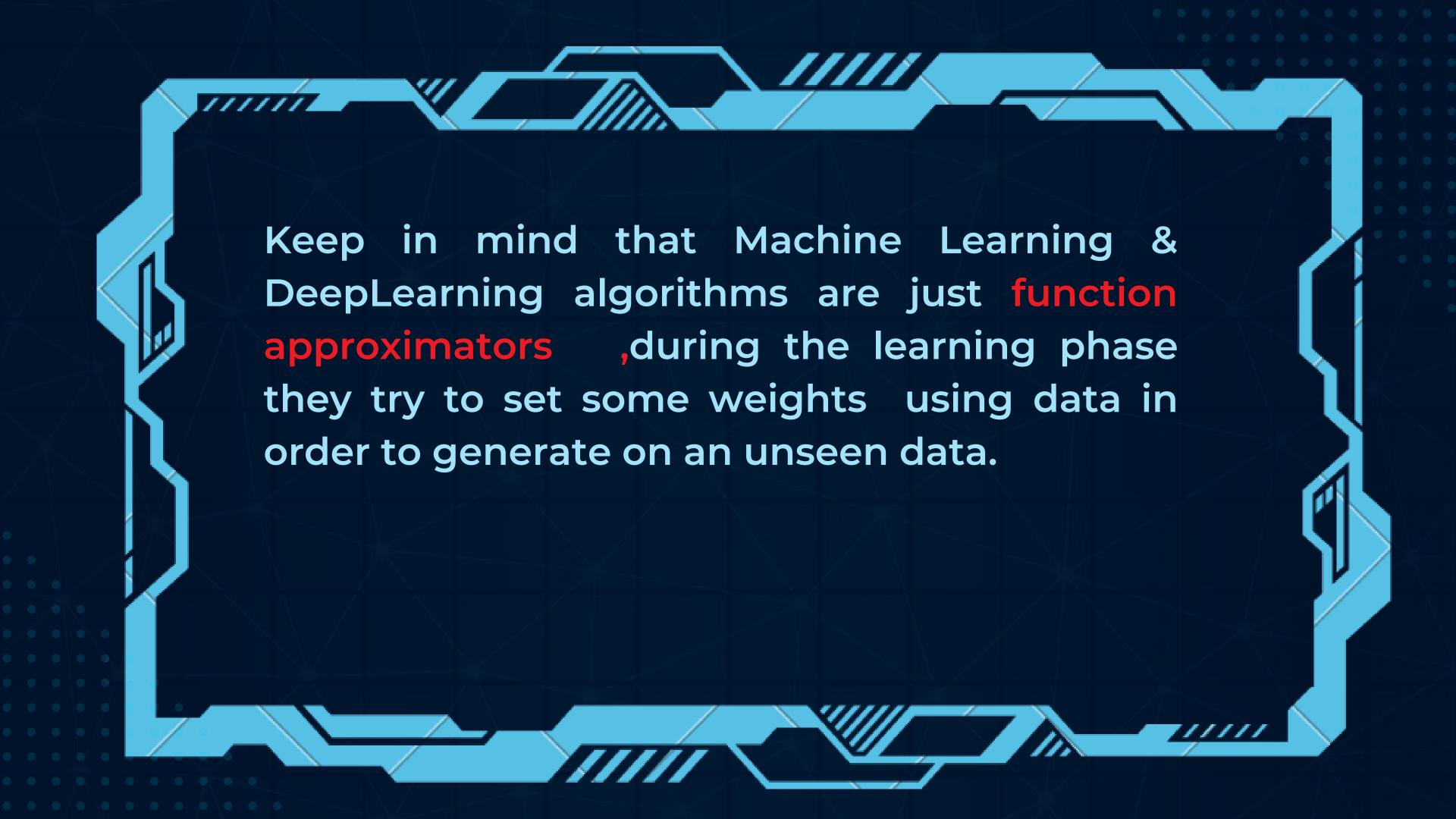


# MODELLING

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## REACAP





### LINEAR REGRESSION:

Linear regression is a supervised algorithm that learns to model a <u>dependent variable</u>, y, as a function of some <u>independent variables</u> (aka "features"), xi, by finding a line (or surface) that best "fits" the data. In general, we assume y to be some number and each xi can be basically anything. For example: predicting the price of a house using the number of rooms in that house (y: price, x1: number of rooms) or predicting weight from height and age (y: weight, x1: height, x2: age).



In general, the equation for linear regression is:



$$y=eta_0+eta_1x_1+eta_2x_2+...+eta_px_p+\epsilon$$
 the thing we're trying to predict

 $\beta$ i: the coefficients (aka "weights") of our regression model. These are the foundations of our model. They are what our model "learns" during optimization.

Fitting a linear regression model is all about finding the set of cofficients that best model y as a function of our features. We may never know the true parameters for our model, but we can estimate them (more on this later). Once we've estimated these coefficients,  $\beta$ i, we predict future values, y\_hat, as:

$$\hat{y} = \hat{eta_0} + \hat{eta_1} x_1 + \hat{eta_2} x_2 + ... + \hat{eta_p} x_p$$

# BUT HOW CAN WE BEST ESTIMATE THESE COEFFICIENTS?

#### LEARNING THE COEFFICIENTS:

An Iterative Solution: Gradient descent an iterative optimization algorithm that estimates some set of coefficients to yield the minimum of a convex function.

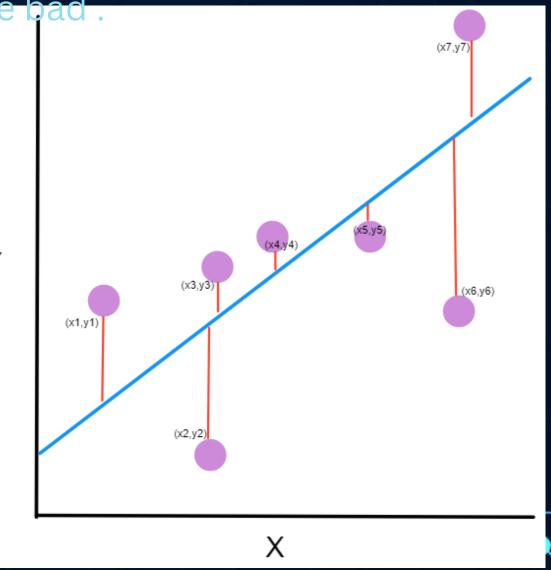
First we need to define an objective function: a loss function in our case to

minimize in such a way that it increases when the predictions are bad.

#### **MSE: Mean Squared Error:**

$$MSE = rac{1}{n}\Sigma_{i=1}^n(y_i - \hat{y_i})^2$$

MSE quantifies how close a predicted value is to the true value.



#### Or our model take the form

$$\hat{y} = \hat{eta_0} + \hat{eta_1} x_1 + \hat{eta_2} x_2 + ... + \hat{eta_p} x_p$$

and then our error function is:

$$MSE = \frac{1}{n} \sum_{1}^{n} (y_i - (\hat{\beta_0} + \hat{\beta_1} x_1 + \hat{\beta_2} x_2 + \dots + \hat{\beta_p} x_p))^2$$

gradient descent : repeat until convergence :

$$\beta_i = \beta_i - \alpha \frac{\delta}{\delta \beta_i} MSE$$
learning rate

#### DIVE DEEPER:

There's a ton of different things we didn't cover. Some of those topics left unmentioned are:

- regularization methods
- selection techniques
- common regression transformations...

we recommend diving deep into the aforementioned topics.

# LET'S PRACTICE

Fitting a linear regression model in practice is quite simple : all we need is the powerfull library sklearn library.

```
from sklearn.linear_model import LinearRegression
from sklearn.model_selection import train_test_split
from sklearn.metrics import r2_score
from sklearn.metrics import mean_squared_error as mse
```

```
#splitting data into train and validation
X_train,X_valid,y_train,y_valid=train_test_split(X,y,test_size=0.2)
```

```
estimator=LinearRegression()
estimator.fit(X_train,y_train)
y_hat=estimator.predict(X_valid)
print(f'MSE ={mse(y_hat,y_valid)}')
print(f'R2 score ={r2_score(y_hat,y_valid)}')
```





# NOW IT'S YOUR TIME TO TRY!