

Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given
$$x$$
, want $y = P(y=1|x)$
 $x \in \mathbb{R}^{n}x$
Parareters: $w \in \mathbb{R}^{n}x$, $b \in \mathbb{R}$.
Output $y = \sigma(w^{T}x + b)$
Output $y = \sigma(x)$

$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$\hat{y} = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Since $\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int_{\mathcal{C}} (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

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Basics of Neural Network Programming

Gradient Descent

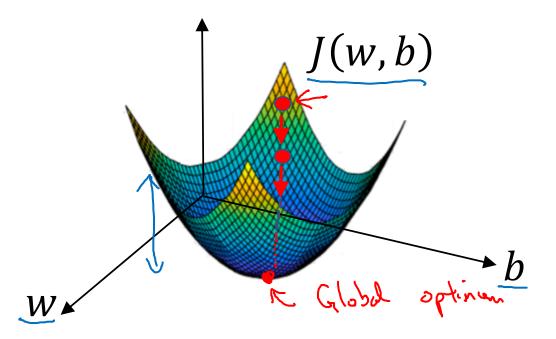
deeplearning.ai

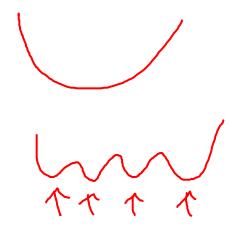
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

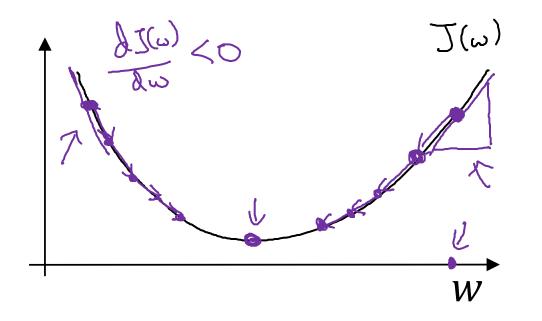
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

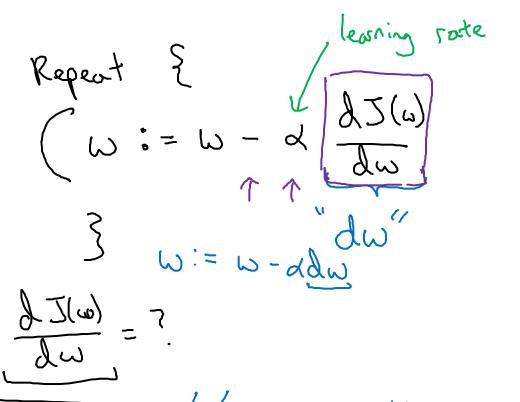
Want to find w, b that minimize J(w, b)





Gradient Descent





$$J(\omega,b)$$

$$b:=b-\lambda \frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

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$$\frac{\partial J(\omega,b)}{\partial \omega}$$

Andrew Ng



Basics of Neural Network Programming

Logistic Regression Gradient descent

Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

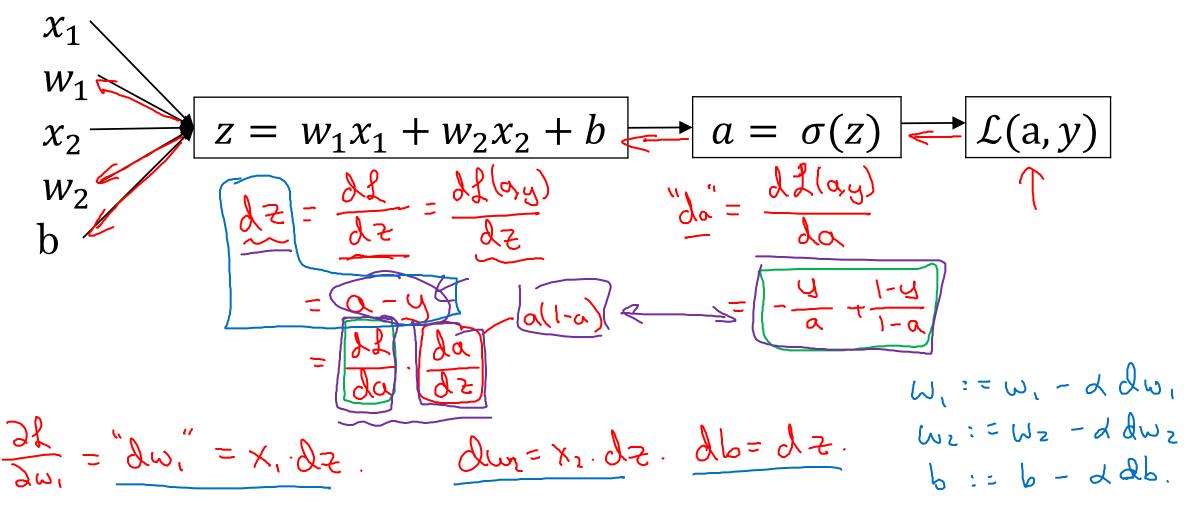
$$\begin{cases} \lambda_{1} \\ \omega_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{2} \\ \lambda_{3} \\ \lambda_{4} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

Logistic regression derivatives





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Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(u,b)}{J(u,b)} = \frac{1}{m} \sum_{i=1}^{m} f(a^{(i)}, y^{(i)}) \\
\Rightarrow a^{(i)} = f(x^{(i)}) = G(x^{(i)}, y^{(i)}) \\
\frac{\partial}{\partial u_i} J(u,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial u_i} f(a^{(i)}, y^{(i)}) \\
\frac{\partial u_i}{\partial u_i} - (x^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0; dw_{1}=0; dw_{2}=0; db=0$$

$$For i=1 to m$$

$$Z^{(i)}=\omega^{T}x^{(i)}+b$$

$$Q^{(i)}=6(Z^{(i)})$$

$$J+=-[y^{(i)}(og Q^{(i)}+(1-y^{(i)})(og(1-q^{(i)})]$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$J=0; dw_{2}(1-q^{(i)})$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dz^{(i)}=Q^{(i)}-y^{(i)}$$

$$dw_{1}+=x^{(i)}dz^{(i)}$$

$$dw_{2}+=x^{(i)}dz^{(i)}$$

$$J=0; dw_{2}(1-q^{(i)})$$

$$dz^{(i)}=Q^{(i)}$$

$$dw_{2}+=Q^{(i)}$$

$$dw_{3}+=Q^{(i)}$$

$$dw_{4}+=Q^{(i)}$$

$$dw_{4}+=Q^{(i)}$$

$$dw_{5}+=Q^{(i)}$$

$$dw_{6}+=Q^{(i)}$$

$$dw_{7}+=m; dw_{7}+=m; db/=m.$$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - \alpha d\omega_2$
 $b := b - d db$

We to right is a sum of the sum o



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Vectorization

What is vectorization?

$$for i in raye (n-x):$$

$$2+= \omega [1] * x (1)$$



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Vectorizing Logistic Regression

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Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



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Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$A = [a^{(1)} - a^{(1)}] \quad Y = [y^{(1)} - y^{(2)}]$$

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$$A = [a^{(1)} - y^{(1)}] \quad a$$

$$db = \frac{1}{m} \sum_{i=1}^{n} dz^{(i)}$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

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$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

Implementing Logistic Regression

J = 0,
$$dw_1 = 0$$
, $dw_2 = 0$, $db = 0$

for i = 1 to m:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)}) \checkmark$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \checkmark$$

$$dw_1 += x_1^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_1 += dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_3 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_5 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

$$dw_7 += dw_7 / m$$

$$dw_8 == dw_8 / m$$

iter in range (1000)!
$$\angle$$

$$Z = \omega^{T} X + b$$

$$= n p \cdot dot (\omega \cdot T \cdot X) + b$$

$$A = \epsilon (Z)$$

$$A = \epsilon (Z)$$

$$A = \Delta - Y$$

$$A$$



Basics of Neural Network Programming

Explanation of logistic regression cost function (Optional)

Logistic regression cost function

Logistic regression cost function

If
$$y = 1$$
: $p(y|x) = \hat{y}$

If $y = 0$: $p(y|x) = 1 - \hat{y}$

$$p(y|x) = \hat{y} \cdot (1 - \hat{y})$$

Cost on *m* examples

log
$$p(lolods)$$
 in troops set) = log $\prod_{i=1}^{m} p(y^{(i)}|\chi^{(i)})$

log $p(----) = \sum_{i=1}^{m} log p(y^{(i)}|\chi^{(i)})$

Movimum likelihood setiment

$$- \chi(y^{(i)}, y^{(i)})$$

$$= -\sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$$

(ost: $J(w, b) = \frac{1}{m} \sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$

(minimize)