

Thesis Proposal

Methodology and Statistics for the Behavioural, Biomedical and Social Sciences

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ShinyMICE: an Evaluation Suite for Multiple Imputation

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Introduction

At some point, any scientist conducting statistical analyses will run into a missing data problem [2]. Missingness is problematic because statistical inference cannot be performed on incomplete data, and ad hoc solutions can yield wildly invalid results [13]. To circumvent the ubiquitous problem of missing information, Rubin [11] proposed the framework of multiple imputation (MI). MI is an iterative algorithmic procedure in which missing data points are ‘guessed’ (i.e. imputed) several times. The variability between the imputations validly reflects how much uncertainty in the inference is due to missing information—that is, if all statistical assumptions are met [11].

With MI, many assumptions are made about the nature of the observed and missing parts of the data and their relation to the ‘true’ *data generating model* [13]. Without proper evaluation of the imputations and the underlying assumptions, any drawn inference may erroneously be deemed valid. Such evaluation measures are currently missing or under-developed in MI software, like the world leading R package MICE [14]. Therefore, I will answer the following question: ‘Which measures are vital for evaluating the validity of multiply imputed data?’.

Literature Review

The validity of the MI solution depends on numerous assumptions that cannot be verified from the observed data alone. So instead of statistical tests for assumptions, evaluation procedures have been developed. For the following assumptions, no reliable procedure has been proposed and/or implemented: 1) *ignorability* of the *missingness mechanism* [11]; 2) *congeniality* of the imputation models [7]; and 3) *compatibility* of the MI modeling procedure [10].

1. A missingness mechanism is said to be ignorable when the probability to be missing does not depend on the missing data itself. Violation of this assumption can gravely affect inferences. Robustness of inferences to varying degrees of violation can be assessed with sensitivity analyses. Some practical guidelines exist (e.g., [9]), but current MI software does not facilitate this methodology for empirical researchers.
2. Congenial imputation models capture all required relations between observed and missing parts of the data. The extent to which this has been successful can be evaluated by plotting conditional distributions [1]. Such visualizations are available in MICE, but subsequent statistical tests to quantify the relations with covariates are not provided.¹
3. The third assumption is met when the MI algorithm converges to a stable distribution. However, conventional measures to diagnose convergence—e.g., Gelman and Rubin’s [5] statistic \hat{R} —are not applicable on multiply imputed data [6]. Therefore, empirical researchers have to rely on visual inspection procedures that are theoretically equivalent to \hat{R} [15]. Visually assessing convergence is not only difficult to the untrained eye, it might also be futile. The convergence properties of MI algorithms lack scientific consensus [12], and some default MICE techniques might not converge to stable distributions at all [8]. Moreover, convergence diagnostics for MI methods have not been systematically studied [13].

In short, the existing literature provides both possibilities and limitations to evaluating the validity of multiply imputed data. The goal of this research project is to develop novel methodology and guidelines for evaluating MI methods, and implement these in an interactive evaluation framework for multiple imputation. This framework will aid applied researchers in drawing valid inference from incomplete datasets.

¹Additionally, there is potential to assess model fit by means of *over-imputation* [13] or *double robustness* [3]—topics that are only pursued if time permits.

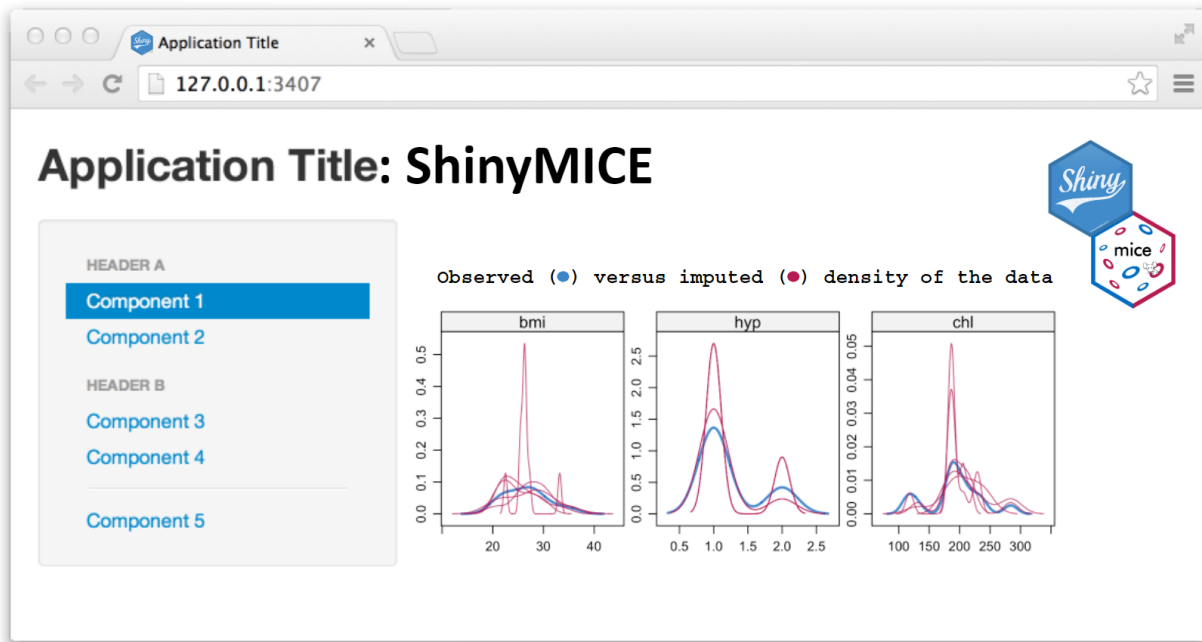


Figure 1: Preliminary impression of the interactive **ShinyMICE** user interface.

Approach

Initially, the research project will consist of an investigation into algorithmic convergence of MI algorithms. I will replicate Lacerda et al.'s simulation study on \hat{R} [6], and develop novel guidelines for assessing convergence. Ideally, I will integrate several diagnostics (e.g., \hat{R} , *auto-correlation*, and *simulation error*) into a single summary indicator to flag non-convergence.

Subsequently, I will use R **Shiny** [4] to implement the convergence indicator and existing evaluation measures in **ShinyMICE**, see Figure 1. The application will at least contain methodology for: sensitivity analyses; data visualizations (e.g., scatter-plots, densities, cross-tabulations); and statistical evaluation of relations between variables pre- versus post-imputation (i.e., χ^2 -tests or *t*-tests).

A working beta version of **ShinyMICE** will be considered a sufficient milestone to proceed with writing a technical paper on the methodology and the software. I will submit the paper for publication in *Journal of Statistical Software*. Finally, **ShinyMICE** will be integrated into the existing **MICE** environment, and a vignette for applied researchers will be written.

The R code and documentation of this project will be open source (available on Github). Since the study does not require the use of unpublished empirical data, I expect that the FETC will grant the label 'exempt'.

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